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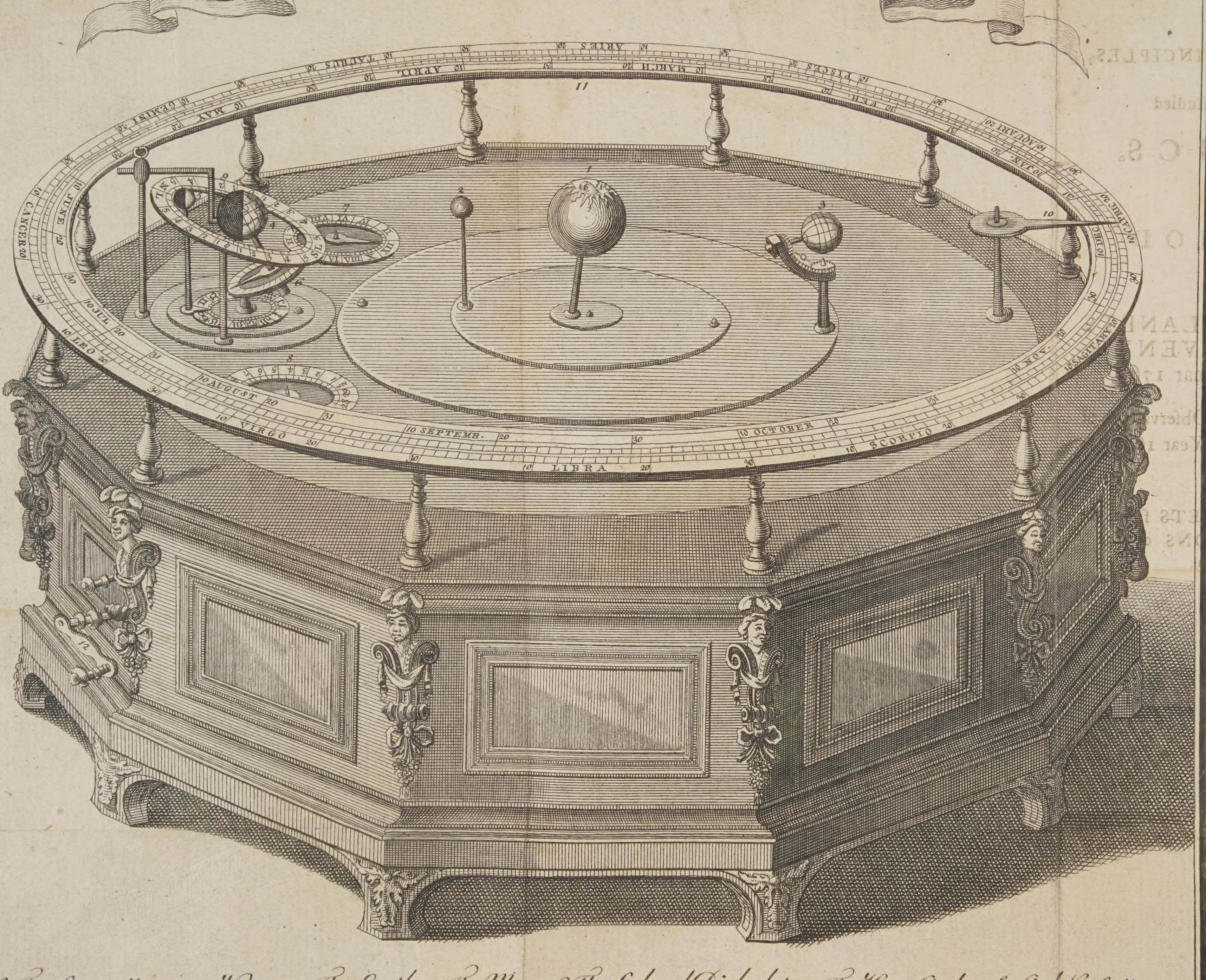

Nº 1 The Sun, 2 Mercury, 3 Venus, 4 The Earth, 5 The Moon, 6 The Sydereal Dial plate, 7 The Hour Circle, 8 ye Circle for ye Moon's Age, 9 The Moon's Orbit, 10 ye Pointer, ſhewing the Sun's Place & Day of the Month, 11 The Ecliptic, 12 The Handle for turning ye whole machine

J. Ferguson inv. et deline. *G. Child Sculp.*

75028

ASTRONOMY

EXPLAINED UPON
Sir ISAAC NEWTON's PRINCIPLES,
And made eaſy to thoſe who have not ſtudied
MATHEMATICS.

To which are added,

A PLAIN METHOD

OF FINDING
The DISTANCES of all the PLANETS
from the SUN, by the TRANSIT of VENUS
over the SUN's DISC, in the Year 1761.

An Account of Mr. HORROX's Obſervation of
the TRANSIT of VENUS in the Year 1639:

AND,

Of the DISTANCES of all the PLANETS from the
SUN, as deduced from OBSERVATIONS of the
TRANSIT in the Year 1761.

By JAMES FERGUSON, *F.R.S.*

HEB. xi. 3. *The Worlds were framed by the Word of* GOD.
JOB xxvi. 7. *He hangeth the Earth upon nothing.*
——— 13. *By his Spirit he hath garniſhed the Heavens.*

THE FOURTH EDITION, corrected.

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TREATISE OF ASTRONOMY
IS INSCRIBED,
With the MOST PROFOUND RESPECT,
By HIS LORDSHIP's
MOST OBLIGED,
AND
MOST HUMBLE SERVANT,

JAMES FERGUSON.

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ASTRONOMY

EXPLAINED UPON

Sir ISAAC NEWTON's PRINCIPLES.

CHAP. I.

Of Aſtronomy in general.

The general uſe of Aſtronomy.

1. OF all the ſciences cultivated by mankind, Aſtronomy is acknowledged to be, and undoubtedly is, the moſt ſublime, the moſt intereſting, and the moſt uſeful. For, by knowledge derived from this ſcience, not only the bulk of the Earth is diſcovered, the ſituation and extent of the countries and kingdoms upon it aſcertained, trade and commerce carried on to the remoteſt parts of the world, and the various products of ſeveral countries diſtributed for the health, comfort, and conveniency of it's inhabitants; but our very faculties are enlarged with the grandeur of the ideas it conveys, our minds exalted above the low contracted prejudices of the vulgar, and our underſtandings clearly convinced, and affected with the conviction of the exiſtence, wiſdom, power, goodneſs, immutability, and ſuperintendency of the SUPREME BEING! So that without an hyperbole,

“ *An undevout Aſtronomer is mad*[*].”

2. From this branch of knowledge we alſo learn by what means or laws the Almighty carries on, and continues the admirable harmony, order, and connexion obſervable throughout the planetary ſyſtem; and are led by very powerful arguments to form the pleaſing deduction, that minds capable of

---

[*] Dr. Young's Night Thoughts.

ſuch deep reſearches not only derive their origin from that adorable Being, but are alſo incited to aſpire after a more perfect knowledge of his nature, and a ſtricter conformity to his will.

The Earth but a point as ſeen from the Sun.

3. By Aſtronomy we diſcover that the Earth is at ſo great a diſtance from the Sun, that if ſeen from thence it would appear no bigger than a point; although it's circumference is known to be 25,020 miles. Yet that diſtance is ſo ſmall, compared with the Earth's diſtance from the Fixed Stars, that if the orbit in which the Earth moves round the Sun were ſolid, and ſeen from the neareſt Star, it would likewiſe appear no bigger than a point, although it is at leaſt 162 millions of miles in diameter. For the Earth in going round the Sun is 162 millions of miles nearer to ſome of the Stars at one time of the year, than at another; and yet their apparent magnitudes, ſituations, and diſtances from one another ſtill remain the ſame; and a teleſcope which magnifies above 200 times does not ſenſibly magnify them: which proves them to be at leaſt 400 thouſand times farther from us than we are from the Sun.

The Stars are Suns,

4. It is not to be imagined that all the Stars are placed in one concave ſurface, ſo as to be equally diſtant from us; but that they are ſcattered at immenſe diſtances from one another through unlimited ſpace. So that there may be as great a diſtance between any two neighbouring Stars, as between our Sun and thoſe which are neareſt to him. Therefore an Obſerver, who is neareſt any fixed Star, will look upon it alone as a real Sun; and conſider the reſt as ſo many ſhining points, placed at equal diſtances from him in the Firmament.

and innumerable.

5. By the help of teleſcopes we diſcover thouſands of Stars which are inviſible to the naked eye; and the better our glaſſes are, ſtill the more become viſible: ſo that we can ſet no limits either to their number or their diſtances. The celebrated HUYGENS carries his thoughts ſo far, as to believe it

not impoſſible that there may be Stars at ſuch inconceivable diſtances, that their light has not yet reached the Earth ſince it's creation; although the velocity of light be a million of times greater than the velocity of a cannon-bullet, as ſhall be demonſtrated afterwards, § 197, 216: and, as Mr. Addison very juſtly obſerves, this thought is far from being extravagant, when we conſider that the Univerſe is the work of infinite power, prompted by infinite goodneſs; having an infinite ſpace to exert itſelf in; ſo that our imaginations can ſet no bounds to it.

Why the Sun appears bigger than the Stars.

6. The Sun appears very bright and large in compariſon of the Fixed Stars, becauſe we keep conſtantly near the Sun, in compariſon of our immenſe diſtance from the Stars. For, a ſpectator, placed as near to any Star as we are to the Sun, would ſee that Star a body as large and bright as the Sun appears to us: and a ſpectator, as far diſtant from the Sun as we are from the Stars, would ſee the Sun as ſmall as we ſee a Star, diveſted of all it's circumvolving Planets; and would reckon it one of the Stars in numbering them.

The Stars are not enlightened by the Sun.

7. The Stars, being at ſuch immenſe diſtances from the Sun, cannot poſſibly receive from him ſo ſtrong a light as they ſeem to have; nor any brightneſs ſufficient to make them viſible to us. For the Sun's rays muſt be ſo ſcattered and diſſipated before they reach ſuch remote objects, that they can never be tranſmitted back to our eyes, ſo as to render theſe objects viſible by reflexion. The Stars therefore ſhine with their own native and unborrowed luſtre, as the Sun does; and ſince each particular Star, as well as the Sun, is confined to a particular portion of ſpace, it is plain that the Stars are of the ſame nature with the Sun.

8. It is no ways probable that the Almighty, who always acts with infinite wiſdom and does nothing in vain, ſhould create ſo many glorious Suns, fit for ſo many important purpoſes, and place them

at ſuch diſtances from one another, without proper objects near enough to be benefited by their influences. Whoever imagines they were created only to give a faint glimmering light to the inhabitants of this Globe, muſt have a very ſuperficial knowledge of Aſtronomy, and a mean opinion of the Divine Wiſdom: ſince, by an infinitely leſs exertion of creating power, the Deity could have given our Earth much more light by one ſingle additional Moon.

They are probably ſurrounded by Planets.

9. Inſtead then of one Sun and one World only in the Univerſe, as the unſkilful in Aſtronomy imagine, *that* Science diſcovers to us ſuch an inconceivable number of Suns, Syſtems, and Worlds, diſperſed through boundleſs Space, that if our Sun, with all the Planets, Moons, and Comets belonging to it, were annihilated, they would be no more miſſed, by an eye that could take in the whole Creation, than a grain of ſand from the ſea-ſhore. The ſpace they poſſeſs being comparatively ſo ſmall, that it would ſcarce be a ſenſible blank in the Univerſe, although Saturn, the outermoſt of our Planets, revolves about the Sun in an Orbit of 4884 millions of miles in circumference, and ſome of our Comets make excurſions upwards of ten thouſand millions of miles beyond Saturn's Orbit; and yet, at that amazing diſtance, they are incomparably nearer to the Sun than to any of the Stars; as is evident from their keeping clear of the attractive power of all the Stars, and returning periodically by virtue of the Sun's attraction.

The ſtellar Planets may be habitable,

10. From what we know of our own Syſtem, it may be reaſonably concluded that all the reſt are with equal wiſdom contrived, ſituated, and provided with accommodations for rational inhabitants. Let us therefore take a ſurvey of the Syſtem to which we belong; the only one acceſſible to us; and from thence we ſhall be the better enabled to judge of the nature and end of the other Syſtems of the Univerſe. For although

there is almoſt an infinite variety in the parts of the Creation which we have opportunities of examining, yet there is a general analogy running through and connecting all the parts into one ſcheme, one deſign, one whole!

11. And then, to an attentive conſiderer, it will appear highly probable, that the Planets of our Syſtem, together with their attendants called Satellites or Moons, are much of the ſame nature with our Earth, and deſtined for the like purpoſes. For, they are ſolid opaque Globes, capable of ſupporting animals and vegetables. Some of them are bigger, ſome leſs, and ſome much about the ſize of our Earth. They all circulate round the Sun, as the Earth does, in a ſhorter or longer time, according to their reſpective diſtances from him; and have, where it would not be inconvenient, regular returns of ſummer and winter, ſpring and autumn. They have warmer and colder climates, as the various productions of our Earth require: and, in ſuch as afford a poſſibility of diſcovering it, we obſerve a regular motion round their axes like that of our Earth, cauſing an alternate return of day and night; which is neceſſary for labour, reſt, and vegetation, and that all parts of their ſurfaces may be expoſed to the rays of the Sun.

as our Solar Planets are.

12. Such of the Planets as are fartheſt from the Sun, and therefore enjoy leaſt of his light, have that deficiency made up by ſeveral Moons, which conſtantly accompany, and revolve about them, as our Moon revolves about the Earth. The remoteſt Planet has, over and above, a broad ring encompaſſing it; which like a lucid Zone in the Heavens reflects the Sun's light very copiouſly on that Planet: ſo that if the remoter Planets have the Sun's light fainter by day than we, they have an addition made to it morning and evening by one or more of their Moons, and a greater quantity of light in the night-time.

The fartheſt from the Sun have moſt Moons to enlighten their nights.

Our Moon mountainous like the Earth.

13. On the ſurface of the Moon, becauſe it is nearer us than any other of the celeſtial Bodies are, we diſcover a nearer reſemblance of our Earth. For, by the aſſiſtance of teleſcopes, we obſerve the Moon to be full of high mountains, large valleys, and deep cavities. Theſe ſimilarities leave us no room to doubt, but that all the Planets and Moons in the Syſtem are deſigned as commodious habitations for creatures endowed with capacities of knowing and adoring their beneficent Creator.

14. Since the Fixed Stars are prodigious ſpheres of fire, like our Sun, and at inconceivable diſtances from one another, as well as from us, it is reaſonable to conclude they are made for the ſame purpoſes that the Sun is; each to beſtow light, heat, and vegetation on a certain number of inhabited Planets, kept by gravitation within the ſphere of it's activity.

Numberleſs Suns and Worlds.

15. What an auguſt! what an amazing conception, if human imagination can conceive it, does this give of the works of the Creator! Thouſands of thouſands of Suns, multiplied without end, and ranged all around us, at immenſe diſtances from each other, attended by ten thouſand times ten thouſand Worlds, all in rapid motion, yet calm, regular, and harmonious, invariably keeping the paths preſcribed them; and theſe Worlds peopled with myriads of intelligent beings, formed for endleſs progreſſion in perfection and felicity.

16. If ſo much power, wiſdom, goodneſs, and magnificence is diſplayed in the material Creation, which is the leaſt conſiderable part of the Univerſe, how great, how wiſe, how good muſt HE be, who made and governs the Whole!

THE SOLAR SYSTEM

Plate I.

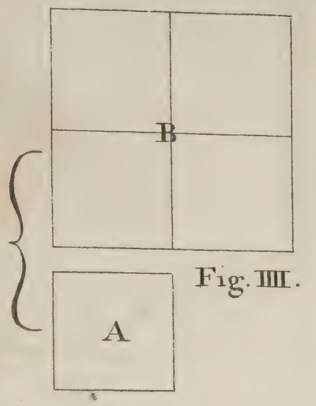


Fig. IIII.

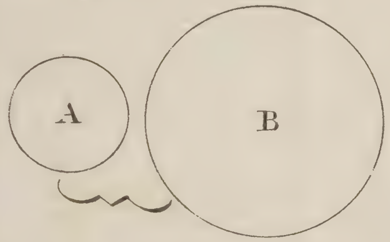


Fig. III.

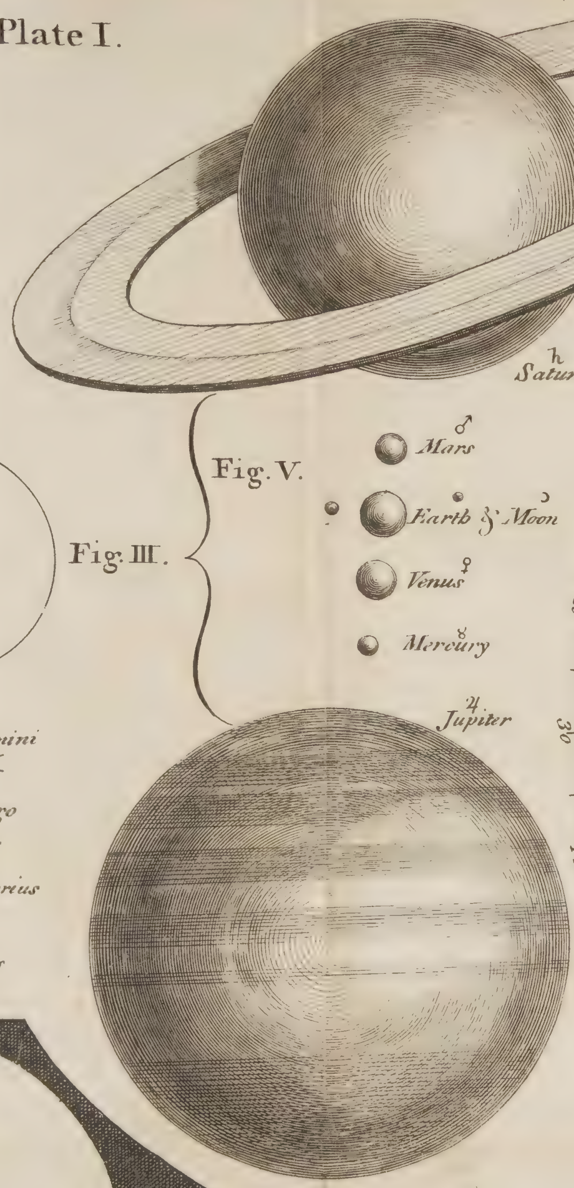


Fig. V.

Aries ♈	*Taurus* ♉	*Gemini* ♊
Cancer ♋	*Leo* ♌	*Virgo* ♍
Libra ♎	*Scorpio* ♏	*Sagittarius* ♐
Capricornus ♑	*Aquarius* ♒	*Pisces* ♓

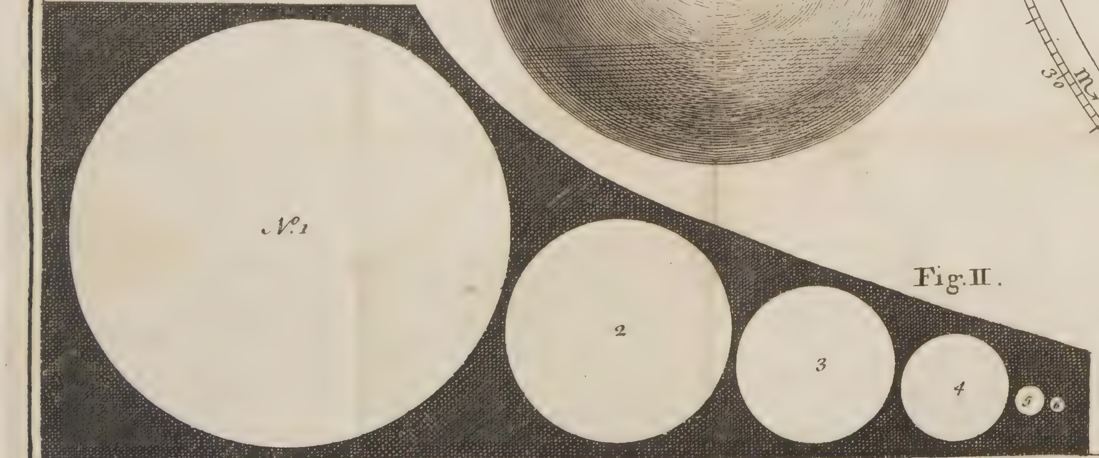
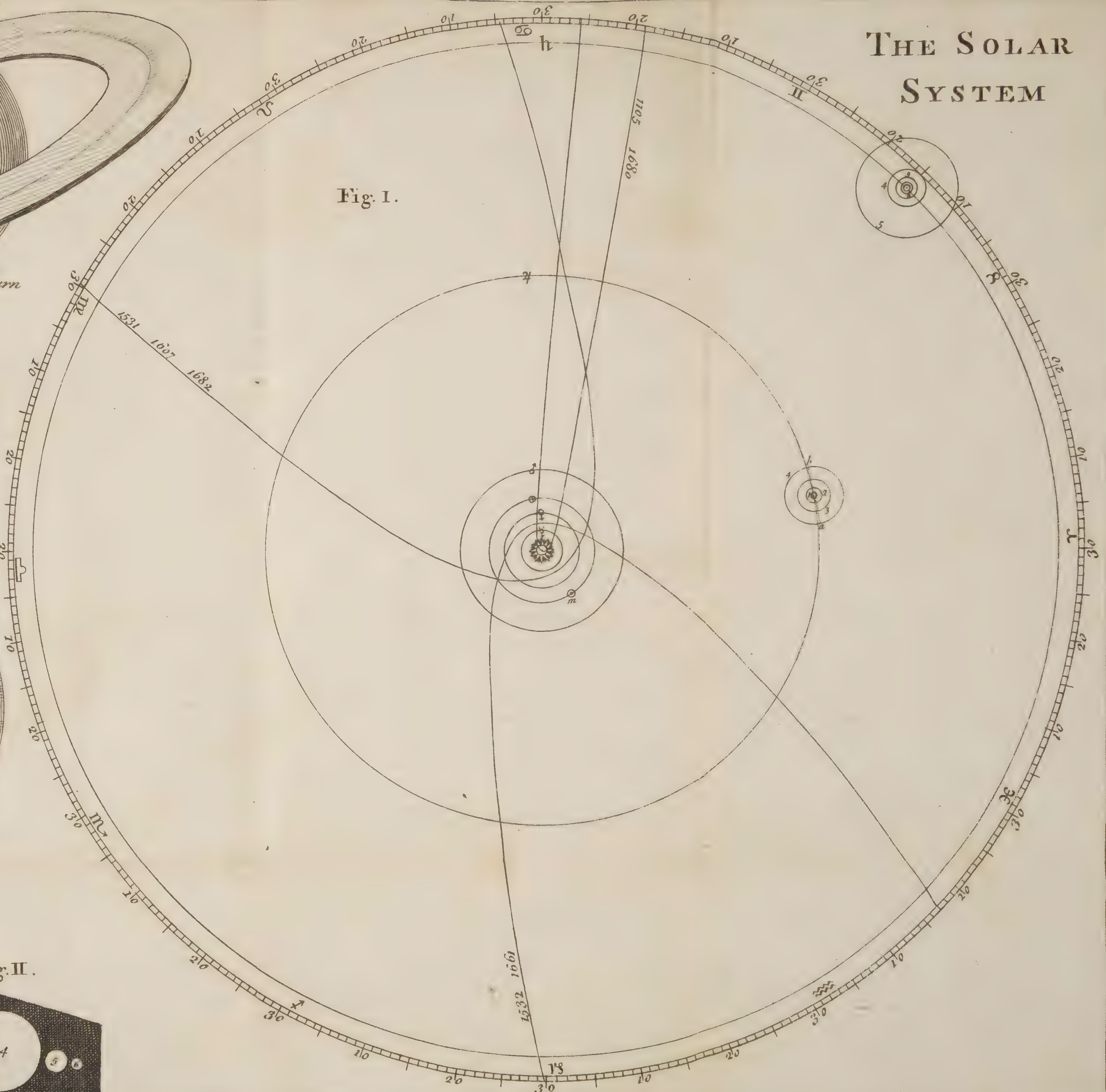


Fig. II.

Fig. I.



J. Ferguson delin.

J. Mynde Sculp.

CHAP. II.

A brief Deſcription of the SOLAR SYSTEM.

17. THE Planets and Comets which move round the SUN as their center, conſtitute the Solar Syſtem. Thoſe Planets which are near the Sun not only finiſh their circuits ſooner, but likewiſe move faſter in their reſpective Orbits, than thoſe which are more remote from him. Their motions are all performed from weſt to eaſt, in Orbits nearly circular. Their names, diſtances, bulks, and periodical revolutions, are as follow. **PLATE I. Fig. I.** **The Solar Syſtem.**

18. The SUN ☉, an immenſe globe of fire, is placed near the common center, or rather in the lower * focus, of the Orbits of all the Planets and Comets †; and turns round his axis in 25 days 6 hours, as is evident by the motion of ſpots ſeen on his ſurface. His diameter is computed to be 763,000 miles; and, by the various attractions of the circumvolving Planets, he is agitated by a **The Sun.** **Fig. I.**

---

* If a thread be tied looſely round two pins ſtuck in a table, and moderately ſtretched by the point of a black-lead pencil carried round by an even motion and light preſſure of the hand, an oval or ellipſis will be deſcribed; the two points where the pins are fixed being called the *foci* or focuſes thereof. The Orbits of all the Planets are elliptical, and the Sun is placed in or near to one of the *foci* of each of them: and *that* in which he is placed, is called the *lower focus*.

† Aſtronomers are not far from the truth, when they reckon the Sun's center to be in the lower focus of all the Planetary Orbit. Though ſtrictly ſpeaking, if we conſider the focus of Mercury's Orbit to be in the Sun's center, the focus of Venus's Orbit will be in the common center of gravity of the Sun and Mercury; the focus of the Earth's Orbit in the common center of gravity of the Sun, Mercury, and Venus; the focus of the Orbit of Mars in the common center of gravity of the Sun, Mercury, Venus, and the Earth; and ſo of the reſt. Yet, the focuſes of the Orbits of all the Planets, except Saturn, will not be ſenſibly removed from the center of the Sun; nor will the focus of Saturn's Orbit recede ſenſibly from the common center of gravity of the Sun and Jupiter.

PLATE I.

ſmall motion round the center of gravity of the Syſtem. All the Planets, as ſeen from him, move the ſame way, and according to the order of Signs in the graduated Circle ♈ ♉ ♊ ♋ &c. which repreſents the great Ecliptic in the Heavens: but, as ſeen from any one Planet, the reſt appear ſometimes to go backward, ſometimes forward, and ſometimes to ſtand ſtill; not in circles nor ellipſes, but in * looped curves which never return into themſelves. The Comets come from all parts of the Heavens, and move in all ſorts of directions.

The Axes of the Planets, what.

19. Having mentioned the Sun's turning round his axis, and as there will be frequent occaſion to ſpeak of the like motion of the Earth and other Planets, it is proper here to inform the young *Tyro* in Aſtronomy, that neither the Sun nor Planets have material axes to turn upon, and ſupport them, as in the little imperfect Machines contrived to repreſent them. For the axis of a Planet is a line conceived to be drawn through it's center, about which it revolves as on a real axis. The extremities of this line, terminating in oppoſite points of the Planet's ſurface, are called it's *Poles*. That which points towards the *northern* part of the Heavens, is called the *North Pole*; and the other, pointing towards the *ſouthern* part, is called the *South Pole*. A bowl whirled from one's hand into the open air turns round ſuch a line within itſelf, whilſt it moves forward; and ſuch are the lines we mean, when we ſpeak of the Axes of the Heavenly bodies.

Their Orbits are not in the ſame plane with the Ecliptic.

20. Let us ſuppoſe the Earth's Orbit to be a thin, even, ſolid plane; cutting the Sun through the center, and extended out as far as the Starry Heavens, where it will mark the great Circle called the *Ecliptic*. This Circle we ſuppoſe to be divided into 12 equal parts, called *Signs*; each Sign into 30 equal parts, called *Degrees*; each Degree into 60 equal parts, called *Minutes*; and every Minute

---

* As repreſented in Plate III. Fig. I. and deſcribed § 138.

into

PLATE I.

into 60 equal parts, called *Seconds*: ſo that a Second is the 60th part of a Minute; a Minute the 60th part of a Degree; and a Degree the 360th part of a Circle, or 30th part of a Sign. The Planes of the Orbits of all the other Planets likewiſe cut the Sun in halves; but extended to the Heavens, form Circles different from one another, and from the Ecliptic; one half of each being on the north ſide, and the other on the ſouth ſide of it. Conſequently the Orbit of each Planet croſſes the Ecliptic in two oppoſite points, which are called the Planet's *Nodes*. Theſe Nodes are all in different parts of the Ecliptic; and therefore, if the planetary Tracks remained viſible in the Heavens, they would in ſome meaſure reſemble the different ruts of waggon-wheels croſſing one another in different parts, but never going far aſunder. That Node, or Interſection of the Orbit of any Planet with the Earth's Orbit, from which the Planet aſcends northward above the Ecliptic, is called the *Aſcending Node* of the Planet; and the other, which is directly oppoſite thereto, is called it's *Deſcending Node*. Saturn's Aſcending Node is in 21 deg. 13 min. of Cancer ♋, Jupiter's in 7 deg. 29 min. of the ſame Sign, Mars's in 17 deg. 17 min. of Taurus ♉, Venus's in 13 deg. 59 min. of Gemini ♊, and Mercury's in 14 deg. 43 min. of Taurus. Here we conſider the Earth's Orbit as the ſtandard, and the Orbits of all the other Planets as oblique to it.

Their Nodes.

Where ſituated.

The Planets Orbits, what.

21. When we ſpeak of the Planets Orbits, all that is meant is their Paths through the open and unreſiſting Space in which they move; and are kept in, by the attractive power of the Sun, and the projectile force impreſſed upon them at firſt: between which power and force there is ſo exact an adjuſtment, that they continue in the ſame tracks without any ſolid Orbits to confine them.

Mercury, Fig. I.

22. Mercury, the neareſt Planet to the Sun, goes round him (as in the circle marked ☿) in 87 days

PLATE I. days 23 hours of our time nearly; which is the length of his year. But, being ſeldom ſeen, and no ſpots appearing on his ſurface or diſc, the time of his rotation on his axis, or the length of his days and nights, is as yet unknown. His diſtance from the Sun is computed to be 32 millions of miles, and his diameter 2600. In his courſe, round the Sun, he moves at the rate of 95 thouſand miles every hour. His light and heat from the Sun are almoſt ſeven times as great as ours; and the Sun appears to him almoſt ſeven times as large as to us. The great heat on this Planet is no argument againſt it's being inhabited; ſince the Almighty could as eaſily ſuit the bodies and conſtitutions of it's inhabitants to the heat of their dwelling, as he has done ours to the temperature of our Earth. And it is very probable that the people there have ſuch an opinion of us, as we have of the inhabitants of Jupiter and Saturn; namely, that we muſt be intolerably cold, and have very little light at ſo great a diſtance from the Sun.

May be inhabited.

Has like phaſes with the Moon.

23. This Planet appears to us with all the various phaſes of the Moon, when viewed at different times by a good teleſcope; ſave only that he never appears quite Full, becauſe his enlightened ſide is never turned directly towards us but when he is ſo near the Sun as to be loſt to our ſight in it's beams. And, as his enlightened ſide is always toward the Sun, it is plain that he ſhines not by any light of his own; for if he did, he would conſtantly appear round. That he moves about the Sun in an Orbit within the Earth's Orbit is alſo plain (as will be more largely ſhewn by and by, § 141, *& ſeq.*) becauſe he is never ſeen oppoſite to the Sun, nor above 56 times the Sun's breadth from his center.

His Orbit and Nodes.

24. His Orbit is inclined ſeven degrees to the Ecliptic; and *that* Node, § 20, from which he aſcends northward above the Ecliptic, is in the

14th degree of Taurus; the oppoſite, in the 14th degree of Scorpio. The Earth is in theſe points on the 6th of *November* and 4th of *May*, new ſtyle; and when Mercury comes to either of his Nodes at his * inferior Conjunction about theſe times, he will appear to paſs over the diſc or face of the Sun, like a dark round ſpot. But in all other parts of his Orbit his Conjunctions are inviſible, becauſe he either goes above or below the Sun.

When he will be ſeen as if upon the Sun.

25. Mr. Whiston has given us an account of ſeveral periods at which Mercury may be ſeen on the Sun's diſc, *viz.* In the year 1782, *Nov.* 12th, at 3 h. 44 m. in the afternoon: 1786, *May* 4th, at 6 h. 57 m. in the forenoon: 1789, *Dec.* 6th, at 3 h. 55 m. in the afternoon; and 1799, *May* 7th, at 2 h. 34 m. in the afternoon. There will be ſeveral intermediate Tranſits, but none of them viſible at *London*.

Venus.

Fig. I.

26. Venus, the next Planet in order, is computed to be 59 millions of miles from the Sun; and by moving at the rate of 69 thouſand miles every hour in her Orbit (as in the circle marked ♀), ſhe goes round the Sun in 224 days 17 hours of our time nearly; in which, though it be the full length of her year, ſhe has only 9¼ days, according to Bianchini's obſervations; ſo that in her, every day and night together is as long as 24⅓ days and nights with us. This odd quarter of a day in every year makes every fourth year a leap-year to Venus; as the like does to our Earth. Her diameter is 7906 miles; and by her diurnal motion the inhabitants about her Equator are carried 43 miles every hour, beſides the 69,000 above-mentioned.

Her Orbit lies between the Earth and Mercury.

27. Her Orbit includes that of Mercury within it; for at her greateſt Elongation, or apparent diſtance from the Sun, ſhe is 96 times his breadth

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* When he is between the Earth and the Sun in the nearer part of his Orbit.

from his center; which is almoſt double of Mercury's. Her Orbit is included by the Earth's; for if it were not, ſhe might be ſeen as often in Oppoſition to the Sun, as ſhe is in Conjunction with him; but ſhe was never ſeen 90 degrees, or a fourth part of a Circle, from the Sun.

She is our morning and evening Star by turns.

28. When Venus appears weſt of the Sun, ſhe riſes before him in the morning, and is called the *Morning Star*: when ſhe appears eaſt of the Sun, ſhe ſhines in the evening after he ſets, and is then called the *Evening Star*: being each in it's turn for 290 days. It may perhaps be ſurpriſing at firſt, that Venus ſhould keep longer on the eaſt or weſt of the Sun, than the whole time of her Period round him. But the difficulty vaniſhes when we conſider that the Earth is all the while going round the Sun the ſame way, though not ſo quick as Venus: and therefore her relative motion to the Earth muſt in every Period be as much ſlower than her abſolute motion in her Orbit, as the Earth during that time advances forward in the Ecliptic; which is 220 degrees. To us ſhe appears through a teleſcope in all the various ſhapes of the Moon.

29. The Axis of Venus is inclined 75 degrees to the Axis of her Orbit; which is 51½ degrees more than our Earth's Axis is inclined to the Axis of the Ecliptic: and therefore her ſeaſons vary much more than ours do. The North Pole of her Axis inclines toward the 20th degree of Aquarius, our Earth's to the beginning of Cancer; conſequently the northern parts of Venus have ſummer in the Signs where thoſe of our Earth have winter, and *vice verſâ*.

Remarkable appearances.

30. The * artificial day at each Pole of Venus is as long as 112½ † natural days on our Earth.

Her Tropics and polar Circles, how ſituated.

31. The Sun's greateſt Declination on each ſide of her Equator amounts to 75 degrees; therefore

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* The time between the Sun's riſing and ſetting.

† One entire revolution, or 24 hours.

her * Tropics are only 15 degrees from her Poles; and her † Polar Circles as far from her Equator. Conſequently, the Tropics of Venus are between her Polar Circles and her Poles; contrary to what thoſe of our Earth are.

The Sun's daily Courſe,

32. As her annual Revolution contains only $9\frac{1}{4}$ of her days, the Sun will always appear to go through a whole Sign, or twelfth Part of her Orbit, in little more than three quarters of her natural day, or nearly in $18\frac{3}{4}$ of our days and nights.

and great Declination.

33. Becauſe her day is ſo great a part of her year, the Sun changes his Declination in one day ſo much, that if he paſſes vertically, or directly over head of any given place on the Tropic, the next day he will be 26 degrees from it: and whatever place he paſſes vertically over when in the Equator, one day's revolution will remove him $36\frac{1}{4}$ degrees from it. So that the Sun changes his Declination every day in Venus about 14 degrees more at a mean rate, than he does in a quarter of a year on our Earth. This appears to be providentially ordered, for preventing the too great effects of the Sun's heat (which is twice as great on Venus as on the Earth) ſo that he cannot ſhine perpendicularly on the ſame places for two days together; and by that means, the heated places have time to cool.

To determine the points of the Compaſs at her Poles.

34. If the inhabitants about the North Pole of Venus fix their South, or Meridian Line, through that part of the Heavens where the Sun comes to his greateſt Height, or North Declination, and call thoſe

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* Theſe are leſſer circles parallel to the Equator, and as many degrees from it, towards the Poles, as the Axis of the Planet is inclined to the Axis of it's Orbit. When the Sun is advanced ſo far north or ſouth of the Equator, as to be directly over either Tropic, he goes no farther; but returns towards the other.

† Theſe are leſſer circles round the Poles, and as far from them as the Tropics are from the Equator. The Poles are the very north and ſouth points of the Planet.

thoſe the Eaſt and Weſt points of their Horizon; which are 90 degrees on each ſide from that point where the Horizon is cut by the Meridian Line, theſe inhabitants will have the following remarkables.

Surpriſing appearances at her Poles.

The Sun will riſe 22½ degrees * north of the Eaſt, and going on 112½ degrees, as meaſured on the plane of the † Horizon, he will croſs the Meridian at an altitude of 12½ degrees; then making an entire revolution without ſetting, he will croſs it again at an altitude of 48½ degrees; at the next revolution he will croſs the Meridian as he comes to his greateſt height and declination, at the altitude of 75 degrees; being then only 15 degrees from the Zenith, or that point of the Heavens which is directly over head: and thence he will deſcend in the like ſpiral manner; croſſing the Meridian firſt at the altitude of 48½ degrees; next at the altitude of 12½ degrees; and going on thence 112½ degrees, he will ſet 22½ degrees north of the Weſt; ſo that, after having been 4⅝ revolutions above the Horizon, he deſcends below it to exhibit the like appearances at the South Pole.

35. At each Pole, the Sun continues half a year without ſetting in ſummer, and as long without riſing in winter; conſequently the polar inhabitants of Venus have only one day and one night in the year; as it is at the Poles of our Earth. But the difference between the heat of ſummer and cold of winter, or of mid-day and mid-night, on Venus, is much greater than on the Earth: becauſe in Venus, as the Sun is for half a year together above the Horizon of each Pole in it's turn, ſo he is for a conſiderable part of that time near the Zenith; and during the other half of the year, always below the Horizon, and for a great part of that time at leaſt 70 degrees from it. Whereas, at the

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* A Degree is a 360th part of any Circle. See § 21.

† The Limit of any inhabitant's view, where the Sky ſeems to touch the Planet all round him.

Poles of our Earth, although the Sun is for half a year together above the Horizon; yet he never aſcends above, nor deſcends below it, more than 23½ degrees. When the Sun is in the Equinoctial, or in that Circle which divides the northern half of the Heavens from the ſouthern, he is ſeen with one half of his Diſc above the Horizon of the North Pole, and the other half above the Horizon of the South Pole; ſo that his center is in the Horizon of both Poles: and then deſcending below the Horizon of one, he aſcends gradually above that of the other. Hence, in a year, each Pole has one ſpring, one harveſt, a ſummer as long as them both, and a winter equal in length to the other three ſeaſons.

At her polar Circles. 36. At the Polar Circles of Venus, the ſeaſons are much the ſame as at the Equator, becauſe there are only 15 degrees betwixt them, § 31; only the winters are not quite ſo long, nor the ſummers ſo ſhort: but the four ſeaſons come twice round every year.

At her Tropics. 37. At Venus's Tropics, the Sun continues for about fifteen of our weeks together without ſetting in ſummer; and as long without riſing in winter. Whilſt he is more than 15 degrees from the Equator, he neither riſes to the inhabitants of the one Tropic, nor ſets to thoſe of the other: whereas, at our terreſtrial Tropics, he riſes and ſets every day of the year.

38. At Venus's Tropics, the Seaſons are much the ſame as at her Poles; only the ſummers are a little longer, and the winters a little ſhorter.

At her Equator. 39. At her Equator, the days and nights are always of the ſame length; and yet the diurnal and nocturnal Arches are very different, eſpecially when the Sun's declination is about the greateſt: for then, his meridian altitude may ſometimes be twice as great as his midnight depreſſion, and at other times the reverſe. When the Sun is at his greateſt Declination, either North or South, his rays are as oblique at Venus's Equator, as they are at *London* on the ſhorteſt day of winter. Therefore, at her Equator there are two winters, two ſummers, two ſprings, and two autumns every year. But becauſe the Sun ſtays for ſome time near the Tropics, and paſſes ſo quickly over the Equator, every winter there will be almoſt twice as long as ſummer: the four ſeaſons returning twice in that time, which conſiſts only of $9\frac{1}{4}$ days.

40. Thoſe parts of Venus which lie between the Poles and Tropics, and between the Tropics and Polar Circles, and alſo between the Polar Circles and Equator, partake more or leſs of the Phenomena of theſe Circles, as they are more or leſs diſtant from them.

Great difference of the Sun's amplitude at riſing and ſetting.

41. From the quick change of the Sun's declination it happens, that if he riſes due eaſt on any day, he will not ſet due weſt on that day, as with us; for if the place where he riſes due eaſt be on the Equator, he will ſet on that day almoſt weſt-north-weſt; or about $18\frac{1}{2}$ degrees north of the weſt. But if the place be in 45 degrees north latitude, then on the day that the Sun riſes due eaſt he will ſet north-weſt by weſt, or 33 degrees north of the weſt. And in 62 degrees north latitude, when he riſes in the eaſt, he ſets not in that revolution, but juſt touches the Horizon 10 degrees to the weſt of the north point; and aſcends again, continuing for $3\frac{1}{4}$ revolutions above the Horizon without ſetting. Therefore, no place has the forenoon and afternoon of the ſame day equally long, unleſs it be in the Equator, or at the Poles.

The longitude of places eaſily found in Venus.

42. The Sun's altitude at noon, or any other time of the day, and his amplitude at riſing and ſetting, being very different at places on the ſame parallel of latitude, according to the different longitudes of thoſe places, the longitude will be almoſt as eaſily found on Venus, as the latitude is found on the Earth: which is an advantage we can never enjoy, becauſe the daily change of the Sun's decli-

nation is by much too ſmall for that important purpoſe.

43. On this Planet, where the Sun croſſes the Equator in any year, he will have 9 degrees of declination from that place on the ſame day and hour next year; and will croſs the Equator 90 degrees farther to the weſt; which makes the time of the Equinox a quarter of a day (or about ſix of our days) later every year. Hence, although the ſpiral in which the Sun's motion is performed, be of the ſame ſort every year, yet it will not be the very ſame, becauſe the Sun will not paſs vertically over the ſame places till four annual revolutions are finiſhed.

Her Equinoxes ſhift a quarter of a day forward every year.

44. We may ſuppoſe that the inhabitants of Venus will be careful to add a day to ſome particular part of every fourth year; which will keep the ſame ſeaſons to the ſame days. For, as the great annual change of the Equinoxes and Solſtices ſhifts the ſeaſons a quarter of a day every year, they would be ſhifted through all the days of the year in 36 years. But by means of this intercalary day, every fourth year will be a leap-year; which will bring her time to an even reckoning, and keep her Calender always right.

Every fourth year a leap-year to Venus.

45. Venus's Orbit is inclined $3\frac{1}{2}$ degrees to the Earth's; and croſſes it in the 14th degree of Gemini and of Sagittarius; and therefore, when the Earth is about theſe points of the Ecliptic at the time that Venus is in her inferior conjunction, ſhe will appear like a ſpot on the Sun, and afford a more certain method of finding the diſtances of all the Planets from the Sun, than any other yet known. But theſe appearances happen very ſeldom; and will only be twice viſible at *London* for one hundred and ten years to come. The firſt time will be in the year 1761, *June* the 6th, in the morning; and the ſecond, on the 3d of *June* in the evening. Excepting ſuch Tranſits as theſe, ſhe ſhews the ſame appearances to us regularly

When ſhe will appear on the Sun.

every eight years; her Conjunctions, Elongations, and Times of riſing and ſetting, being very nearly the ſame, on the ſame days, as before.

She may have a Moon, although we cannot ſee it.

46. Venus may have a Satellite or Moon, although it be undiſcovered by us: which will not appear very ſurpriſing, if we conſider how inconveniently we are placed for ſeeing it. For it's enlightened ſide can never be fully turned towards us, but when Venus is beyond the Sun; and then, as Venus appears little bigger than an ordinary Star, her Moon may be too ſmall to be perceived at ſuch a diſtance. When ſhe is between us and the Sun, her full Moon has it's dark ſide towards us; and then we cannot ſee it any more than we can our own Moon at the time of Change. When Venus is at her greateſt Elongation, we have but one half of the enlightened ſide of her Full Moon towards us; and even then it may be too far diſtant to be ſeen by us. But if ſhe has a Moon, it may certainly be ſeen with her upon the Sun, in the year 1761, unleſs it's Orbit be conſiderably inclined to the Ecliptic: for if it ſhould be in conjunction or oppoſition at that time, we can hardly imagine that it moves ſo ſlow as to be hid by Venus all the ſix hours that ſhe will appear on the Sun's Diſc *.

The Earth.

47. The EARTH is the next Planet above Venus in the Syſtem. It is 82 millions of miles from the Sun, and goes round him (as in the circle ⊕) in 365 days 5 hours 49 minutes, from any Equinox or Solſtice to the ſame again: but from any fixed Star to the ſame again, as ſeen from the Sun, in 365 days 6 hours and 9 minutes; the former being the length of the Tropical year, and the latter the length of the Sydereal. It travels at the rate of 58 thouſand miles every hour; which motion, though 120 times ſwifter than that of a cannon-

Fig. I.

It's diurnal and annual motion.

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* The tranſit is over ſince this was wrote, and no Satellite was ſeen with Venus on the Sun's Diſc.

cannon-ball, is little more than half as ſwift as Mercury's motion in his Orbit. The Earth's diameter is 7970 miles; and by turning round it's Axis every 24 hours from Weſt to Eaſt, it cauſes an apparent diurnal motion of all the heavenly Bodies from Eaſt to Weſt. By this rapid motion of the Earth on it's Axis, the inhabitants about the Equator are carried 1042 miles every hour, whilſt thoſe on the parallel of *London* are carried only about 580, beſides the 58 thouſand miles by the annual motion above-mentioned, which is common to all places whatever.

Inclination of it's Axis.

48. The Earth's Axis makes an angle of $23\frac{1}{2}$ degrees with the Axis of it's Orbit; and keeps always the ſame oblique direction; inclining towards the ſame fixed Stars * throughout it's annual courſe; which cauſes the returns of ſpring, ſummer, autumn, and winter; as will be explained at large in the tenth Chapter.

A proof of it's being round.

49. The Earth is round like a globe; as appears, 1. By it's ſhadow in Eclipſes of the Moon; which ſhadow is always bounded by a circular line, § 314. 2. By our ſeeing the maſts of a ſhip whilſt the hull is hid by the convexity of the water. 3. By it's having been ſailed round by many navigators. The hills take off no more from the roundneſs of the Earth in compariſon, than grains of duſt do from the roundneſs of a common Globe.

It's number of ſquare miles.

50. The ſeas and unknown parts of the Earth (by a meaſurement of the beſt Maps) contain 160 million 522 thouſand and 26 ſquare miles; the inhabited parts 38 million 990 thouſand 569: *Europe* 4 million 456 thouſand and 65; *Aſia* 10

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* This is not ſtrictly true, as will appear when we come to treat of the Receſſion of the Equinoctial Points in the Heavens, § 246; which receſſion is equal to the deviation of the Earth's Axis from it's paralleliſm: but this is rather too ſmall to be ſenſible in an age, except to thoſe who make very nice obſervations.

million 768 thouſand 823; *Africa* 9 million 654 thouſand 807; *America* 14 million 110 thouſand 874. In all, 199 million 512 thouſand 595; which is the number of ſquare miles on the whole ſurface of our Globe.

The proportion of land and ſea.

51. Dr. LONG, in the firſt volume of his Aſtronomy, p. 168, mentions an ingenious and eaſy method of finding nearly what proportion the land bears to the ſea; which is, to take the papers of a large terreſtrial globe, and after ſeparating the land from the ſea with a pair of ſciſſars, to weigh them carefully in ſcales. This ſuppoſes the globe to be exactly delineated, and the papers all of equal thickneſs. The Doctor made the experiment on the papers of Mr. SENEX's ſeventeen-inch globe; and found that the ſea papers weighed 349 grains, and the land only 124: by which it appears that almoſt three fourth parts of the ſurface of our Earth between the Polar Circles are covered with water, and that little more than one fourth is dry land. The Doctor omitted weighing all within the Polar Circles; becauſe there is no certain meaſurement of the land within them, ſo as to know what proportion it bears to the ſea.

The Moon.

52. The MOON is not a Planet, but only a Satellite or Attendant of the Earth; going round the Earth from Change to Change in 29 days 12 hours and 44 minutes; and round the Sun with it every year. The Moon's diameter is 2180 miles; and her diſtance from the Earth's center 240 thouſand. She goes round her Orbit in 27 days 7 hours 43 minutes, moving about 2290 miles every hour; and turns round her Axis exactly in the time that ſhe goes round the Earth, which is the reaſon of her keeping always the ſame ſide towards us, and that her day and night taken together is as long as our lunar month.

53. The Moon is an opaque Globe like the Earth, and ſhines only by reflecting the light of

the Sun: therefore whilſt that half of her which is towards the Sun is enlightened, the other half muſt be dark and inviſible. Hence, ſhe diſappears when ſhe comes between us and the Sun; becauſe her dark ſide is then towards us. When ſhe is gone a little way forward, we ſee a little of her enlightened ſide; which ſtill increaſes to our view, as ſhe advances forward, until ſhe comes to be oppoſite to the Sun; and then her whole enlightened ſide is towards the Earth, and ſhe appears with a round, illumined Orb, which we call the *Full Moon*: her dark ſide being then turned away from the Earth. From the Full ſhe ſeems to decreaſe gradually as ſhe goes through the other half of her courſe; ſhewing us leſs and leſs of her enlightened ſide every day, till her next change or conjunction with the Sun, and then ſhe diſappears as before. Her Phaſes.

54. This continual change of the Moon's phaſes demonſtrates that ſhe ſhines not by any light of her own: for if ſhe did, being globular, we ſhould always ſee her with a round full Orb like the Sun. Her Orbit is repreſented in the Scheme by the little circle *m*, upon the Earth's Orbit ⊕: but it is drawn fifty times too large in proportion to the Earth's; and yet is almoſt too ſmall to be ſeen in the Diagram. A proof that ſhe ſhines not by her own light. Fig. I.

55. The Moon has ſcarce any difference of ſeaſons; her Axis being almoſt perpendicular to the Ecliptic. What is very ſingular, one half of her has no darkneſs at all; the Earth conſtantly affording it a ſtrong light in the Sun's abſence; while the other half has a fortnight's darkneſs and a fortnight's light by turns. One half of her always enlightened.

56. Our Earth is a Moon to the Moon, waxing and waneing regularly, but appearing thirteen times as big, and affording her thirteen times as much light, as ſhe does to us. When ſhe changes to us, the Earth appears full to her; and when ſhe is in her firſt quarter to us, the Earth is in it's third quarter to her; and *vice verſâ.* Our Earth is her Moon.

57. But

57. But from one half of the Moon, the Earth is never ſeen at all: from the middle of the other half, it is always ſeen over head; turning round almoſt thirty times as quick as the Moon does. From the circle which limits our view of the Moon, only one half of the Earth's ſide next her is ſeen; the other half being hid below the Horizon of all places on that circle. To her, the Earth ſeems to be the biggeſt body in the Univerſe; for it appears thirteen times as big as ſhe does to us.

A Proof of the Moon's having no Atmoſphere.

58. The Moon has no Atmoſphere of any viſible denſity ſurrounding her as we have: for if ſhe had, we could never ſee her edge ſo well defined as it appears; but there would be a ſort of a miſt or hazineſs around her, which would make the Stars look fainter, when they are ſeen through it. But obſervation proves, that the Stars which diſappear behind the Moon, retain their full luſtre until they ſeem to touch her very edge, and then they vaniſh in a moment. This has been often obſerved by Aſtronomers, but particularly by CASSINI* of the Star γ in the breaſt of Virgo, which appears ſingle and round to the bare eye; but through a refracting Teleſcope of 16 feet appears to be two Stars ſo near together, that the diſtance between them ſeems to be but equal to one of their apparent diameters. The Moon was obſerved to paſs over them on the 21ſt of *April*, 1720, *N. S.* and as her dark edge drew near to them, it cauſed no change in their colour or ſituation. At 25 min. 14 ſec. paſt 12 at night, the moſt weſterly of theſe Stars was hid by the dark edge of the Moon; and in 30 ſeconds afterward, the moſt eaſterly Star was hid: each of them diſappearing behind the Moon in an inſtant, without any preceding diminution of magnitude or brightneſs; which by no means could have been the caſe if there were an Atmoſphere round the Moon; for then, one of the Stars falling obliquely into it before the other, ought by

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* *Memoires d'Acad. ann.* 1720.

refraction to have ſuffered ſome change in it's colour, or in it's diſtance from the other Star which was not yet entered into the Atmoſphere. But no ſuch alteration could be perceived, though the obſervation was performed with the utmoſt attention to that particular; and was very proper to have made ſuch a diſcovery. The faint light, which has been ſeen all round the Moon, in total Eclipſes of the Sun, has been obſerved, during the time of darkneſs, to have it's center coincident with the center of the Sun; and was therefore much more likely to ariſe from the Atmoſphere of the Sun, than from that of the Moon; for if it had been owing to the latter, it's center would have gone along with the Moon's.

Nor Seas.

59. If there were ſeas in the Moon, ſhe could have no clouds, rains, nor ſtorms, as we have; becauſe ſhe has no ſuch Atmoſphere to ſupport the vapours which occaſion them. And every one knows, that when the Moon is above our Horizon in the night-time, ſhe is viſible, unleſs the clouds of our Atmoſphere hide her from our view; and all parts of her appear conſtantly with the ſame clear, ſerene, and calm aſpect. But thoſe dark parts of the Moon, which were formerly thought to be ſeas, are now found to be only vaſt deep cavities, and places which reflect not the Sun's light ſo ſtrongly as others, having many caverns and pits whoſe ſhadows fall within them, and are always dark on the ſides next the Sun; which demonſtrates their being hollow: and moſt of theſe pits have little knobs like hillocks ſtanding within them, and caſting ſhadows alſo; which cauſe theſe places to appear darker than others which have fewer, or leſs remarkable caverns. All theſe appearances ſhew that there are no ſeas in the Moon; for if there were any, their ſurfaces would appear ſmooth and even, like thoſe on the Earth.

She is full of caverns and deep pits.

The Stars always viſible to the Moon.

60. There being no Atmoſphere about the Moon, the heavens in the day-time have the ap-

pearance of night to a Lunarian who turns his back toward the Sun; and when he does, the Stars appear as bright to him as they do in the night to us. For, it is entirely owing to our Atmoſphere that the Heavens are bright about us in the day.

The Earth a Dial to the Moon.

61. As the Earth turns round it's Axis, the ſeveral continents, ſeas, and iſlands appear to the Moon's inhabitants like ſo many ſpots of different forms and brightneſs, moving over it's ſurface; but much fainter at ſome times than others, as our clouds cover them or leave them. By theſe ſpots the Lunarians can determine the time of the Earth's diurnal motion, juſt as we do the motion of the Sun: and perhaps they meaſure their time by the motion of the Earth's ſpots; for they cannot have a truer dial.

How the Lunarians may know the length of their year,

62. The Moon's Axis is ſo nearly perpendicular to the Ecliptic, that the Sun never removes ſenſibly from her Equator: and the * obliquity of her Orbit, which is next to nothing as ſeen from the Sun, cannot cauſe the Sun to decline ſenſibly from her Equator. Yet her inhabitants are not deſtitute of means for aſcertaining the length of their year, though their method and ours muſt differ. For we can know the length of our year by the return of our Equinoxes; but the Lunarians, having always equal day and night, muſt have recourſe to another method; and we may ſuppoſe, they meaſure their year by obſerving when either of the Poles of our Earth begins to be enlightened, and the other to diſappear, which is always at our Equinoxes; they being conveniently ſituated for obſerving great tracks of land about our Earth's Poles, which are entirely unknown to us. Hence we may conclude, that the year is of the ſame abſolute length both to the

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* The Moon's Orbit croſſes the Ecliptic in two oppoſite points, called the Moon's Nodes; ſo that one half of her Orbit is above the Ecliptic, and the other half below it. The Angle of it's Obliquity is $5\frac{1}{3}$ degrees.

Earth

PLATE I.

Earth and Moon, though very different as to the number of days: we having $365\frac{1}{4}$ natural days, and the Lunarians only $12\frac{7}{19}$; every day and night in the Moon being as long as $29\frac{1}{2}$ on the Earth.

and the longitudes of their places.

63. The Moon's inhabitants on the ſide next the Earth may as eaſily find the longitude of their places as we can find the latitude of ours. For the Earth keeping conſtantly, or very nearly ſo, over one Meridian of the Moon, the eaſt or weſt diſtances of places from that Meridian are as eaſily found, as we can find our diſtance from the Equator by the Altitude of our celeſtial Poles.

Mars.

64. The Planet MARS is next in order, being the firſt above the Earth's Orbit. His diſtance from the Sun is computed to be 125 millions of miles; and by travelling at the rate of 47 thouſand miles every hour, as in the circle ♂, he goes round the Sun in 686 of our days and 23 hours; which is the length of his year, and contains $667\frac{3}{4}$ of his days; every day and night together being 40 minutes longer than with us. His diameter is 4444 miles, and by his diurnal rotation the inhabitants about his Equator are carried 556 miles every hour. His quantity of light and heat is equal but to one half of ours; and the Sun appears but half as big to him as to us.

Fig. I.

65. This Planet being but a fifth part ſo big as the Earth, if any Moon attends him, ſhe muſt be very ſmall, and has not yet been diſcovered by our beſt teleſcopes. He is of a fiery red colour, and by his Appulſes to ſome of the fixed Stars, ſeems to be encompaſſed by a very groſs Atmoſphere. He appears ſometimes gibbous, but never horned; which both ſhews that his Orbit includes the Earth's within it, and that he ſhines not by his own light.

His Atmoſphere and Phaſes.

66. To Mars, our Earth and Moon appear like two Moons, a bigger and a leſs; changing places with one another, and appearing ſometimes

horned, ſometimes half or three quarters illuminated, but never full; nor at moſt above one quarter of a degree from each other, although they are 240 thouſand miles aſunder.

How the other Planets appear to Mars.

67. Our Earth appears almoſt as big to Mars as Venus does to us, and at Mars it is never ſeen above 48 degrees from the Sun; ſometimes it appears to paſs over the Diſc of the Sun, and ſo do Mercury and Venus: but Mercury can never be ſeen from Mars by ſuch eyes as ours, unaſſiſted by proper inſtruments; and Venus will be as ſeldom ſeen as we ſee Mercury. Jupiter and Saturn are as viſible to Mars as to us. His Axis is perpendicular to the Ecliptic, and his Orbit is 2 degrees inclined to it.

Jupiter.

68. JUPITER, the biggeſt of all the Planets, is ſtill higher in the Syſtem, being about 426 millions of miles from the Sun: and going at the rate of 25 thouſand miles every hour in his Orbit, as in the circle ♃, finiſhes his annual period in eleven of our years 314 days and 12 hours. He is above 1000 times as big as the Earth, for his diameter is 81,000 miles; which is more than ten times the diameter of the Earth.

Fig. I.

The number of days in his year.

69. Jupiter turns round his Axis in 9 hours 56 minutes; ſo that his year contains 10 thouſand 470 days; and the diurnal velocity of his equatoreal parts is greater than the ſwiftneſs with which he moves in his annual Orbit; a ſingular circumſtance, as far as we know. By this prodigious quick Rotation, his equatoreal inhabitants are carried 25 thouſand 920 miles every hour (which is 920 miles an hour more than an inhabitant of our Earth's equator moves in twenty-four hours) beſides the 25 thouſand above-mentioned, which is common to all parts of his ſurface, by his annual motion.

His Belts and ſpots.

70. Jupiter is ſurrounded by faint ſubſtances, called *Belts*, in which ſo many changes appear,

that they are generally thought to be clouds: for ſome of them have been firſt interrupted and broken, and then have vaniſhed entirely. They have ſometimes been obſerved of different breadths, and afterwards have all become nearly of the ſame breadth. Large ſpots have been ſeen in theſe Belts; and when a Belt vaniſhes, the contiguous ſpots diſappear with it. The broken ends of ſome Belts have been generally obſerved to revolve in the ſame time with the ſpots; only thoſe nearer the Equator in ſomewhat leſs time than thoſe near the Poles; perhaps on account of the Sun's greater heat near the Equator, which is parallel to the Belts and courſe of the ſpots. Several large ſpots, which appear round at one time, grow oblong by degrees, and then divide into two or three round ſpots. The periodical time of the ſpots near the Equator is 9 hours 50 minutes, but of thoſe near the Poles 9 hours 56 minutes. *See Dr.* SMITH'*s Optics*, § 1004, *& ſeq.*

He has no change of ſeaſons;

71. The Axis of Jupiter is ſo nearly perpendicular to his Orbit, that he has no ſenſible change of ſeaſons; which is a great advantage, and wiſely ordered by the Author of Nature. For, if the Axis of this Planet were inclined any conſiderable number of degrees, juſt ſo many degrees round each Pole would in their turn be almoſt ſix of our years together in darkneſs. And, as each degree of a great Circle on Jupiter contains 706 of our miles at a mean rate, it is eaſy to judge what vaſt tracts of land would be rendered uninhabitable by any conſiderable inclination of his Axis.

but has four Moons.

72. The Sun appears but $\frac{1}{28}$ part ſo big to Jupiter as to us; and his light and heat are in the ſame ſmall proportion, but compenſated by the quick returns thereof, and by four Moons (ſome bigger and ſome leſs than our Earth) which revolve about him: ſo that there is ſcarce any part of this huge Planet but what is during the whole night enlightened by one or more of theſe Moons,

except his Poles, whence only the fartheſt Moons can be ſeen, and where their light is not wanted, becauſe the Sun conſtantly circulates in or near the Horizon, and is very probably kept in view of both Poles by the refraction of Jupiter's Atmoſphere, which, if it be like ours, has certainly refractive power enough for that purpoſe.

Their periods round Jupiter.

73. The Orbits of theſe Moons are repreſented in the Scheme of the Solar Syſtem by four ſmall circles marked 1. 2. 3. 4. on Jupiter's Orbit ♃; but they are drawn fifty times too large in proportion to it. The firſt Moon, or that neareſt to Jupiter, goes round him in 1 day 18 hours and 36 minutes of our time; and is 229 thouſand miles diſtant from his center: The ſecond performs it's revolution in three days 13 hours and 15 minutes, at 364 thouſand miles diſtance: The third in 7 days three hours and 59 minutes, at the diſtance of 580 thouſand miles: And the fourth, or outermoſt, in 16 days 18 hours and 30 minutes, at the diſtance of one million of miles from his center.

Parallax of their Orbits, and diſtances from Jupiter.

74. The Angles under which the Orbits of Jupiter's Moons are ſeen from the Earth, as it's mean diſtance from Jupiter, are as follow: The firſt, 3′ 55″; the ſecond, 6′ 14″; the third, 9′ 58″; and the fourth, 17′ 30″. And their diſtances from Jupiter, meaſured by his ſemidiameters, are thus: The firſt, $5\frac{2}{3}$; the ſecond, 9; the third, $14\frac{23}{60}$; and the fourth, $25\frac{18}{60}$*. This Planet, ſeen from it's neareſt Moon, appears 1000 times as large as our Moon does to us; waxing and waneing in all her monthly ſhapes, every $42\frac{1}{2}$ hours.

How he appears to his neareſt Moon.

Two grand diſcoveries made by the Eclipſe of Jupiter's Moons.

75. Jupiter's three neareſt Moons fall into his ſhadow, and are eclipſed in every Revolution: but the Orbit of the fourth Moon is ſo much inclined, that it paſſeth by it's oppoſition to Jupiter, without falling into his ſhadow, two years in every ſix. By theſe Eclipſes, Aſtronomers have not only diſ-

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* CASSINI *Elements d'Aſtronomie, Liv.* ix. *Chap.* 3.

covered that the Sun's light takes up eight minutes of time in coming to us; but they have alſo determined the longitudes of places on this Earth with greater certainty and facility, than by any other method yet known; as ſhall be explained in the eleventh Chapter.

PLATE I.

The great difference between the Equatoreal and Polar diameters of Jupiter.

76. The difference between the Equatoreal and Polar diameters of Jupiter is 6230 miles; for his equatoreal diameter is to his polar, as 13 to 12. So that his Poles are 3115 miles nearer his center than his Equator is. This reſults from his quick motion round his Axis; for the fluids, together with the light particles, which they can carry or waſh away with them, recede from the Poles which are at reſt, towards the Equator where the motion is quickeſt, until there be a ſufficient number accumulated to make up the deficiency of gravity loſt by the centrifugal force, which always ariſes from a quick motion round an axis: and when the deficiency of weight or gravity of the particles is made up by a ſufficient accumulation, there is an *equilibrium*, and the equatoreal parts riſe no higher. Our Earth being but a very ſmall Planet compared to Jupiter, and it's motion on it's Axis being much ſlower, it is leſs flattened of courſe; for the difference between it's equatoreal and polar diameters is only as 230 to 229, namely, 35 miles.

The difference little in thoſe of our Earth.

77. Jupiter's Orbit is 1 degree 20 minutes inclined to the Ecliptic. His North Node is in the 7th degree of Cancer, and his South Node in the 7th degree of Capricorn.

Place of his Nodes.

78. Saturn, the remoteſt of all the Planets, is about 780 millions of miles from the Sun; and, travelling at the rate of 18 thouſand miles every hour, as in the circle marked ♄, performs it's annual circuit in 29 years 167 days and 5 hours of our time; which makes only one year to that Planet. It's diameter is 67,000 miles; and therefore it is near 600 times as big as the Earth.

Saturn.

Fig. I.

79. This

PLATE I. Fig. V. His Ring. 79. This Planet is ſurrounded by a thin broad Ring, as an artificial Globe is by a Horizon. The Ring appears double when ſeen through a good teleſcope, and is repreſented by the figure in ſuch an oblique view as it is generally ſeen. It is inclined 30 degrees to the Ecliptic, and is about 21 thouſand miles in breath; which is equal to it's diſtance from Saturn on all ſides. There is reaſon to believe that the Ring turns round it's Axis, becauſe, when it is almoſt edge-wiſe to us, it appears ſomewhat thicker on one ſide of the Planet than on the other; and the thickeſt edge has been ſeen on different ſides at different times. But Saturn having no viſible ſpots on his body, whereby to determine the time of his turning round his Axis, the length of his days and nights, and the poſition of his Axis, are unknown to us.

80. To Saturn, the Sun appears only $\frac{1}{90}$th part ſo big as to us; and the light and heat he receives from the Sun are in the ſame proportion to ours. His five Moons. But to compenſate for the ſmall quantity of ſunlight, he has five Moons, all going round him on the outſide of his Ring, and nearly in the ſame plane with it. The firſt, or neareſt Moon to Saturn, goes round him in 1 day 21 hours 19 minutes; and is 140 thouſand miles from his center: The ſecond, in 2 days 17 hours 40 minutes; at the diſtance of 187 thouſand miles: The third, in 4 days 12 hours 25 minutes; at 263 thouſand miles diſtance: The fourth, in 15 days 22 hours 41 minutes; at the diſtance of 600 thouſand miles: And the fifth, or outermoſt, at one million 800 thouſand miles from Saturn's center, goes round him in 79 days 7 hours 48 minutes. Their Fig. I. Orbits in the Scheme of the Solar Syſtem are repreſented by the five ſmall circles, marked 1. 2. 3. 4. 5. on Saturn's Orbit; but theſe, like the Orbits of the other Satellites, are drawn fifty times too large in proportion to the Orbits of their Primary Planets.

81. The Sun ſhines almoſt fifteen of our years together on one ſide of Saturn's Ring without ſetting, and as long on the other in it's turn. So that the Ring is viſible to the inhabitants of that Planet for almoſt fifteen of our years, and as long inviſible by turns, if it's Axis has no Inclination to it's Ring: but if the Axis of the Planet be inclined to the Ring, ſuppoſe about 30 degrees, the Ring will appear and diſappear once every natural day to all the inhabitants within 30 degrees of the Equator, on both ſides, frequently eclipſing the Sun in a Saturnian day. Moreover, if Saturn's Axis be ſo inclined to his Ring, it is perpendicular to his Orbit; and thereby the inconvenience of different ſeaſons to that Planet is avoided. For conſidering the length of Saturn's year, which is almoſt equal to thirty of ours, what a dreadful condition muſt the inhabitants of his Polar regions be in, if they be half that time deprived of the light and heat of the Sun? which is not their caſe alone, if the Axis of the Planet be perpendicular to the Ring, for then the Ring muſt hide the Sun from vaſt tracks of land on each ſide of the Equator for 13 or 14 of our years together, on the ſouth ſide and north ſide by turns, as the Axis inclines to or from the Sun: the reverſe of which inconvenience is another good preſumptive proof of the Inclination of Saturn's Axis to it's Ring, and alſo of his Axis being perpendicular to his Orbit.

His Axis probably inclined to his Ring.

82. This Ring, ſeen from Saturn, appears like a vaſt luminous Arch in the Heavens, as if it did not belong to the Planet. When we ſee the Ring moſt open, it's ſhadow upon the Planet is broadeſt; and from that time the ſhadow grows narrower, as the Ring appears to do to us; until, by Saturn's annual motion, the Sun comes to the plane of the Ring, or even with it's edge; which being then directed towards us, becomes inviſible on account of it's thinneſs; as ſhall be explained more largely in

How the Ring appears to Saturn and to us.

In what Signs Saturn appears to loſe his Ring; and in what Signs it appears moſt open to us.

in the tenth Chapter, and illuſtrated by a figure. The Ring diſappears twice in every annual Revolution of Saturn, namely, when he is in the 19th degree both of Piſces and of Virgo. And when Saturn is in the middle between theſe points, or in the 19th degree either of Gemini or of Sagittarius, his Ring appears moſt open to us; and then it's longeſt diameter is to it's ſhorteſt, as 9 to 4.

No Planet but Saturn can be ſeen from Jupiter; nor any from Jupiter beſides Saturn.

83. To ſuch Eyes as ours, unaſſiſted by inſtruments, Jupiter is the only Planet that can be ſeen from Saturn; and Saturn the only Planet that can be ſeen from Jupiter. So that the inhabitants of theſe two Planets muſt either ſee much farther than we do, or have equally good inſtruments to carry their ſight to remote objects, if they know that there is ſuch a body as our Earth in the Univerſe: for the Earth is no bigger ſeen from Jupiter, than his Moons are ſeen from the Earth; and if his large body had not firſt attracted our ſight, and prompted our curioſity to view him with the teleſcope, we ſhould never have known any thing of his Moons; unleſs by chance we had directed the teleſcope toward that ſmall part of the Heavens where they were at the time of obſervation. And the like is true of the Moons of Saturn.

Place of Saturn's Nodes.

84. The Orbit of Saturn is $2\frac{1}{2}$ degrees inclined to the Ecliptic, or Orbit of our Earth, and interſects it in the 21ſt degree of Cancer and of Capricorn; ſo that Saturn's Nodes are only 14 degrees from Jupiter's, § 77.

The Sun's light much ſtronger on Jupiter and Saturn than is generally believed.

85. The quantity of light, afforded by the Sun to Jupiter, being but $\frac{1}{28}$th part, and to Saturn only $\frac{1}{90}$th part, of what we enjoy; may at firſt thought induce us to believe that theſe two Planets are entirely unfit for rational beings to dwell upon. But, that their light is not ſo weak as we imagine, is evident from their brightneſs in the night-time; and alſo from this remarkable Phenomenon, that when the Sun is ſo much eclipſed to us, as to have

only the 40th part of his diſc left uncovered by the Moon, the decreaſe of light is not very ſenſible: and juſt at the end of darkneſs in Total Eclipſes, when his weſtern limb begins to be viſible, and ſeems no bigger than a bit of fine ſilver wire, every one is ſurpriſed at the brightneſs wherewith that ſmall part of him ſhines. The Moon when Full affords travellers light enough to keep them from miſtaking their way; and yet, according to Dr. SMITH*, it is equal to no more than a 90 thouſandth part of the light of the Sun: that is, the Sun's light is 90 thouſand times as ſtrong as the light of the Moon when Full. Conſequently, the Sun gives a thouſand times as much light to Saturn as the Full Moon does to us; and above three thouſand times as much to Jupiter. So that theſe two Planets, even without any Moons, would be much more enlightened than we at firſt imagine; and by having ſo many, they may be very comfortable places of reſidence. Their heat, ſo far as it depends on the force of the Sun's rays, is certainly much leſs than ours; to which no doubt the bodies of their inhabitants are as well adapted as ours are to the ſeaſons we enjoy. And if we conſider, that Jupiter never has any winter, even at his Poles; which probably is alſo the caſe with Saturn, the cold cannot be ſo intenſe on theſe two Planets as is generally imagined. Beſides, there may be ſomething in their nature or ſoil much warmer than in that of our Earth: and we find that all our heat depends not on the rays of the Sun; for if it did, we ſhould always have the ſame months equally hot or cold at their annual returns. But it is far otherwiſe, for *February* is ſometimes warmer than *May*; which muſt be owing to vapours and exhalations from the Earth.

All our heat depends not on the Sun's rays.

86. Every perſon who looks upon, and compares the Syſtems of Moons together, which belong to

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* Optics, Art. 95.

Jupiter and Saturn, muſt be amazed at the vaſt magnitude of theſe two Planets, and the noble attendance they have in reſpect of our little Earth: and can never bring himſelf to think, that an infinitely wiſe Creator ſhould diſpoſe of all his animals and vegetables here, leaving the other Planets bare and deſtitute of rational creatures. To ſuppoſe that he had any view to our benefit, in creating theſe Moons and giving them their motions round Jupiter and Saturn; to imagine that he intended theſe vaſt Bodies for any advantage to us, when he well knew that they could never be ſeen but by a few Aſtronomers peeping through teleſcopes; and that he gave to the Planets regular returns of days and nights, and different ſeaſons to all where they would be convenient; but of no manner of ſervice to us, except only what immediately regards our own Planet the Earth; to imagine, I ſay, that he did all this on our account, would be charging him impiouſly with having done much in vain: and as abſurd, as to imagine that he has created a little Sun and a Planetary Syſtem within the Shell of our Earth, and intended them for our uſe. Theſe conſiderations amount to little leſs than a poſitive proof, that all the Planets are inhabited: for if they are not, why all this care in furniſhing them with ſo many Moons, to ſupply thoſe with light which are at the greater diſtances from the Sun? Do we not ſee, that the farther a Planet is from the Sun, the greater Apparatus it has for that purpoſe? ſave only Mars, which being but a ſmall Planet, may have Moons too ſmall to be ſeen by us. We know that the Earth goes round the Sun, and turns round it's own Axis, to produce the viciſſitudes of ſummer and winter by the former, and of day and night by the latter motion, for the benefit of it's inhabitants. May we not then fairly conclude, by parity of reaſon, that the end and deſign of all the other Planets, is the ſame? and is not this agreeable to the beautiful

It is highly probable that all the Planets are inhabited.

PLATE I.

harmony which exiſts throughout the Univerſe? Surely it is: and raiſes in us the moſt magnificent ideas of the SUPREME BEING, who is every where, and at all times preſent; diſplaying his power, wiſdom and goodneſs, among all his creatures! and diſtributing happineſs to innumerable ranks of various beings!

Fig. II. How the Sun appears to the different Planets.

87. In Fig. 2d, we have a view of the proportional breadth of the Sun's face or diſc, as ſeen from the different Planets. The Sun is repreſented N° 1, as ſeen from Mercury; N° 2, as ſeen from Venus; N° 3, as ſeen from the Earth; N° 4, as ſeen from Mars; N° 5, as ſeen from Jupiter; and N° 6, as ſeen from Saturn.

Fig. III. Fig. IV.

Let the circle *B* be the Sun as ſeen from any Planet, at a given diſtance; to another Planet, at double that diſtance, the Sun will appear juſt of half that breadth, as *A*; which contains only one fourth part of the area, or ſurface of *B*. For, all circles, as well as ſquare ſurfaces, are to one another, as the ſquares of their diameters. Thus, the ſquare *A* is juſt half as broad as the ſquare *B*; and yet it is plain to ſight, that *B* contains four times as much ſurface as *A*. Hence, by comparing the diameters of the above Circles (Fig. II.) together, it will be found, that in round numbers, the Sun appears 7 times larger to Mercury than to us, 90 times larger to us than to Saturn, and 630 times as large to Mercury as to Saturn.

Fig. V. Proportional bulks and diſtances of the Planets.

88. In Fig. 5th, we have a view of the bulks of the Planets in proportion to each other, and to a ſuppoſed globe of two feet diameter for the Sun. The Earth is 27 times as big as Mercury, very little bigger than Venus, 5 times as big as Mars; but Jupiter is 1049 times as big as the Earth, Saturn 586 times as big, excluſive of his Ring; and the Sun is 877 thouſand 650 times as big as the Earth. If the Planets in this Figure were ſet at their due diſtances from a Sun of two feet diameter,

PLATE I. according to their proportional bulks, as in our Syſtem, Mercury would be 28 yards from the Sun's center; Venus 51 yards 1 foot; the Earth 70 yards 2 feet; Mars 107 yards 2 feet; Jupiter 370 yards 2 feet; and Saturn 760 yards 2 feet. The Comet of the year 1680, at it's greateſt diſtance, 10 thouſand 760 yards. In this proportion, the Moon's diſtance from the center of the Earth would be only $7\frac{1}{2}$ inches.

An idea of their diſtances. 89. To aſſiſt the imagination in forming an idea of the vaſt diſtances of the Sun, Planets, and Stars, let us ſuppoſe, that a body projected from the Sun ſhould continue to fly with the ſwiftneſs of a cannon-ball; *i. e.* 480 miles every hour; this body would reach the Orbit of Mercury, in 7 years 221 days; of Venus, in 14 years 8 days; of the Earth, in 19 years 91 days; of Mars, in 29 years 85 days; of Jupiter, in 100 years 280 days; of Saturn, in 184 years 240 days; to the Comet of 1680, at it's greateſt diſtance from the Sun, in 2660 years; and to the neareſt fixed Stars in about 7 million 600 thouſand years.

Why the Planets appear bigger and leſs at different times. 90. As the Earth is not the center of the Orbits in which the Planets move, they come nearer to it and go farther from it, and at different times; on which account they appear bigger and leſs by turns. Hence, the apparent magnitudes of the Planets are not always a certain rule to know them by.

Fig. I. 91. Under Fig. 3, are the names and characters of the twelve Signs of the Zodiac, which the Reader ſhould be perfectly well acquainted with; ſo as to know the characters without ſeeing the names. Every Sign contains 30 degrees, as in the Circle bounding the Solar Syſtem; to which the characters of the Signs are ſet in their proper places.

The Comets. 92. The Comets are ſolid opaque bodies, with long tranſparent trains or tails, iſſuing from that ſide which is turned away from the Sun. They move about the Sun, in very excentric ellipſes; and are

PLATE I.

are of a much greater denſity than the Earth; for ſome of them are heated in every period to ſuch a degree, as would vitrify or diſſipate any ſubſtance known to us. Sir ISAAC NEWTON computed the heat of the Comet which appeared in the year 1680, when neareſt the Sun, to be 2000 times hotter than red-hot iron, and that being thus heated, it muſt retain it's heat until it comes round again, although it's Period ſhould be more than twenty thouſand years; and it is computed to be only 575. The method of computing the heat of bodies, keeping at any known diſtance from the Sun, ſo far as their heat depends on the force of the Sun's rays, is very eaſy; and ſhall be explained in the eighth Chapter.

Fig. I.

They prove that the Orbits of the Planets are not ſolid.

93. Part of the Paths of three Comets are delineated in the Scheme of the Solar Syſtem, and the years marked in which they made their appearance. It is believed, that there are at leaſt 21 Comets belonging to our Syſtem, moving in all ſorts of directions: and all thoſe which have been obſerved, have moved through the ethereal Regions and the Orbits of the Planets without ſuffering the leaſt ſenſible reſiſtance in their motions; which plainly proves that the Planets do not move in ſolid Orbs. Of all the Comets, the Periods of the above-mentioned three only are known with any degree of certainty. The firſt of theſe Comets appeared in the years 1531, 1607, and 1682; and is expected to appear again in the year 1758, and every 75th year afterwards. The ſecond of them appeared in 1532 and 1661, and may be expected to return in 1789, and every 129th year afterwards. The third, having laſt appeared in 1680, and it's Period being no leſs than 575 years, cannot return until the year 2225. This Comet, at it's greateſt diſtance, is about 11 thouſand two hundred millions of miles from the Sun; and at it's leaſt diſtance from the Sun's center, which is 49,000 miles, is within leſs than a thirt part of the Sun's ſemidiameter from

The Periods only of three are known.

his ſurface. In that part of it's Orbit which is neareſt the Sun, it flies with the amazing ſwiftneſs of 880,000 miles in an hour; and the Sun, as ſeen from it, appears an hundred degrees in breadth; conſequently, 40 thouſand times as large as he appears to us. The aſtoniſhing length that this Comet runs out into empty Space, ſuggeſts to our minds an idea of the vaſt diſtance between the Sun and the neareſt fixed Stars; of whoſe Attractions all the Comets muſt keep clear, to return periodically, and go round the Sun; and it ſhews us alſo, that the neareſt Stars, which are probably thoſe that ſeem the largeſt, are as big as our Sun, and of the ſame nature with him; otherwiſe, they could not appear ſo large and bright to us as they do at ſuch an immenſe diſtance.

They prove the Stars to be at immenſe diſtances.

Inferences drawn from the above phenomena.

94. The extreme heat, the denſe atmoſphere, the groſs vapours, the chaotic ſtate of the Comets, ſeem at firſt ſight to indicate them altogether unfit for the purpoſes of animal life, and a moſt miſerable habitation for rational beings; and therefore * ſome are of opinion that they are ſo many hells for tormenting the damned with perpetual viciſſitudes of heat and cold. But when we conſider, on the other hand, the infinite power and goodneſs of the Deity; the latter inclining, the former enabling him to make creatures ſuited to all ſtates and circumſtances; that matter exiſts only for the ſake of intelligent beings; and that wherever we find it, we always find it pregnant with life, or neceſſarily ſubſervient thereto; the numberleſs ſpecies, the aſtoniſhing diverſity of animals in earth, air, water, and even on other animals; every blade of graſs, every tender leaf, every natural fluid, ſwarming with life; and every one of theſe enjoying ſuch gratifications as the nature and ſtate of each requires: when we reflect moreover that ſome centuries ago, till experience undeceived us, a great part of the Earth was judged uninhabitable; the Torid

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* Mr. WHISTON, in his Aſtronomical Principles of Religion.

Zone by reaſon of exceſſive heat, and the two Frigid Zones becauſe of their intolerable cold; it ſeems highly probable, that ſuch numerous and large maſſes of durable matter as the Comets are, however unlike they be to our Earth, are not deſtitute of beings capable of contemplating with wonder, and acknowledging with gratitude, the wiſdom, ſymmetry, and beauty of the Creation; which is more plainly to be obſerved in their extenſive Tour through the Heavens, than in our more confined Circuit. If farther conjecture is permitted, may we not ſuppoſe them inſtrumental in recruiting the expended fuel of the Sun; and ſupplying the exhauſted moiſture of the Planets? However difficult it may be, circumſtanced as we are, to find out their particular deſtination, this is an undoubted truth, that wherever the Deity exerts his power, there he alſo manifeſts his wiſdom and goodneſs.

This Syſtem very ancient, and demonſtrable.

95. THE SOLAR SYSTEM here deſcribed is not a late invention; for it was known and taught by the wiſe *Samian* philoſopher PYTHAGORAS, and others among the ancients; but in latter times was loſt, 'till the 15th century, when it was again reſtored by the famous *Poliſh* philoſopher, NICHOLAUS COPERNICUS, who was born at *Thorn* in the year 1473. In this, he was followed by the greateſt mathematicians and philoſophers that have ſince lived; as KEPLER, GALILEO, DESCARTES, GASSENDUS, and Sir ISAAC NEWTON; the laſt of whom has eſtabliſhed this Syſtem on ſuch an everlaſting foundation of mathematical and phyſical demonſtration, as can never be ſhaken: and none who underſtand him can heſitate about it.

The Ptolemean Syſtem abſurd.

96. In the *Ptolemean Syſtem* the Earth was ſuppoſed to be fixed in the Center of the Univerſe; and that the Moon, Mercury, Venus, the Sun, Mars, Jupiter, and Saturn, moved round the Earth: above the Planets, this Hypotheſis placed the Firmament of Stars, and then the two Cryſtalline

Spheres; all which were included in and received motion from the *Primum Mobile*, which conſtantly revolved about the Earth in 24 hours from Eaſt to Weſt. But as this rude Scheme was found incapable to ſtand the teſt of art and obſervation, it was ſoon rejected by all true philoſophers; notwithſtanding the oppoſition and violence of blind and zealous bigots.

The Tychonic Syſtem, partly true and partly falſe.

97. The *Tychonic Syſtem* ſucceeded the *Ptolemean*, but was never ſo generally received. In this the Earth was ſuppoſed to ſtand ſtill in the Center of the Univerſe or Firmament of Stars, and the Sun to revolve about it every 24 hours; the Planets, Mercury, Venus, Mars, Jupiter, and Saturn, going round the Sun in the times already mentioned. But ſome of TYCHO's diſciples ſuppoſed the Earth to have a diurnal motion round it's Axis, and the Sun with all the above Planets to go round the Earth in a year; the Planets moving round the Sun in the foreſaid times. This hypotheſis, being partly true and partly falſe, was embraced by few; and ſoon gave way to the only true and rational Syſtem, reſtored by COPERNICUS and demonſtrated by Sir ISAAC NEWTON.

98. To bring the foregoing particulars at once in view, with ſeveral others which follow, concerning the Periods, Diſtances, Bulks, &c. of the Planets, the following Table is inſerted.

A TABLE of the PERIODS, REVOLUTIONS, MAGNITUDES, &c. of the PLANETS, as formerly computed by Aſtronomers.——For their true Diſtances of the SUN, as lately determined from Obſervations of the Tranſit of Venus, *See* § 194.

SUN and Planets.	Annual period round the Sun.	Diurnal rotation on it's Axis.	Diameter in Engliſh miles.	Mean diam. as ſeen fr. the Sun.	Mean diſtance from the Sun in Engliſh miles	Excentricity of it's Orbit in miles.	Axis inclined to Orbit.	Orbit inclined to Ecliptic.	Place of it's Aphelion.	Place of it's Aſcending Node.	Proportion of Diameters	Proportion of Bulk	Prop. of Gravity on the ſurface	Proportion of Denſity.
SUN	——	25 d. 6 h.	763000	——	——	——	8° 0′	——	——	——	10000	877650	24	25½
Mercury	87^d 23^h	Unknown.	2600	20″	32,000,000	6,720,000	Unkn.	6° 54′	♐ 13° 8′	♉ 14° 43′	34$\frac{1}{10}$	$\frac{1}{27}$	Unkn.	Unkn.
Venus	224^d 17^h	24 d. 8 h.	7906	30″	59,000,000	413,000	75° 0′	3° 20′	♒ 4° 20′	♊ 13° 59′	103½	1	Unkn.	Unkn.
Earth	365^d 6^h	1 d. 0 h.	7970	21″	82,000,000	1,377,000	23° 29′	0° 0′	♑ 8° 1′	——	104½	1	1	100
Moon	365^d 6^h	29 d. 12¾ h.	2180	6″	82,000,000	13,000	2° 10′	5° 18′	——	Variable.	28½	$\frac{1}{50}$	$\frac{34}{100}$	123½
Mars	686^d 23^h	24 h. 40 m.	4444	11″	125,000,000	11,439,000	0° 0′	1° 52′	♍ 0° 32′	♉ 17° 17′	58$\frac{1}{6}$	$\frac{1}{5}$	Unkn.	Unkn.
Jupiter	4332^d 12^h	9 h. 56 m.	81000	37″	426,000,000	20,352,000	0° 0′	1° 20′	♎ 9° 10′	♋ 7° 29′	1061$\frac{2}{3}$	1049	2	19
Saturn	10759^d 7^h	Unknown.	67000	16″	780,000,000	42,735,000	Unkn.	2° 30′	♐ 27° 50′	♋ 21° 13′	878$\frac{1}{9}$	586	1½	15

SUN and Planets.	Proportion of Light & Heat.	Propor. quantity of Matter.	Hourly motion in it's Orbit.	Hourly motion of it's Equator	Square miles in ſurface.	Cubic miles in ſolidity.	Would fall to the Sun in	
							days h.	
SUN	45000	227500	——	3818	1,828,911,000,000	232,577,115,137,000,000		If the projectile force was deſtroyed.
Mercury	6½	Unkn.	95000	Unkn.	21,236,800	9,195,534,500	15 13	
Venus	1¾	Unkn.	69000	43	691,361,300	258,507,832,200	39 17	
Earth	1	1	58000	1042	199,852,860	265,404,598,080	64 10	
Moon	1 ±	$\frac{1}{40}$	2290	9½	14,898,750	5,408,246,000	64 10	
Mars	$\frac{3}{7}$	Unkn.	47000	556	62,038,240	45,969,335,840	121 0	
Jupiter	$\frac{1}{28}$	220	25000	25920	20,603,970,000	278,153,095,000,000	290 0	
Saturn	$\frac{1}{90}$	94	18000	Unkn.	14,102,562,000	155,128,182,000,000	767 0	

Jupiter's Moons. N°	Periods round Jupiter. D.	H.	M
1	1	18	36
2	3	13	15
3	7	3	59
4	16	18	30

Saturn's Moons. N°	Periods round Saturn. D.	H.	M.
1	1	21	19
2	2	17	40
3	4	12	25
4	15	22	41
5	79	7	48

If the Moon's projectile force was deſtroyed, ſhe would fall to the Earth in 4 days 21 hours.

CHAP. III.

The COPERNICAN SYSTEM *demonſtrated to be true.*

Of matter and motion.

99. MATTER is of itſelf inactive, and indifferent to motion or reſt. A body at reſt can never put itſelf in motion; a body in motion can never ſtop or move ſlower of itſelf. Hence, when we ſee a body in motion, we conclude ſome other ſubſtance muſt have given it that motion; when we ſee a body fall from motion to reſt, we conclude ſome other body or cauſe ſtopt it.

100. All motion is naturally rectilineal. A bullet thrown by the hand, or diſcharged from a cannon, would continue to move in the ſame direction it received at firſt, if no other power diverted it's courſe. Therefore, when we ſee a body moving in a curve of whatever kind, we conclude it muſt be acted upon by two powers at leaſt: one to put it in motion, and another drawing it off from the rectilineal courſe which it would otherwiſe have continued to move in.

Gravity demonſtrable.

101. The power by which bodies fall towards the Earth, is called *Gravity* or *Attraction.* By this power in the Earth it is, that all bodies, on whatever ſide, fall in lines perpendicular to it's ſurface. On oppoſite parts of the Earth bodies fall in oppoſite directions, all towards the center, where the whole force of gravity is as it were accumulated. By this power conſtantly acting on bodies near the Earth they are kept from leaving it altogether; and thoſe on it's ſurface are kept thereto on all ſides, ſo that they cannot fall from it. Bodies thrown with any obliquity are drawn by this power from a ſtraight line into a curve, until they fall to the ground: the greater the force by which they are thrown, the greater is the diſtance they are carried before they fall. If we ſuppoſe a body carried

ſeveral miles above the Earth, and there projected in an horizontal direction with ſo great a velocity, that it would move more than a ſemidiameter of the Earth, in the time it would take to fall to the Earth by gravity; in that caſe, if there were no reſiſting medium in the way, the body would not fall to the Earth at all, but continue to circulate round the Earth, keeping always the ſame path, and returning to the point from whence it was projected with the ſame velocity as at firſt.

Projectile force demonſtrable.

102. We find the Moon moves round the Earth in an Orbit nearly circular. The Moon therefore muſt be acted on by two powers or forces; one which would cauſe her to move in a right line, another bending her motion from that line into a curve. This attractive power muſt be ſeated in the Earth; for there is no other body within the Moon's Orbit to draw her. The attractive power of the Earth therefore extends to the Moon; and, in combination with her projectile force, cauſes her to move round the Earth in the ſame manner as the circulating body above ſuppoſed.

The Sun and Planets attract each other.

103. The Moons of Jupiter and Saturn are obſerved to move round their primary Planets: therefore there is ſuch a power as gravity in theſe Planets. All the Planets move round the Sun, and reſpect it for their center of motion: therefore the Sun muſt be endowed with an attracting force, as well as the Earth and Planets. The like may be proved of the Comets. So that all the bodies or matter of the Solar Syſtem are poſſeſſed of this power; and perhaps ſo is all matter whatſoever.

104. As the Sun attracts the Planets with their Satellites, and the Earth the Moon, ſo the Planets and Satellites re-attract the Sun, and the Moon the Earth: action and re-action being always equal. This is alſo confirmed by obſervation; for the Moon raiſes tides in the ocean, the Satellites and Planets diſturb one another's motions.

105. Every particle of matter being poſſeſſed of an attracting power, the effect of the whole muſt be in proportion to the number of attracting particles; that is, to the quantity of matter in the body. This is demonſtrated from experiments on pendulums: for, if they are of equal lengths, whatever their weights be, they always vibrate in equal times. Now, if one be double the weight of another, the force of gravity or attraction muſt be double to make it oſcillate with the ſame celerity: if one is thrice the weight or quantity of matter of another, it requires thrice the force of gravity to make it move with the ſame celerity. Hence it is certain, that the power of gravity is always porportional to the quantity of matter in bodies, whatever their bulks or figures are.

106. Gravity alſo, like all other virtues or emanations, either drawing or impelling a body towards a center, decreaſes as the ſquare of the diſtance increaſes: that is, a body at twice the diſtance attracts another with only a fourth part of the force; at four times the diſtance, with a ſixteenth part of the force. This too is confirmed from obſervation, by comparing the diſtance which the Moon falls in a minute from a right line touching her Orbit, with the ſpace which bodies near the Earth fall in the ſame time: and alſo by comparing the forces which retain Jupiter's Moons in their Orbits. This will be more fully explained in the ſeventh Chapter.

Gravitation and projection exemplified.

107. The mutual attraction of bodies may be exemplified by a boat and a ſhip on the Water, tied by a rope. Let a man either in a ſhip or boat pull the rope (it is the ſame in effect at which end he pulls, for the rope will be equally ſtretched throughout) the ſhip and boat will be drawn towards one another; but with this difference, that the boat will move as much faſter than the ſhip, as the ſhip is heavier than the boat. Suppoſe the boat as heavy as the ſhip, and they will draw one

another equally (ſetting aſide the greater reſiſtance of the Water on the bigger body) and meet in the middle of the firſt diſtance between them. If the ſhip is a thouſand or ten thouſand times heavier than the boat, the boat will be drawn a thouſand or ten thouſand times faſter than the ſhip; and meet proportionably nearer the place from which the ſhip ſet out. Now, whilſt one man pulls the rope, endeavouring to bring the ſhip and boat together, let another man, in the boat, endeavour to row it off ſidewiſe, or at right Angles to the rope; and the former, inſtead of being able to draw the boat to the ſhip, will find it enough for him to keep the boat from going further off; whilſt the latter, endeavouring to row off the boat in a ſtraight line, will, by means of the other's pulling it towards the ſhip, row the boat round the ſhip at the rope's length from her. Here, the power employed to draw the ſhip and boat to one another repreſents the mutual attraction of the Sun and Planets, by which the Planets would fall freely towards the Sun with a quick motion; and would alſo in falling attract the Sun towards them. And the power employed to row off the boat repreſents the projectile force impreſſed on the Planets at right angles, or nearly ſo, to the Sun's attraction; by which means the Planets move round the Sun, and are kept from falling to it. On the other hand, if it be attempted to make a heavy ſhip go round a light boat, they will meet ſooner than the ſhip can get round; or the ſhip will drag the boat after it.

108. Let the above principles be applied to the Sun and Earth; and they will evince, beyond a poſſibility of doubt, that the Sun, not the Earth, is the center of the Syſtem; and that the Earth moves round the Sun as the other Planets do.

For, if the Sun moves about the Earth, the Earth's attractive power muſt draw the Sun towards it from the line of projection ſo, as to bend it's motion into a curve. But the Sun being at leaſt 227 thouſand times as heavy as the Earth, by being ſo much weightier as it's quantity of matter is greater, it muſt move 227 thouſand times as ſlowly toward the Earth, as the Earth does toward the Sun; and conſequently the Earth would fall to the Sun in a ſhort time, if it had not a very ſtrong projectile motion to carry it off. The Earth therefore, as well as every other Planet in the Syſtem, muſt have a rectilineal impulſe, to prevent it's falling into the Sun. To ſay, that gravitation retains all the other Planets in their Orbits without affecting the Earth, which is placed between the Orbits of Mars and Venus, is as abſurd as to ſuppoſe that ſix cannon-bullets might be projected upwards to different heights in the Air, and that five of them ſhould fall down to the ground; but the ſixth, which is neither the higheſt nor the loweſt, ſhould remain ſuſpended in the Air without falling, and the Earth move round about it.

The abſurdity of ſuppoſing the Earth at reſt.

109. There is no ſuch thing in nature as a heavy body moving round a light one as it's center of motion. A pebble faſtened to a mill-ſtone by a ſtring, may by an eaſy impulſe be made to circulate round the mill-ſtone: but no impulſe can make a mill-ſtone circulate round a looſe pebble, for the heavieſt would undoubtedly carry the lighteſt along with it wherever it goes.

110. The Sun is ſo immenſely bigger and heavier than the Earth *, that if he was moved out of his place, not only the Earth, but all the other Planets, if they were united into one maſs, would be carried along with the Sun, as the pebble would be with the mill-ſtone.

111. By conſidering the law of gravitation, which takes place throughout the Solar Syſtem, in another light, it will be evident that the Earth moves round the Sun in a year; and not the Sun round the Earth. It has been ſhewn (§ 106) that

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* As will be demonſtrated in the ninth Chapter.

the power of gravity decreaſes as the ſquare of the diſtance increaſes: and from this it follows with mathematical certainty, that when two or more bodies move round another as their center of motion, the ſquares of their periodic times will be to one another in the ſame proportion, as the cubes of their diſtances from the central body. This holds preciſely with regard to the Planets round the Sun, and the Satellites round the Planets; the relative diſtances of all which, are well known. But, if we ſuppoſe the Sun to move round the Earth, and compare it's period with the Moon's by the above rule, it will be found that the Sun would take no leſs than 173,510 days to move round the Earth, in which caſe our year would be 475 times as long as it now is. To this we may add, that the aſpects of increaſe and decreaſe of the Planets, the times of their ſeeming to ſtand ſtill, and to move direct and retrograde, anſwer preciſely to the Earth's motion; but not at all to the Sun's, without introducing the moſt abſurd and monſtrous ſuppoſitions, which would deſtroy all harmony, order, and ſimplicity in the Syſtem. Moreover, if the Earth is ſuppoſed to ſtand ſtill, and the Stars to revolve in free ſpaces about the Earth in 24 hours, it is certain that the forces by which the Stars revolve in their Orbits are not directed to the Earth, but to the centers of the ſeveral Orbits; that is, of the ſeveral parallel Circles which the Stars on different ſides of the equator deſcribe every day: and the like inferences may be drawn from the ſuppoſed diurnal motion of the Planets, ſince they are never in the Equinoctial but twice, in their courſes with regard to the ſtarry Heavens. But, that forces ſhould be directed to no central body, on which they phyſically depend, but to innumerable imaginary points in the Axe of the Earth produced to the Poles of the Heavens, is an hypotheſis too abſurd to be allowed of by any rational creature. And it is ſtill more abſurd

The harmony of the celeſtial motions.

The abſurdity of ſuppoſing the Stars and Planets to move round the Earth.

ſurd to imagine that theſe forces ſhould increaſe exactly in proportion to the diſtances from this Axe; for this is an indication of an increaſe to infinity; whereas the force of attraction is found to decreaſe in receding from the fountain from whence it flows. But, the farther any Star is from the quiescent Pole, the greater muſt be the Orbit which it deſcribes; and yet it appears to go round in the ſame time as the neareſt Star to the Pole does. And if we take into conſideration the two-fold motion obſerved in the Stars, one diurnal round the Axis of the Earth in 24 hours, and the other round the Axis of the Ecliptic in 25920 years, § 251, it would require an explication of ſuch a perplexed compoſition of forces, as could by no means be reconciled with any phyſical Theory.

Objections againſt the Earth's motion anſwered.

112. There is but one objection of any weight that can be made againſt the Earth's motion round the Sun; which is, that in oppoſite points of the Earth's Orbit, it's Axis, which always keeps a parallel direction, would point to different fixed Stars; which is not found to be fact. But this objection is eaſily removed, by conſidering the immenſe diſtance of the Stars in reſpect of the diameter of the Earth's Orbit; the latter being no more than a point when compared to the former. If we lay a ruler on the ſide of a table, and along the edge of the ruler view the top of a ſpire at ten miles diſtance; then lay the ruler on the oppoſite ſide of the table in a parallel ſituation to what it had before, and the ſpire will ſtill appear along the edge of the ruler; becauſe our eyes, even when aſſiſted by the beſt inſtruments, are incapable of diſtinguiſhing ſo ſmall a change at ſo great a diſtance.

113. Dr. BRADLEY, our preſent Aſtronomer Royal, has found by a long ſeries of the moſt accurate obſervations, that there is a ſmall apparent motion of the fixed Stars, occaſioned by the aberration of their light, and ſo exactly anſwering to

an annual motion of the Earth, as evinces the ſame, even to a mathematical demonſtration. Thoſe who are qualified to read the Doctor's modeſt Account of this great diſcovery, may conſult the *Philoſophical Tranſactions*, N° 406. Or they may find it treated of at large by Drs. SMITH *, LONG †, DESAGULIERS ‡, RUTHERFURTH ||, Mr. MACLAURIN, and M. DE LA CAILLE **.

Why the Sun appears to change his place.

114. It is true that the Sun ſeems to change his place daily, ſo as to make a tour round the ſtarry Heavens in a year. But whether the Sun or Earth moves, this appearance will be the ſame; for, when the Earth is in any part of the Heavens, the Sun will appear in the oppoſite. And therefore, this appearance can be no objection againſt the motion of the Earth.

115. It is well known to every perſon who has ſailed on ſmooth Water, or been carried by a ſtream in a calm, that however faſt the veſſel goes, he does not feel it's progreſſive motion. The motion of the Earth is incomparably more ſmooth and uniform than that of a ſhip, or any machine made and moved by human art: and therefore it is not to be imagined that we can feel it's motion.

The Earth's motion on it's Axis demonſtrated.

116. We find that the Sun, and thoſe Planets on which there are viſible ſpots, turn round their Axes: for the ſpots move regularly over their Diſks ††. From hence we may reaſonably conclude that the other Planets, on which we ſee no ſpots, and the Earth, which is likewiſe a Planet, have ſuch rotations. But being incapable of leaving the Earth, and viewing it at a diſtance, and it's rotation being ſmooth and uniform, we can neither

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* Optics, B. I. § 1178. † Aſtronomy, B. II. § 838.

‡ Philoſophy, Vol. I. p. 401. || Account of Sir Iſaac Newton's *Philoſophical Diſcoveries*, B. III. c. 2. § 3.

** *Elements d'Aſtronomie*, § 381.

†† The face of the Sun, Moon, or any Planet, as it appears to the eye, is called it's Diſk.

ſee it move on it's Axis as we do the Planets, nor feel ourſelves affected by it's motion. Yet there is one effect of ſuch a motion, which will enable us to judge with certainty whether the Earth revolves on it's Axis or not. All Globes which do not turn round their Axes will be perfect ſpheres, on account of the equality of the weight of bodies on their ſurfaces; eſpecially of the fluid parts. But all Globes which turn on their Axes will be oblate ſpheroids; that is, their ſurfaces will be higher, or farther from the center, in the equatoreal than in the polar Regions: for, as the equatoreal parts move quickeſt, they will recede farther from the Axis of motion, and enlarge the equatoreal diameter. That our Earth is really of this figure, is demonſtrable from the unequal vibrations of a pendulum, and the unequal lengths of degrees in different latitudes. Since then the Earth is higher at the Equator than at the Poles, the ſea, which naturally runs downward, or towards the places which are neareſt the center, would run towards the polar Regions, and leave the equatoreal parts dry, if the centrifugal force of theſe parts, by which the waters were carried thither, did not keep them from returning. The Earth's equatoreal diameter is 35 miles longer than it's Axis.

All bodies heavier at the Poles than they would be at the Equator.

117. Bodies near the Poles are heavier than thoſe towards the Equator, becauſe they are nearer the Earth's center, where the whole force of the Earth's attraction is accumulated. They are alſo heavier, becauſe their centrifugal force is leſs, on account of their diurnal motion being ſlower. For both theſe reaſons, bodies carried from the Poles toward the Equator, gradually loſe of their weight. Experiments prove that a pendulum, which vibrates ſeconds near the Poles, vibrates ſlower near the Equator, which ſhews that it is lighter or leſs attracted there. To make it oſcillate in the ſame time, it is found neceſſary to diminiſh it's length. By comparing the different lengths of pendulums

ſwinging ſeconds at the Equator and at *London*, it is found that a pendulum muſt be $2\frac{169}{1000}$ lines ſhorter at the Equator than at the Poles. A line is a twelfth part of an inch.

How they might loſe all their weight.

118. If the Earth turned round it's Axis in 84 minutes 43 ſeconds, the centrifugal force would be equal to the power of gravity at the Equator; and all bodies there would entirely loſe their weight. If the Earth revolved quicker, they would all fly off, and leave it.

The Earth's motion cannot be felt.

119. One on the Earth can no more be ſenſible of it's undiſturbed motion on it's Axis, than one in the cabbin of a ſhip on ſmooth water can be ſenſible of her motion when ſhe turns gently and uniformly round. It is therefore no argument againſt the Earth's diurnal motion that we do not feel it: nor is the apparent revolutions of the celeſtial bodies every day a proof of the reality of theſe motions; for whether we or they revolve, the appearance is the very ſame. A perſon looking through the cabbin-windows of a ſhip as ſtrongly fancies the objects on land to go round when the ſhip turns, as if they were actually in motion.

To the different Planets the Heavens appear to turn round on different Axes.

120. If we could tranſlate ourſelves from Planet to Planet, we ſhould ſtill find that the Stars would appear of the ſame magnitudes, and at the ſame diſtances from each other, as they do to us here; becauſe the width of the remoteſt Planet's Orbit bears no ſenſible proportion to the diſtance of the Stars. But then, the Heavens would ſeem to revolve about very different Axes; and conſequently, thoſe quieſcent points, which are our Poles in the Heavens, would ſeem to revolve about other points, which, though apparently in motion as ſeen from the Earth, would be at reſt as ſeen from any other Planet. Thus the Axis of Venus, which lies almoſt at right Angles to the Axis of the Earth, would have it's motionleſs Poles in two oppoſite points of the Heavens lying almoſt in our Equinoctial,

noctial, where the motion appears quickeſt, becauſe it is ſeemingly performed in the greateſt Circle. And the very Poles, which are at reſt to us, have the quickeſt motion of all as ſeen from Venus. To Mars and Jupiter the Heavens appear to turn round with very different velocities on the ſame Axis, whoſe Poles are about 23½ degrees from ours. Were we on Jupiter, we ſhould be at firſt amazed at the rapid motion of the Heavens; the Sun and Stars going round in 9 hours 56 minutes. Could we go from thence to Venus, we ſhould be as much ſurpriſed at the ſlowneſs of the heavenly motions; the Sun going but once round in 584 hours, and the Stars in 540. And could we go from Venus to the Moon, we ſhould ſee the Heavens turn round with a yet ſlower motion; the Sun in 708 hours, the Stars in 655. As it is impoſſible theſe various circumvolutions in ſuch different times, and on ſuch different Axes, can be real, ſo it is unreaſonable to ſuppoſe the Heavens to revolve about our Earth more than it does about any other Planet. When we reflect on the vaſt diſtance of the fixed Stars, to which 162,000,000 of miles, the diameter of the Earth's Orbit, is but a point, we are filled with amazement at the immenſity of their diſtance. But if we try to frame an idea of the extreme rapidity with which the Stars muſt move, if they move round the Earth in 24 hours, the thought becomes ſo much too big for our imagination, that we can no more conceive it than we do infinity or eternity. If the Sun was to go round the Earth in 24 hours, he muſt travel upwards of 300,000 miles in a minute: but the Stars being at leaſt 400,000 times as far from the Sun, as the Sun is from us, thoſe about the Equator muſt move 400,000 times as quick. And all this to ſerve no other purpoſe than what can be as fully and much more ſimply obtained by the Earth's turning round eaſtward, as on an Axis, every 24 hours, cauſing thereby an apparent diurnal motion of the Sun weſtward, and bringing about the alternate returns of day and night.

Objections againſt the Earth's diurnal motion anſwered.

121. As to the common objections againſt the Earth's motion on it's Axis, they are all eaſily anſwered and ſet aſide. That it may turn without being ſeen or felt by us to do ſo, has been already ſhewn, § 119. But ſome are apt to imagine that if the Earth turns eaſtward (as it certainly does if it turns at all) a ball fired perpendicularly upward in the air muſt fall conſiderably weſtward of the place it was projected from. The objection, which at firſt ſeems to have ſome weight, will be found to have none at all, when we conſider that the gun and ball partake of the Earth's motion; and therefore the ball being carried forward with the air as quick as the Earth and air turn, muſt fall down on the ſame place. A ſtone let fall from the top of a main-maſt, if it meets with no obſtacle, falls on the deck as near the foot of the maſt when the ſhip ſails as when it does not. If an inverted bottle, full of liquor, be hung up to the ceiling of the cabbin, and a ſmall hole be made in the cork to let the liquor drop through on the floor, the drops will fall juſt as far forward on the floor when the ſhip ſails as when it is at reſt. And gnats or flies can as eaſily dance among one another in a moving cabbin as in a fixed chamber. As for thoſe ſcripture expreſſions which ſeem to contradict the Earth's motion, this general anſwer may be made to them all, *viz.* it is plain from many inſtances that the Scriptures were never intended to inſtruct us in Philoſophy or Aſtronomy; and therefore, on thoſe ſubjects, expreſſions are not always to be taken in the ſtricteſt ſenſe; but for the moſt part as accommodated to the common apprehenſions of mankind. Men of ſenſe in all ages, when not treating of the ſciences purpoſely, have followed this method: and it would be in vain to follow any other in addreſſing ourſelves to the vulgar, or bulk of

any community. *Moſes* calls the Moon A GREAT LUMINARY (as it is in the Hebrew) as well as the Sun: but the Moon is known to be an opaque body, and the ſmalleſt that Aſtronomers have obſerved in the Heavens; and ſhines upon us not by any inherent light of it's own, but by reflecting the light of the Sun. If *Moſes* had known this, and told the *Iſraelites* ſo, they would have ſtared at him; and conſidered him rather as a madman than as a perſon commiſſioned by the Almighty to be their leader.

CHAP. IV.

The Phenomena of the Heavens as ſeen from different parts of the Earth.

We are kept to the Earth by gravity.

122. WE are kept to the Earth's ſurface on all ſides by the power of it's central attraction; which, laying hold of all bodies according to their denſities or quantities of matter without regard to their bulks, conſtitutes what we call their *weight*. And having the ſky over our heads, go where we will, and our feet towards the center of the Earth, we call it *up* over our heads, and *down* under our feet: although the ſame right line which is *down* to us, if continued through and beyond the oppoſite ſide of the Earth, would be *up* to the inhabitants on the oppoſite ſide. For, the inhabitants n, i, e, m, s, o, q, l ſtand with their feet toward the Earth's center C; and have the ſame figure of PLATE II. Fig. I. ſky N, I, E, M, S, O, Q, L over their heads. Therefore, the point S is as directly upward to the inhabitant s on the South Pole, as N is to the inhabitant n on the North Pole: ſo is E to the inhabitant e, ſuppoſed to be on the north end of *Peru*; and Q to the oppoſite inhabitant q on the middle of the iſland *Sumatra*. Each of theſe obſervers is Antipodes. ſurpriſed that his oppoſite or *Antipodē* can ſtand with his head hanging downwards. But let either

Pl. II.

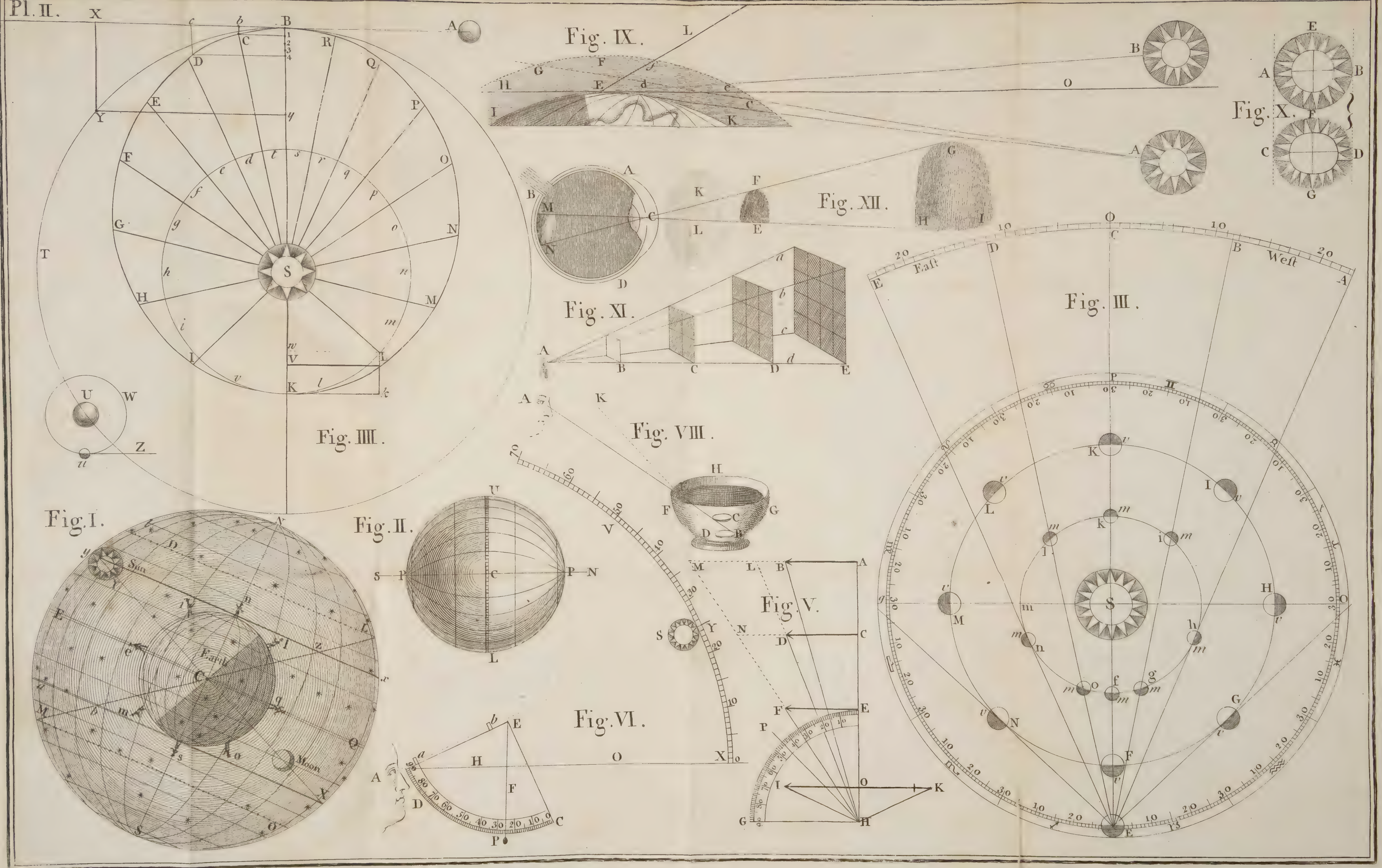
Fig. IX.
Fig. X.
Fig. XII.
Fig. XI.
Fig. III.
Fig. IIII.
Fig. VIII.
Fig. I.
Fig. II.
Fig. V.
Fig. VI.
East
West
Sun
Earth
Moon
S
A
B
C
D
E
F
G
H
I
K
L
M
N
O
P
Q
R
T
U
V
W
X
Y
Z

go to the other, and he will tell him that he ſtood as upright and firm on the place where he was, as he now ſtands where he is. To all theſe obſervers the Sun, Moon and Stars, ſeem to turn round the points *N* and *S*, as the Poles of the fixed Axis *NCS*; becauſe the Earth does really turn round the mathematical line *nCs* as round an Axis, of which *n* is the North Pole and *s* the South Pole. The Inhabitant *U* (Fig. II.) affirms that he is on the uppermoſt ſide of the Earth, and wonders how another at *L* can ſtand on the undermoſt ſide with his head hanging downwards. But *U* in the mean time forgets that in twelve hours time he will be carried half round with the Earth, and then be in the very ſituation that *L* now is, although as far from him as before. And yet, when *U* comes there, he will find no difference as to his manner of ſtanding; only he will ſee the oppoſite half of the Heavens, and imagine the Heavens to have gone half round the Earth.

PLATE II.

Axis of the World.

It's Poles.

Fig. II.

123. When we ſee a Globe hung up in a room, we cannot help imagining it to have an upper and an under ſide, and immediately form a like idea of the Earth; from whence we conclude, that it is as impoſſible for people to ſtand on the under ſide of the Earth, as for pebbles to lie on the under ſide of a common Globe, which inſtantly fall down from it to the ground; and well they may, becauſe the attraction of the Earth, being greater than the attraction of the Globe, pulls them away. Juſt ſo would be the caſe with our Earth, if it were placed near a Globe much bigger than itſelf, ſuch as Jupiter: for then it would really have an upper and an under ſide with reſpect to that large Globe; which, by it's Attraction, would pull away every thing from the ſide of the Earth next to it; and only thoſe on the top of the oppoſite or upper ſide could remain upon it. But there is no larger Globe near enough our Earth to overcome it's central attrac-

How our Earth might have an upper and an under ſide.

PLATE II. attraction; and therefore it has no ſuch thing as an upper and an under ſide: for all bodies on or near it's ſurface, even to the Moon, gravitate towards it's center.

124. Let any man imagine that the Earth and every thing but himſelf is taken away, and he left alone in the midſt of indefinite Space; he could then have no idea of *up* or *down*; and were his pockets full of gold, he might take the pieces one by one, and throw them away on all ſides of him, without any danger of loſing them; for the attraction of his body would bring them all back by the ways they went, and *he* would be *down* to every one of them. But then, if a Sun or any other large body were created, and placed in any part of Space ſeveral millions of miles from him, he would be attracted towards it, and could not ſave himſelf from falling *down* to it.

Fig. I.

One half of the Heavens viſible to an inhabitant on any part of the Earth.

125. The Earth's bulk is but a point, as that at *C*, compared to the Heavens; and therefore every inhabitant upon it, let him be where he will, as at *n*, *e*, *m*, *s*, &c. ſees half of the Heavens. The inhabitant *n*, on the North Pole of the Earth, conſtantly ſees the Hemiſphere *ENQ*; and having the North Pole *N* of the Heavens juſt over his head, his * Horizon coincides with the Celeſtial Equator *ECQ*. Therefore all the Stars in the Northern Hemiſphere *ENQ*, between the Equator and North Pole, appear to turn round the line *NC*, moving parallel to the Horizon. The Equatoreal Stars keep in the Horizon, and all thoſe in the Southern Hemiſphere *ESQ* are inviſible. The like Phenomena are ſeen by the obſerver *s* on the South Pole, with reſpect to the Hemiſphere *ESQ*; and to him the oppoſite Hemiſphere is always inviſible. Hence, under either Pole, only one

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* The utmoſt limit of a perſon's view, where the Sky ſeems to touch the Earth all around, is called his Horizon; which ſhifts as the perſon changes his place.

half of the Heavens is ſeen; for thoſe parts which are once viſible never ſet, and thoſe which are once inviſible never riſe. But the Ecliptic *ϒCX*, or Orbit which the Sun appears to deſcribe once a year by the Earth's annual motion, has the half *ϒC* conſtantly above the Horizon *ECQ* of the North Pole *n*; and the other half *CX* always below it. Therefore whilſt the Sun deſcribes the northern half *ϒC* of the Ecliptic, he neither ſets to the North Pole nor riſes to the South; and whilſt he deſcribes the ſouthern half *CX*, he neither ſets to the South Pole nor riſes to the North. The ſame things are true with reſpect to the Moon; only with this difference, that as the Sun deſcribes the Ecliptic but once a year, he is for half that time viſible to each Pole in it's turn, and as long inviſible; but as the Moon goes round the Ecliptic in 27 days 8 hours, ſhe is only viſible for 13 days 16 hours, and as long inviſible to each Pole by turns. All the Planets likewiſe riſe and ſet to the Poles, becauſe their Orbits are cut obliquely in halves by the Horizon of the Poles. When the Sun (in his apparent way from *X*) arrives at *C*, which is on the 20th of *March*, he is juſt riſing to an obſerver at *n* on the North Pole, and ſetting to another at *s* on the South Pole. From *C* he riſes higher and higher in every apparent Diurnal revolution, 'till he comes to the higheſt point of the Ecliptic *y*, on the 21ſt of *June*, and then he is at his greateſt Altitude, which is 23½ degrees, or the Arc *Ey*, equal to his greateſt North declination; and from thence he ſeems to deſcend gradually in every apparent Circumvolution, 'till he ſets at *C* on the 23d of *September*; and then he goes to exhibit the like Appearances at the South Pole for the other half of the year. Hence the Sun's apparent motion round the Earth is not in parallel Circles, but in Spirals; ſuch as might be repreſented by a thread wound round a Globe from Tropic to Tropic; the Spirals being at ſome diſtance from one another about the Equator, and gradually

Phenomena at the Poles.

PLATE II. gradually nearer to each other as they approach toward the Tropics.

Phenomena at the Equator. 126. If the obſerver be any where on the Terreſtrial Equator *eCq*, as ſuppoſe at *e*, he is in the plane of the Celeſtial Equator; or under the Equinoctial *ECQ*; and the Axis of the earth *nCs* is coincident with the Plane of his Horizon, extended out to *N* and *S*, the North and South Poles of the Heavens. As the Earth turns round the line *NCS*, the whole Heavens *MOLl* ſeem to turn round the ſame line, but the contrary way. It is plain that this obſerver has the celeſtial Poles conſtantly in his Horizon, and that his Horizon cuts the Diurnal paths of all the Celeſtial bodies perpendicularly and in halves. Therefore the Sun, Planets and Stars, riſe every day, and aſcend perpendicularly above the Horizon for ſix hours, and paſſing over the Meridian, deſcend in the ſame manner for the ſix following hours; then ſet in the Horizon, and continue twelve hours below it. Conſequently at the Equator the days and nights are equally long throughout the year. When the obſerver is in the ſituation *e*, he ſees the Hemiſphere *SEN*; but in twelve hours after, he is carried half round the Earth's Axis to *q*, and then the Hemiſphere *SQN* becomes viſible to him; and *SEN* diſappears. Thus we find, that to an obſerver at either of the Poles one half of the Sky is always viſible, and the other half never ſeen; but to an obſerver on the Equator the whole Sky is ſeen every 24 hours.

Fig. I.

The Figure here referred to, repreſents a Celeſtial globe of glaſs, having a Terreſtrial globe within it; after the manner of the Glaſs Sphere invented by my generous friend Dr. Long, *Lowndes*'s Profeſſor of Aſtronomy in *Cambridge*.

Remark. 127. If a Globe be held ſidewiſe to the eye, at ſome diſtance, and ſo that neither of it's Poles can be ſeen, the Equator *ECQ*, and all Circles parallel to it, as *DL*, *yzx*, *abX*, *MO*, &c. will appear to be ſtraight lines, as projected in this Figure; which is requiſite to be mentioned here, becauſe we ſhall have occaſion to call them Circles in the following Articles of this Chapter*.

Phenomena between the Equator and Poles.

128. Let us now ſuppoſe that the obſerver has gone from the Equator *e* towards the North Pole *n*, and that he ſtops at *i*, from which place he then ſees the Hemiſphere *MElNL*; his Horizon *MCL* having ſhifted as many † Degrees from the Celeſtial Poles *N* and *S*, as he has travelled from under the Equinoctial *E*. And as the Heavens ſeem conſtantly to turn round the line *NCS* as an Axis, all thoſe Stars which are not ſo many degrees from the North Pole *N* as the obſerver is from the Equinoctial, namely, the Stars north of the dotted parallel *DL*, never ſet below the Horizon; and thoſe which are ſouth of the dotted parallel *MC*, never riſe above it. Hence, the former of theſe two parallel Circles is called *the Circle of perpetual Apparition*, and the latter *the Circle of perpetual Occultation*: but all the Stars between theſe two Circles riſe and ſet every day. Let us imagine many Circles to be drawn between theſe two, and parallel to them; thoſe which are on the north ſide of the Equinoctial will be unequally cut by the Horizon *MCL*, having larger portions above the Horizon than below it; and the more ſo, as they are nearer to the Circle of perpetual Apparition; but the reverſe happens to thoſe on the ſouth ſide of the Equinoctial, whilſt the Equinoctial is divided in two equal parts by the Horizon. Hence, by the apparent turning of the Heavens, the northern Stars deſcribe greater Arcs or Portions of Circles above the Horizon than below it; and the greater, as they are farther from the Equinoctial towards the Circle of perpetual Apparition; whilſt the con-

The Circles of perpetual Apparition and Occultation.

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* The Plane of a Circle, or a thin circular Plate, being turned edgewiſe to the eye, appears to be a ſtraight line.

† A Degree is the 360th part of a Circle.

PLATE II. trary happens to all Stars ſouth of the Equinoctial: but thoſe upon it deſcribe equal Arcs both above and below the Horizon, and therefore they are juſt as long above as below it.

129. An obſerver on the Equator has no Circle of perpetual Apparition or Occultation, becauſe all the Stars, together with the Sun and Moon, riſe and ſet to him every day. But, as a bare view of the Figure is ſufficient to ſhew that theſe two Circles *DL* and *MO* are juſt as far from the Poles *N* and *S* as the obſerver at *i* (or one oppoſite to him at *o*) is from the Equator *ECQ*; it is plain, that if an obſerver begins to travel from the Equator towards either Pole, his Circle of perpetual Apparition riſes from that Pole as from a Point, and his Circle of perpetual Occultation from the other. As the obſerver advances toward the nearer Pole, theſe two Circles enlarge their diameters, and come nearer one another, until he comes to the Pole; and then they meet and coincide in the Equinoctial. On different ſides of the Equator, to obſervers at equal diſtances from it, the Circle of perpetual Apparition to one is the Circle of perpetual Occultation to the other.

Why the Stars always deſcribe the ſame parallel of motion, and the Sun a different.

130. Becauſe the Stars never vary their diſtances from the Equinoctial, ſo as to be ſenſible in an age, the lengths of their diurnal and nocturnal Arcs are always the ſame to the ſame places on the Earth. But as the Earth goes round the Sun every year in the Ecliptic, one half of which is on the north ſide of the Equinoctial and the other half on it's ſouth ſide, the Sun appears to change his place every day, ſo as to go once round the Circle *YCX* every year, § 114. Therefore whilſt the Sun appears to advance northward, from having deſcribed the Parallel *abX* touching the Ecliptic in *X*, the days continually lengthen and the nights ſhorten, until he comes to *y* and deſcribes the Parallel *yzx*, when the days are at the longeſt and the nights at the

PLATE II.

the ſhorteſt: for then, as the Sun goes no farther northward, the greateſt portion that is poſſible of the diurnal Arc *yz* is above the Horizon of the inhabitant *i*; and the ſmalleſt portion *zx* below it. As the Sun declines ſouthward from *y*, he deſcribes ſmaller diurnal and greater nocturnal Arcs, or Portions of Circles, every day; which cauſeth the days to ſhorten and nights to lengthen, until he arrives again at the Parallel *abX*; which having only the ſmall part *ab* above the Horizon *MCL*, and the great part *bX* below it, the days are at the ſhorteſt and the nights at the longeſt; becauſe the Sun recedes no farther ſouth, but returns northward as before. It is eaſy to ſee that the Sun muſt be in the Equinoctial *ECQ* twice every year, and then the days and nights are equally long; that is, 12 hours each. Theſe hints ſerve at preſent to give an idea of ſome of the Appearances reſulting from the motions of the Earth; which will be more particularly deſcribed in the tenth Chapter.

Fig. I. Parallel, Oblique, and Right ſphere, what.

131. To an obſerver at either Pole, the Horizon and Equinoctial are coincident; and the Sun and Stars ſeem to move parallel to the Horizon: therefore, ſuch an obſerver is ſaid to have a parallel poſition of the Sphere. To an obſerver any where between either Pole and Equator, the Parallels deſcribed by the Sun and Stars are cut obliquely by the Horizon, and therefore he is ſaid to have an Oblique poſition of the Sphere. To an obſerver any where on the Equator, the Parallels of Motion, deſcribed by the Sun and Stars, are cut perpendicularly, or at Right angles, by the Horizon; and therefore he is ſaid to have a right poſition of the Sphere. And theſe three are all the different ways that the Sphere can be poſited to all people on the Earth.

CHAP.

CHAP. V.

The Phenomena of the Heavens as ſeen from different Parts of the Solar Syſtem.

132. SO vaſtly great is the diſtance of the ſtarry Heavens, that if viewed from any part of the Solar Syſtem, or even many millions of miles beyond it, it's appearance would be the very ſame to us. The Sun and Stars would all ſeem to be fixed on one concave ſurface, of which the Spectator's eye would be the center. But the Planets, being much nearer than the Stars, their appearances will vary conſiderably with the place from which they are viewed.

133. If the Spectator is at reſt without their Orbits, the Planets will ſeem to be at the ſame diſtance as the Stars; but continually changing their places with reſpect to the Stars, and to one another: aſſuming various phaſes of increaſe and decreaſe like the Moon. And notwithſtanding their regular motions about the Sun, will ſometimes appear to move quicker, ſometimes ſlower, be as often to the weſt as to the eaſt of the Sun; and at their greateſt diſtances ſeem quite ſtationary. The duration, extent, and diſtance of thoſe points in the Heavens where theſe digreſſions begin and end, would be more or leſs, according to the reſpective diſtances of the ſeveral Planets from the Sun: but in the ſame Planet they would continue invariably the ſame at all times; like pendulums of unequal lengths oſcillating together, the ſhorter move quick and go over a ſmall ſpace, the longer move ſlow and go over a large ſpace. If the obſerver is at reſt within the Orbits of the Planets, but not near the common center, their apparent motions will be irregular, but leſs ſo than in the former caſe. Each of the ſeveral Planets will appear bigger and leſs by turns, as they approach

nearer or recede farther from the obſerver; the neareſt varying moſt in their ſize. They will alſo move quicker or ſlower with regard to their fixed Stars, but will never be retrograde or ſtationary.

134. If an obſerver in motion views the Heavens, the ſame apparent irregularities will be obſerved, but with ſome variation reſulting from it's own motion. If he is on a Planet which has a rotation on it's Axis, not being ſenſible of his own motion, he will imagine the whole Heavens, Sun, Planets, and Stars, to revolve about him in the ſame time that his Planet turns round, but the contrary way; and will not be eaſily convinced of the deception. If his Planet moves round the Sun, the ſame irregularities and aſpects as above-mentioned will appear in the motions of the other Planets; and the Sun will ſeem to move among the fixed Stars or Signs, directly oppoſite to thoſe in which his Planet moves, changing it's place every day as he does. In a word, whether our obſerver be in motion or at reſt, whether within or without the Orbits of the Planets, their motions will ſeem irregular, intricate and perplexed, unleſs he is in the center of the Syſtem; and from thence, the moſt beautiful order and harmony will be ſeen by him.

The Sun's center the only point from which the true motions and places of the Planets could be ſeen.

135. The Sun being the center of all the Planets motions, the only place from which their motions could be truly ſeen, is the Sun's center; where the obſerver being ſuppoſed not to turn round with the Sun (which, in this caſe, we muſt imagine to be a tranſparent body) would ſee all the Stars at reſt, and ſeemingly equidiſtant from him. To ſuch an obſerver, the Planets would appear to move among the fixed Stars, in a ſimple, regular, and uniform manner; only, that as in equal times they deſcribe equal Areas, they would deſcribe ſpaces ſomewhat unequal, becauſe they move in elliptic Orbits, § 155. Their motions would alſo appear to be what they are in fact, the ſame way round the Heavens; in

paths which croſs at ſmall Angles in different parts of the Heavens, and then ſeparate a little from one another, § 20. So that, if the ſolar Aſtronomer ſhould make the Path or Orbit of any other Planet a ſtandard, and conſider it as having no obliquity, § 201, he would judge the paths of all the reſt to be inclined to it; each Planet having one half of it's path on one ſide, and the other half on the oppoſite ſide of the ſtandard Path or Orbit. And if he ſhould ever ſee all the Planets ſtart from a conjunction with each other *, Mercury would move ſo much faſter than Venus, as to overtake her again (though not in the ſame point of the Heavens) in a quantity of time almoſt equal to 145 of our days and nights; or, as we commonly call them, *Natural Days*, which include both the days and nights: Venus would move ſo much faſter than the Earth, as to overtake it again in 585 natural days: the Earth ſo much faſter than Mars, as to overtake him again in 778 ſuch days: Mars ſo much faſter than Jupiter, as to overtake him again in 817 ſuch days: and Jupiter ſo much faſter than Saturn, as to overtake him again in 7236 days, all of our time.

The judgment that a ſolar Aſtronomer would probably make concerning the diſtances and bulks of the Planets.

136. But as our ſolar Aſtronomer could have no idea of meaſuring the courſes of the Planets by our days, he would probably take the period of Mercury, which is the quickeſt moving Planet, for a meaſure to compare the periods of the others by. As all the Stars would appear quieſcent to him, he would never think that they had any dependance upon the Sun; but would naturally imagine that the Planets have, becauſe they move round the Sun. And it is by no means improbable, that he

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* Here we do not mean ſuch a conjunction, as that the nearer Planet ſhould hide all the reſt from the obſerver's ſight; (for that would be impoſſible unleſs the interſections of all their Orbits were coincident, which they are not, *See* § 21.) but when they were all in a line croſſing the ſtandard Orbit at right Angles.

would conclude thoſe Planets, whoſe periods are quickeſt, to move in Orbits proportionably leſs than thoſe do which make ſlower circuits. But being deſtitute of a method for finding their Parallaxes, or, more properly ſpeaking, as they could have no Parallax to him, he could never know any thing of their real diſtances or magnitudes. Their relative diſtances he might perhaps gueſs at by their periods, and from thence infer ſomething of truth concerning their relative bulks, by comparing their apparent bulks with one another. For example, Jupiter appearing bigger to him than Mars, he would conclude it to be much bigger in fact; becauſe it appears ſo, and muſt be farther from him, on account of it's longer period. Mercury and the Earth would ſeem much of the ſame bulk; but by comparing it's period with the Earth's, he would conclude that the Earth is much farther from him than Mercury, and conſequently that it muſt be really bigger, though apparently of the ſame bulk; and ſo of the reſt. And as each Planet would appear ſomewhat bigger in one part of it's Orbit than in the oppoſite, and to move quickeſt when it ſeems biggeſt, the obſerver would be at no loſs to determine that all the Planets move in Orbits, of which the Sun is not preciſely in the center.

The Planetary motions very irregular as ſeen from the Earth.

137. The apparent magnitudes of the Planets continually change as ſeen from the Earth, which demonſtrates that they approach nearer to it, and recede farther from it by turns. From theſe Phenomena, and their apparent motions among the Stars, they ſeem to deſcribe looped curves which never return into themſelves, Venus's path excepted. And if we were to trace out all their apparent paths, and put the figures of them together in one diagram, they would appear ſo anomalous and confuſed, that no man in his ſenſes could believe them to be repreſentations of their real paths; but would immediately conclude, that ſuch appa-

PLATE III. rent irregularities muſt be owing to ſome Optic illuſions. And after a good deal of enquiry, he might perhaps be at a loſs to find out the true cauſe of theſe inequalities; eſpecially if he were one of thoſe who would rather, with the greateſt juſtice, charge frail man with ignorance, than the Almighty with being the author of ſuch confuſion.

Thoſe of Mercury and Venus repreſented.

138. Dr. Long, in his firſt volume of *Aſtronomy*, has given us figures of the apparent paths of all the Planets, ſeparately, from Cassini; and on ſeeing them I firſt thought of attempting to trace ſome of them by a machine * that ſhews the motions of the Sun, Mercury, Venus, the Earth and Moon, according to the *Copernican Syſtem*. Having taken off the Sun, Mercury, and Venus, I put black-lead pencils in their places, with the points turned upward; and fixed a circular ſheet of paſte-board ſo, that the Earth kept conſtantly under it's center in going round the Sun; and the paſte-board kept it's paralleliſm. Then, preſſing gently with one hand upon the paſte-board to make it touch the three pencils, with the other hand I turned the winch that moves the whole machinery: and as the Earth, together with the pencils in the places of Mercury and Venus, had their proper motions round the Sun's pencil, which kept at reſt in the center of the machine, all the three pencils deſcribed a diagram from which the firſt Figure of the third Plate is truly copied in a ſmaller ſize. As the Earth moved round the Sun, the Sun's pencil deſcribed the dotted Circle of Months, whilſt Mercury's pencil drew the curve with the greateſt number of loops, and Venus's that with the feweſt. In their inferior conjunctions they come as much nearer the Earth, or within the Circle of the Sun's apparent motion round the Heavens, as they go beyond it in their ſuperior conjunctions. On each ſide of the loops they appear ſtationary; in that part of

Fig. I.

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* The Orrery fronting the Title-page.

each

Plate III.

Fig. I.

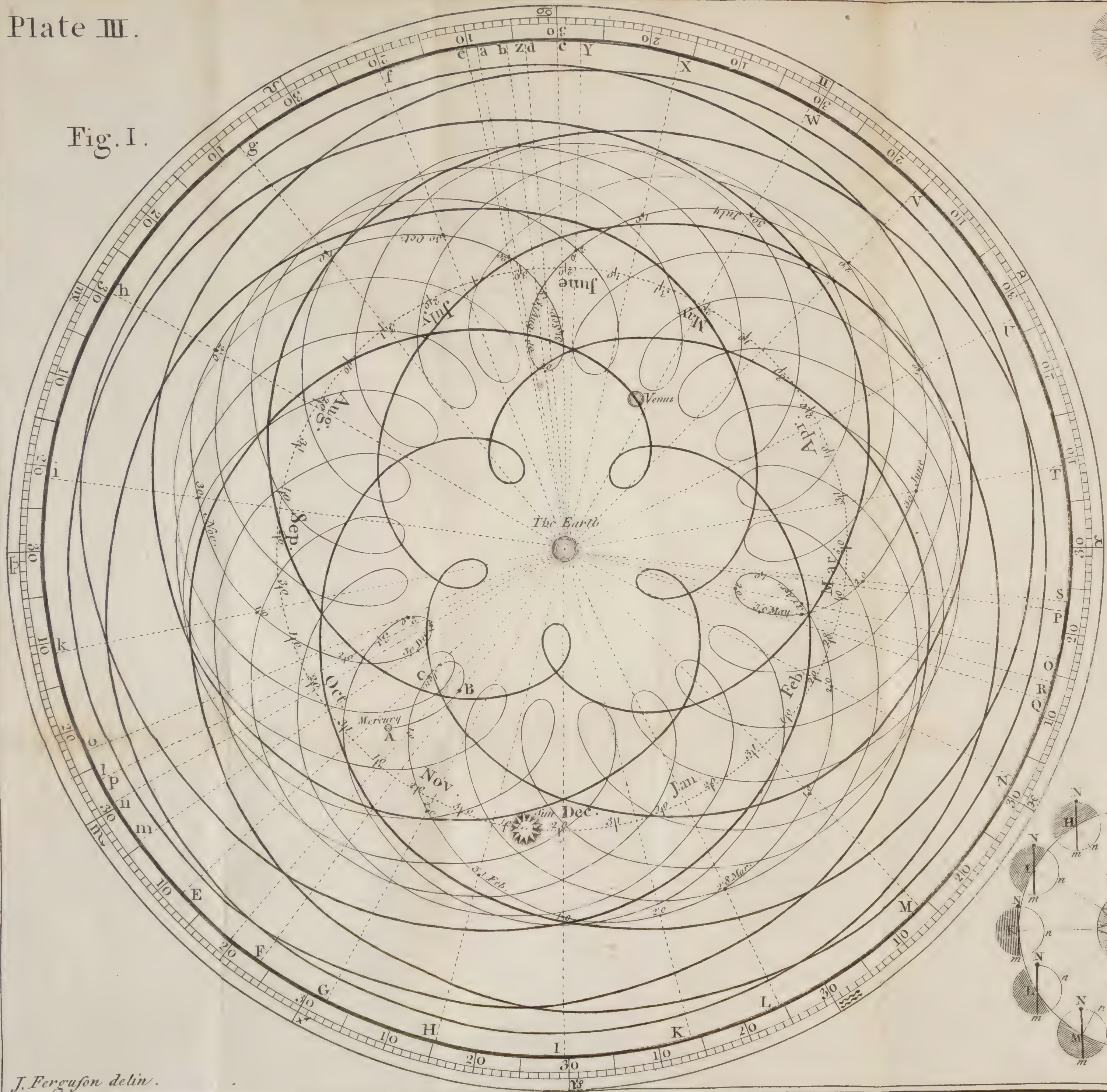


Fig. IIII.

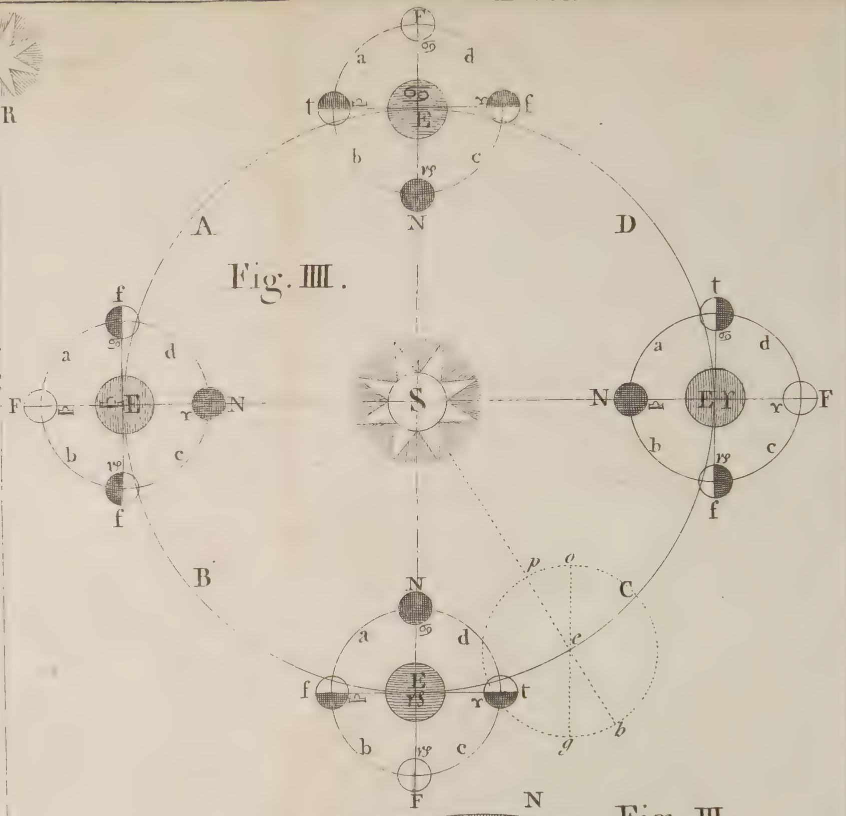


Fig. III.

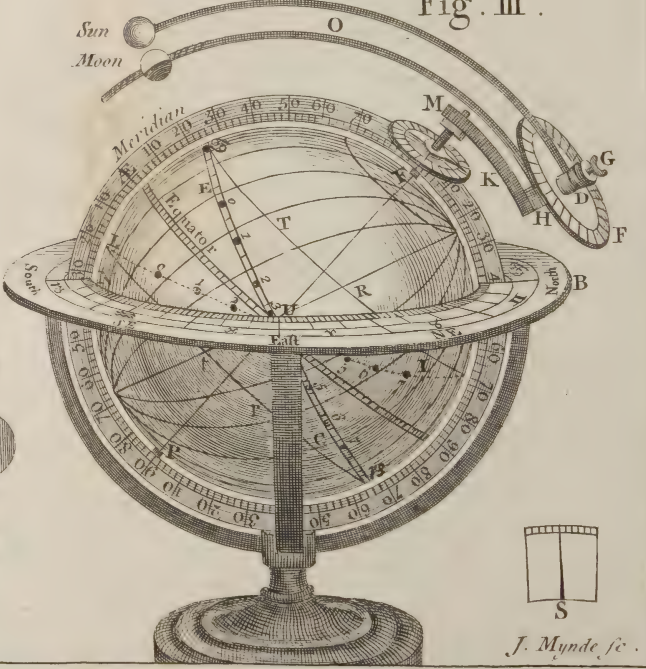
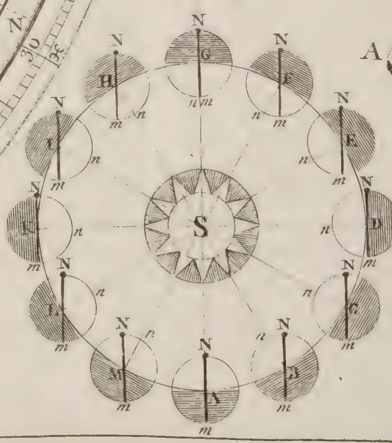


Fig. II.



J. Ferguson delin.

J. Mynde sc.

PLATE III.

each loop next the Earth retrograde; and in all the reſt of their paths direct.

If *Caſſini*'s Figures of the paths of the Sun, Mercury and Venus, were put together, the Figure as above traced out, would be exactly like them. It repreſents the Sun's apparent motion round the Ecliptic, which is the ſame every year; Mercury's motion for ſeven years; and Venus's for eight; in which time Mercury's path makes 23 loops, croſſing itſelf ſo many times, and Venus's only five. In eight years Venus falls ſo nearly into the ſame apparent path again, as to deviate very little from it in ſome ages; but in what number of years Mercury and the reſt of the Planets would deſcribe the ſame viſible paths over again, I cannot at preſent determine. Having finiſhed the above Figure of the paths of Mercury and Venus, I put the Ecliptic round them as in the Doctor's Book; and added the dotted lines from the Earth to the Ecliptic for ſhewing Mercury's apparent or geocentric motion therein for one year; in which time his path makes three loops, and goes on a little farther; which ſhews that he has three inferior, and as many ſuperior conjunctions with the Sun in that time; and alſo that he is ſix times ſtationary, and thrice retrograde. Let us now trace his motion for one year in the Figure.

Suppoſe Mercury to be ſetting out from *A* towards *B* (between the Earth and left-hand corner of the Plate) and as ſeen from the Earth his motion Fig. I. will then be direct, or according to the order of the Signs. But when he comes to *B*, he appears to ſtand ſtill in the 23d degree of ♏ at *F*, as ſhewn by the line *BF*. Whilſt he goes from *B* to *C*, the line *BF*, ſuppoſed to move with him, goes backward from *F* to *E*, or contrary to the order of Signs; and when he is at *C*, he appears ſtationary at *E*; having gone back $11\frac{1}{2}$ degrees. Now, ſuppoſe him ſtationary on the firſt of *January* at *C*, on the 10th thereof he will appear in the Heavens as at 20, near *F*; on the 20th he will be ſeen as at *G*; on the 31ſt at *H*; on the 10th of *February* at *I*; on the 20th at *K*; and on the 28th at *L*; as the dotted lines ſhew, which are drawn through every tenth day's motion in his looped path, and continued to the Ecliptic. On the 10th of *March* he appears at *M*; on the 20th at *N*; and on the 31ſt at *O*. On the 10th of *April* he appears ſtationary at *P*; on the 20th he ſeems to have gone back again to *O*; and on the 30th he appears ſtationary at *Q*, having gone back 11½ degrees. Thus Mercury ſeems to go forward 4 Signs 11 Degrees, or 131 Degrees; and to go back only 11 or 12 Degrees, at a mean rate. From the 30th of *April* to the 10th of *May*, he ſeems to move from *Q* to *R*; and on the 20th he is ſeen at *S*, going forward in the ſame manner again, according to the order of letters; and backward when they go back; which it is needleſs to explain any farther, as the reader can trace him out ſo eaſily, through the reſt of the year. The ſame appearances happen in Venus's motion; but as ſhe moves ſlower than Mercury, there are longer intervals of time between them.

Having already, § 120, given ſome account of the apparent diurnal motions of the Heavens as ſeen from the different Planets, we ſhall not trouble the reader any more with that ſubject.

CHAP. VI.

The Ptolemean *Syſtem refuted. The Motions and Phaſes of Mercury and Venus explained.*

139. THE *Tychonic Syſtem*, § 97, being ſufficiently refuted by the 109th Article, we ſhall ſay nothing more about it.

140. The *Ptolemean Syſtem*, § 96, which aſſerts the Earth to be at reſt in the Center of the Univerſe, and all the Planets with the Sun and Stars to move round it, is evidently falſe and abſurd.

For if this hypotheſis were true, Mercury and Venus could never be hid behind the Sun, as their Orbits are included within the Sun's: and again, theſe two Planets would always move direct, and be as often in Oppoſition to the Sun as in Conjunction with him. But the contrary of all this is true: for they are juſt as often behind the Sun as before him, appear as often to move backwards as forwards, and are ſo far from being ſeen at any time in the ſide of the Heavens oppoſite to the Sun, that they were never ſeen a quarter of a circle in the Heavens diſtant from him.

Appearances of Mercury and Venus.

141. Theſe two Planets, when viewed at different times with a good teleſcope, appear in all the various ſhapes of the Moon; which is a plain proof that they are enlightened by the Sun, and ſhine not by any light of their own: for if they did, they would conſtantly appear round as the Sun does; and could never be ſeen like dark ſpots upon the Sun when they paſs directly between him and us. Their regular Phaſes demonſtrate them to be ſpherical bodies; as may be ſhewn by the following experiment.

Experiment to prove they are round.

Hang an ivory ball by a thread, and let any Perſon move it round the flame of a candle, at two or three yards diſtance from your Eye: when the ball is beyond the candle, ſo as to be almoſt hid by the flame, it's enlightened ſide will be towards you, and appear round like the Full Moon: When the ball is between you and the candle, it's enlightened ſide will diſappear, as the Moon does at the Change: When it is half way between theſe two poſitions, it will appear half illuminated, like the Moon in her Quarters: But in every other place between theſe poſitions, it will appear more or leſs horned or gibbous. If this experiment be made with a flat circular plate, you may make it appear fully enlightened, or not enlightened at all; but can never make it ſeem either horned or gibbous.

PLATE II.

Experiment to repreſent the motions of Mercury and Venus.

142. If you remove about ſix or ſeven yards from the candle, and place yourſelf ſo that it's flame may be juſt about the height of your eye, and then deſire the other perſon to move the ball ſlowly round the candle as before, keeping it as near of an equal height with the flame as he poſſibly can, the ball will appear to you not to move in a circle, but to vibrate backward and forward like a pendulum, moving quickeſt when it is directly between you and the candle, and when directly beyond it; and gradually ſlower as it goes farther to the right or left ſide of the flame, until it appears at the greateſt diſtance from the flame; and then, though it continues to move with the ſame velocity, it will ſeem to ſtand ſtill for a moment. In every Revolution it will ſhew all the above Phaſes, § 141; and if two balls, a ſmaller and a greater, be moved in this manner round the candle, the ſmaller ball being kept neareſt the flame, and carried round almoſt three times as often as the greater, you will have a tolerable good repreſentation of the apparent Motions of Mercury and Venus; eſpecially, if the bigger ball deſcribes a circle almoſt twice as large in diameter as the circle deſcribed by the leſſer.

Fig. III.

143. Let *ABCDE* be a part or ſegment of the viſible Heavens, in which the Sun, Moon, Planets and Stars, appear to move at the ſame diſtance from the Earth *E*. For there are certain limits, beyond which the eye cannot judge of different diſtances; as is plain from the Moon's appearing to be no nearer to us than the Sun and Stars are. Let the circle *fghiklmno* be the Orbit in which Mercury *m* moves round the Sun *S*, according to the order of of the letters. When Mercury is at *f*, he diſappears to the Earth at *E*, becauſe his enlightened ſide is turned from it; unleſs he be then in one of his Nodes, § 20, 25; in which caſe, he will appear like a dark ſpot upon the Sun. When he is at *g* in his Orbit, he appears at *B* in the Heavens, weſtward

The Elongations or Digreſſions of Mercury from the Sun, ward of the Sun *S*, which is ſeen at *C*: when at *h*, he appears at *A*, at his greateſt weſtern elongation or diſtance from the Sun; and then ſeems to ſtand ſtill. But, as he moves from *h* to *i*, he appears to go from *A* to *B*; and ſeems to be in the ſame place when at *i* as when he was at *g*, only not near ſo big: at *k* he is hid from the Earth *E* by the Sun *S*; being then in his ſuperior Conjunction. In going from *k* to *l*, he appears to move from *C* to *D*; and when he is at *n*, he appears ſtationary at *E*; being ſeen as far eaſt from the Sun then, as he was weſt from him at *A*. In going from *n* to *o* in his Orbit, he ſeems to go back again in the Heavens, from *E* to *D*; and is ſeen in the ſame place (with reſpect to the Sun) at *o*, as when he was at *l*; but of a larger diameter at *o*, becauſe he is then nearer the Earth *E*: and when he comes to *f*, he again paſſes by the Sun, and diſappears as before. In going from *n* to *h* in his Orbit, he ſeems to go backward in the Heavens from *E* to *A*; and in going from *h* to *n*, he ſeems to go forward from *A* to *E*. As he goes on from *f*, a little of his enlightened ſide at *g* is ſeen from *E*; at *h* he appears half full, becauſe half of his enlightened ſide is ſeen; at *i*, gibbous, or more than half full; and at *k* he would appear quite full, were he not hid from the Earth *E* by the Sun *S*. At *l* he appears gibbous again; at *n* half decreaſed, at *o* horned, and at *f* new like the Moon at her Change. He goes ſooner from his eaſtern ſtation at *n* to his weſtern ſtation at *h*, than from *h* to *n* again; becauſe he goes through leſs than half his Orbit in the former caſe, and more in the latter.

PLATE II.

144. In the ſame Figure, let *FGHIKLMN* be the Orbit in which Venus *v* moves round the Sun *S*, according to the order of the letters: and let *E* be the Earth as before. When Venus is at *F*, ſhe is in her inferior Conjunction; and diſappears like the New Moon, becauſe her dark ſide is toward the Earth. At *G*, ſhe appears half enlightened

Fig. III.

The Elongations and Phaſes of Venus.

to the Earth, like the Moon in her firſt quarter: at *H*, ſhe appears gibbous; at *I*, almoſt full; her enlightened ſide being then nearly towards the Earth: at *K*, ſhe would appear quite full to the Earth *E*; but is hid from it by the Sun *S*: at *L*, ſhe appears upon the decreaſe, or gibbous; at *M*, more ſo; at *N*, only half enlightened; and at *F*, ſhe diſappears again. In moving from *N* to *G*, ſhe ſeems to go backward in the Heavens; and from *G* to *N*, forward: but, as ſhe deſcribes a much greater portion of her Orbit in going from *G* to *N*, than from *N* to *G*, ſhe appears much longer direct than retrograde in her motion. At *N* and *G* ſhe appears ſtationary; as Mercury does at *n* and *h*. Mercury, when ſtationary, ſeems to be only 28 degrees from the Sun; and Venus, when ſo, 47; which is a demonſtration that Mercury's Orbit is included within Venus's, and Venus's within the Earth's.

The greateſt Elongations of Mercury and Venus.

Morning and Evening Star, what.

145. Venus, from her ſuperior Conjunction at *K* to her inferior Conjunction at *F*, is ſeen on the eaſt ſide of the Sun *S* from the Earth *E*; and therefore ſhe ſhines in the Evening after the Sun ſets, and is called *the Evening Star*: for, the Sun being then to the weſtward of Venus, he muſt ſet firſt. From her inferior Conjunction to her ſuperior, ſhe appears on the weſt ſide of the Sun; and therefore riſes before him, for which reaſon ſhe is called *the Morning Star*. When ſhe is about *N* or *G*, ſhe ſhines ſo bright, that bodies caſt ſhadows in the night-time.

The ſtationary places of the Planets variable.

146. If the Earth kept always at *E*, it is evident that the ſtationary places of Mercury and Venus would always be in the ſame points of the Heavens where they were before. For example; whilſt Mercury *m* goes from *h* to *n*, according to the order of the letters, he appears to deſcribe the arc *ABCDE* in the Heavens, direct: and whilſt he goes from *n* to *h*, he ſeems to deſcribe the ſame arc back again, from *E* to *A*, retrograde: always

at *n* and *b* he appears ſtationary at the ſame points *E* and *A* as before. But Mercury goes round his Orbit, from *f* to *f* again, in 88 days; and yet there are 116 days from any one of his Conjunctions, or apparent Stations, to the ſame again: and the places of theſe Conjunctions and Stations are found to be about 114 degrees eaſtward from the points of the Heavens where they were laſt before; which proves that the Earth has not kept all that time at *E*, but has had a progreſſive motion in it's Orbit from *E* to *t*. Venus alſo differs every time in the places of her Conjunctions and Stations; but much more than Mercury; becauſe, as Venus deſcribes a much larger Orbit than Mercury does, the Earth advances ſo much the farther in it's annual path before Venus comes round again.

The Elongations of all Saturn's inferior Planets as ſeen from him.

147. As Mercury and Venus, ſeen from the Earth, have their reſpective Elongations from the Sun, and ſtationary places; ſo has the Earth, ſeen from Mars; and Mars, ſeen from Jupiter; and Jupiter, ſeen from Saturn. That is, to every ſuperior Planet, all the inferior ones have their Stations and Elongations; as Venus and Mercury have to the Earth. As ſeen from Saturn, Mercury never goes more than $2\frac{1}{2}$ degrees from the Sun; Venus $4\frac{1}{3}$; the Earth 6; Mars $9\frac{1}{2}$; and Jupiter $33\frac{1}{4}$: ſo that Mercury, as ſeen from the Earth, has almoſt as great a Digreſſion or Elongation from the Sun, as Jupiter ſeen from Saturn.

A proof of the Earth's annual motion.

148. Becauſe the Earth's Orbit is included within the Orbits of Mars, Jupiter, and Saturn, they are ſeen on all ſides of the Heavens; and are as often in Oppoſition to the Sun as in Conjunction with him. If the Earth ſtood ſtill, they would always appear direct in their motions; never retrograde nor ſtationary. But they ſeem to go juſt as often backward as forward; which, if gravity be allowed to exiſt, affords a ſufficient proof of the Earth's annual motion: and without it's exiſtence, the Planets could never fall from the tangents of their

PLATE II. their Orbits towards the Sun, nor could a ſtone which is once thrown up from the Earth ever fall to the Earth again.

149. As Venus and the Earth are ſuperior Planets to Mercury, they ſhew much the ſame Appearances to him that Mars and Jupiter do to us. Let Mercury *m* be at *f*, Venus *v* at *F*, and the Earth at *E*; in which ſituation Venus hides the Earth from Mercury; but, being in oppoſition to the Sun, ſhe ſhines on Mercury with a full illumined Orb; though, with reſpect to the Earth, ſhe is in conjunction with the Sun, and inviſible. When Mercury is at *f*, and Venus at *G*, her enlightened ſide not being directly towards him, ſhe appears a little gibbous; as Mars does in a like ſituation to us: but, when Venus is at *I*, her enlightened ſide is ſo much towards Mercury at *f*, that ſhe appears to him almoſt of a round figure. At *K*, Venus diſappears to Mercury at *f*, being then hid by the Sun; as well as all our ſuperior Planets are to us, when in conjunction with the Sun. When Venus has, as it were, emerged out of the Sun beams, as at *L*, ſhe appears almoſt full to Mercury at *f*; at *M* and *N*, a little gibbous; quite full at *F*, and largeſt of all; being then in oppoſition to the Sun, and conſequently neareſt to Mercury at *f*; ſhining ſtrongly on him in the night, becauſe her diſtance from him then is ſomewhat leſs than a fifth part of her diſtance from the Earth, when ſhe appears roundeſt to it between *I* and *K*, or between *K* and *L*, as ſeen from the Earth *E*. Conſequently, when Venus is oppoſite to the Sun as ſeen from Mercury, ſhe appears more than 25 times as large to him as ſhe does to us when at the fulleſt. Our caſe is almoſt ſimilar with reſpect to Mars, when he is oppoſite to the Sun; becauſe he is then ſo near the Earth, and has his whole enlightened ſide towards it. But, becauſe the Orbits of Jupiter and Saturn are very large in proportion to the Earth's Orbit, theſe two Planets appear much leſs magnified

Fig. III. General Phenomena of a ſuperior Planet to an inferior.

fied at their Oppoſitions, or diminiſhed at their Conjunctions, than Mars does, in proportion to their mean apparent Diameters. PLATE II.

CHAP. VII.

The phyſical Cauſes of the Motions of the Planets. The Excentricities of their Orbits. The Times in which the Action of Gravity would bring them to the Sun. ARCHIMEDES's *ideal Problem for moving the Earth. The World not eternal.*

150. FROM the uniform projectile motion of bodies in ſtraight lines, and the univerſal power of attraction which draws them off from theſe lines, the curvilineal motions of all the Planets ariſe. If the body *A* be projected along the right line *ABX*, in open Space, where it meets with no reſiſtance, and is not drawn aſide by any other power, it will for ever go on with the ſame velocity, and in the ſame direction. For, the force which moves it from *A* to *B* in any given time, will carry it from *B* to *X* in as much more time, and ſo on, there being nothing to obſtruct or alter it's motion. But if, when this projectile force has carried it, ſuppoſe to *B*, the body *S* begins to attract it, with a power duly adjuſted, and perpendicular to it's motion at *B*, it will then be drawn from the ſtraight line *ABX*, and forced to revolve about *S* in the Circle *BYTU*. When the body *A* comes to *U*, or any other part of it's Orbit, if the ſmall body *u*, within the ſphere of *U*'s attraction, be projected as in the right line *Z*, with a force perpendicular to the attraction of *U*, then *u* will go round *U* in the Orbit *W*, and accompany it in it's whole courſe round the body *S*. Here, *S* may repreſent the Sun, *U* the Earth, and *u* the Moon.

Gravitation and Projection. Fig. IV.

Circular Orbits.

Fig. IV.

151. If a Planet at *B* gravitates, or is attracted, toward the Sun, ſo as to fall from *B* to *y* in the

time that the projectile force would have carried it from *B* to *X*, it will deſcribe the curve *BY* by the combined action of theſe two forces, in the ſame time that the projectile force ſingly would have carried it from *B* to *X*, or the gravitating power ſingly have cauſed it to deſcend from *B* to *y*; and theſe two forces being duly proportioned, and perpendicular to one another, the Planet obeying them both, will move in the circle *BYTU**.

Elliptical Orbits.

152. But if, whilſt the projectile force carries the Planet from *B* to *b*, the Sun's attraction (which conſtitutes the Planet's gravitation) ſhould bring it down from *B* to 1, the gravitating power would then be too ſtrong for the projectile force; and would cauſe the Planet to deſcribe the curve *BC*. When the Planet comes to *C*, the gravitating power (which always increaſes as the ſquare of the diſtance from the Sun *S* diminiſhes) will be yet ſtronger for the projectile force; and by conſpiring in ſome degree therewith, will accelerate the Planet's motion all the way from *C* to *K*; cauſing it to to deſcribe the arcs *BC*, *CD*, *DE*, *EF*, &c. all in equal times. Having it's motion thus accelerated, it thereby gains ſo much centrifugal force, or tendency to fly off at *K* in the line *Kk*, as overcomes the Sun's attraction: and the centrifugal force being too great to allow the Planet to be brought nearer the Sun, or even to move round him in the Circle *Klmn*, &c. it goes off, and aſcends in the curve *KLMN*, &c. it's motion decreaſing as gradually from *K* to *B*, as it increaſed from *B* to *K*, becauſe the Sun's attraction now acts againſt the Planet's projectile motion juſt as much as it acted with it before. When the Planet has got round to *B*, it's projectile force is as much diminiſhed from it's mean ſtate about

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* To make the projectile force balance the gravitating power ſo exactly, as that the body may move in a Circle, the projectile velocity of the body muſt be ſuch as it would have acquired by gravity alone in falling through half the radius of the circle.

PLATE II.

G or *N*, as it was augmented at *K*; and ſo, the Sun's attraction being more than ſufficient to keep the Planet from going off at *B*, it deſcribes the the ſame Orbit over again, by virtue of the ſame forces or powers.

153. A double projectile force will always balance a quadruple power of gravity. Let the Planet at *B* have twice as great an impulſe from thence towards *X*, as it had before; that is, in the ſame length of time that it was projected from *B* to *b*, as in the laſt example, let it now be projected from *B* to *c*; and it will require four times as much gravity to retain it in it's Orbit: that is, it muſt fall as far as from *B* to 4 in the time that the projectile force would carry it from *B* to *c*; otherwiſe it could not deſcribe the curve *BD*, as is evident by the Figure. But, in as much time as the Planet moves from *B* to *C* in the higher part of it's Orbit, it moves from *I* to *K*, or from *K* to *L*, in the lower part thereof; becauſe, from the joint action of theſe two forces, it muſt always deſcribe equal Areas in equal times, throughout it's annual courſe. Theſe Areas are repreſented by the triangles *BSC*, *CSD*, *DSE*, *ESF*, &c. whoſe contents are equal to one another, quite round the Figure.

Fig. IV.

The Planets deſcribe equal Areas in equal times.

154. As the Planets approach nearer the Sun, and recede farther from him, in every Revolution; there may be ſome difficulty in conceiving the reaſon why the power of gravity, when it once gets the better of the projectile force, does not bring the Planets nearer and nearer the Sun in every Revolution, till they fall upon and unite with him. Or why the projectile force, when it once gets the better of gravity, does not carry the Planets farther and farther from the Sun, till it removes them quite out of the ſphere of his attraction, and cauſes them to go in ſtraight lines for ever afterward. But by conſidering the effects of theſe powers as deſcribed in the two laſt Articles, this difficulty will be removed.

A difficulty removed.

moved. Suppoſe a Planet at *B* to be carried by the projectile force as far as from *B* to *b*, in the time that gravity would have brought it down from *B* to 1: by theſe two forces it will deſcribe the curve *BC*. When the Planet comes down to *K*, it will be but half as far from the Sun *S* as it was at *B*; and therefore, by gravitating four times as ſtrongly towards him, it would fall from *K* to *V* in the ſame length of time that it would have fallen from *B* to 1 in the higher part of it's Orbit, that is, through four times as much ſpace; but it's projectile force is then ſo much increaſed at *K*, as would carry it from *K* to *k* in the ſame time; being double of what it was at *B*, and is therefore too ſtrong for the gravitating power, either to draw the Planet to the Sun, or cauſe it to go round him in the circle *Klmn*, &c. which would require it's falling from *K* to *w*, through a greater ſpace than gravity can draw it, whilſt the projectile force is ſuch as would carry it from *K* to *k*: and therefore the Planet aſcends in it's Orbit *KLMN*, decreaſing in it's velocity for the cauſes already aſſigned in § 152.

The Planetary Orbits elliptical.

155. The Orbits of all the Planets are Ellipſes, very little different from Circles: but the Orbits of the Comets are very long Ellipſes; and the lower focus of them all is in the Sun. If we ſuppoſe the mean diſtance (or middle between the greateſt and leaſt) of every Planet and Comet from the Sun to be divided into 1000 equal parts, the Excentricities of their Orbits, both in ſuch parts and in *Engliſh* miles, will be as follow. Mercury's, 210 parts, or 6,720,000 miles; Venus's, 7 parts, or 413,000 miles; the Earth's, 17 parts, or 1,377.000 miles; Mars's, 93 parts, or 11,439,000 miles; Jupiter's, 48 parts, or 20,352,000 miles; Saturn's, 55 parts, or 42,735,000 miles. Of the neareſt of the three forementioned Comets, 1,458,000 miles; of the middlemoſt, 2,025,000,000 miles; and of the outermoſt, 6,600,000,000.

Their Excentricities.

156. By

The above laws ſufficient for motions both in circular and elliptic Orbits.

156. By the above-mentioned law, § 150 *& ſeq.* bodies will move in all kinds of Ellipſes, whether long or ſhort, if the ſpaces they move in be void of reſiſtance. Only, thoſe which move in the longer Ellipſes, have ſo much the leſs projectile force impreſſed upon them in the higher parts of their Orbits; and their velocities, in coming down towards the Sun, are ſo prodigiouſly increaſed by his attraction, that their centrifugal forces in the lower parts of their Orbits are ſo great, as to overcome the Sun's attraction there, and cauſe them to aſcend again towards the higher parts of their Orbits; during which time, the Sun's attraction acting ſo contrary to the motions of thoſe bodies, cauſes them to move ſlower and ſlower, until their projectile forces are diminiſhed almoſt to nothing; and then they are brought back again by the Sun's attraction, as before.

In what times the Planets would fall to the Sun by the power of gravity.

157. If the projectile forces of all the Planets and comets were deſtroyed at their mean diſtances from the Sun, their gravities would bring them down ſo, as that Mercury would fall to the Sun in 15 days 13 hours; Venus in 39 days 17 hours; the Earth or Moon in 64 days 10 hours; Mars in 121 days; Jupiter in 290; and Saturn in 767. The neareſt Comet in 13 thouſand days; the middlemoſt in 23 thouſand days; and the outermoſt in 66 thouſand days. The Moon would fall to the Earth in 4 days 20 hours; Jupiter's firſt Moon would fall to him in 7 hours, his ſecond in 15, his third in 30, and his fourth in 71 hours. Saturn's firſt Moon would fall to him in 8 hours, his ſecond in 12, his third in 19, his fourth in 68 hours, and his fifth in 336. A ſtone would fall to the Earth's center, if there were an hollow paſſage, in 21 minutes 9 ſeconds. Mr. WHISTON gives the following Rule for ſuch Computations. "* It is demonſtrable, that half the Period of any Planet, when it is diminiſhed in the ſeſquialteral propor-

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[*] Aſtronomical Principles of Religion, p. 66.

tion of the number 1 to the number 2, or nearly in the proportion of 1000 to 2828, is the time that it would fall to the center of it's Orbit." This proportion is, when a quantity or number contains another once and a half as much more.

The prodigious attraction of the Sun and Planets.

158. The quick motions of the Moons of Jupiter and Saturn round their Primaries, demonſtrate that theſe two Planets have ſtronger attractive powers than the Earth has. For, the ſtronger that one body attracts another, the greater muſt be the projectile force, and conſequently the quicker muſt be the motion of that other body to keep it from falling to it's primary or central Planet. Jupiter's ſecond Moon is 124 thouſand miles farther from Jupiter than our Moon is from us; and yet this ſecond Moon goes almoſt eight times round Jupiter whilſt our Moon goes only once round the Earth. What a prodigious attractive power muſt the Sun then have, to draw all the Planets and Satellites of the Syſtem towards him; and what an amazing power muſt it have required to put all theſe Planets and Moons into ſuch rapid Motions at firſt! Amazing indeed to us, becauſe impoſſible to be effected by the ſtrength of all the living Creatures in an unlimited number of Worlds; but no ways hard for the Almighty, whoſe Planetarium takes in the whole Univerſe!

ARCHIMEDES's Problem for raiſing the Earth.

159. The celebrated ARCHIMEDES affirmed he could move the Earth, if he had a place at a diſtance from it to ſtand upon to manage his machinery*. This aſſertion is true in Theory, but, upon examination, will be found abſolutely impoſſible in fact, even though a proper place and materials of ſufficient ſtrength could be had.

The ſimpleſt and eaſieſt method of moving a heavy body a little way is by a lever or crow, where a ſmall weight or power applied to the long arm will raiſe a great weight on the ſhort one. But then, the ſmall weight muſt move as much quicker than the great weight, as the latter is heavier than the former; and the length of the long arm of the lever to the length of the ſhort arm muſt be in the ſame proportion. Now, ſuppoſe a man pulls or preſſes the end of the long arm with the force of 200 pound weight, and that the Earth contains in round numbers, 4,000,000,000,000,000,000,000 or 4000 Trillions of cubic feet, each at a mean rate weighing 100 pound; and that the prop or center of motion of the lever is 6000 miles from the Earth's center: in this caſe, the length of the lever from the *Fulcrum* or center of motion to the moving power or weight ought to be 12,000,000,000,000,000,000,000 or 12 Quadrillions of miles; and ſo many miles muſt the power move, in order to raiſe the Earth but one mile: whence it is eaſy to compute, that if ARCHIMEDES, or the power applied, could move as ſwift as a cannon-bullet, it would take 27,000,000,000,000 or 27 Billions of years to raiſe the Earth one inch.

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* *Δὸς ϖȣ̃ ϛῶ, καὶ τὸν κοσμὸν κινήσω, i. e.* Give me a place to ſtand on, and I ſhall move the Earth.

If any other machine, ſuch as a combination of wheels and ſcrews, was propoſed to move the Earth, the time it would require, and the ſpace gone through by the hand that turned the machine, would be the ſame as before. Hence we may learn, that however boundleſs our Imagination and Theory may be, the actual operations of man are confined within narrow bounds; and more ſuited to our real wants than to our deſires.

Hard to determine what Gravity is.

160. The Sun and Planets mutually attract each other: the power by which they do ſo we call *Gravity*. But whether this power be mechanical or no, is very much diſputed. Obſervation proves that the Planets diſturb one another's motions by it, and that it decreaſes according to the ſquares of the diſtances of the Sun and Planets; as light, which is known to be material, likewiſe does.

Hence

Hence Gravity ſhould ſeem to ariſe from the agency of ſome ſubtle matter preſſing towards the Sun and Planets, and acting, like all mechanical cauſes, by contact. But on the other hand, when we conſider that the degree or force of Gravity is exactly in proportion to the quantities of matter in thoſe bodies, without any regard to their bulks or quantities of ſurface, acting as freely on their internal as external parts; it ſeems to ſurpaſs the power of mechaniſm; and to be either the immediate agency of the Deity, or effected by a law originally eſtabliſhed and impreſt on all matter by him. But ſome affirm that matter, being altogether inert, cannot be impreſſed with any Law, even by almighty Power: and that the Deity, or ſome ſubordinate intelligence, muſt therefore be conſtantly impelling the Planets toward the Sun, and moving them with the ſame irregularities and diſturbances which Gravity would cauſe, if it could be ſuppoſed to exiſt. But, if a man may venture to publiſh his own thoughts, it ſeems to me no greater abſurdity, to ſuppoſe the Deity capable of infuſing a Law, or what Laws he pleaſes, into matter, than to ſuppoſe him capable of giving it exiſtence at firſt. The manner of both is equally inconceivable to us; but neither of them imply a contradiction in our ideas: and what implies no contradiction, is within the power of Omnipotence.

161. That the projectile force was at firſt given by the Deity is evident. For, ſince matter can never put itſelf in motion, and all bodies may be moved in any direction whatſoever; and yet the Planets, both primary and ſecondary, move from weſt to eaſt, in planes nearly coincident; whilſt the Comets move in all directions, and in planes very different from one another; theſe motions can be owing to no mechanical cauſe or neceſſity, but to the free will and power of an intelligent Being.

162. Whatever Gravity be, it is plain that it acts every moment of time: for ſhould it's action ceaſe, the projectile force would inſtantly carry off the Planets in ſtraight lines from thoſe parts of their Orbits where Gravity left them. But, the Planets being once put into motion, there is no occaſion for any new projectile force, unleſs they meet with ſome reſiſtance in their Orbits; nor for any mending hand, unleſs they diſturb one another too much by their mutual attractions.

The Planets diſturb one another's motions.

163. It is found that there are diſturbances among the Planets in their motions, ariſing from their mutual attractions when they are in the ſame quarter of the Heavens; and the beſt modern obſervers find that our years are not always preciſely of the ſame length*. Beſides, there is reaſon to believe that the Moon is ſomewhat nearer the Earth now than ſhe was formerly; her periodical month being ſhorter than it was in former ages. For, our Aſtronomical Tables, which in the preſent Age ſhew the times of Solar and Lunar Eclipſes to great preciſion, do not anſwer ſo well for very ancient Eclipſes. Hence it appears, that the Moon does not move in a medium void of all reſiſtance, § 174; and therefore her projectile force being a little weakened, whilſt there is nothing to diminiſh her gravity, ſhe muſt be gradually approaching nearer the Earth, deſcribing ſmaller and ſmaller Circles round it in every Revolution, and finiſhing her Period ſooner, although her abſolute motion

The conſequences thereof.

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* If the Planets did not act mutually upon one another, the areas deſcribed by them would be exactly proportionate to the times of deſcription, § 153. But obſervations prove that theſe areas are not in ſuch exact proportion, and are moſt varied when the greateſt number of Planets are in any particular quarter of the Heavens. When any two Planets are in conjunction, their mutual attractions, which tend to bring them nearer to one another, draws the inferior one a little farther from the Sun, and the ſuperior one a little nearer to him; by which means, the figure of their Orbits is ſomewhat altered; but this alteration is too ſmall to be diſcovered in ſeveral ages.

with regard to ſpace be not ſo quick now as it was formerly: and, therefore, ſhe muſt come to the Earth at laſt; unleſs that Being, which gave her a ſufficient projectile force at the beginning, adds a little more to it in due time. And, as all the Planets move in ſpaces full of ether and light, which are material ſubſtances, they too muſt meet with ſome reſiſtance. And therefore, if their gravities are not diminiſhed, nor their projectile forces increaſed, they muſt neceſſarily approach nearer and nearer the Sun, and at length fall upon and unite with him.

The World not eternal.

164. Here we have a ſtrong philoſophical argument againſt the eternity of the World. For, had it exiſted from eternity, and been left by the Deity to be governed by the combined actions of the above forces or powers, generally called Laws, it had been at an end long ago. And if it be left to them, it muſt come to an end. But we may be certain that it will laſt as long as was intended by it's Author, who ought no more to be found fault with for framing ſo periſhable a work, than for making man mortal.

CHAP. VIII.

Of Light. It's proportional quantities on the different Planets. It's Refractions in Water and Air. The Atmoſphere; it's weight and properties. The Horizontal Moon.

165. LIGHT conſiſts of exceeding ſmall particles of matter iſſuing from a luminous body; as from a lighted candle ſuch particles of matter conſtantly flow in all directions. Dr. NIEWENTYT* computes, that in one ſecond of time there flows 418,660,000,000,000,000,000,000,000,000,000,000,000,000,000,000 particles of light out of a burning candle; which number contains at leaſt

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* Religious Philoſopher, Vol. III. page 65.

6,337,242,000,000 times the number of grains of ſand in the whole Earth; ſuppoſing 100 grains of ſand to be equal in length to an inch, and conſequently, every cubic inch of the Earth to contain one million of ſuch grains.

The dreadful effects that would enſue from their being larger.

166. Theſe amazingly ſmall particles, by ſtriking upon our eyes, excite in our minds the idea of light: and, if they were ſo large as the ſmalleſt particles of matter diſcernible by our beſt microſcopes, inſtead of being ſerviceable to us, they would ſoon deprive us of ſight by the force ariſing from their immenſe velocity, which is above 164 thouſand miles every ſecond *, or 1,230,000 times ſwifter than the motion of a cannon-bullet. And therefore, if the particles of light were ſo large, that a million of them were equal in bulk to an ordinary grain of ſand, we durſt no more open our eyes to the light, than ſuffer ſand to be ſhot point blank againſt them.

How objects become viſible to us.

167. When theſe ſmall particles, flowing from the Sun or from a candle, fall upon bodies, and are thereby reflected to our eyes, they excite in us the idea of that body, by forming it's picture on the retina †. And ſince bodies are viſible on all ſides, light muſt be reflected from them in all directions.

The rays of Light naturally move in ſtraight lines.

168. A ray of light is a continued ſtream of theſe particles, flowing from any viſible body in a ſtraight line. That the rays move in ſtraight, and not in crooked lines, unleſs they be refracted, is evident from bodies not being viſible if we endeavour to look at them through the bore of a bended pipe; and from their ceaſing to be ſeen by the interpoſition of other bodies, as the fixed Stars by the interpoſition of the Moon and Planets, and the Sun wholely or in part by the interpoſition of the Moon, Mercury, or Venus. And that theſe rays do not interfere, or joſtle one another out of their

A proof that they hinder not one another's motions.

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* This will be demonſtrated in the eleventh Chapter.

† A fine net-work membrane in the bottom of the eye.

PLATE II. their ways, in flowing from different bodies all around, is plain from the following Experiment. Make a little hole in a thin plate of metal, and ſet the plate upright on a table, facing a row of lighted candles ſtanding by one another; then place a ſheet of paper or paſteboard at a little diſtance from the other ſide of the plate, and the rays of all the candles, flowing through the hole, will form as many ſpecks of light on the paper as there are candles before the plate; each ſpeck as diſtinct and large, as if there were only one candle to caſt one ſpeck; which ſhews that the rays are no hinderance to each other in their motions, although they all croſs in the hole.

169. Light, and therefore heat ſo far as it depends on the Sun's rays (§ 85, towards the end) decreaſes in proportion to the ſquares of the diſtances of the Planets from the Sun. This is eaſily demonſtrated by a Figure which, together with it's deſcription, I have taken from Dr. SMITH's Optics *. Fig. XI. Let the light which flows from a point *A*, and paſſes through a ſquare hole *B*, be received upon a plane *C*, parallel to the plane of the hole; or, if you pleaſe, let the figure *C* be the ſhadow of the plane *B*; and when the diſtance *C* is double of *B*, the length and breadth of the ſhadow *C* will be each double of the length and breadth of the plane *B*; and treble when *AD* is treble of *AB*; and ſo on: which may be eaſily examined by the light of a candle placed at *A*. Therefore the ſurface of the ſhadow *C*, at the diſtance *AC* double of *AB*, is diviſible into four ſquares, and at a treble diſtance, into nine ſquares, ſeverally equal to the ſquare *B*, as repreſented in the Figure. The light then which falls upon the plane *B*, being ſuffered to paſs to double that diſtance, will be uniformly ſpread over four times the ſpace, and conſequently will be four times thinner

In what proportion light and heat decreaſe at any given diſtance from the Sun.

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* Book I. Art. 57.

thinner in every part of that ſpace; and at a treble diſtance, it will be nine times thinner; and at a quadruple diſtance, ſixteen times thinner, than it was at firſt; and ſo on, according to the increaſe of the ſquare ſurfaces *B*, *C*, *D*, *E*, built upon the diſtances *AB*, *AC*, *AD*, *AE*. Conſequently, the quantities of this rarefied light received upon a ſurface of any given ſize and ſhape whatever, removed ſucceſſively to theſe ſeveral diſtances, will be but one quarter, one ninth, one fixteenth of the whole quantity received by it at the firſt diſtance *AB*. Or in general words, the denſities and quantities of light, received upon any given plane, are diminiſhed in the ſame proportion, as the ſquares of the diſtances of that plane, from the luminous body, are increaſed: and on the contrary, are increaſed in the ſame proportion as theſe ſquares are diminiſhed. PLATE II.

Why the Planets appear dimmer when viewed thro' teleſcopes than by the bare eye.

170. The more a teleſcope magnifies the diſks of the Moon and Planets, they appear ſo much dimmer than to the bare eye; becauſe the teleſcope cannot magnify the quantity of light, as it does the ſurface; and, by ſpreading the ſame quantity of light over a ſurface ſo much larger than the naked eye beheld, juſt ſo much dimmer muſt it appear when viewed by a teleſcope than by the bare eye.

171. When a ray of light paſſes out of one medium * into another, it is refracted, or turned out of it's firſt courſe, more or leſs, as it falls more or leſs obliquely on the refracting ſurface which divides the two mediums. This may be proved by ſeveral experiments; of which we ſhall only give three for example's ſake. 1. In a baſon *FGH* put a piece of money as *DB*, and then retire from it as to *A*, till the edge of the baſon at *E* juſt hides the money from your ſight: then, keep- Fig. VIII.

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* A medium, in this ſenſe, is any tranſparent body, or that through which the rays of light can paſs; as water, glaſs, diamond, air; and even a vacuum is ſometimes called a Medium.

ing your head ſteady, let another perſon fill the baſon gently with water. As he fills it, you will ſee more and more of the piece *DB*; which will be all in view when the baſon is full, and appear as if lifted up to *C*. For, the ray *AEB*, which was ſtraight whilſt the baſon was empty, is now bent at the ſurface of the water in *E*, and turned out of it's rectilineal courſe into the direction *ED*. Or, in other words, the ray *DEK*, that proceeded in a ſtraight line from the edge *D* whilſt the baſon was empty, and went above the eye at *A*, is now bent at *E*; and inſtead of going on in the rectilineal direction *DEK*, goes in the angled direction *DEA*, and by entering the eye at *A* renders the object *DB* viſible. Or, 2dly, place the baſon where the Sun ſhines obliquely, and obſerve where the ſhadow of the rim *E* falls on the bottom, as at *B*: then fill it with water, and the ſhadow will fall at *D*; which proves, that the rays of light, falling obliquely on the ſurface of the water, are refracted, or bent downwards into it.

Refraction of the rays of light.

172. The leſs obliquely the rays of light fall upon the ſurface of any medium, the leſs they are refracted; and if they fall perpendicularly thereon, they are not refracted at all. For, in the laſt experiment, the higher the Sun riſes, the leſs will be the difference between the places where the edge of the ſhadow falls, in the empty and full baſon. And, 3dly, if a ſtick be laid over the baſon, and the Sun's rays be reflected perpendicularly into it from a looking-glaſs, the ſhadow of the ſtick will fall upon the ſame place of the bottom, whether the baſon be full or empty.

173. The denſer that any medium is, the more is light refracted in paſſing through it.

The Atmoſphere.

174. The Earth is ſurrounded by a thin fluid maſs of matter, called the *Air*, or *Atmoſphere*, which gravitates to the Earth, revolves with it in it's diurnal motion, and goes round the Sun with

it every year. This fluid is of an elaſtic or ſpringy nature, and it's lowermoſt parts being preſſed by the weight of all the Air above them, are ſqueezed the cloſer together; and are therefore denſeſt of all at the Earth's ſurface, and gradually rarer the higher up. "It is well known * that the Air near the ſurface of our Earth poſſeſſes a ſpace about 1200 times greater than Water of the ſame weight. And therefore, a cylindric column of Air 1200 feet high is of equal weight with a cylinder of Water of the ſame breadth, and but one foot high. But a cylinder of Air reaching to the top of the Atmoſphere is of equal weight with a cylinder of Water about 33 feet high †; and therefore if from the whole cylinder of Air, the lower part of 1200 feet high is taken away, the remaining upper part will be of equal weight with a cylinder of Water 32 feet high; wherefore, at the height of 1200 feet, or two furlongs, the weight of the incumbent Air is leſs, and conſequently the rarity of the compreſſed Air is greater than near the Earth's ſurface, in the ratio of 33 to 32. And having this ratio, we may compute the rarity of the Air at all heights whatſoever, ſuppoſing the expanſion thereof to be reciprocally proportional to it's compreſſion; and this proportion has been proved by the experiments of Dr. *Hooke* and others. The reſult of the computation I have ſet down in the annexed Table; in the firſt column of which you have the height of the Air in miles, whereof 4000 make a ſemi-diameter of the Earth; in the ſecond the compreſſion of the Air, or the incumbent weight; in the third it's rarity or expanſion, ſuppoſing gravity to decreaſe in the duplicate ratio of the diſtances from the Earth's center. And the ſmall numeral figures are here uſed to ſhew what number of cyphers muſt be joined to the numbers expreſſed by the larger figures, as $0.^{17}1224$ for 0.000000000000000001224, and 26956^{15} for 26956000000000000000.

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* NEWTON's *Syſtem of the World*, p. 120.

† This is evident from pumps, ſince none can draw water higher than 33 feet.

The Air's compreſſion and rarity at different heights.

	Air's	
Height.	Compreſſion.	Expanſion.
0	33	1
5	17.8515	1.8486
10	9.6717	3.4151
20	2.852	11.571
40	0.2525	136.83
400	$0.^{17}1224$	26956^{15}
4000	$0.^{105}4465$	73907^{102}
40000	$0.^{192}1628$	26263^{189}
400000	$0.^{210}7895$	41798^{207}
4000000	$0.^{212}9878$	33414^{209}
Infinite	$0.^{212}9941$	54622^{209}

From the above Table it appears that the Air in proceeding upwards is rarefied in ſuch manner, that a ſphere of that Air which is neareſt the Earth but of one inch diameter, if dilated to an equal rarefaction with that of the Air at the height of ten ſemi-diameters of the Earth, would fill up more ſpace than is contained in the whole Heavens on this ſide the fixed Stars." And it likewiſe appears that the Moon does not move in a perfectly free and unreſiſting medium; although the Air, at a height equal to her diſtance, is at leaſt 34000^{190} times thinner than at the Earth's ſurface; and therefore cannot reſiſt her motion, ſo as to be ſenſible in many ages.

Its weight how found.

175. The weight of the Air, at the Earth's ſurface, is found by experiments made with the air-pump; and alſo by the quantity of mercury that the Atmoſphere balances in the barometer; in which, at a mean ſtate, the mercury ſtands 29½ inches high. And if the tube were a ſquare inch wide, it would at that height contain 29½ cubic inches of mercury, which is juſt 15 pound weight;

and ſo much weight of Air every ſquare inch of the Earth's ſurface ſuſtains; and every ſquare foot 144 times as much, becauſe it contains 144 ſquare inches. Now, as the Earth's ſurface contains, in round numbers, 200,000,000 ſquare miles, it muſt contain no leſs than 5,575,680,000,000,000 ſquare feet; which being multiplied by 2160, the number of pounds on each ſquare foot, amounts to 12,043,468,800,000,000,000 pounds, for the weight of the whole Atmoſphere. At this rate, a middle-ſized man, whoſe ſurface is about 15 ſquare feet, is preſſed by 32,400 pound weight of Air all around; for fluids preſs equally up and down, and on all ſides. But, becauſe this enormous weight is equal on all ſides, and counter-balanced by the ſpring of the Air diffuſed through all parts of our bodies, it is not in the leaſt degree felt by us.

A common miſtake about the weight of the Air.

176. Oftentimes the ſtate of the Air is ſuch, that we feel ourſelves languid and dull; which is commonly thought to be occaſioned by the Air's being foggy and heavy about us. But that the Air is then too light, is evident from the mercury's ſinking in the barometer, at which time it is generally found that the Air has not ſufficient ſtrength to bear up the Vapours which compoſe the Clouds: for, when it is otherwiſe, the Clouds mount high, and the Air is more elaſtic and weighty about us, by which means it balances the internal ſpring of the Air within us, braces up our blood-veſſels and nerves, and makes us briſk and lively.

Without an Atmoſphere the Heavens would always appear dark, and we ſhould have no twilight.

177. According to * Dr. KEILL, and other aſtronomical writers, it is entirely owing to the Atmoſphere that the Heavens appear bright in the day-time. For, without an Atmoſphere, only that part of the Heavens would ſhine in which the Sun was placed: and if we could live without Air, and ſhould turn our backs towards the Sun, the whole Heavens would appear as dark as in the

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* See his Aſtronomy, p. 232.

night,

PLATE II. night, and the Stars would be ſeen as clear as in the nocturnal ſky. In this caſe, we ſhould have no twilight; but a ſudden tranſition from the brighteſt ſunſhine to the blackeſt darkneſs immediately after ſun-ſet; and from the blackeſt darkneſs to the brighteſt ſun-ſhine at ſun riſing; which would be extremely inconvenient, if not blinding, to all mortals. But, by means of the Atmoſphere, we enjoy the Sun's light, reflected from the aerial particles, for ſome time before he riſes and after he ſets. For, when the Earth by it's rotation has withdrawn the Sun from our ſight, the Atmoſphere being ſtill higher than we, has his light imparted to it; which gradually decreaſes until he has got 18 degrees below the Horizon; and then, all that part of the Atmoſphere which is above us is dark. From the length of twilight, the Doctor has calculated the height of the Atmoſphere (ſo far as it is denſe enough to reflect any light) to be about 44 miles. But it is ſeldom denſe enough at two miles height to bear up the Clouds.

It brings the Sun in view before he riſes, and keeps him in view after he ſets.

178. The Atmoſphere refracts the Sun's rays ſo, as to bring him in ſight every clear day, before he riſes in the Horizon; and to keep him in view for ſome minutes after he is really ſet below it. For, at ſome times of the year, we ſee the Sun ten minutes longer above the Horizon than he would be if there were no refractions: and about ſix minutes every day at a mean rate.

Fig. IX.

179. To illuſtrate this, let *IEK* be a part of the Earth's ſurface, covered with the Atmoſphere *HGFC*; and let *HEO* be the * ſenſible Horizon of an obſerver at *E*. When the Sun is at *A*, really below the Horizon, a ray of light *AC* proceeding from him comes ſtraight to *C*, where it falls on the ſurface of the Atmoſphere, and there entering a denſer medium, it is turned out of it's rectilineal

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* As far as one can ſee round him on the Earth.

courſe *ACdG*, and bent down to the obſerver's eye at *E*; who then ſees the Sun in the direction of the refracted ray *Ede*, which lies above the Horizon, and being extended out to the Heavens, ſhews the Sun at *B*, § 171.

180. The higher the Sun riſes, the leſs his rays are refracted, becauſe they fall leſs obliquely on the ſurface of the Atmoſphere, § 172. Thus, when the Sun is in the direction of the line *EfL* continued, he is ſo nearly perpendicular to the ſurface of the Earth at *E*, that his rays are but very little bent from a rectilineal courſe.

The quantity of Refraction.

181. The Sun is about $32\frac{1}{4}$ min. of a deg. in breadth, when at his mean diſtance from the Earth; and the horizontal refraction of his rays is $33\frac{3}{4}$ min. which being more than his whole diameter, brings all his Diſc in view, when his uppermoſt edge riſes in the Horizon. At ten deg. height the refraction is not quite 5 min.; at 20 deg. only 2 min. 26 ſec.; at 30 deg. but 1 min. 32 ſec.; between which and the Zenith, it is ſcarce ſenſible: the quantity throughout, is ſhewn by the annexed table, calculated by Sir Isaac Newton.

182. *A* TABLE *ſhewing the Refractions of the Sun, Moon, and Stars; adapted to their apparent Altitudes.*

Appar. Alt.		Refraction.		Ap. Alt.	Refraction.		Ap. Alt.	Refraction.	
D.	M.	M.	S.	D.	M.	S.	D.	M.	S.
0	0	33	45	21	2	18	56	0	36
0	15	30	24	22	2	11	57	0	35
0	30	27	35	23	2	5	58	0	34
0	45	25	11	24	1	59	59	0	32
1	0	23	7	25	1	54	60	0	31
1	15	21	20	26	1	49	61	0	30
1	30	19	46	27	1	44	62	0	28
1	45	18	22	28	1	40	63	0	27
2	0	17	8	29	1	36	64	0	26
2	30	15	2	30	1	32	65	0	25
3	0	13	20	31	1	28	66	0	24
3	30	11	57	32	1	25	67	0	23
4	0	10	48	33	1	22	68	0	22
4	30	9	50	34	1	19	69	0	21
5	0	9	2	35	1	16	70	0	20
5	30	8	21	36	1	13	71	0	19
6	0	7	45	37	1	11	72	0	18
6	30	7	14	38	1	8	73	0	17
7	0	6	47	39	1	6	74	0	16
7	30	6	22	40	1	4	75	0	15
8	0	6	0	41	1	2	76	0	14
8	30	5	40	42	1	0	77	0	13
9	0	5	22	43	0	58	78	0	12
9	30	5	6	44	0	56	79	0	11
10	0	4	52	45	0	54	80	0	10
11	0	4	27	46	0	52	81	0	9
12	0	4	5	47	0	50	82	0	8
13	0	3	47	48	0	48	83	0	7
14	0	3	31	49	0	47	84	0	6
15	0	3	17	50	0	45	85	0	5
16	0	3	4	51	0	44	86	0	4
17	0	2	53	52	0	42	87	0	3
18	0	2	43	53	0	40	88	0	2
19	0	2	34	54	0	39	89	0	1
20	0	2	26	55	0	38	90	0	0

PLATE II.

183. In all obſervations, to have the true altitude of the Sun, Moon, or Stars, the refraction muſt be ſubtracted from the obſerved altitude. But the quantity of refraction is not always the ſame at the ſame altitude; becauſe heat diminiſhes the Air's refractive power and denſity, and cold increaſes both; and therefore no one table can ſerve preciſely for the ſame place at all ſeaſons, nor even at all times of the ſame day; much leſs for different climates: it having been obſerved that the horizontal refractions are near a third part leſs at the Equator than at *Paris*, as mentioned by Dr. SMITH in the 370th remark on his Optics, where the following account is given of an extraordinary refraction of the Sun-beams by cold. "There is a famous obſervation of this kind made by ſome *Hollanders* that wintered in *Nova Zembla* in the year 1596, who were ſurprized to find, that after a continual night of three months, the Sun began to riſe ſeventeen days ſooner than according to computation, deduced from the Altitude of the Pole obſerved to be 76°: which cannot otherwiſe be accounted for, than by an extraordinary quantity of refraction of the Sun's rays, paſſing through the cold denſe air in that climate. KEPLER computes that the Sun was almoſt five degrees below the Horizon when he firſt appeared; and conſequently the refraction of his rays was about nine times greater than it is with us."

The inconſtancy of Refractions.

A very remarkable caſe concerning refraction.

184. The Sun and Moon appear of an oval figure, as *FCGD*, juſt after their riſing, and before their ſetting: the reaſon is, that the refraction being greater in the Horizon than at any diſtance above it, the lowermoſt limb *G* appears more elevated than the uppermoſt. But although the refraction ſhortens the vertical Diameter *FG*, it has no ſenſible effect on the horizontal Diameter *CD*, which is all equally elevated. When the refraction is ſo ſmall as to be imperceptible, the Sun and Moon appear perfectly round, as *AEBF*.

Fig. X.

185.

Our imagination cannot judge rightly of the diſtance of inacceſſible objects.

185. We daily obſerve, that the objects which appear moſt diſtinct are generally thoſe which are neareſt to us; and conſequently, when we have nothing but our imagination to aſſiſt us in eſtimating of diſtances, bright objects ſeem nearer to us than thoſe which are leſs bright, or than the ſame objects do when they appear leſs bright and worſe defined, even though their diſtance in both caſes be the ſame. And if in both caſes they are ſeen under the ſame Angle *, our imagination naturally

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PLATE II. Fig. V.

* An Angle is the inclination of two right lines, as *IH* and *KH*, meeting in a point at *H*; and in deſcribing an Angle by three letters, the middle letter always denotes the angular point: thus, the above lines *IH* and *KH* meeting each other at *H*, make the Angle *IHK*. And the point *H* is ſuppoſed to be the center of a Circle, the circumference of which contains 360 equal parts, called Degrees. A fourth part of a Circle, called a Quadrant, as *GE*, contains 90 degrees; and every Angle is meaſured by the number of degrees in the Arc it cuts off; as the Angle *EHP* is 45 degrees, the Angle *EHF* 33, &c. and ſo the Angle *EHF* is the ſame with the Angle *CHN*, and alſo with the Angle *AHM*, becauſe they all cut off the ſame Arc or portion of the Quadrant *EG*; and ſo likewiſe the Angle *EHF* is greater than the Angle *CHD* or *AHL*, becauſe it cuts off a greater Arc.

The nearer an object is to the eye, the bigger it appears, and under the greater Angle is it ſeen. To illuſtrate this a little, ſuppoſe an Arrow in the poſition *IK*, perpendicular to the right line *HA* drawn from the eye at *H* through the middle of the Arrow at *O*. It is plain that the Arrow is ſeen under the Angle *IHK*, and that *HO*, which is it's diſtance from the eye, divides into halves both the Arrow and the Angle under which it is ſeen; *viz.* the Arrow into *IO* *OK* and the Angle into *IHO* and *KHO*: and this will be the caſe whatever diſtance the Arrow is placed at. Let now three Arrows, all of the ſame length with *IK*, be placed at the diſtances *HA*, *HC*, *HE*, ſtill perpendicular to, and biſected by the right line *HA*; then will *AB*, *CD*, *EF*. be each equal to, and repreſent *IO*; and *AB* (the ſame as *IO*) will be ſeen from *H* under the Angle *AHB*; but *CD* (the ſame as *IO*) will be ſeen under the Angle *CHD* or *AHL*; and *EF* the ſame as *IO*) will be ſeen under the Angle *EHF*, or *CHN*, or *AHM*. Alſo, *EF* or *IO* at the diſtance *HE* will appear as long as *CN* would at the diſtance *HC*, or as *AM* would at the diſtance *HA*; and *CD* or *IO* at the diſtance *HC* will appear as long as *AL* would at the diſtance *HA*.

rally ſuggeſts an idea of a greater diſtance between us and thoſe objects which appear fainter and worſe defined than thoſe which appear brighter under the ſame Angles; eſpecially if they be ſuch objects as we were never near to, and of whoſe real Magnitudes we can be no judges by ſight.

Nor always of thoſe which are acceſſible.

186. But, it is not only in judging of the different apparent Magnitudes of the ſame objects, which are better or worſe defined by their being more or leſs bright, that we may be deceived: for we may make a wrong concluſion even when we view them under equal degrees of brightneſs, and under equal Angles; although they be objects whoſe bulks we are generally acquainted with, ſuch as houſes or trees: for proof of which, the two following inſtances may ſuffice.

The reaſon aſſigned.

Firſt, When a houſe is ſeen over a very broad river by a perſon ſtanding on low ground, who ſees nothing of the river, nor knows of it beforehand; the breadth of the river being hid from him, becauſe the banks ſeem contiguous, he loſes the idea of a diſtance equal to that breadth; and the houſe ſeems ſmall, becauſe he refers it to a leſs diſtance than it really is at. But, if he goes to a place from which the river and interjacent ground can be ſeen, though no farther from the houſe, he then perceives the houſe to be at a greater diſtance than he imagined; and therefore fancies it to be bigger than he did at firſt; although in both caſes it appears under the ſame Angle, and conſequently makes no bigger picture on the retina of his eye in the latter caſe than it did in the former. Many have been deceived, by taking a red coat of arms, fixed upon the iron gate in *Clare Hall* walks at

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HA. So that as an object approaches the eye, both it's Magnitude and the Angle under which it is ſeen increaſe; and as the object recedes, the contrary.

PLATE II. *Cambridge*, for a brick houſe at a much greater diſtance *.

Secondly, In foggy weather, at firſt ſight, we generally imagine a ſmall houſe, which is juſt at hand, to be a great caſtle at a diſtance; becauſe it appears ſo dull and ill defined when ſeen through the Miſt, that we refer it to a much greater diſtance than it really is at; and therefore, under the ſame Angle, we judge it to be much bigger. For, the near object *FE*, ſeen by the eye *ABD*, appears under the ſame Angle *GCH*, that the remote object *GHI* does: and the rays *GFCN* and *HECM* Fig. XII. croſſing one another at *C* in the pupil of the eye, limit the ſize of the picture *MN* on the retina; which is the picture of the object *FE*, and if *FE* were taken away, would be the picture of the object *GHI*, only worſe defined; becauſe *GHI*, being farther off, appears duller and fainter than *FE* did. But when a Fog, as *KL*, comes between the eye and the object *FE*, it appears dull and ill defined like *GHI*; which cauſes our imagination to refer *FE* to the greater diſtance *CH*, inſtead of the ſmall diſtance *CE* which it really is at. And conſequently, as miſ-judging the diſtance does not in the leaſt diminiſh the Angle under which the object appears, the ſmall hay-rick *FE* ſeems to be as big as *GHI*.

* The fields which are beyond the gate riſe gradually till they are juſt ſeen over it; and the arms, being red, are often miſtaken for a houſe at a conſiderable diſtance in thoſe fields.

I once met with a curious deception in a gentleman's garden at *Hackney*, occaſioned by a large pane of glaſs in the garden-wall at ſome diſtance from his houſe. The glaſs (through which the fields and ſky were diſtinctly ſeen) reflected a very faint image of the houſe; but the image ſeemed to be in the Clouds near the Horizon, and at that diſtance looked as if it were a huge caſtle in the Air. Yet, the Angle under which the image appeared, was equal to that under which the houſe was ſeen: but the image being mentally referred to a much greater diſtance than the houſe, appeared much bigger to the imagination.

PLATE II. Fig. IX.

Why the Sun and Moon appear biggeſt in the Horizon.

187. The Sun and Moon appear bigger in the Horizon than at any conſiderable height above it. Theſe Luminaries, although at great diſtances from the Earth, appear floating, as it were, on the ſurface of our Atmoſphere *HGFfeC*, a little way beyond the Clouds; of which, thoſe about *F*, directly over our heads at *E*, are nearer us than thoſe about *H* or *e* in the Horizon *HEe*. Therefore, when the Sun or Moon appear in the Horizon at *e*, they are not only ſeen in a part of the Sky which is really farther from us than if they were at any conſiderable Altitude, as about *f*; but they are alſo ſeen through a greater quantity of Air and Vapours at *e* than at *f*. Here we have two concurring appearances which deceive our imagination, and cauſe us to refer the Sun and Moon to a greater diſtance at their riſing or ſetting about *e*, than when they are conſiderably high, as at *f*: firſt, their ſeeming to be on a part of the Atmoſphere at *e*, which is really farther than *f* from a ſpectator at *E*; and ſecondly, their being ſeen through a groſſer medium when at *e* than when at *f*; which, by rendering them dimmer, cauſes us to imagine them to be at a yet greater diſtance. And as, in both caſes, they are ſeen * much under the ſame Angle, we naturally judge them to be biggeſt when they ſeem fartheſt from us; like the above-mentioned houſe, § 186, ſeen from a higher ground, which ſhewed it to be farther off than it appeared from low ground; or the hay-rick, which appeared at a greater diſtance by means of an interpoſing Fog.

Their apparent Diameters are not leſs on the Meridian than in the Horizon.

188. Any one may ſatisfy himſelf that the Moon appears under no greater Angle in the Horizon than on the Meridian, by taking a large ſheet of paper, and rolling it up in the form of a Tube, of ſuch a width, that obſerving the Moon through

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* The Sun and Moon ſubtend a greater Angle on the Meridian than in the Horizon, being nearer the Obſerver's Place in the former caſe than in the latter.

it when ſhe riſes, ſhe may, as it were, juſt fill the Tube; then tie a thread round it to keep it of that ſize; and when the Moon comes to the Meridian, and appears much leſs to the eye, look at her again through the ſame Tube, and ſhe will fill it juſt as much, if not more, than ſhe did at her riſing.

189. When the full Moon is in *perigeo*, or at her leaſt diſtance from the Earth, ſhe is ſeen under a larger Angle, and muſt therefore appear bigger than when ſhe is Full at other times: and if that part of the Atmoſphere where ſhe riſes be more replete with Vapours than uſual, ſhe appears ſo much the dimmer; and therefore we fancy her to be ſtill the bigger, by referring her to an unuſually great diſtance; knowing that no objects which are very far diſtant can appear big unleſs they be really ſo.

CHAP. IX.

The Method of finding the Diſtances of the Sun, Moon, and Planets.

190. THOSE who have not learnt how to take the * Altitude of any Celeſtial Phenomenon by a common Quadrant, nor know any

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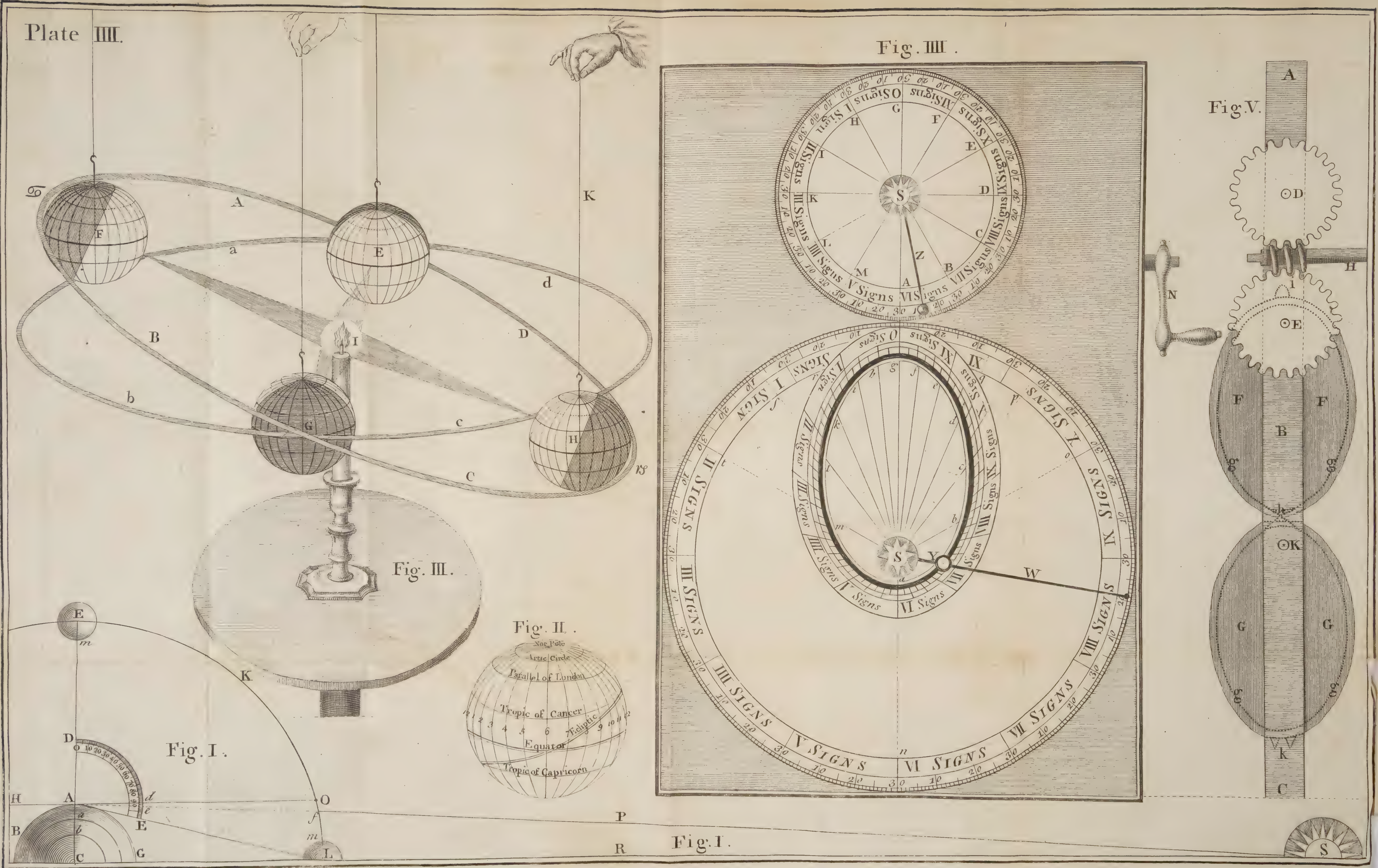
* The Altitude of any celeſtial Phenomenon is an arc of the Sky intercepted between the Horizon and the Phenomenon. In Fig. VI. of Plate II. let *HOX* be a horizontal line, ſuppoſed to be extended from the eye at *A* to *X*, where the Sky and Earth ſeem to meet at the end of a long and level plain; and let *S* be the Sun. The arc *XY* will be the Sun's height above the Horizon at *X*, and is found by the inſtrument *ECD*, which is a quadrantal board, or plate of metal, divided into 90 equal parts or degrees on it's limb *DPC*; and has a couple of little braſs plates, as *a* and *b*, with a ſmall hole in each of them, called *Sight-Holes*, for looking through, parallel to the edge of the Quadrant whereon they ſtand. To the center *E* is fixed one end of a thread *F*, called *the Plumb-Line*, which has a ſmall weight or plummet *P* fixed to its other end. Now, if an obſerver holds the Quadrant upright, without inclining it to either

Plate IIII.



J. Ferguson delin.

J. Mynde Sculp.

any thing of Plain Trigonometry, may paſs over the firſt Article of this ſhort Chapter, and take the Aſtronomer's word for it, that the diſtances of the Sun and Planets are as ſtated in the firſt Chapter of this Book. But, to every one who knows how to take the Altitude of the Sun, the Moon, or a Star, and can ſolve a plain right-angled Triangle, the following method of finding the diſtances of the Sun and Moon will be eaſily underſtood. PLATE IV.

Let *BAG* be one half of the Earth, *AC* it's ſemi-diameter, *S* the Sun, *m* the Moon, and *EKOL* a quarter of the Circle deſcribed by the Moon in revolving from the Meridian to the Meridian again. Let *CRS* be the rational Horizon of an obſerver at *A*, extended to the Sun in the Heavens; and *HAO* his ſenſible Horizon, extended to the Moon's Orbit. *ALC* is the angle under which the Earth's ſemi-diameter *AC* is ſeen from the Moon at *L*, which is equal to the Angle *OAL*, becauſe the right lines *AO* and *CL* which include both theſe Angles are parallel. *ASC* is the Angle Fig. I.

either ſide, and ſo that the Horizon at *X* is ſeen through the ſight-holes *a* and *b*. the plumb-line will cut or hang over the beginning of the degrees at 0, in the edge *EC*; but if he elevates the Quadrant ſo as to look through the ſight-holes at any part of the Heavens, ſuppoſe to the Sun at *S*; juſt ſo many degrees as he elevates the ſight-hole *b* above the horizontal line *HOX*, ſo many degrees will the plumb-line cut in the limb *CP* of the Quadrant. For, let the obſerver's eye at *A* be in the center of the celeſtial Arc *XYV* (and he may be ſaid to be in the center of the Sun's apparent diurnal Orbit, let him be on what part of the Earth he will) in which Arc the Sun is at that time, ſuppoſe 25 degrees high, and let the obſerver hold the Quadrant ſo that he may ſee the Sun through the ſight-holes; the plumb-line freely playing on the Quadrant will cut the 25th degree in the limb *CP*, equal to the number of degrees of the Sun's Altitude at the time of obſervation. *N. B.* Whoever looks at the Sun, muſt have a ſmoked glaſs before his eyes to ſave them from hurt. The better way is not to look at the Sun through the ſight-holes, but to hold the Quadrant facing the eye, at a little diſtance, and ſo that the Sun ſhining through one hole, the ray may be ſeen to fall on the other.

under which the Earth's ſemi-diameter *AC* is ſeen from the Sun at *S*, and is equal to the Angle *OAf*, becauſe the lines *AO* and *CRS* are parallel. Now, it is found by obſervation, that the Angle *OAL* is much greater than the Angle *OAf*; but *OAL* is equal to *ALC*, and *OAf* is equal to *ASC*. Now, as *ASC* is much leſs than *ALC*, it proves that the Earth's ſemi-diameter *AC* appears much greater as ſeen from the Moon at *L*, than from the Sun at *S*; and therefore the Earth is much farther from the Sun than from the Moon *. The Quantities of theſe Angles are determined by obſervation in the following manner.

Let a graduated inſtrument, as *DAE* (the larger the better) having a moveable Index with Sight-holes, be fixed in ſuch a manner, that it's plane ſurface may be parallel to the Plane of the Equator, and it's edge *AD* in the Meridian: ſo that when the Moon is in the Equinoctial, and on the Meridian *ADE*, ſhe may be ſeen through the ſight-holes when the edge of the moveable index cuts the beginning of the diviſions at o, on the graduated limb *DE*; and when ſhe is ſo ſeen, let the *preciſe* time be noted. Now, as the Moon revolves about the Earth from the Meridian to the Meridian again in 24 hours 48 minutes, ſhe will go a fourth part round it in a fourth part of that time, *viz.* in 6 hours 12 minutes, as ſeen from *C*, that is, from the Earth's center or Pole. But as ſeen from *A*, the obſerver's place on the Earth's ſurface, the Moon will ſeem to have gone a quarter round the Earth when ſhe comes to the ſenſible Horizon at *O*; for the Index through the ſights of which ſhe is then viewed will be at *d*, 90 degrees from *D*, where it was when ſhe was ſeen at *E*. Now, let the exact moment when the Moon is ſeen at *O* (which will be when ſhe is in or near the ſenſible Horizon) be carefully noted *, that it may be known in what time ſhe has gone from *E* to *O*; which time ſubtracted from 6 hours 12 minutes (the time of her going from *E* to *L*) leaves the time of her going from *O* to *L*, and affords an eaſy method for finding the Angle *OAL* (called *the Moon's horizontal Parallax*, which is equal to the Angle *ALC*) by the following Analogy: As the time of the Moon's deſcribing the Arc *EO* is to 90 degrees, ſo is 6 hours 12 minutes to the degrees of the Arc *DdE*, which meaſures the Angle *EAL*; from which ſubtract 90 degrees, and there remains the Angle *OAL*, equal to the Angle *ALC*, under which the Earth's ſemi-diameter *AC* is ſeen from the Moon. Now, ſince all the Angles of a right-lined Triangle are equal to 180 degrees, or to two right Angles, and the ſides of a Triangle are always proportional to the Sines of the oppoſite Angles, ſay, by the *Rule of Three*, as the Sine of the Angle *ALC* at the Moon *L* is to it's oppoſite ſide *AC*, the Earth's ſemi-diameter, which is known to be 3985 miles, ſo is Radius, *viz.* the Sine of 90 degrees, or of the right Angle *ACL*, to it's oppoſite ſide *AL*, which is the Moon's diſtance at *L* from the obſerver's place at *A* on the Earth's ſurface; or, ſo is the Sine of the Angle *CAL* to it's oppoſite ſide *CL*, which is the Moon's diſtance from the Earth's center, and comes out at a mean rate to be 240,000 miles. The Angle *CAL* is equal to what *OAL* wants of 90 degrees.

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* See the Note on § 185.

The Moon's horizontal Parallax, what.

The Moon's diſtance determined.

191. The Sun's diſtance from the Earth is found the ſame way, but with much greater difficulty; becauſe his horizontal Parallax, or the Angle *OAS* equal to the Angle *ASC*, is ſo ſmall, as to be hardly perceptible, being only 10 ſeconds of a minute, or the 360th part of a degree. But

The Sun's diſtance cannot be yet ſo exactly determined as the Moon's.

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* Here proper allowance muſt be made for the Refraction, which being about 34 minutes of a degree in the Horizon, will cauſe the Moon's center to appear 34 minutes above the Horizon when her center is really in it.

the Moon's horizontal Parallax, or Angle *OAL* equal to the Angle *ALC*, is very diſcernible, being 57′ 49″, or 3469″ at it's mean ſtate; which is more than 340 times as great as the Sun's: and therefore, the diſtances of the heavenly bodies being inverſely as the Tangents of their horizontal Parallaxes, the Sun's diſtance from the Earth is at leaſt 340 times as great as the Moon's; and is rather under-rated at 81 millions of miles, when the Moon's diſtance is certainly known to be 240 thouſand. But becauſe, according to ſome Aſtronomers, the Sun's horizontal Parallax is 11 ſeconds, and according to others only 10, the former Parallax making the Sun's diſtance to be about 75,000,000 of miles, and the latter 82,000,000; we may take it for granted, that the Sun's diſtance is not leſs than as deduced from the former, nor more than as ſhewn by the latter: and every one who is accuſtomed to make ſuch obſervations, knows how hard it is, if not impoſſible, to avoid an error of a ſecond; eſpecially on account of the inconſtancy of horizontal Refractions. And here, the error of one ſecond, in ſo ſmall an Angle, will make an error of 7 millions of miles in ſo great a diſtance as that of the Sun's. But Dr. HALLEY has ſhewn us how the Sun's diſtance from the Earth, and conſequently the diſtances of all the Planets from the Sun, may be known to within a 500th part of the whole, by a Tranſit of Venus over the Sun's Diſc, which will happen on the 6th of *June*, in the year 1761; till which time we muſt content ourſelves with allowing the Sun's diſtance to be about 81 millions of miles, as commonly ſtated by Aſtronomers.

How near the truth it may ſoon be determined.

192. The Sun and Moon appear much about the ſame bulk: And every one who underſtands Geometry, knows how their true bulks may be deduced from the apparent, when their real diſtances are known. Spheres are to one another as the Cubes of their Diameters; whence, if the Sun be

The Sun proved to be much bigger than the Moon.

be 81 millions of miles from the Earth, to appear as big as the Moon, whoſe diſtance does not exceed 240 thouſand miles, he muſt, in ſolid bulk, be 42 millions 875 thouſand times as big as the Moon.

193. The horizontal Parallaxes are beſt obſerved at the Equator; 1. Becauſe the heat is ſo nearly equal every day, that the Refractions are almoſt conſtantly the ſame. 2. Becauſe the parallactic Angle is greater there, as at *A* (the diſtance from thence to the Earth's Axis being greater) than upon any parallel of Latitude, as *a* or *b*.

194. The Earth's diſtance from the Sun being determined, the diſtances of all the other Planets from him are eaſily found by the following analogy, their periods round him being aſcertained by obſervation. As the ſquare of the Earth's period round the Sun is to the cube of it's diſtance from him, ſo is the ſquare of the period of any other Planet to the cube of it's diſtance, in ſuch parts or meaſures as the Earth's diſtance was taken; ſee § 111. This proportion gives us the relative mean diſtances of the Planets from the Sun to the greateſt degree of exactneſs; and they are as follows, having been deduced from their periodical times, according to the law juſt mentioned, which was diſcovered by Kepler, and demonſtrtaed by Sir Isaac Newton.

The relative diſtances of the Planets from the Sun are known to great preciſion, though their real diſtances are not well known.

Periodical Revolution to the ſame fixed Star in days and decimal parts of a day.

Mercury	Venus	The Earth	Mars	Jupiter	Saturn
87.9692	224.6176	365.2564	686.9785	4332.514	10759.275

Relative mean diſtances from the Sun.

38710	72333	100000	152369	520096	954006

From theſe numbers we deduce, that if the Sun's horizontal Parallax be 10″, *the real mean diſtances of the Planets from the Sun in Engliſh miles are*

31,742,200	59,313,060	82,000,000	124,942,580	426,478,720	782,284,920

But if the Sun's Parallax be 11″, *their diſtances are no more than*

29,032,500	54,238,570	75,000,000	114,276,750	390,034,500	715,504,500

Errors in diſtance ariſing from the miſtake of 1″ *in the Sun's Parallax.*

2,709,700	5,074,490	7,000,000	10,665,830	36,444,220	66,780,420

But, from the late Tranſit of Venus, A. D. 1761, *the Sun's Parallax appears to be only* $8' \frac{6}{100}$; *and according to that, their real diſtances in miles are*

36,668,373	68,518,044	94,725,840	144,588,575	492,665,307	903,690,197.

195. Theſe numbers ſhew, that although we have the relative diſtances of the Planets from the Sun to the greateſt nicety, yet the beſt obſervers could not aſcertain their true diſtances, until the late long wiſhed-for Tranſit appeared, which we muſt confeſs was embarraſſed with ſeveral difficulties. But there will be another Tranſit of Venus over the Sun on the third of *June*, 1769, much better ſuited to this great Problem.—We wiſh the Sky may be clear at all Places of obſervation (none of which can well be in *England*) ſince there will not be ſuch an opportunity again in leſs than 105 years afterward.

Why the celeſtial Poles ſeem to keep ſtill in the ſame points of the Heavens, notwithſtanding the Earth's motion round the Sun.

196. The Earth's Axis produced to the Stars, being carried * parallel to itſelf during the Earth's annual revolution, deſcribes a circle in the Sphere of the fixed Stars equal to the Orbit of the Earth. But this Orbit, though very large, would ſeem no bigger than a point if it were viewed from the Stars; and conſequently, the circle deſcribed in

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* By this is meant, that if a line be ſuppoſed to be drawn parallel to the Earth's Axis in any part of it's Orbit, the Axis keeps parallel to that line in every other part of it's Orbit: as in Fig. I. of Plate V; where *abcdefgh* repreſents the Earth's Orbit in an oblique view, and *Ns* the Earth's Axis keeping always parallel to the line *MN*.

the Sphere of the Stars by the Axis of the Earth produced, if viewed from the Earth, muſt appear but as a point; that is, it's diameter appears too little to be meaſured by obſervation: for Dr. BRADLEY has aſſured us, that if it had amounted to a ſingle ſecond, or two at moſt, he ſhould have perceived it in the great number of obſervations he has made, eſpecially upon γ *Dragonis*; and that it ſeemed to him very probable that the annual Parallax of this Star is not ſo great as a ſingle ſecond; and conſequently, that it is above 400 thouſand times farther from us than the Sun. Hence the celeſtial poles ſeem to continue in the ſame points of the Heavens throughout the year; which by no means diſproves the Earth's annual motion, but plainly proves the diſtance of the Stars to be exceeding great.

197. The ſmall apparent motion of the Stars, § 113, diſcovered by that great Aſtronomer, he found to be no ways owing to their annual Parallax (for it came out contrary thereto) but to the Aberration of their light, which can reſult from no known cauſe beſides that of the Earth's annual motion; and as it agrees ſo exactly therewith, it proves beyond diſpute that the Earth has ſuch a motion: for this Aberration compleats all it's various Phenomena every year; and proves that the velocity of ſtar-light is ſuch as carries it through a ſpace equal to the Sun's diſtance from us in 8 minutes 13 ſeconds of time. Hence, the velocity of Light is * 10 thouſand 210 times as great as the Earth's velocity in it's Orbit; which velocity (from what we know already of the Earth's diſtance from the Sun) may be aſſerted to be at leaſt between 57 and 58 thouſand miles every hour: and ſuppoſing it to be 58000, this number multiplied by the 10210, gives 592 million 180 thouſand miles for the hourly motion of Light: which laſt number divided by 3600, the number of ſeconds in an hour, ſhews that Light flies at the rate of more

The amazing velocity of light.

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* SMITH's Optics, § 1197.

than

PLATE IV. than 164 thouſand miles every ſecond of time, or ſwing of a common clock pendulum.

CHAP. X.

The Circles of the Globe deſcribed. The different lengths of days and nights, and the viciſſitudes of ſeaſons, explained. The explanation of the Phenomena of Saturn's Ring concluded. (See § 81 and 82.)

Circles of the Sphere. 198. IF the reader be hitherto unacquainted with the principal circles of the Globe, he ſhould now learn to know them; which he may do ſufficiently for his preſent purpoſe in a quarter of an hour, if he ſets the ball of a terreſtrial Globe before him, or looks at the Figure of it, wherein these circles are drawn and named. (Fig. II.) The *Equator* is that great circle which divides the northern half of the Earth from the ſouthern. The *Tropics* are leſſer circles parallel to the Equator, and each of them is 23½ degrees from it; a degree in this ſenſe being the 360th part of any great circle which divides the Earth into two equal parts. The *Tropic of Cancer* lies on the north ſide of the Equator, and the *Tropic of Capricorn* on the ſouth. The *Arctic Circle* has the *North Pole* for it's center, and is juſt as far from the north Pole as the Tropics are from the Equator: and the *Antarctic Circle* (hid by the ſuppoſed convexity of the Figure) is juſt as far from the *South Pole*, every way round it. These Poles are the very north and ſouth points of the Globe: and all other places are denominated *northward* or *ſouthward*, according to the ſide of the Equator they lie on, and the Pole to which they are neareſt. The *Earth's Axis* is a ſtraight line paſſing through the center of the Earth, perpendicular to the Equator, and terminating in the Poles at it's ſurface. This, in the real Earth and Planets, is only an imaginary line; but in artificial Globes or Planets it is a wire by which they are ſupported,

Equator, Tropics, Polar Circles, and Poles. Fig. II.

Earth's Axis.

ſupported, and turned round in *Orreries*, or ſuch like machines, by wheel-work. The circles 12. 1. 2. 3. 4, *&c.* are Meridians to all places they paſs through; and we muſt ſuppoſe thouſands more to be drawn, becauſe every place that is ever ſo little to the eaſt or weſt of any other place, has a different Meridian from that other place. All the Meridians meet in the Poles; and whenever the Sun's center is paſſing over any Meridian, in his apparent motion round the Earth, it is mid-day or noon to all places on that Meridian.

PLATE IV.

Meridians.

199. The *broad Space* lying between the Tropics, like a girdle ſurrounding the Globe, is called the *torrid Zone*, of which the Equator is in the middle, all around. The *Space* between the Tropic of Cancer and Arctic Circle is called the *North temperate Zone*. *That* between the Tropic of Capricorn and the Antarctic Circle, the *South temperate Zone*. And the two *circular Spaces* bounded by the Polar Circles are the two *Frigid Zones*; denominated *north* or *ſouth*, from that Pole which is in the center of the one or the other of them.

Zones.

200. Having acquired this eaſy branch of knowledge, the learner may proceed to make the following experiment with his terreſtrial ball; which will give him a plain idea of the diurnal and annual motions of the Earth, together with the different lengths of days and nights, and all the beautiful variety of ſeaſons, depending on thoſe motions.

Take about ſeven feet of ſtrong wire, and bend it into a circular form, as *abcd*, which being viewed obliquely, appears elliptical as in the Figure. Place a lighted candle on a table, and having fixed one end of a ſilk thread *K*, to the north pole of a ſmall terreſtrial Globe *H*, about three inches diameter, cauſe another perſon to hold the wire circle, ſo that it may be parallel to the table, and as high as the flame of the candle *I*, which ſhould be

Fig. III. A pleaſant experiment, ſhewing the different lengths of days and nights, and the variety of ſeaſons.

be in or near the center. Then, having twiſted the thread as towards the left hand, that by untwiſting it may turn the Globe round eaſtward, or contrary to the way that the hands of a watch move; hang the Globe by the thread within this circle, almoſt contiguous to it; and as the thread untwiſts, the Globe (which is enlightened half round by the candle as the Earth is by the Sun) will turn round it's Axis, and the different places upon it will be carried through the light and dark Hemiſpheres, and have the appearance of a regular ſucceſſion of days and nights, as our Earth has in reality by ſuch a motion. As the Globe turns, move your hand ſlowly, ſo as to carry the Globe round the candle according to the order of the letters *abcd*, keeping it's center even with the wire circle; and you will perceive, that the candle being ſtill perpendicular to the Equator, will enlighten the Globe from pole to pole in it's whole motion round the circle; and that every place on the Globe goes equally through the light and the dark, as it turns round by the untwiſting of the thread, and therefore has a perpetual Equinox. The Globe thus turning round repreſents the Earth turning round it's Axis; and the motion of the Globe round the candle repreſents the Earth's annual motion round the Sun, and ſhews, that if the Earth's Orbit had no inclination to it's Axis, all the days and nights of the year would be equally long, and there would be no different ſeaſons. But now, deſire the perſon who holds the wire to hold it obliquely in the poſition *ABCD*, raiſing the ſide ♋ juſt as much as he depreſſes the ſide ♑, that the flame may be ſtill in the plane of the circle; and twiſting the thread as before, that the Globe may turn round it's Axis the ſame way as you carry it round the candle; that is, from weſt to eaſt, let the Globe down into the lowermoſt part of the wire circle at ♑, and if the circle be properly inclined, the candle will ſhine perpendicularly on the Tropic of Cancer, and the *frigid* Summer Solſtice. *Zone*, lying within the *arctic* or *north polar Circle*, will be all in the light, as in the Figure; and will keep in the light let the Globe turn round it's Axis ever ſo often. From the Equator to the north polar Circle all the places have longer days and ſhorter nights; but from the Equator to the ſouth polar Circle juſt the reverſe. The Sun does not ſet to any part of the north frigid Zone, as ſhewn by the candle's ſhining on it, ſo that the motion of the Globe can carry no place of that Zone into the dark: and at the ſame time the *ſouth frigid Zone* is involved in darkneſs, and the turning of the Globe brings none of it's places into the light. If the Earth were to continue in the like part of it's Orbit, the Sun would never ſet to the inhabitants of the north frigid Zone, nor riſe to thoſe of the ſouth. At the Equator it would be always equal day and night; and as places are gradually more and more diſtant from the Equator, towards the arctic Circle, they would have longer days and ſhorter nights; whilſt thoſe on the ſouth ſide of the Equator would have their nights longer than their days. In this caſe there would be continual ſummer on the north ſide of the Equator, and continual winter on the ſouth ſide of it.

But as the Globe turns round it's Axis, move your hand ſlowly forward, ſo as to carry the Globe from *H* towards *E*, and the boundary of light and darkneſs will approach towards the north Pole, and recede towards the ſouth Pole; the northern places will go through leſs and leſs of the light, and the ſouthern places through more and more of it; ſhewing how the northern days decreaſe in length, and the ſouthern days increaſe, whilſt the Globe proceeds from *H* to *E*. When the Globe Autumnal Equinox. is at *E*, it is at a mean ſtate between the loweſt and higheſt parts of it's Orbit; the candle is directly over the Equator, the boundary of light and darkneſs juſt reaches to both the Poles, and all places on the Globe go equally through the light and dark Hemiſpheres, ſhewing that the days and nights are then equal at all places of the Earth, the Poles only excepted; for the Sun is then ſetting to the north Pole, and riſing to the ſouth Pole.

Continue moving the Globe forward, and as it goes through the quarter *A*, the north Pole recedes ſtill farther into the dark Hemiſphere, and the ſouth Pole advances more into the light, as the Globe comes nearer to ♋: and when it comes there at *F*, the candle is directly over the Tropic of Capricorn, the days are at the ſhorteſt, and nights at the longeſt, in the northern Hemiſphere, all the way from the Equator to the arctic Circle; and the reverſe in the ſouthern Hemiſphere from the Equator to the antarctic Circle; within which Circles it is dark to the north frigid Zone, and light to the ſouth.

Winter Solſtice.

Continue both motions, and as the Globe moves through the quarter *B*, the north Pole advances towards the light, and the ſouth Pole recedes towards the dark; the days lengthen in the northern Hemiſphere, and ſhorten in the ſouthern; and when the Globe comes to *G*, the candle will be again over the Equator (as when the Globe was at *E*) and the days and nights will again be equal as formerly: and the north Pole will be juſt coming into the light, the ſouth Pole going out of it.

Vernal Equinox.

Thus we ſee the reaſon why the days lengthen and ſhorten from the Equator to the polar Circles every year; why there is ſometimes no day or night for many turnings of the Earth, within the polar Circles; why there is but one day and one night in the whole year at the Poles; and why the days and nights are equally long all the year round at the Equator, which is always equally cut by the circle bounding light and darkneſs. PLATE IV.

201. The inclination of an Axis or Orbit is merely relative, becauſe we compare it with ſome other Axis or Orbit which we conſider as not inclined at all. Thus, our Horizon being level to us, whatever place of the Earth we are upon, we conſider it as having no inclination; and yet, if we travel 90 degrees from that place, we ſhall then have an Horizon perpendicular to the former; but it will ſtill be level to us. And, if this Book be held ſo that the * Circle *ABCD* be parallel to the Horizon, both the Circle *abcd*, and the Thread or Axis *K*, will be inclined to it. But if the Book or Plate be held, ſo that the Thread be perpendicular to the Horizon, then the Orbit *ABCD* will be inclined to the Thread, and the Orbit *abcd* perpendicular to it, and parallel to the Horizon. We generally conſider the Earth's annual Orbit as having no inclination, and the Orbits of all the other Planets as inclined to it, § 20. **Remark.** Fig. III.

202. Let us now take a view of the Earth in it's annual courſe round the Sun, conſidering it's Orbit as having no inclination; and it's Axis as inclining $23\frac{1}{2}$ degrees from a line perpendicular to the plane of it's Orbit, and keeping the ſame oblique direction in all parts of it's annual courſe; or, as commonly termed, keeping always parallel to itſelf, § 196.

Let *a,b,c,d,e,f,g,h* be the Earth in eight different parts of it's Orbit, equidiſtant from one another; *Ns* it's Axis, *N* it's north Pole, *s* it's ſouth Pole, PLATE V. Fig. I.

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* All Circles appear Ellipſes in an oblique view, as is evident by looking obliquely at the rim of a baſon. For the true figure of a Circle can only be ſeen when the eye is directly over it's center. The more obliquely it is viewed, the more elliptical it appears; until the eye be in the ſame plane with it, and then it appears like a ſtraight line.

PLATE V. and *S* the Sun nearly in the center of the Earth's Orbit, § 18. As the Earth goes round the Sun according to the order of the letters *abcd*, &c. it's Axis *Ns* keeps the ſame obliquity, and is ſtill parallel to the line *MNs*. When the Earth is at *a*, its north Pole inclines towards the Sun *S*, and brings all the northern places more into the light than at any other time of the year. But when the Earth is at *e* in the oppoſite time of the year, the north Pole declines from the Sun, which occaſions the northern places to be more in the dark than in the light; and the reverſe at the ſouthern places, as is evident by the Figure, which I have taken from Dr. Long's Aſtronomy. When the Earth is either at *c* or *g*, it's Axis inclines not either to or from the Sun, but lies ſidewiſe to him; and then the Poles are in the boundary of light and darkneſs; and the Sun, being directly over the Equator, makes equal day and night at all places. When the Earth is at *b*, it is half way between the Summer Solſtice and Harveſt Equinox; when it is at *d*, it is half way from the Harveſt Equinox to the Winter Solſtice; at *f*, half way from the Winter Solſtice to the Spring Equinox; and at *h*, half way from the Spring Equinox to the Summer Solſtice.

A conciſe view of the ſeaſons.

Fig. II.

203. From this oblique view of the Earth's Orbit, let us ſuppoſe ourſelves to be raiſed far above it, and placed juſt over it's center *S*, looking down upon it from it's north Pole; and as the Earth's Orbit differs but very little from a Circle, we ſhall have it's figure in ſuch a view repreſented by the Circle *ABCDEFGH*. Let us ſuppoſe this Circle to be divided into 12 equal parts, called *Signs*, having their names affixed to them; and each Sign into 30 equal parts, called *Degrees*, numbered 10, 20, 30, as in the outermoſt Circle of the Figure, which repreſents the great Ecliptic in the Heavens. The Earth is ſhewn in eight different poſitions in this Circle, and in each poſition *Æ* is

The ſeaſons ſhewn in another view of the Earth, and it's Orbit.

the Equator, *T* the Tropic of Cancer, the *dotted Circle* the parallel of *London*, *U* the arctic or north polar Circle, and *P* the north Pole, where all the Meridians or Hour-Circles meet, § 198. As the Earth goes round the Sun, the north Pole keeps conſtantly towards one part of the Heavens, as it keeps in the Figure towards the right hand ſide of the Plate.

Vernal Equinox.

When the Earth is at the beginning of Libra, namely on the 20th of *March*, in this Figure (as at *g* in Fig. I.) the Sun *S* as ſeen from the Earth appears at the beginning of Aries in the oppoſite part of the Heavens *, the north Pole is juſt coming into the light, and the Sun is vertical to the Equator; which, together with the Tropic of Cancer, parallel of *London*, and arctic Circle, are all equally cut by the Circle bounding light and darkneſs, coinciding with the ſix o'clock hour Circle, and therefore the days and nights are equally long at all places: for every part of the Meridian *ÆTLa* comes into the light at ſix in the morning, and revolving with the Earth according to the order of the hour-letters, goes into the dark at ſix in the evening. There are 24 Meridians or Hour-Circles drawn on the Earth in this Figure, to ſhew the time of Sun-riſing and ſetting at different Seaſons of the Year.

As the Earth moves in the Ecliptic according to the order of the letters *ABCD*, &c. through the Signs Libra, Scorpio, and Sagittarius, the north Pole comes more and more into the light; the days increaſe as the nights decreaſe in length, at all places north of the Equator *Æ*; which is plain by viewing the Earth at *b* on the 5th of *May*, when it is in the 15th degree of Scorpio †, and

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* Here we muſt ſuppoſe the Sun to be no bigger than an ordinary point (as .) becauſe he only covers a Circle half a degree in diameter in the Heavens; whereas in the Figure he hides a whole ſign at once from the Earth.

† Here we muſt ſuppoſe the Earth to be a much ſmaller point than that in the preceding note marked for the Sun.

PLATE V. Fig. II. the Sun as ſeen from the Earth appears in the 15th degree of Taurus. For then, the Tropic of Cancer *T* is in the light from a little after five in the morning till almoſt ſeven in the evening; the parallel of *London* from half an hour paſt four till half an hour paſt ſeven; the polar Circle *U* from three till nine; and a large track round the north Pole *P* has day all the 24 hours, for many rotations of the Earth on it's Axis.

When the Earth comes to *c*, at the beginning of Capricorn, and the Sun as ſeen from the Earth appears at the beginning of Cancer, on the 21ſt of *June*, as in this Figure, it is in the poſition *a* in Fig. I; and it's north Pole inclines towards the Sun, ſo as to bring all the north frigid Zone into the light, and the northern parallels of Latitude more into the light than the dark from the Equator to the polar Circle; and the more ſo as they are farther from the Equator. The Tropic of Cancer is in the light from five in the morning till ſeven at night, the parallel of *London* from a quarter before four till a quarter after eight; and the polar Circle juſt touches the dark, ſo that the Summer Solſtice. Sun has only the lower half of his Diſc hid from the inhabitants on that Circle for a few minutes about midnight, ſuppoſing no inequalities in the Horizon, and no Refractions.

A bare view of the Figure is enough to ſhew, that as the Earth advances from Capricorn towards Aries, and the Sun appears to move from Cancer towards Libra, the north Pole recedes towards the dark, which cauſes the days to decreaſe, and the Autumnal Equinox. nights to increaſe in length, till the Earth comes to the beginning of Aries, and then they are equal as before; for the boundary of light and darkneſs cuts the Equator and all it's parallels equally, or in halves. The north pole then goes into the dark, and continues therein until the Earth goes half way round it's Orbit; or, from the 23d of *September* till the 20th of *March*. In the middle

between

Plate V.

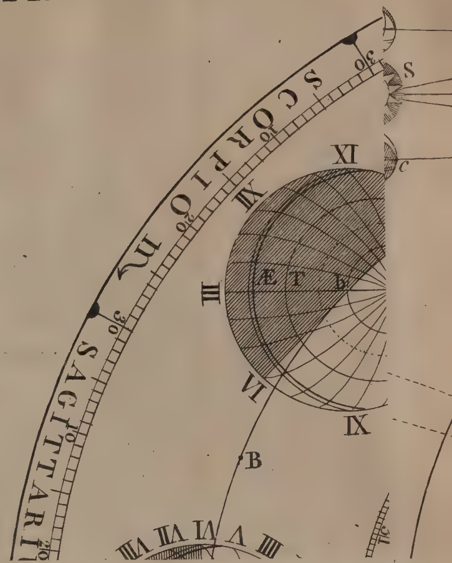

S
c
SCORPIO ♏
30
10
20
30
SAGITTARI
10
20
XI
XII
III
Æ
T
b
VI
IX
B
VIII
VII
VI
V
IIII
31

Plate V.

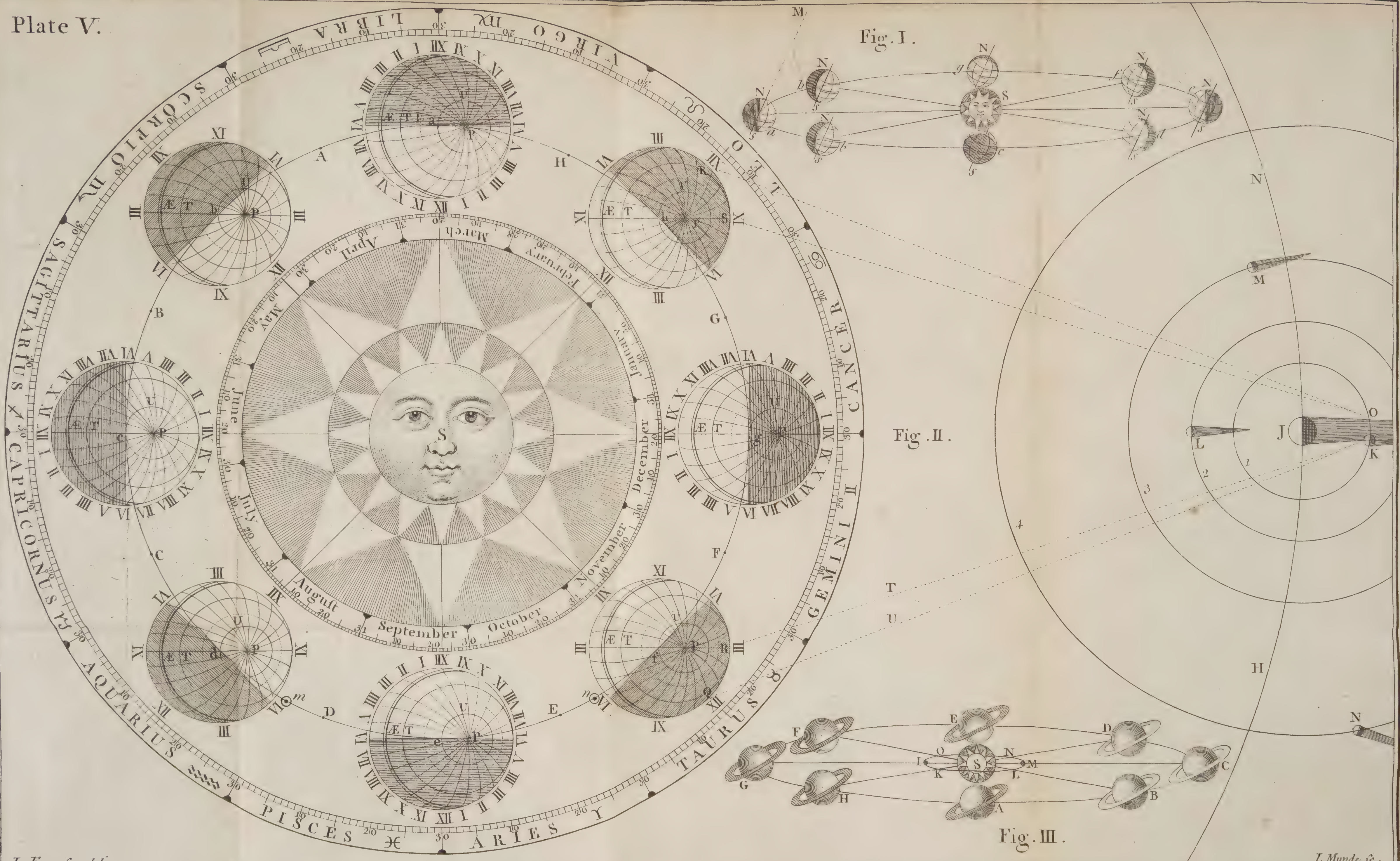


Fig. I.

Fig. II.

Fig. III.

J. Ferguſon delin.

J. Mynde ſc.

between theſe times, *viz.* on the 22d of *December*, the north Pole is as far as it can be in the dark, which is $23\frac{1}{2}$ degrees, equal to the inclination of the Earth's Axis from a perpendicular to it's Orbit: and then, the northern parallels are as much in the dark as they were in the light on the 21ſt of *June*; the winter nights being as long as the ſummer days, and the winter days as ſhort as the ſummer nights. It is needleſs to enlarge farther on this ſubject, as we ſhall have occaſion to mention the ſeaſons again in deſcribing the *Orrery*, § 439. Only this muſt be noted, that all that has been ſaid of the northern Hemiſphere, the contrary muſt be underſtood of the ſouthern; for on different ſides of the Equator the ſeaſons are contrary, becauſe, when the northern Hemiſphere inclines towards the Sun, the ſouthern declines from him. Winter Solſtice.

204. As Saturn goes round the Sun, his obliquely poſited ring, like our Earth's Axis, keeps parallel to itſelf, and is therefore turned edgewiſe to the Sun twice in a Saturnian year, which is almoſt as long as 30 of our years, § 81. But the ring, though conſiderably broad, is too thin to be ſeen by us when it is turned edgewiſe to the Sun, at which time it is alſo edgewiſe to the Earth; and therefore it diſappears once in every fifteen years to us. As the Sun ſhines half a year together on the north Pole of our Earth, then diſappears to it, and ſhines as long on the ſouth Pole; ſo, during one half of Saturn's year, the Sun ſhines on the north ſide of his ring, then diſappears to it, and ſhines as long on it's ſouth ſide. When the Earth's Axis inclines neither to nor from the Sun, but ſidewiſe to him, he inſtantly ceaſes to ſhine on one Pole, and begins to enlighten the other; and when Saturn's Ring inclines neither to nor from the Sun, but ſidewiſe The Phenomena of Saturn's Ring.

PLATE V. to him, he ceaſes to ſhine on the one ſide of it, and begins to ſhine upon the other.

Fig. III. Let *S* be the Sun, *ABCDEFGH* Saturn's Orbit, and *IKLMNO* the Earth's Orbit. Both Saturn and the Earth move according to the order of the letters, and when Saturn is at *A* his ring is turned edgewiſe to the Sun *S*, and he is then ſeen from the Earth as if he had loſt his ring, let the Earth be in any part of it's Orbit whatever, except between *N* and *O*; for whilſt it deſcribes that ſpace, Saturn is apparently ſo near the Sun as to be hid in his beams. As Saturn goes from *A* to *C*, his ring appears more and more open to the Earth: at *C* the ring appears moſt open of all; and ſeems to grow narrower and narrower as Saturn goes from *C* to *E*; and when he comes to *E*, the ring is again turned edgewiſe both to the Sun and Earth: and as neither of it's ſides are illuminated, it is inviſible to us, becauſe it's edge is too thin to be perceptible: and Saturn appears again as if he had loſt his ring. But as he goes from *E* to *G*, his ring opens more and more to our view on the under ſide; and ſeems juſt as open at *G* as it was at *C*; and may be ſeen in the night-time from the Earth in any part of it's Orbit, except about *M*, when the Sun hides the Planet from our view. As Saturn goes from *G* to *A*, his ring turns more and more edgewiſe to us, and therefore it ſeems to grow narrower and narrower; and at *A* it diſappears as before. Hence, while Saturn goes from *A* to *E*, the Sun ſhines on the upper ſide of his ring, and the under ſide is dark; and whilſt he goes from *E* to *A*, the Sun ſhines on the under ſide of his ring, and the upper ſide is dark.

It may perhaps be imagined that this Article might have been placed more properly after § 81, than here: but when the candid reader conſiders that all the various Phenomena of Saturn's Ring depend upon a cauſe ſimilar to that of our Earth's

Fig. I. and III. ſeaſons, he will readily allow that they are beſt explained together; and that the two Figures ſerve to illuſtrate each other.

PLATE VI.

The Earth nearer the Sun in winter than in ſummer.

205. The Earth's Orbit being elliptical, and the Sun conſtantly keeping in it's lower Focus, which is 1,377,000 miles from the middle point of the longer Axis, the Earth comes twice ſo much, or 2,754,000 miles nearer the Sun at one time of the year than at another: for the Sun appearing under a larger Angle in our winter than ſummer, proves that the Earth is nearer the Sun in winter, (*ſee the Note on Art.* 185.) But here, this natural queſtion will ariſe, Why have we not the hotteſt weather when the Earth is neareſt the Sun? In anſwer it muſt be obſerved, that the excentricity of the Earth's Orbit, or 1 million 377 miles bears no greater proportion to the Earth's mean diſtance from the Sun than 17 does to 1000; and therefore, this ſmall difference of diſtance cannot occaſion any great difference of heat or cold. But the principal cauſe of this difference is, that in winter the Sun's rays fall ſo obliquely upon us, that any given number of them is ſpread over a much greater portion of the Earth's ſurface where we live; and therefore each point muſt then have fewer rays than in ſummer. Moreover, there comes a greater degree of cold in the long winter nights, than there can return of heat in ſo ſhort days; and on both theſe accounts the cold muſt increaſe. But in ſummer the Sun's rays fall more perpendicularly upon us, and therefore come with greater force, and in greater numbers on the ſame place; and by their long continuance, a much greater degree of heat is imparted by day than can fly off by night.

Why the weather is coldeſt when the Earth is neareſt the Sun.

206. That a greater number of rays fall on the ſame place, when they come perpendicularly, than when they come obliquely on it, will appear by the Figure. For, let *AB* be a certain number of the Sun's rays falling on *CD* (which, let us ſuppoſe to be *London*) on the 22d of *June*: but, on

Fig. II.

the 22d of *December*, the line *CD*, or *London*, has the oblique poſition *Cd* to the ſame rays; and therefore ſcarce a third part of them falls upon it, or only thoſe between *A* and *e*; all the reſt *eB* being expended on the ſpace *dP*, which is more than double the length of *CD* or *Cd*. Beſides, thoſe parts which are once heated, retain the heat for ſome time; which, with the additional heat daily imparted, makes it continue to increaſe, though the Sun declines towards the ſouth: and this is the reaſon why *July* is hotter than *June*, although the Sun has withdrawn from the ſummer Tropic; as we find it is generally hotter at three in the afternoon, when the Sun has gone towards the weſt, than at noon when he is on the Meridian. Likewiſe, thoſe places which are well cooled require time to be heated again; for the Sun's rays do not heat even the ſurface of any body till they have been ſome time upon it. And therefore we find *January* for the moſt part colder than *December*, although the Sun has withdrawn from the winter Tropic, and begins to dart his beams more perpendicularly upon us, when we have the poſition *CF*. An iron bar is not heated immediately upon being put into the fire, nor grows cold till ſome time after it has been taken out.

CHAP. XI.

The Method of finding the Longitude by the Eclipſes of Jupiter's Satellites: The amazing Velocity of Light demonſtrated by theſe Eclipſes.

First Meridian, and Longitude of places, what.

207. GEographers arbitrarily chooſe to call the Meridian of ſome remarkable place *the firſt Meridian*. There they begin their reckoning; and juſt ſo many degrees and minutes as any other place is to the eaſtward or weſtward of that Meridian, ſo much eaſt or weſt Longitude they ſay it has. A degree is the 360th part of a Circle, be it

great or ſmall; and a minute the 60th part of a degree. The *Engliſh* Geographers reckon the Longitude from the Meridian of the Royal Obſervatory at *Greenwich*, and the *French* from the Meridian of *Paris*. PLATE V.

208. If we imagine twelve great Circles, one of which is the Meridian of any given place, to interſect each other in the two Poles of the Earth, and to cut the Equator *Æ* at every 15th degree, they will be divided by the Poles into 24 Semicircles which divide the Equator into 24 equal parts; and as the Earth turns on it's Axis, the planes of theſe Semicircles come ſucceſſively after one another every hour to the Sun. As in an hour of time there is a revolution of 15 degrees of the Equator, in a minute of time there will be a revolution of 15 minutes of the Equator, and in a ſecond of time a revolution of 15 ſeconds. There are two tables annexed to this Chapter, for reducing mean ſolar time into degrees and minutes of the terreſtrial Equator; and alſo for converting degrees and parts of the Equator into mean ſolar time. Fig. II. Hour Circles. An hour of time equal to 15 degrees of motion.

209. Becauſe the Sun enlightens only one half of the Earth at once, as it turns round it's Axis, he riſes to ſome places at the ſame moments of abſolute Time when he ſets to others; and when it is mid-day to ſome places, it is mid-night to others. The XII on the middle of the Earth's enlightened ſide, next the Sun, ſtands for mid-day; and the oppoſite XII on the middle of the dark ſide, for mid-night. If we ſuppoſe this Circle of hours to be fixed in the plane of the Equinoctial, and the Earth to turn round within it, any particular Meridian will come to the different hours ſo, as to ſhew the true time of the day or night at all places on that Meridian. Therefore,

210. To every place 15 degrees eaſtward from any given Meridian, it is noon an hour ſooner than on that Meridian; becauſe their Meridian comes

to the Sun an hour ſooner: and to all places 15 degrees weſtward, it is noon an hour later, § 208, becauſe their Meridian comes an hour later to the Sun; and ſo on: every 15 degrees of motion cauſing an hour's difference of time. Therefore they who have noon an hour later than we, have their Meridian, that is, their Longitude, 15 degrees weſtward from us; and they who have noon an hour ſooner than we, have their Meridian 15 degrees eaſtward from ours: and ſo for every hour's difference of time 15 degrees difference of Longitude. Conſequently, if the beginning or ending of a Lunar Eclipſe be obſerved, ſuppoſe at *London*, to be exactly at mid-night, and in ſome other place at 11 at night, that place is 15 degrees weſtward from the Meridian of *London*: if the ſame Eclipſe be obſerved at one in the morning at another place, that place is 15 degrees eaſtward from the ſaid Meridian.

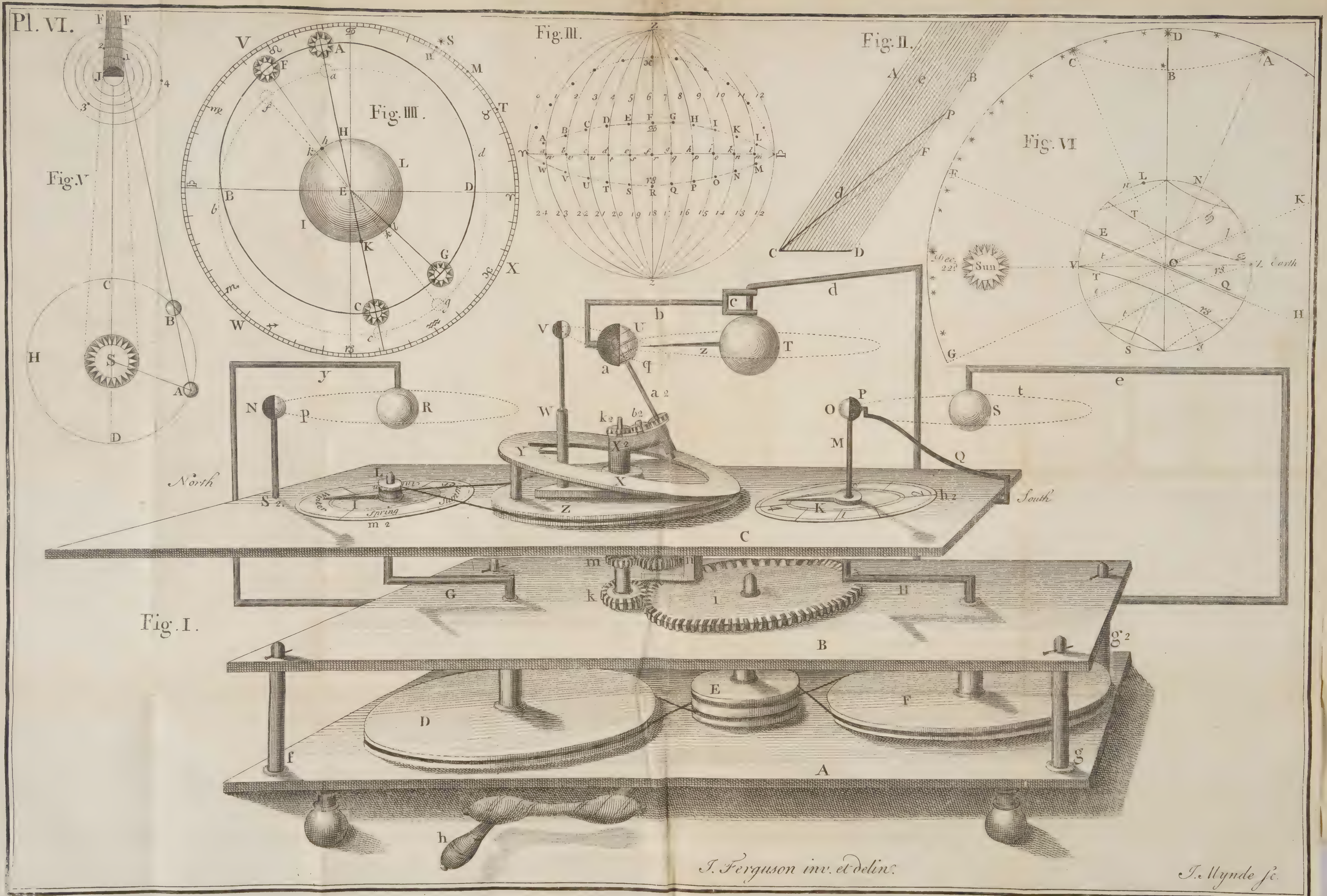
And conſequently to 15 degrees of Longitude.

Lunar Eclipſes uſeful in finding the Longitude.

211. But as it is not eaſy to determine the exact moment either of the beginning or ending of a Lunar Eclipſe, becauſe the Earth's ſhadow through which the Moon paſſes is faint and ill defined about the edges; we have recourſe to the Eclipſes of Jupiter's Satellites, which diſappear ſo inſtantaneouſly as they enter into Jupiter's ſhadow, and emerge ſo ſuddenly out of it, that we may fix the phenomenon to a ſecond of time. The firſt or neareſt Satellite to Jupiter is the moſt advantageous for this purpoſe, becauſe it's motion is quicker than the motion of any of the reſt, and therefore it's immerſions and emerſions are more frequent.

Eclipſes of Jupiter's Satellites much better for that purpoſe.

212. The *Engliſh* Aſtronomers have calculated Tables for ſhewing the times of the Eclipſes of Jupiter's Satellites to great preciſion, for the Meridian of *Greenwich*. Now, let an obſerver, who has theſe Tables with a good Teleſcope and a well-regulated Clock at any other place of the Earth, obſerve the beginning or ending of an Eclipſe of



J. Ferguson inv. et delin.

J. Mynde sc.

PLATE V.

How to ſolve this important problem.

one of Jupiter's Satellites, and note the preciſe moment of time that he ſaw the Satellite either immerge into, or emerge out of the ſhadow, and compare that time with the time ſhewn by the Tables for *Greenwich*; then, 15 degrees difference of Longitude being allowed for every hour's difference of time, will give the Longitude of that place from *Greenwich*, as above, § 210; and if there be any odd minutes of time, for every minute a quarter of a degree, eaſt or weſt, muſt be allowed, as the time of obſervation is later or earlier than the time ſhewn by the Tables. Such Eclipſes are very convenient for this purpoſe at land, becauſe they happen almoſt every day; but are of no uſe at ſea, becauſe the rolling of the ſhip hinders all nice teleſcopical obſervations.

Fig. II.

Illuſtrated by an example.

213. To explain this by a Figure, let *J* be Jupiter, *K*, *L*, *M*, *N* his four Satellites in their reſpective Orbits 1, 2, 3, 4; and let the Earth be at *f* (ſuppoſe in *November*, although that month is no otherways material than to find the Earth readily in this ſcheme, where it is ſhewn in eight different parts of it's Orbit.) Let *Q* be a place on the Meridian of *Greenwich*, and *R* a place on ſome other Meridian eaſtward from *Greenwich*. Let a perſon at *R* obſerve the inſtantaneous vaniſhing of the firſt Satellite *K* into Jupiter's ſhadow, ſuppoſe at three o'clock in the morning; but by the Tables he finds the immerſion of that Satellite to be at mid-night at *Greenwich*: he can then immediately determine, that as there are three hours difference of time between *Q* and *R*, and that *R* is three hours forwarder in reckoning than *Q*, it muſt be 45 degrees of eaſt Longitude from the Meridian of *Q*. Were this method as practicable at ſea as at land, any ſailor might almoſt as eaſily, and with equal certainty, find the Longitude as the Latitude.

Fig. II.

214. Whilſt the Earth is going from *C* to *F* in it's Orbit, only the immerſions of Jupiter's Satellites

We ſeldom ſee the beginning and end of the ſame Eclipſe of any of Jupiter's Moons.

lites into his ſhadow are generally ſeen; and their emerſions out of it while the Earth goes from *G* to *B*. Indeed, both theſe appearances may be ſeen of the ſecond, third, and fourth Satellite when eclipſed, whilſt the Earth is between *D* and *E*, or between *G* and *A*; but never of the firſt Satellite, on account of the ſmallneſs of it's Orbit and the bulk of Jupiter; except only when Jupiter is directly oppoſite to the Sun; that is, when the Earth is at *g*: and even then, ſtrictly ſpeaking, we cannot ſee either the immerſions or emerſions of any of his Satellites, becauſe his body being directly between us and his conical ſhadow, his Satellites are hid by his body a few moments before they touch his ſhadow; and are quite emerged from thence before we can ſee them, as it were, juſt dropping from him. And when the Earth is at *c*, the Sun, being between it and Jupiter, hides both him and his Moons from us.

In this Diagram, the Orbits of Jupiter's Moons are drawn in true proportion to his diameter; but, in proportion to the Earth's Orbit, they are drawn 81 times too large.

Jupiter's conjunctions with the Sun, or oppoſitions to him, are every year in different parts of the Heavens.

215. In whatever month of the year Jupiter is in conjunction with the Sun, or in oppoſition to him, in the next year it will be a month later at leaſt. For whilſt the Earth goes once round the Sun, Jupiter deſcribes a twelfth part of his Orbit. And therefore, when the Earth has finiſhed it's annual period from being in a line with the Sun and Jupiter, it muſt go as much forwarder as Jupiter has moved in that time, to overtake him again: juſt like the minute-hand of a watch, which muſt, from any conjunction with the hour-hand, go once round the dial-plate and ſomewhat above a twelfth part more, to overtake the hour-hand again.

216. It is found by obſervation, that when the Earth is between the Sun and Jupiter, as at *g*, his

PLATE VI.

The ſurpriſing velocity of Light.

Satellites are eclipſed about 8 minutes ſooner than they ſhould be according to the Tables: and when the Earth is at *B* or *C*, theſe Eclipſes happen about 8 minutes later than the Tables predict them. Hence it is undeniably certain, that the motion of Light is not inſtantaneous, ſince it takes about $16\frac{1}{2}$ minutes of time to go through a ſpace equal to the diameter of the Earth's Orbit, which is 162 millions of miles in length: and conſequently the particles of Light fly about 164 thouſand 494 miles every ſecond of time, which is above a million of times ſwifter than the motion of a cannon-bullet. And as light is $16\frac{1}{2}$ minutes in travelling acroſs the Earth's Orbit, it muſt be $8\frac{1}{4}$ minutes in coming from the Sun to us: therefore, if the Sun were annihilated, we ſhould ſee him for $8\frac{1}{4}$ minutes after; and if he were again created, he would be $8\frac{1}{4}$ minutes old before we could ſee him.

Fig. V.

Illuſtrated by a Figure.

217. To illuſtrate this progreſſive motion of Light, let *A* and *B* be the Earth in two different parts of it's Orbit, whoſe diſtance from each other is 81 millions of miles, equal to the Earth's diſtance from the Sun *S*. It is plain, that if the motion of Light were inſtantaneous, the Satellite 1 would appear to enter into Jupiter's ſhadow *FF* at the ſame moment of time to a ſpectator in *A* as to another in *B*. But by many years obſervations it has been found, that the immerſion of the Satellite into the ſhadow is ſeen $8\frac{1}{4}$ minutes ſooner when the Earth is at *B*, than when it is at *A*. And ſo, as Mr. Romer firſt diſcovered, the motion of Light is thereby proved to be progreſſive, and not inſtantaneous, as was formerly believed. It is eaſy to compute in what time the Earth moves from *A* to *B*; for the Chord of 60 degrees of any Circle is equal to the Semi-diameter of that Circle; and as the Earth goes through all the 360 degrees of it's Orbit in a year, it goes through 60 of thoſe degrees in about 61 days. Therefore,

if on any given day, ſuppoſe the firſt of *June*, the Earth is at *A*, on the firſt of *Auguſt* it will be at *B*: the chord, or ſtraight line *AB*, being equal to *DS* the Radius of the Earth's Orbit, the ſame with *AS* it's diſtance from the Sun.

218. As the Earth moves from *D* to *C*, through the ſide *AB* of it's Orbit, it is conſtantly meeting the light of Jupiter's Satellites ſooner, which occaſions an apparent acceleration of their Eclipſes: and as it moves through the other half *H* of it's Orbit, from *C* to *D*, it is receding from their light, which occaſions an apparent retardation of their Eclipſes, becauſe their light is then longer before it overtakes the Earth.

219. That theſe accelerations of the immerſions of Jupiter's Satellites into his ſhadow, as the Earth approaches towards Jupiter, and the retardations of their emerſions out of his ſhadow, as the Earth is going from him, are not occaſioned by any inequality ariſing from the motions of the Satellites in excentric Orbits, is plain, becauſe it affects them all alike, in whatever parts of their Orbits they are eclipſed. Beſides, they go often round their Orbits every year, and their motions are no way commenſurate to the Earth's. Therefore, a Phenomenon not to be accounted for from the real motions of the Satellites, but ſo eaſily deducible from the Earth's motion, and ſo anſwerable thereto, muſt be allowed to reſult from it. This affords one very good proof of the Earth's annual motion.

220. TABLES for converting mean ſolar TIME into Degrees and Parts of the terreſtrial EQUATOR; and alſo for converting Degrees and Parts of the EQUATOR into mean ſolar Time.

TABLE I. For converting Time into Degrees and Parts of the Equator.

Hours	Degrees	*Min. | Sec. | Thirds	Deg. | Min. | Sec.	Min. | Sec. | Thirds	*Min. | Sec. | Thirds	Deg. | Min. | Sec.	Min. | Sec. | Thirds
1	15	1	0	15	31	7	45
2	30	2	0	30	32	8	0
3	45	3	0	45	33	8	15
4	60	4	1	0	34	8	30
5	75	5	1	15	35	8	45
6	90	6	1	30	36	9	0
7	105	7	1	45	37	9	15
8	120	8	2	0	38	9	30
9	135	9	2	15	39	9	45
10	150	10	2	30	40	10	0
11	165	11	2	45	41	10	15
12	180	12	3	0	42	10	30
13	195	13	3	15	43	10	45
14	210	14	3	30	44	11	0
15	225	15	3	45	45	11	15
16	240	16	4	0	46	11	30
17	255	17	4	15	47	11	45
18	270	18	4	30	48	12	0
19	285	19	4	45	49	12	15
20	300	20	5	0	50	12	30
21	315	21	5	15	51	12	45
22	330	22	5	30	52	13	0
23	345	23	5	45	53	13	15
24	360	24	6	0	54	13	30
25	375	25	6	15	55	13	45
26	390	26	6	30	56	14	0
27	405	27	6	45	57	14	15
28	420	28	7	0	58	14	30
29	435	29	7	15	59	14	45
30	450	30	7	30	60	15	0

TABLE II. For converting Degrees and Parts of the Equator into Time.

*Deg. | Min. | Sec.	Hours | Min. | Sec.	Min. | Sec. | Thirds	*Deg. | Min. | Sec.	Hours | Min. | Sec.	Min. | Sec. | Thirds	Degrees	Hours	Minutes
1	0	4	31	2	4	70	4	40
2	0	8	32	2	8	80	5	20
3	0	12	33	2	12	90	6	0
4	0	16	34	2	16	100	6	40
5	0	20	35	2	20	110	7	20
6	0	24	36	2	24	120	8	0
7	0	28	37	2	28	130	8	40
8	0	32	38	2	32	140	9	20
9	0	36	39	2	36	150	10	0
10	0	40	40	2	40	160	10	40
11	0	44	41	2	44	170	11	20
12	0	48	42	2	48	180	12	0
13	0	52	43	2	52	190	12	40
14	0	56	44	2	56	200	13	20
15	1	0	45	3	0	210	14	0
16	1	4	46	3	4	220	14	40
17	1	8	47	3	8	230	15	20
18	1	12	48	3	12	240	16	0
19	1	16	49	3	16	250	16	40
20	1	20	50	3	20	260	17	20
21	1	24	51	3	24	270	18	0
22	1	28	52	3	28	280	18	40
23	1	32	53	3	32	290	19	20
24	1	36	54	3	36	300	20	0
25	1	40	55	3	40	310	20	40
26	1	44	56	3	44	320	21	20
27	1	48	57	3	48	330	22	0
28	1	52	58	3	52	340	22	40
29	1	56	59	3	56	350	23	20
30	2	0	60	4	0	360	24	0

Theſe are the Tables mentioned in the 208th Article, and are ſo eaſy, that they ſcarce require any farther explanation than to inform the reader, that if, in Table I. he reckons the columns marked with Aſteriſks to be minutes of time, the other columns give the equatoreal parts or motion in degrees and minutes; if he reckons the Aſteriſk columns to be ſeconds, the others give the motion in minutes and ſeconds of the Equator; if thirds, in ſeconds and thirds: And if in Table II. he reckons the Aſteriſk columns to be degrees of motion, the others give the time anſwering thereto in hours and minutes; if minutes of motion, the time is minutes and ſeconds; if ſeconds of motion, the correſponding time is given in ſeconds and thirds. An example in each caſe will make the whole very plain.

EXAMPLE I.

In 10 hours 15 minutes 24 ſeconds 20 thirds, *Qu.* How much of the Equator revolves through the Meridian?

		Deg.	M.	S.
Hours	10	150	0	0
Min.	15	3	45	0
Sec.	24		6	0
Thirds	20			5
Anſwer		153	51	5

EXAMPLE II.

In what time will 153 degrees 51 minutes 5 ſeconds of the Equator revolve through the Meridian?

		H.	M.	S.	T.
Deg.	150	10	0	0	0
	3		12	0	0
Min.	51		3	24	0
Sec.	5				20
Anſwer		10	15	24	20

CHAP. XII.

Of Solar and Sydereal Time.

Sydereal days ſhorter than ſolar days, and why.

221. THE Stars appear to go round the Earth in 23 hours 56 minutes 4 ſeconds, and the Sun in 24 hours: ſo that the Stars gain three minutes 56 ſeconds upon the Sun every day, which

amounts to one diurnal revolution in a year; and therefore, in 365 days as meaſured by the returns of the Sun to the Meridian, there are 366 days as meaſured by the Stars returning to it: the former are called *Solar Days*, and the latter *Sydereal.* PLATE III.

The diameter of the Earth's Orbit is but a phyſical point in proportion to the diſtance of the Stars; for which reaſon, and the Earth's uniform motion on it's Axis, any given Meridian will revolve from any Star to the ſame Star again in every abſolute turn of the Earth on it's Axis, without the leaſt perceptible difference of time ſhewn by a clock which goes exactly true.

If the Earth had only a diurnal motion, without an annual, any given Meridian would revolve from the Sun to the Sun again in the ſame quantity of time as from any Star to the ſame Star again; becauſe the Sun would never change his place with reſpect to the Stars. But, as the Earth advances almoſt a degree eaſtward in it's Orbit in the time that it turns eaſtward round it's Axis, whatever Star paſſes over the Meridian on any day with the Sun, will paſs over the ſame Meridian on the next day when the Sun is almoſt a degree ſhort of it; that is, 3 minutes 56 ſeconds ſooner. If the year contained only 360 days, as the Ecliptic does 360 degrees, the Sun's apparent place, ſo far as his motion is equable, would change a degree every day; and then the ſydereal days would be juſt 4 minutes ſhorter than the ſolar.

Let *ABCDEFGHIKLM* be the Earth's Orbit, Fig. II. in which it goes round the Sun every year, according to the order of the letters, that is, from weſt to eaſt; and turns round it's Axis the ſame way from the Sun to the Sun again every 24 hours. Let *S* be the Sun, and *R* a fixed Star at ſuch an immenſe diſtance, that the diameter of the Earth's Orbit bears no ſenſible proportion to that diſtance. Let *Nn* be any particular Meridian of the Earth, and *N* a given point or place upon that Meridian.

When the Earth is at *A*, the Sun *S* hides the Star *R*, which would always be hid if the Earth never removed from *A*; and conſequently, as the Earth turns round it's Axis, the point *N* would always come round to the Sun and Star at the ſame time. But when the Earth has advanced, ſuppoſe a twelfth part of it's Orbit from *A* to *B*, it's motion round it's Axis will bring the point *N* a twelfth part of a natural day, or two hours, ſooner to the Star than to the Sun; for the Angle *NBn* is equal to the Angle *ASB*; and therefore any Star, which comes to the Meridian at noon with the Sun when the Earth is at *A*, will come to the Meridian at 10 in the forenoon when the Earth is at *B*. When the Earth comes to *C*, the point *N* will have the Star on it's Meridian at 8 in the morning, or four hours ſooner than it comes round to the Sun; for it muſt revolve from *N* to *n*, before it has the Sun in it's Meridian. When the Earth comes to *D*, the point *N* will have the Star on it's Meridian at 6 in the morning, but that point muſt revolve ſix hours more from *N* to *n*, before it has mid-day by the Sun: for now the Angle *ASD* is a right Angle, and ſo is *NDn*; that is, the Earth has advanced 90 degrees in it's Orbit, and muſt turn 90 degrees on it's Axis to carry the point *N* from the Star to the Sun: for the Star always comes to the Meridian when *Nm* is parallel to *RSA*; becauſe *DS* is but a point in reſpect of *RS*. When the Earth is at *E*, the Star comes to the Meridian at 4 in the morning; at *F*, at 2 in the morning; and at *G*, the Earth having gone half round it's Orbit, *N* points to the Star *R* at midnight, it being then directly oppoſite to the Sun; and therefore, by the Earth's diurnal motion, the Star comes to the Meridian 12 hours before the Sun. When the Earth is at *H*, the Star comes to the Meridian at 10 in the evening; at *I* it comes to the Meridian at 8, that is, 16 hours before the Sun; at *K* 18 hours before him; at *L* 20 hours; at *M* 22; and at *A* equally with the Sun again.

A TABLE, ſhewing how much of the Celeſtial Equator paſſes over the Meridian in any part of a mean SOLAR DAY; and how much the FIXED STARS gain upon the mean SOLAR TIME every Day, for a Month.

Time	Motion.			Time	Motion.			Time	Motion.			Acceleration of the Fixed Stars.			
Hours	Degrees	Minutes	Seconds	*Min. Sec. Th.	Deg. Min. Sec.	Min. Sec. Th.	Sec. Th. ''''	*Min Sec. Th.	Deg. Min. Sec.	Min. Sec. Th	Sec. Th. ''''	D.	H.	M.	S.
1	15	2	28	1	0	15	2	31	7	45	16	1	0	3	56
2	30	4	56	2	0	30	5	32	8	1	19	2	0	7	52
3	45	7	24	3	0	45	7	33	8	16	2	3	0	11	48
4	60	9	51	4	1	0	10	34	8	31	24	4	0	15	44
5	75	12	19	5	1	15	12	35	8	46	26	5	0	19	39
6	90	14	47	6	1	30	15	36	9	1	29	6	0	23	35
7	105	17	15	7	1	45	17	37	9	16	31	7	0	27	31
8	120	19	43	8	2	0	20	38	9	31	34	8	0	31	27
9	135	22	11	9	2	15	22	39	9	46	36	9	0	35	23
10	150	24	38	10	2	30	25	40	10	1	39	10	0	39	19
11	165	27	6	11	2	45	27	41	10	16	41	11	0	43	15
12	180	29	34	12	3	0	30	42	10	31	43	12	0	47	11
13	195	32	2	13	3	15	32	43	10	46	46	13	0	51	7
14	210	34	30	14	3	30	34	44	11	1	48	14	0	55	3
15	225	36	58	15	3	45	37	45	11	16	51	15	0	58	58
16	240	39	26	16	4	0	39	46	11	31	53	16	1	2	54
17	255	41	53	17	4	15	41	47	11	46	56	17	1	6	50
18	270	44	21	18	4	30	44	48	12	1	58	18	1	10	46
19	285	46	49	19	4	45	47	49	12	17	1	19	1	14	42
20	300	49	17	20	5	0	49	50	12	32	3	20	1	18	38
21	315	51	45	21	5	15	52	51	12	47	6	21	1	22	34
22	330	54	13	22	5	30	54	52	13	2	8	22	1	26	30
23	345	56	40	23	5	45	57	53	13	17	11	23	1	30	26
24	360	59	8	24	6	0	59	54	13	32	13	24	1	34	22
25	376	1	36	25	6	16	2	55	13	47	16	25	1	38	17
26	391	4	4	26	6	31	4	56	14	2	18	26	1	42	13
27	406	6	32	27	6	46	7	57	14	17	21	27	1	46	9
28	421	9	0	28	7	1	9	58	14	32	23	28	1	50	5
29	436	11	28	29	7	16	11	59	14	47	26	29	1	54	1
30	451	13	56	30	7	31	14	60	15	2	28	30	1	57	57

PLATE III.

An abſolute turn of the Earth on it's Axis never finiſhes a ſolar day.

222. Thus it is plain, that an abſolute turn of the Earth on it's Axis (which is always completed when any particular Meridian comes to be parallel to it's ſituation at any time of the day before) never brings the ſame Meridian round from the Sun to the Sun again; but that the Earth requires as much more than one turn on it's Axis to finiſh a natural day, as it has gone forward in that time; which, at a mean ſtate, is a 365th part of a Circle. Hence, in 365 days the Earth turns 366 times round it's Axis; and therefore, as a turn of the Earth on it's Axis completes a ſydereal day, there muſt be one ſydereal day more in a year than the number of ſolar days, be the number what it will, on the Earth, or any other Planet. One turn being loſt with reſpect to the number of ſolar days in a year, by the Planet's going round the Sun; juſt as it would be loſt to a traveller, who, in going round the Earth, would loſe one day by following the apparent diurnal motion of the Sun; and conſequently would reckon one day leſs at his return (let him take what time he would to go round the Earth) than thoſe who remained all the while at the place from which he ſet out. So, if there were two Earths revolving equably on their Axes, and if one remained at *A* until the other had gone round the Sun from *A* to *A* again, *that* Earth which kept it's place at *A* would have it's ſolar and ſydereal days always of the ſame length; and ſo would have one ſolar day more than the other at it's return. Hence, if the Earth turned but once round it's Axis in a year, and if *that* turn was made the ſame way as the Earth goes round the Sun, there would be continual day on one ſide of the Earth, and continual night on the other.

Fig. II.

223. The firſt part of the preceding Table ſhews how much of the celeſtial Equator paſſes over the Meridian in any given part of a mean ſolar day, and is to be underſtood the ſame way as the Table in the 220th article. The latter part, intitled,

Accelerations of the fixed Stars, affords us an eaſy method of knowing whether or no our clocks and watches go true: For if, through a ſmall hole in a window-ſhutter, or in a thin plate of metal fixed to a window, we obſerve at what time any Star diſappears behind a chimney, or corner of a houſe, at a little diſtance; and if the ſame Star diſappears the next night 3 minutes 56 ſeconds ſooner by the clock or watch; and on the ſecond night, 7 minutes 52 ſeconds ſooner; the third night 11 minutes 48 ſeconds ſooner; and ſo on, every night, as in the Table, which ſhews this difference for 30 natural days, it is an infallible ſign that the machine goes true; otherwiſe it does not go true; and muſt be regulated accordingly: and as the diſappearing of a Star is inſtantaneous, we may depend on this information to half a ſecond.

To know by the Stars whether a Clock goes true or not.

CHAP. XIII.

Of the Equation of Time.

224. THE Earth's motion on it's Axis being perfectly uniform, and equal at all times of the year, the ſydereal days are always preciſely of an equal length; and ſo would the ſolar or natural days be, if the Earth's Orbit were a perfect Circle, and it's Axis perpendicular to it's Orbit. But the Earth's diurnal motion on an inclined Axis, and it's annual motion in an elliptic Orbit, cauſe the Sun's apparent motion in the Heavens to be unequal: for ſometimes he revolves from the Meridian to the Meridian again in ſomewhat leſs than 24 hours, ſhewn by a well-regulated clock; and at other times in ſomewhat more: ſo that the time ſhewn by an equal going clock and a true Sun-dial is never the ſame but on the 15th of *April*, the 16th of *June*, the 31ſt of *Auguſt*, and the 24th of *December*. The clock, if it goes equally, and true all the year round, will be before the Sun from

The Sun and Clocks equal only on four days of the year.

from the 24th of *December* till the 15th of *April*; from that time till the 16th of *June* the Sun will be before the clock; from the 16th of *June* till the 31ſt of *Auguſt* the clock will be again before the Sun; and from thence to the 24th of *December* the Sun will be faſter than the clock.

Uſe of the Equation Table.

225. The Tables of the Equation of natural days, at the end of the following Chapter, ſhew the time that ought to be pointed out by a well-regulated clock or watch, every day of the year, at the preciſe moment of ſolar noon; that is, when the Sun's center is on the Meridian, or when a true Sun-dial ſhews it to be preciſely Twelve. Thus, on the 5th of *January* in Leap-year, when the Sun is on the Meridian, it ought to be 5 minutes 51 ſeconds paſt twelve by the clock: and on the 15th of *May*, when the Sun is on the Meridian, the time by the clock ſhould be but 55 minutes 57 ſeconds paſt eleven: in the former caſe, the clock is 5 minutes 51 ſeconds beforehand with the Sun; and in the latter caſe, the Sun is 4 minutes 3 ſeconds faſter than the clock. The column at the right hand of each month ſhews the daily difference of this equation, as it increaſes or decreaſes. But without a Meridian Line, or a Tranſit-Inſtrument fixed in the plane of the Meridian, we cannot ſet a Sun-dial true.

How to draw a Meridian Line.

226. The eaſieſt and moſt expeditious way of drawing a Meridian Line is this: Make four or five concentric Circles, about a quarter of an inch from one another, on a flat board about a foot in breadth; and let the outmoſt Circle be but little leſs than the board will contain. Fix a pin perpendicularly in the center, and of ſuch a length that it's whole ſhadow may fall within the innermoſt Circle for at leaſt four hours in the middle of the day. The pin ought to be about an eighth part of an inch thick, and to have a round blunt point. The board being ſet exactly level in a place

where the Sun ſhines, ſuppoſe from eight in the morning till four in the afternoon, about which hours the end of the ſhadow ſhould fall without all the Circles; watch the times in the forenoon, when the extremity of the ſhortening ſhadow juſt touches the ſeveral Circles, and *there* make marks. Then, in the afternoon of the ſame day, watch the lengthening ſhadow, and where it's end touches the ſeveral Circles in going over them, make marks alſo. Laſtly, with a pair of compaſſes, find exactly the middle point between the two marks on any Circle, and draw a ſtraight line from the center to that point; which Line will be covered at noon by the ſhadow of a ſmall upright wire, which ſhould be put in the place of the pin. The reaſon for drawing ſeveral Circles is, that in caſe one part of the day ſhould prove clear, and the other part ſomewhat cloudy, if you miſs the time when the point of the ſhadow ſhould touch one Circle, you may perhaps catch it in touching another. The beſt time for drawing a Meridian Line in this manner is about the ſummer ſolſtice; becauſe the Sun changes his declination ſloweſt and his altitude faſteſt in the longeſt days.

If the caſement of a window on which the Sun ſhines at noon be quite upright, you may draw a line along the edge of it's ſhadow on the floor, when the ſhadow of the pin is exactly on the Meridian Line of the board: and as the motion of the ſhadow of the caſement will be much more ſenſible on the floor, than that of the ſhadow of the pin on the board, you may know to a few ſeconds when it touches the Meridian Line on the floor; and ſo regulate your clock for the day of obſervation by that line and the Equation Tables above-mentioned, § 225.

Equation of natural days explained.

227. As the Equation of time, or difference between the time ſhewn by a well-regulated Clock and a true Sun-dial, depends upon two cauſes,

namely,

namely, the obliquity of the Ecliptic, and the unequal motion of the Earth in it, we ſhall firſt explain the effects of theſe cauſes ſeparately conſidered, and then the united effects reſulting from their combination.

228. The Earth's motion on it's Axis being perfectly equable, or always at the ſame rate, and the * plane of the Equator being perpendicular to it's Axis, it is evident that in equal times equal portions of the Equator paſs over the Meridian; and ſo would equal portions of the Ecliptic, if it were parallel to or coincident with the Equator. But, as the Ecliptic is oblique to the Equator, the equable motion of the Earth carries unequal portions of the Ecliptic over the Meridian in equal times, the difference being proportionate to the obliquity; and as ſome parts of the Ecliptic are much more oblique than others, thoſe differences are unequal among themſelves. Therefore, if two Suns ſhould ſtart either from the beginning of Aries or Libra, and continue to move through equal arcs in equal times, one in the Equator, and the other in the Ecliptic, the equatoreal Sun would always return to the Meridian in 24 hours time, as meaſured by a well-regulated clock; but the Sun in the Ecliptic would return to the Meridian ſometimes ſooner, and ſometimes later than the equatoreal Sun; and only at the ſame moments with him on four days of the year; namely, the 20th of *March*, when the Sun enters Aries; the 21ſt of *June*, when he enters Cancer; the 23d of *September*, when he enters Libra; and the 21ſt of *December*, when he enters Capricorn. But, as there is only one Sun, and his apparent motion is always in the Ecliptic,

The firſt part of the Equation of time.

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* If the Earth were cut along the Equator, quite through the center, the flat ſurface of this ſection would be the plane of the Equator; as the paper contained within any Circle may be juſtly termed the plane of that Circle.

let us henceforth call him the real Sun, and the other, which is ſuppoſed to move in the Equator, the fictitious; to which laſt, the motion of a well-regulated clock always anſwers. PLATE VI.

Let *Z*♈*z*♎ be the Earth, *ZFRz* it's Axis, *abcde* &c. the Equator, *ABCDE* &c. the northern half of the Ecliptic from ♈ to ♎ on the ſide of the Globe next the eye; and *MNOP* &c. the ſouthern half on the oppoſite ſide from ♎ to ♈. Let the points at *A*, *B*, *C*, *D*, *E*, *F*, &c. quite round from ♈ to ♈ again bound equal portions of the Ecliptic, gone through in equal times by the real Sun; and thoſe at *a*, *b*, *c*, *d*, *e*, *f*, &c. equal portions of the Equator deſcribed in equal times by the fictitious Sun; and let *Z*♈*z* be the Meridian. Fig. III.

As the real Sun moves obliquely in the Ecliptic, and the fictitious Sun directly in the Equator, with reſpect to the Meridian; a degree, or any number of degrees, between ♈ and *F* on the Ecliptic, muſt be nearer the Meridian *Z*♈*z*, than a degree, or any correſponding number of degrees on the Equator from ♈ to *f*; and the more ſo, as they are the more oblique: and therefore the true Sun comes ſooner to the Meridian every day whilſt he is in the quadrant ♈ *F*, than the fictitious Sun does in the quadrant ♈ *f*; for which reaſon, the ſolar noon precedes noon by the Clock, until the real Sun comes to *F*, and the fictitious to *f*; which two points, being equidiſtant from the Meridian, both Suns will come to it preciſely at noon by the Clock.

Whilſt the real Sun deſcribes the ſecond quadrant of the Ecliptic *FGHIKL* from ♋ to ♎, he comes later to the Meridian every day, than the fictitious Sun moving through the ſecond quadrant of the Equator from *f* to ♎; for the points at *G*, *H*, *I*, *K*, and *L* being farther from the Meridian than their correſponding points at *g*, *h*, *i*, *k*, and *l*, they muſt be later of coming to it: and as both Suns come at the ſame moment to the point ♎, they come to the Meridian at the moment of noon by the Clock.

In departing from Libra, through the third quadrant, the real Sun going through *MNOPQ* towards ♑ at *R*, and the fictitious Sun through *mnopq* towards *r*, the former comes to the Meridian every day ſooner than the latter, until the real Sun comes to ♑, and the fictitious to *r*, and then they both come to the Meridian at the ſame time.

Laſtly, as the real Sun moves equably through *STUVW*, from ♑ towards ♈; and the fictitious Sun through *stuvw*, from *r* towards ♈, the former comes later every day to the Meridian than the latter, until they both arrive at the point ♈, and then they make it noon at the ſame time with the clock.

A Table of the Equation of Time depending on the Sun's place in the Ecliptic.

229. The annexed Table ſhews how much the Sun is faſter or ſlower than the clock ought to be, ſo far as the difference depends upon the obliquity of the Ecliptic; of which the Signs of the firſt and third quadrants are at the head of the Table, and their Degrees at the left hand; and in theſe the Sun is faſter than the Clock: the Signs of the ſecond and fourth quadrants are at the foot of the Table, and their degrees at the right hand; in all which the Sun is ſlower than the Clock: ſo that entering the Table with the given Sign of the Sun's place at the head of the Table, and the Degree of his place in that Sign at the left hand; or with the given Sign at the foot of the Table, and Degree at the right hand; in the Angle of meeting is the number of minutes and ſeconds that the Sun is faſter or ſlower than the clock: or in other words, the quantity of time in which the real Sun, when in that part of the Ecliptic, comes ſooner or later to the meridian than the fictitious Sun in the Equator. Thus,

when the Sun's place is ♉ Taurus 12 degrees, he is 9 minutes 49 ſeconds faſter than the clock; and when his place is ♋ Cancer 18 degrees, he is 6 minutes 2 ſeconds ſlower.

Sun faſter than the Clock in

Degrees.	♈ ♎		♉ ♏		♊ ♐		1ſt Q. 3d Q.
	′	″	′	″	′	″	Deg.
0	0	0	8	24	8	46	30
1	0	20	8	35	8	36	29
2	0	40	8	45	8	25	28
3	1	0	8	54	8	14	27
4	1	19	9	3	8	1	26
5	1	39	9	11	7	49	25
6	1	59	9	18	7	35	24
7	2	18	9	24	7	21	23
8	2	37	9	31	7	6	22
9	2	56	9	36	6	51	21
10	3	16	9	41	6	35	20
11	3	34	9	45	6	19	19
12	3	53	9	49	6	2	18
13	4	11	9	51	5	45	17
14	4	29	9	53	5	27	16
15	4	47	9	54	5	9	15
16	5	4	9	55	4	50	14
17	5	21	9	55	4	31	13
18	5	38	9	54	4	12	12
19	5	54	9	52	3	52	11
20	6	10	9	50	3	32	10
21	6	26	9	47	3	12	9
22	6	41	9	43	2	51	8
23	6	55	9	38	2	30	7
24	7	9	9	33	2	9	6
25	7	23	9	27	1	48	5
26	7	36	9	20	1	27	4
27	7	49	9	13	1	5	3
28	8	1	9	5	0	43	2
29	8	13	8	56	0	22	1
30	8	24	8	46	0	0	0
2d Q. 4th Q.	♍ ♓		♌ ♒		♋ ♑		Deg.

Sun ſlower than the Clock in

230. This

PLATE VI. Fig. III. 230. This part of the Equation of time may perhaps be ſomewhat difficult to underſtand by a Figure, becauſe both halves of the Ecliptic ſeem to be on the ſame ſide of the Globe; but it may be made very eaſy to any perſon who has a real Globe before him, by putting ſmall patches on every tenth or fifteenth degree both of the Equator and Ecliptic, beginning at Aries ♈; and then, turning the ball ſlowly round weſtward, he will ſee all the patches from Aries to Cancer come to the brazen Meridian ſooner than the correſponding patches on the Equator; all thoſe from Cancer to Libra will come later to the Meridian than their correſponding patches on the Equator; thoſe from Libra to Capricorn ſooner, and thoſe from Capricorn to Aries later: and the patches at the beginnings of Aries, Cancer, Libra, and Capricorn, being either on, or even with thoſe on the Equator, ſhew that the two Suns either meet there, or are even with one another, and ſo come to the Meridian at the ſame moment.

A machine for ſhewing the ſydereal, the equal, and the ſolar Time. 231. Let us ſuppoſe that there are two little balls moving equably round a celeſtial Globe by clock-work, one always keeping in the Ecliptic, and gilt with gold, to repreſent the real Sun; and the other keeping in the Equator, and ſilvered, to repreſent the fictitious Sun: and that whilſt theſe balls move once round the Globe according to the order of Signs, the Clock turns the Globe 366 times round it's Axis weſtward. The Stars will make 366 diurnal revolutions from the braſen Meridian to it again; and the two balls repreſenting the real and fictitious Sun always going farther eaſtward from any given Star, will come later than it to the Meridian every following day; and each ball will make 365 revolutions to the Meridian; coming equally to it at the beginnings of Aries, Cancer, Libra, and Capricorn: but in every other point of the Ecliptic, the gilt ball will come either ſooner or later to the Meridian than the ſilvered ball, like the patches above-mentioned. This would be a pretty enough way of ſhewing the reaſon why any given Star, which, on a certain day of the year, comes to the Meridian with the Sun, paſſes over it ſo much ſooner every following day, as on that day twelvemonth to come to the Meridian with the Sun again; and alſo to ſhew the reaſon why the real Sun comes to the Meridian ſometimes ſooner, ſometimes later, than it is noon by the clock; and, on four days of the year, at the ſame time; whilſt the fictitious Sun always comes to the Meridian when it is twelve at noon by the clock. This would be no difficult taſk for an artiſt to perform; for the gold ball might be carried round the Ecliptic by a wire from it's north Pole, and the ſilver ball round the Equator by a wire from it's ſouth Pole, by means of a few wheels to each; which might be eaſily added to my improvement of the celeſtial Globe, deſcribed in N° 483 of the *Philoſophical Tranſactions*; and of which I ſhall give a deſcription in the latter part of this Book, from the third Figure of the third plate. PLATE VI.

232. It is plain that if the Ecliptic were more obliquely poſited to the Equator, as the dotted Circle ♈ *x* ♎, the equal diviſions from ♈ to *x* would come ſtill ſooner to the Meridian *Z o* ♈ than thoſe marked *A*, *B*, *C*, *D*, and *E* do: for two diviſions containing 30 degrees, from ♈ to the ſecond dot, a little ſhort of the figure 1, come ſooner to the Meridian than one diviſion containing only 15 degrees from ♈ to *A* does, as the Ecliptic now ſtands; and thoſe of the ſecond quadrant from *x* to ♎ would be ſo much later. The third quadrant would be as the firſt, and the fourth as the ſecond. And it is likewiſe plain, that where the Ecliptic is moſt oblique, namely about Aries and Libra, the difference would be greateſt; and leaſt about Cancer and Capricorn, where the obliquity is leaſt. Fig. III.

234. Having

PLATE VI. The ſecond part of the Equation of Time. 234. Having explained one cauſe of the difference of time ſhewn by a well-regulated Clock and a true Sun-dial; and conſidered the Sun, not the Earth, as moving in the Ecliptic; we now proceed to explain the other cauſe of this difference, namely, the inequality of the Sun's apparent motion, § 205, which is ſloweſt in ſummer, when the Sun is fartheſt from the Earth, and ſwifteſt in winter when he is neareſt to it. But the Earth's motion on it's Axis is equable all the year round, and is performed from weſt to eaſt; which is the way that the Sun appears to change his place in the Ecliptic.

235. If the Sun's motion were equable in the Ecliptic, the whole difference between the equal time as ſhewn by a Clock, and the unequal time as ſhewn by the Sun, would ariſe from the obliquity of the Ecliptic. But the Sun's motion ſometimes exceeds a degree in 24 hours, though generally it is leſs: and when his motion is ſloweſt, any particular Meridian will revolve ſooner to him than when his motion is quickeſt; for it will overtake him in leſs time when he advances a leſs ſpace than when he moves through a larger.

236. Now, if there were two Suns moving in the plane of the Ecliptic, ſo as to go round it in a year; the one deſcribing an equal arc every 24 hours, and the other deſcribing ſometimes a leſs arc in 24 hours, and at other times a larger; gaining at one time of the year what it loſt at the oppoſite; it is evident that either of theſe Suns would come ſooner or later to the Meridian than the other, as it happened to be behind or before the other: and when they were both in conjunction, they would come to the Meridian at the ſame moment.

237. As the real Sun moves unequably in the Ecliptic, let us ſuppoſe a fictitious Sun to move equably in a circle coincident with the plane of the Ecliptic. Fig. IV. Let *ALCD* be the Ecliptic or Orbit

in which the real Sun moves, and the dotted Circle *abcd* the imaginary Orbit of the fictitious Sun; each going round in a year according to the order of letters, or from weſt to eaſt. Let *HIKL* be the Earth turning round it's Axis the ſame way every 24 hours; and ſuppoſe both Suns to ſtart from *A* and *a*, in a right line with the plane of the Meridian *EH*, at the ſame moment: the real Sun at *A*, being then at his greateſt diſtance from the Earth, at which time his motion is ſloweſt; and the fictitious Sun at *a*, whoſe motion is always equable, becauſe his diſtance from the Earth is ſuppoſed to be always the ſame. In the time that the Meridian revolves from *H* to *H* again, according to the order of the letters *HIKL*, the real Sun has moved from *A* to *F*; and the fictitious with a quicker motion from *a* to *f*, through a larger arc: therefore, the Meridian *EH* will revolve ſooner from *H* to *h* under the real Sun at *F*, than from *H* to *k* under the fictitious Sun at *f*; and conſequently it will then be noon by the Sun-dial ſooner than by the Clock.

As the real Sun moves from *A* towards *C*, the ſwiftneſs of his motion increaſes all the way to *C*, where it is at the quickeſt. But notwithſtanding this, the fictitious Sun gains ſo much upon the real, ſoon after his departing from *A*, that the increaſing velocity of the real Sun does not bring him up with the equally moving fictitious Sun till the former comes to *C*, and the latter to *c*, when each has gone half round it's reſpective Orbit; and then being in conjunction, the Meridian *EH* revolving to *EK* comes to both Suns at the ſame time, and therefore it is noon by them both at the ſame moment.

But the increaſed velocity of the real Sun, now being at the quickeſt, carries him before the fictitious one; and therefore, the ſame Meridian will come to the fictitious Sun ſooner than to the real: for whilſt the fictitious Sun moves from *c* to *g*, the

PLATE VI. the real Sun moves through a greater arc from *C* to *G*: conſequently the point *K* has it's noon by the Clock when it comes to *k*, but not it's noon by the Sun till it comes to *l*. And although the velocity of the real Sun diminiſhes all the way from *C* to *A*, and the fictitious Sun by an equable motion is ſtill coming nearer to the real Sun, yet they are not in conjunction till the one comes to *A* and the other to *a*; and then it is noon by them both at the ſame moment.

Thus it appears, that the ſolar noon is always later than noon by the clock whilſt the Sun goes from *C* to *A*, ſooner whilſt he goes from *A* to *C*, and at theſe two points the Sun and Clock being equal, it is noon by them both at the ſame moment.

Apogee, Perigee, and Apſides, what.

238. The point *A* is called *the Sun's Apogee*, becauſe when he is there he is at his greateſt diſtance from the Earth; the point *C* his *Perigee*, becauſe when in it he is at his leaſt diſtance from the Earth: and a right line, as *AEC*, drawn through the Earth's center, from one of theſe points to the other, is called *the line of the Apſides*. Fig. IV.

239. The diſtance that the Sun has gone in any time from his Apogee (not the diſtance he has to go to it, though ever ſo little) is called *his mean Anomaly*, and is reckoned in Signs and Degrees, allowing 30 Degrees to a Sign. Thus, when the Sun has gone ſuppoſe 174 degrees from his Apogee at *A*, he is ſaid to be 5 Signs 24 Degrees from it, which is his mean Anomaly: and when he is gone ſuppoſe 355 degrees from his Apogee, he is ſaid to be 11 Signs 25 Degrees from it, although he be but 5 Degrees ſhort of *A* in coming round to it again.

Mean Anomaly, what.

240. From what was ſaid above, it appears, that when the Sun's Anomaly is leſs than 6 Signs, that is, when he is any where between *A* and *C*, in the half *ABC* of his Orbit, the ſolar noon pre-

cedes the clock noon; but when his Anomaly is more than 6 Signs, that is, when he is any where between *C* and *A*, in the half *CDA* of his Orbit, the clock noon precedes the ſolar. When his Anomaly is 0 Signs 0 Degrees, that is, when he is in his Apogee at *A*; or 6 Signs 0 Degrees, which is when he is in his Perigee at *C*; he comes to the Meridian at the moment that the fictitious Sun does, and then it is noon by them both at the ſame inſtant.

241. The following Table ſhews the Variation, or Equation of time depending on the Sun's Anomaly, and ariſing from his unequal motion in the Ecliptic; as the former Table, § 229, ſhews the Variation depending on the Sun's place, and reſulting from the obliquity of the Ecliptic: this is to be underſtood the ſame way as the other, namely, that when the Signs are at the head of the Table, the Degrees are at the left hand; but when the Signs are at the foot of the Table, the reſpective Degrees are at the right hand; and in both caſes the Equation is in the Angle of meeting. When both the above-mentioned Equations are either faſter or ſlower, their ſum is the abſolute Equation of Time; but when the one is faſter, and the other ſlower, it is their difference. Thus, ſuppoſe the Equation depending on the Sun's place, be 6 minutes 41 ſeconds too ſlow, and the Equation depending on the Sun's Anomaly, be 4 minutes 20 ſeconds too ſlow, their Sun is 11 minutes 1 ſecond too ſlow. But if the one had been 6 minutes 41 ſeconds too faſt, and the other 4 minutes 20 ſeconds too ſlow, their difference would have been 2 minutes 21 ſeconds too faſt, becauſe the greater quantity is too faſt.

A Table of the Equation of Time, depending on the Sun's Anomaly.

Sun faſter than the Clock if his Anomaly be

D.	0 Signs		1		2		3		4		5		
	′	″	′	″	′	″	′	″	′	″	′	″	
0	0	0	3	48	6	39	7	45	6	47	3	57	30
1	0	8	3	55	6	43	7	45	6	43	3	50	29
2	0	16	4	2	6	47	7	45	6	39	3	43	28
3	0	24	4	9	6	51	7	45	6	35	3	35	27
4	0	32	4	16	6	54	7	45	6	30	3	28	26
5	0	40	4	22	6	58	7	44	6	26	3	20	25
6	0	48	4	29	7	1	7	44	6	21	3	13	24
7	0	56	4	35	7	5	7	43	6	16	3	5	23
8	1	3	4	42	7	8	7	42	6	11	2	58	22
9	1	11	4	48	7	11	7	41	6	6	2	50	21
10	1	19	4	54	7	14	7	40	6	1	2	42	20
11	1	27	5	0	7	17	7	38	5	56	2	35	19
12	1	35	5	6	7	20	7	37	5	51	2	27	18
13	1	43	5	12	7	22	7	35	5	45	2	19	17
14	1	50	5	18	7	25	7	34	5	40	2	11	16
15	1	58	5	24	7	27	7	32	5	34	2	3	15
16	2	6	5	30	7	29	7	30	5	28	1	55	14
17	2	13	5	35	7	31	7	28	5	22	1	47	13
18	2	21	5	41	7	33	7	25	5	16	1	39	12
19	2	28	5	46	7	35	7	23	5	10	1	31	11
20	2	36	5	52	7	36	7	20	5	4	1	22	10
21	2	43	5	57	7	38	7	18	4	58	1	14	9
22	2	51	6	2	7	39	7	15	4	51	1	6	8
23	2	58	6	7	7	41	7	12	4	45	0	58	7
24	3	6	6	12	7	42	7	9	4	38	0	50	6
25	3	13	6	16	7	43	7	5	4	31	0	41	5
26	3	20	6	21	7	43	7	2	4	25	0	33	4
27	3	27	6	26	7	44	6	58	4	18	0	25	3
28	3	34	6	30	7	44	6	55	4	11	0	17	2
29	3	41	6	34	7	45	6	51	4	4	0	8	1
30	3	48	6	39	7	45	6	47	3	57	0	0	0
	11 Signs		10		9		8		7		6		D.

Sun ſlower than the Clock if his Anomaly be

242. The obliquity of the Ecliptic to the Equator, which is the firſt mentioned cauſe of the Equation of Time, would make the Sun and Clocks agree on four days of the year; which are, when the Sun enters Aries, Cancer, Libra, and Capricorn: but the other cauſe, now explained,

would make the Sun and Clocks equal only twice in a year; that is, when the Sun is in his Apogee and Perigee. Conſequently, when theſe two points fall in the beginnings of Cancer and Capricorn, or of Aries and Libra, they concur in making the Sun and Clocks equal in theſe points. But the Apogee at preſent is in the 9th degree of Cancer, and the Perigee in the 9th degree of Capricorn; and therefore the Sun and Clocks cannot be equal about the beginnings of theſe Signs, nor at any time of the year, except when the ſwiftneſs or ſlowneſs of Equation reſulting from one cauſe juſt balances the ſlowneſs or ſwiftneſs ariſing from the other.

243. The ſecond Table in the following Chapter ſhews the Sun's place in the Ecliptic at the noon of every day by the Clock, for the ſecond year after Leap-year; and alſo the Sun's Anomaly to the neareſt degree, neglecting the odd minutes of that degree. It's uſe is only to aſſiſt in the method of making a general Equation Table from the two fore-mentioned Tables of Equation depending on the Sun's Place and Anomaly, § 229, 241; concerning which method we ſhall give a few examples preſently. The next following Tables are made from thoſe two; and ſhew the abſolute Equation of Time reſulting from the combination of both it's cauſes; in which the minutes, as well as degrees, both of the Sun's Place and Anomaly are conſidered. The uſe of theſe Tables is already explained, § 225; and they ſerve for every day in Leap-year, and the firſt, ſecond, and third years after: For on moſt of the ſame days of all theſe years the Equation differs, becauſe of the odd ſix hours more than the 365 days of which the year conſiſts.

Examples for making Equation Tables.

EXAMPLE I. On the 15th of *April*, the Sun is in the 25th degree of ♈ Aries, and his Anomaly is 9 Signs 15 Degrees; the Equation reſulting from the former is 7 minutes 23 ſeconds of time too faſt, § 229; and from the latter, 7 minutes 27 ſeconds too ſlow, § 241; the difference is 4 ſeconds that the Sun is too ſlow at the noon of that day; taking it in groſs for the degrees of the Sun's Place and Anomaly, without making proportionable allowance for the odd minutes. Hence, at noon the ſwiftneſs of the one Equation balancing ſo nearly the ſlowneſs of the other, makes the Sun and Clocks equal on ſome part of that day.

EXAMPLE II. On the 16th of *June*, the Sun is in the 25th degree of ♊ Gemini, and his Anomaly is 11 Signs 16 Degrees; the Equation ariſing from the former is 1 minute 48 ſeconds too faſt; and from the latter 1 minute 50 ſeconds too ſlow; which balancing one another at noon to 2 ſeconds, the Sun and Clocks are again equal on that day,

EXAMPLE III. On the 31ſt of *Auguſt*, the Sun's place is 7 degrees 52 minutes of ♍ Virgo (which we call the 8th degree, as it is ſo near) and his Anomaly is 2 Signs 0 Degrees; the Equation ariſing from the former is 6 minutes 41 ſeconds too ſlow; and from the latter 6 minutes 39 ſeconds too faſt; the difference being only 2 ſeconds too ſlow at noon, and decreaſing towards an equality, will make the Sun and Clocks equal in the afternoon of that day.

EXAMPLE IV. On the 23d of *December*, the Sun's place is 1 degree 41 minutes (call it 2 degrees) of ♑ Capricorn, and his Anomaly is 5 Signs 23 Degrees; the Equation for the former is 43 ſeconds too ſlow, and for the latter 58 ſeconds too faſt; the difference is 15 ſeconds too faſt at noon; which decreaſing will come to an equality, and ſo make the Sun and Clocks equal in the evening of that day.

And thus we find, that on ſome part of each of the above-mentioned four days, the Sun and Clocks are equal; but if we work examples for all other days of the year, we ſhall find them different. And,

Remark.

244. On thoſe days which are equidiſtant from any Equinox or Solſtice, we do not find that the Equation is as much too faſt or too ſlow, on the one ſide, as it is too ſlow or too faſt on the other. The reaſon is, that the line of the Apſides, § 238, does not, at preſent, fall either into the Equinoctial or Solſtitial points, § 242.

The reaſon why Equation Tables are but temporary.

The four following Equation Tables, for Leap-year, and the firſt, ſecond, and third years after, would ſerve for ever, if the Sun's Place and Anomaly were always the ſame on every given day of the year as on the ſame day four years before or after. But ſince that is not the caſe, no general Equation Tables can be ſo conſtructed as to be perpetual.

C H A P. XIV.

Of the Preceſſion of the Equinoxes.

246. IT has been already obſerved, § 116, that by the Earth's motion on it's Axis, there is more matter accumulated all around the equatoreal parts than any where elſe on the Earth.

The Sun and Moon, by attracting this redundancy of matter, bring the Equator ſooner under them in every return towards it, than if there was no ſuch accumulation. Therefore, if the Sun ſets out, as from any Star, or other fixed point in the Heavens, the moment when he is departing from the Equinoctial or from either Tropic, he will come to the ſame Equinox or Tropic again 20 min. 17$\frac{1}{2}$ ſec. of time, or 50 ſeconds of a degree, before he compleats his courſe ſo, as to arrive at the ſame fixed Star or Point from whence he ſet out. For, the

PLATE VI. the Equinoctial points recede 50 ſeconds of a degree weſtward every year, contrary to the Sun's annual progreſſive motion.

When the Sun arrives at the ſame * Equinoctial or Solſtitial point, he finiſhes what we call the *Tropical Year*; which, by obſervation, is found to contain 365 days 5 hours 48 minutes 57 ſeconds; and when he arrives at the ſame fixed Star again, as ſeen from the Earth, he compleats the *Sydereal Year*, which contains 365 days 6 hours 9 minutes 14½ ſeconds. The *Sydereal Year* is therefore 20 minutes 17½ ſeconds longer than the Solar or Tropical year, and 9 minutes 14½ ſeconds longer than the Julian or Civil year, which we ſtate at 365 days 6 hours: ſo that the Civil year is almoſt a mean betwixt the Sydereal and Tropical.

247. As the Sun deſcribes the whole Ecliptic, or 360 degrees, in a Tropical year, he moves 59′ 8″ of a degree every day at a mean rate; and conſequently 50″ of a degree in 20 minutes 17½ ſeconds of time: therefore, he will arrive at the ſame Equinox or Solſtice when he is 50″ of a degree ſhort of the ſame Star or fixed point in the Heavens from which he ſet out in the year before. So that with reſpect to the fixed Stars, the Sun and Equinoctial points fall back (as it were) 30 degrees in 2160 years; which will make the Stars appear to have gone 30 deg. forward, with reſpect to the Signs of the Ecliptic in that time: for the ſame Signs always keep in the ſame points of the Ecliptic, without regard to the Conſtellations.

Fig. IV. To explain this by a Figure, let the Sun be in Conjunction with a fixed Star at *S*, ſuppoſe in the 30th degree of ♉, on the 21ſt day of *May* 1756. Then making 2160 revolutions through the Ecliptic

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* The two oppoſite points in which the Ecliptic croſſes the Equinoctial, are called *the Equinoctial points:* and the two points where the Ecliptic touches the Tropics (which are likewiſe oppoſite, and 90 degrees from the former) are called *the Solſtitial points.*

A TABLE *ſhewing the Preceſſion of the Equinoctial Points in the Heavens, both in Motion and Time; and the Anticipation of the Equinoxes on Earth.*

Julian years.	Preceſſion of the Equinoctial Points in the Heavens.								Anticipation of the Equinoxes on the Earth.			
	Motion.				Time.							
	s	°	′	″	Days	H.	M.	S.	D.	H.	M.	S.
1	0	0	0	50	0	0	20	17½	0	0	11	3
2	0	0	1	40	0	0	40	35	0	0	22	6
3	0	0	2	30	0	1	0	52½	0	0	33	9
4	0	0	3	20	0	1	21	10	0	0	44	12
5	0	0	4	10	0	1	41	27½	0	0	55	15
6	0	0	5	0	0	2	1	45	0	1	6	18
7	0	0	5	50	0	2	22	2½	0	1	17	21
8	0	0	6	40	0	2	42	20	0	1	28	24
9	0	0	7	30	0	3	2	37½	0	1	39	27
10	0	0	8	20	0	3	22	55	0	1	50	30
20	0	0	16	40	0	6	45	50	0	3	41	0
30	0	0	25	0	0	10	8	45	0	5	31	30
40	0	0	33	20	0	13	31	40	0	7	22	0
50	0	0	41	40	0	16	54	35	0	9	12	30
60	0	0	50	0	0	20	17	30	0	11	3	0
70	0	0	58	20	0	23	40	25	0	12	53	30
80	0	1	6	40	1	3	3	20	0	14	44	0
90	0	1	15	0	1	6	26	15	0	16	34	30
100	0	1	23	20	1	9	49	10	0	18	25	0
200	0	2	46	40	2	19	38	20	1	12	50	0
300	0	4	10	0	4	5	27	30	2	7	15	0
400	0	5	33	20	5	15	16	40	3	1	40	0
500	0	6	56	40	7	1	5	50	3	20	5	0
600	0	8	20	0	8	10	55	0	4	14	30	0
700	0	9	43	20	9	20	44	10	5	8	55	0
800	0	11	6	40	11	6	33	20	6	3	20	0
900	0	12	30	0	12	16	22	30	6	21	45	0
1000	0	13	53	20	14	2	11	40	7	16	10	0
2000	0	27	46	40	28	4	23	20	15	8	20	0
3000	1	11	40	0	42	6	35	0	23	0	30	0
4000	1	25	33	20	56	8	46	40	30	16	40	0
5000	2	9	26	40	70	10	58	20	38	8	50	0
6000	2	23	20	0	84	13	10	0	46	1	0	0
7000	3	7	13	20	98	15	21	40	53	17	10	0
8000	3	21	6	40	112	17	33	20	61	9	20	0
9000	4	5	0	0	126	19	45	0	69	1	30	0
10000	4	18	53	20	140	21	56	40	76	17	40	0
20000	9	7	46	40	281	19	53	20	153	11	20	0
25920	12	0	0	0	365	6	0	0	198	21	36	0

tic *VWX*, at the end of ſo many Sydereal years, he will be found again at *S*: but at the end of ſo many Julian years, he will be found at *M*, ſhort of *S*: and at the end of ſo many Tropical years, he will be found ſhort of *M*, in the 30th deg. of Taurus at *T*, which has receded back from *S* to *T* in that time, by the Preceſſion of the Equinoctial points ♈ *Aries* and ♎ *Libra*. The Arc *ST* will be equal to the amount of the Preceſſion of the Equinox in 2160 years, at the rate of $50''$ of a degree, or 20 min. $17\frac{1}{2}$ ſec. of time, annually: this, in ſo many years, makes 30 days $10\frac{1}{2}$ hours; which is the difference between 2160 Sydereal and Tropical years: And the Arc *MT* will be equal to the ſpace moved through by the Sun in 2160 times 11 min. 3 ſec. or 16 days 13 hours 48 minutes, which is the difference between 2160 Julian and Tropical years.

248. From the ſhifting of the Equinoctial points, and with them, all the Signs of the Ecliptic, it follows that thoſe Stars which in the infancy of Aſtronomy were in *Aries* are now got into *Taurus*; thoſe of *Taurus* into *Gemini*, &c. Hence likewiſe it is, that the Stars which roſe or ſet at any particular ſeaſon of the year, in the times of HESIOD, EUDOXUS, VIRGIL, PLINY, &c. by no means anſwer at this time to their deſcriptions. The preceding Table ſhews the quantity of this ſhifting both in the Heavens and on the Earth, for any number of years to 25,920; which compleats the grand celeſtial period: within which any number and it's quantity is eaſily found; as in the following example, for 5763 years; which at the Autumnal Equinox, *A. D.* 1756, is thought to be the age of the world. So that with regard to the fixed Stars, the Equinoctial points in the Heavens, have receded $2^{s}\ 20^{\circ}\ 2'\ 30''$ ſince the creation; which is as much as the Sun moves in $81^{d}\ 5^{h}\ 0^{m}\ 52^{s}$. And ſince that time, or in 5763 years, the Equinoxes with

us have fallen back 44^{d} 5^{h} 21^{m} 9^{s}; hence, reckoning from the time of the *Julian* Equinox, *A. D.* 1756, *viz. Sept.* 11th, it appears that the Autumnal Equinox at the creation was on the 25th of *October*.

Julian years.	Preceſſion of the Equinoctial Points in the Heavens.								Anticipation of the Equinoxes on the Earth.			
	Motion.				Time.							
	s	°	′	″	D.	H.	M.	S.	D.	H.	M.	S.
5000	2	9	26	40	70	10	58	20	38	8	50	0
700	0	9	43	20	9	20	44	10	5	8	55	0
60	0	0	50	0	0	20	17	30	0	11	3	0
3	0	0	2	30	0	1	0	52	0	0	33	9
5763	2	20	2	30	81	5	0	52	44	5	21	9

The anticipation of the Equinoxes and Seaſons.

249. The anticipation of the Equinoxes, and conſequently of the Seaſons, is by no means owing to the Preceſſion of the Equinoctial and Solſtitial points in the Heavens (which can only affect the apparent motions, places and declinations of the fixed Stars) but to the difference between the Civil and ſolar year, which is 11 minutes 3 ſeconds; the Civil year containing 365 days 6 hours, and the Solar year 365 days 5 hours 48 minutes 57 ſeconds. The following Table ſhews the length, and conſequently the difference of any number of Sydereal, Civil, and Solar years from 1 to 10,000.

The reaſon for altering the Style.

250. The above 11 minutes 3 ſeconds, by which the Civil or Julian year exceeds the Solar, amounts to 11 days in 1433 years: and ſo much our ſeaſons have fallen back with reſpect to the days of the months, ſince the time of the *Nicene* Council in *A. D.* 325, and therefore in order to bring back all the Faſts and Feſtivals to the days then ſettled, it

PLATE VI. it was requiſite to ſuppreſs 11 nominal days. And that the ſame ſeaſons might be kept to the ſame times of the year for the future, to leave out the Biſſextile-day in *February* at the end of every century of years not diviſible by 4; reckoning them only common years, as the 17th, 18th, and 19th centuries, *viz.* the years 1700, 1800, 1900, *&c.* becauſe a day intercalated every fourth year was too much, and retaining the Biſſextile-day at the end of thoſe Centuries of years which are diviſible by 4, as the 16th, 20th, and 24th Centuries; *viz.* the years 1600, 2000, 2400, *&c.* Otherwiſe, in length of time the ſeaſons would be quite reverſed with regard to the months of the year; though it would have required near 23,783 years to have brought about ſuch a total change. If the Earth had made exactly $365\frac{1}{4}$ diurnal rotations on it's Axis, whilſt it revolved from any Equinoctial or Solſtitial point to the ſame again, the Civil and ſolar years would always have kept pace together; and the Style would never have needed any alteration.

The Preceſſion of the Equinoctial points. 251. Having already mentioned the cauſe of the Preceſſion of the Equinoctial points in the Heavens, § 246, which occaſions a ſlow deviation of the Earth's axis from it's paralleliſm, and thereby a change of the declination of the Stars from the Equator, together with a ſlow apparent motion of the Stars forward with reſpect to the Signs of the Ecliptic; we ſhall now deſcribe the Phenomena by a Diagram.

Fig. VI. Let *NZSVL* be the Earth, *SONA* it's Axis produced to the ſtarry Heavens, and terminating in *A*, the preſent north Pole of the Heavens, which is vertical to *N* the north Pole of the Earth. Let *EOQ* be the Equator, *T*♋*Z* the Tropic of Cancer, and *VT*♑ the Tropic of Capricorn: *VOZ* the Ecliptic, and *BO* it's Axis, both which are immoveable among the Stars. But, as * the Equinoctial points recede in the Ecliptic, the Earth's Axis *SON* is in motion upon the Earth's center *O*, in in ſuch a manner, as to deſcribe the double Cone *NOn* and *SOs*, round the Axis of the Ecliptic *BO*, in the time that the Equinoctial points move quite round the Ecliptic, which is 25,920 years; and in that length of time, the north Pole of the Earth's Axis produced, deſcribes the Circle *ABCDA* in the ſtarry Heavens, round the Pole of the Ecliptic, which keeps immoveable in the center of that Circle. The Earth's Axis being 23½ degrees inclined to the Axis of the Ecliptic, the Circle *ABCDA* deſcribed by the north Pole of the Earth's Axis produced in *A*, is 47 degrees in diameter, or double the inclination of the Earth's Axis. In conſequence of this, the point *A*, which at preſent is the north Pole of the Heavens, and near to a Star of the ſecond magnitude in the tail of the conſtellation called *the Little Bear*, muſt be deſerted by the Earth's Axis; which moving backwards a degree every 72 years, will be directed towards the Star or Point *B* in 6480 years hence: and in double of that time, or 12,960 years, it will be directed towards the Star or Point *C*; which will then be the north Pole of the Heavens, although it is at preſent 8½ degrees ſouth of the Zenith of *London L*. The preſent poſition of the Equator *EOQ*, will then be changed into *eOq*, the Tropic of Cancer *T*♋*Z* into *Vt*♋, and the Tropic of Capricorn *VT*♑ into *t*♑*Z*; as is evident by the Figure. And the Sun, in the ſame part of the Heavens where he is now over the earthly Tropic of Capricorn, and makes the ſhorteſt days and longeſt nights in the Northern Hemiſphere, will then be over the earthly Tropic of Cancer, and make the days longeſt, and nights ſhorteſt. So that it will require 12,960 years yet more, or 25,920 from the then preſent time, to bring the north Pole *N* quite round, ſo as to be directed toward that point of the Heavens which is vertical to it at preſent. And then, and not till then, the ſame Stars which at preſent deſcribe the Equator, Tropics, and polar Circles, *&c.* by the Earth's diurnal motion, will deſcribe them over again.

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* The Equinoctial Circle interſects the Ecliptic in two oppoſite points, called *Aries* and *Libra*, from the Signs which always keep in theſe points: They are called the Equinoctial Points, becauſe when the Sun is in either of them, he is directly over the terreſtrial Equator; and then the days and nights are equal.

TABLE *ſhewing the Time contained in any number of Sydereal, Julian, and Solar Years, from* 1 *to* 10000.

	Sydereal Years.				Julian Years.		Solar Years.			
Years	Days	H.	M.	S.	Days	H.	Days	H.	M.	S.
1	365	6	9	14½	365	6	365	5	48	57
2	730	12	18	29	730	12	730	11	37	54
3	1095	18	27	43½	1095	18	1095	17	26	51
4	1461	0	36	58	1461	0	1460	23	15	48
5	1826	6	46	12½	1826	6	1826	5	4	45
6	2191	12	55	27	2191	12	2191	10	53	42
7	2556	19	5	41½	2556	18	2556	16	42	39
8	2922	1	13	56	2922	0	2921	22	31	36
9	3287	7	23	10½	3287	6	3287	4	20	33
10	3652	13	32	25	3652	12	3652	10	9	30
20	7305	3	4	50	7305	0	7304	20	19	0
30	10957	16	37	15	10957	12	10957	6	28	30
40	14610	6	9	40	14610	0	14609	16	38	0
50	18262	19	42	5	18262	12	18262	2	47	30
60	21915	9	14	30	21915	0	21914	12	57	0
70	25567	22	46	55	25567	12	25566	23	6	30
80	29220	12	19	20	29220	0	29219	9	16	0
90	32873	1	51	45	32872	12	32871	19	25	30
100	36525	15	24	10	36525		36524	5	35	
200	73051	6	48	20	73050		73048	11	10	
300	109576	22	12	30	109575		109572	16	45	
400	146102	13	36	40	146100		146096	22	20	
500	182628	5	0	50	182625		182621	3	55	
600	219153	20	25		219150		219145	9	30	
700	255679	11	49	10	255675		255669	15	5	
800	292205	3	13	20	292200		292193	20	40	
900	328730	18	37	30	328725		328718	2	15	
1000	365256	10	1	40	365250		365242	7	50	
2000	730512	20	3	20	730500		730484	15	40	
3000	1095769	6	5		1095750		1095726	23	30	
4000	1461025	16	6	40	1461000		1460969	7	20	
5000	1826282	2	8	20	1826250		1826211	15	10	
6000	2191538	12	10		2191500		2191453	23	0	
7000	2556794	22	11	40	2556750		2556696	6	50	
8000	2922051	8	13	20	2922000		2921938	14	40	
9000	3287037	18	15		3287250		3287180	22	30	
10000	3652564	4	16	40	3652500		3652423	6	20	

A TABLE ſhewing the Sun's true Place, and Diſtance from his Apogee, for the ſecond Year after Leap-year.

Days	January				February				March				April			
	Sun's Place.		Sun's Anom.		Sun's Place.		Sun's Anom.		Sun's Place.		Sun's Anom.		Sun's Place.		Sun's Anom.	
	D.	M.	S.	D.	D.	M.	S.	D.	D.	M	S.	D.	D.	M.	S.	D.
1	11 ♑	7	6	2	12 ♒	39	7	3	10 ♓	53	8	0	11 ♈	40	9	1
2	12	8	6	3	13	40	7	4	11	53	8	1	12	39	9	2
3	13	9	6	4	14	41	7	5	12	53	8	2	13	38	9	3
4	14	10	6	5	15	42	7	6	13	53	8	3	14	37	9	4
5	15	11	6	6	16	43	7	7	14	53	8	4	15	36	9	5
6	16	12	6	7	17	43	7	8	15	53	8	5	16	35	9	6
7	17	14	6	8	18	44	7	9	16	53	8	6	17	34	9	7
8	18	15	6	9	19	45	7	10	17	53	8	7	18	33	9	8
9	19	16	6	10	20	46	7	11	18	53	8	8	19	32	9	9
10	20	17	6	11	21	46	7	12	19	53	8	9	20	30	9	10
11	21	18	6	12	22	47	7	13	20	52	8	10	21	29	9	11
12	22	19	6	13	23	47	7	14	21	52	8	11	22	28	9	12
13	23	21	6	14	24	48	7	15	22	52	8	12	23	26	9	13
14	24	22	6	15	25	48	7	16	23	52	8	13	24	25	9	14
15	25	23	6	16	26	49	7	17	24	51	8	14	25	24	9	15
16	26	24	6	17	27	49	7	18	25	51	8	15	26	22	9	16
17	27	25	6	18	28	50	7	19	26	51	8	16	27	21	9	17
18	28	26	6	19	29	50	7	20	27	50	8	17	28	19	9	18
19	29	27	6	20	♓	51	7	21	28	50	8	18	29	18	9	19
20	♒	28	6	21	1	51	7	22	29	49	8	19	♉	16	9	20
21	1	29	6	22	2	51	7	23	♈	49	8	20	1	15	9	21
22	2	30	6	23	3	52	7	24	1	48	8	21	2	13	9	22
23	3	31	6	24	4	52	7	25	2	47	8	22	3	11	9	23
24	4	32	6	25	5	52	7	26	3	47	8	23	4	10	9	24
25	5	33	6	26	6	52	7	27	4	46	8	24	5	8	9	25
26	6	34	6	27	7	53	7	28	5	45	8	25	6	6	9	26
27	7	35	6	28	8	53	7	29	6	45	8	26	7	4	9	27
28	8	36	6	29	9	53	8	0	7	44	8	27	8	3	9	28
29	9	37	7	0					8	43	8	28	9	1	9	29
30	10	38	7	1					9	42	8	29	9	59	9	29
31	11	39	7	2					10	41	9	0				

A TABLE ſhewing the Sun's true Place, and Diſtance from his Apogee, for the ſecond Year after Leap-year.

Days	May				June				July				Auguſt			
	Sun's Place.		Sun's Anom.		Sun's Place.		Sun's Anom		Sun's Place.		Sun's Anom.		Sun's Place.		Sun's Anom.	
	D.	M.	S.	D.	D.	M.	S	D.	D.	M.	S.	D.	D.	M.	S.	D.
1	10 ♉	57	10	0	10 ♊	46	11	1	9 ♋	24	0	0	8 ♌	59	1	0
2	11	55	10	1	11	44	11	2	10	21	0	1	9	57	1	1
3	12	53	10	2	12	41	11	3	11	18	0	2	10	54	1	2
4	13	51	10	3	13	38	11	4	12	15	0	3	11	52	1	3
5	14	49	10	4	14	35	11	5	13	13	0	4	12	49	1	4
6	15	47	10	5	15	33	11	6	14	10	0	5	13	47	1	5
7	16	45	10	6	16	30	11	7	15	7	0	6	14	44	1	6
8	17	43	10	7	17	28	11	8	16	4	0	7	15	42	1	7
9	18	41	10	8	18	25	11	9	17	1	0	8	16	39	1	8
10	19	39	10	9	19	22	11	10	17	59	0	8	17	37	1	9
11	20	37	10	10	20	20	11	11	18	56	0	9	18	35	1	10
12	21	34	10	11	21	17	11	12	19	53	0	10	19	32	1	11
13	22	32	10	12	22	14	11	13	20	50	0	11	20	30	1	12
14	23	30	10	13	23	11	11	14	21	47	0	12	21	28	1	13
15	24	28	10	14	24	8	11	15	22	45	0	13	22	25	1	14
16	25	26	10	15	25	6	11	16	23	42	0	14	23	23	1	15
17	26	23	10	16	26	3	11	17	24	39	0	15	24	21	1	16
18	27	21	10	17	27	0	11	18	25	36	0	16	25	19	1	17
19	28	19	10	18	27	58	11	18	26	34	0	17	26	17	1	18
20	29	16	10	19	28	55	11	19	27	31	0	18	27	14	1	19
21	♊	15	10	20	29	52	11	20	28	28	0	19	28	12	1	20
22	1	11	10	21	♋	49	11	21	29	26	0	20	29	10	1	21
23	2	9	10	22	1	46	11	22	♌	23	0	21	♍	8	1	22
24	3	6	10	23	2	44	11	23	1	20	0	22	1	6	1	23
25	4	4	10	24	3	41	11	24	2	18	0	23	2	4	1	24
26	5	2	10	25	4	38	11	25	3	15	0	24	3	2	1	25
27	5	59	10	26	5	35	11	26	4	12	0	25	4	0	1	26
28	6	56	10	27	6	32	11	27	5	10	0	26	4	58	1	27
29	7	54	10	28	7	30	11	28	6	7	0	27	5	56	1	28
30	8	51	10	29	8	27	11	29	7	5	0	28	6	54	1	29
31	9	48	11	0					8	2	0	29	7	52	2	0

A TABLE ſhewing the Sun's true Place, and Diſtance from his Apogee, for the ſecond Year after Leap-year.

Days	September				October				November				December			
	Sun's Place.		Sun's Anom.		Sun's Place.		Sun's Anom.		Sun's Place.		Sun's Anom.		Sun's Place.		Sun's Anom.	
	D.	M.	S.	D	D.	M.	S.	D.	D.	M.	S.	D.	D.	M.	S.	D.
1	8 ♍	51	2	1	8 ♎	10	3	1	9 ♏	0	4	2	9 ♐	18	5	1
2	9	49	2	2	9	9	3	2	10	0	4	3	10	19	5	2
3	10	47	2	3	10	8	3	3	11	0	4	4	11	20	5	3
4	11	45	2	4	11	8	3	4	12	1	4	5	12	21	5	4
5	12	43	2	5	12	7	3	5	13	1	4	6	13	22	5	5
6	13	42	2	6	13	6	3	6	14	1	4	7	14	23	5	6
7	14	40	2	7	14	6	3	7	15	2	4	8	15	24	5	7
8	15	39	2	8	15	5	3	8	16	2	4	9	16	25	5	8
9	16	37	2	9	16	4	3	9	17	2	4	10	17	26	5	9
10	17	35	2	10	17	4	3	10	18	3	4	11	18	27	5	10
11	18	34	2	11	18	3	3	11	19	3	4	12	19	28	5	11
12	19	32	2	12	19	3	3	12	20	4	4	13	20	29	5	12
13	20	31	2	13	20	2	3	13	21	4	4	14	21	30	5	13
14	21	29	2	14	21	2	3	14	22	5	4	15	22	31	5	14
15	22	28	2	15	22	2	3	15	23	5	4	16	23	32	5	15
16	23	27	2	16	23	1	3	16	24	6	4	17	24	33	5	16
17	24	25	2	17	24	1	3	17	25	7	4	18	25	34	5	17
18	25	24	2	18	25	1	3	18	26	7	4	19	26	35	5	18
19	6	23	2	19	26	0	3	19	27	8	4	20	27	36	5	19
20	27	21	2	20	27	0	3	20	28	9	4	21	28	38	5	20
21	28	20	2	21	28	0	3	21	29	9	4	22	29	39	5	21
22	29	19	2	22	29	0	3	22	♐	10	4	23	♑	40	5	22
23	♎	18	2	23	♏	0	3	23	1	11	4	24	1	41	5	23
24	1	17	2	24	1	0	3	24	2	12	4	25	2	42	5	24
25	2	16	2	25	2	0	3	25	3	12	4	26	3	44	5	25
26	3	15	2	26	3	0	3	26	4	13	4	27	4	45	5	26
27	4	14	2	27	4	0	3	27	5	14	4	28	5	46	5	27
28	5	13	2	28	5	0	3	28	6	15	4	29	6	47	5	28
29	6	12	2	29	6	0	3	29	7	16	4	29	7	48	5	29
30	7	11	3	0	7	0	4	0	8	17	5	0	8	49	6	0
31					8	0	4	1					9	51	6	1

A TABLE

A TABLE of the Equation of natural Days, ſhewing what Time it ought to be by the Clock when the Sun is on the Meridian.

The Biſſextile, or Leap-year.

Days	January			Dif.	February			Dif.	March			Dif.	April			Dif.
	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S.	S.
				Inc.				Inc.				Dec.				Dec.
1	12	4	0	28	12	14	5	7	12	12	36	13	12	3	48	18
2	12	4	28	28	12	14	12	7	12	12	23	13	12	3	30	19
3	12	4	56	28	12	14	19	6	12	12	10	14	12	3	11	18
4	12	5	24	27	12	14	25	5	12	11	56	14	12	2	53	18
5	12	5	51	27	12	14	30	4	12	11	42	14	12	2	35	18
6	12	6	18	26	12	14	34	3	12	11	28	15	12	2	17	17
7	12	6	44	26	12	14	37	3	12	11	13	15	12	2	0	17
8	12	7	10	25	12	14	40	2	12	10	58	16	12	1	43	17
9	12	7	35	25	12	14	42	1	12	10	42	16	12	1	26	17
10	12	8	0	24	12	14	43	Dec.	12	10	4[illegible]	16	12	1	9	16
11	12	8	24	23	12	14	44	1	12	10	10	17	12	0	53	16
12	12	8	47	23	12	14	43	1	12	9	53	17	12	0	37	16
13	12	9	10	22	12	14	42	2	12	9	36	17	12	0	21	15
14	12	9	32	22	12	14	40	3	12	9	19	17	12	0	6	15
15	12	9	54	21	12	14	37	4	12	9	2	18	11	59	51	15
16	12	10	15	20	12	14	33	4	12	8	44	18	11	59	36	15
17	12	10	35	19	12	14	29	5	12	8	26	18	11	59	21	14
18	12	10	54	19	12	14	24	5	12	8	8	18	11	59	7	13
19	12	11	13	18	12	14	19	6	12	7	50	18	11	58	54	13
20	2	11	31	17	12	14	13	7	12	7	32	18	11	58	41	13
21	12	11	48	17	12	14	6	8	12	7	14	19	11	58	28	12
22	12	12	5	16	12	13	58	8	12	6	55	19	11	58	1[illegible]	12
23	12	12	21	15	12	13	50	9	12	6	36	19	11	58	4	12
24	12	12	36	14	12	13	41	9	12	6	17	19	11	57	52	1
25	12	12	50	13	12	13	32	10	12	5	58	18	11	57	4[illegible]	10
26	12	13	3	12	12	13	22	11	12	5	40	19	11	57	31	10
27	12	13	15	12	12	13	11	11	12	5	21	19	11	57	21	9
28	12	13	27	11	12	13	0	12	12	5	2	18	11	57	12	9
29	12	13	38	10	12	12	48	12	12	4	44	19	11	57	3	8
30	12	13	48	9					12	4	25	19	11	56	55	8
31	12	13	57	8					12	4	6	18				

Incr. 9′ 57″

Incr. 0′ 39″
Decr. 1 56

Decr. 8′ 30″

Decr. 6′ 53″

A TABLE of the Equation of natural Days, ſhewing what Time it ought to be by the Clock when the Sun is on the Meridian.

The Biſſextile, or Leap-year.

Days	May			Dif	June			Dif.	July			Dif.	Auguſt			Dif.
	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S.	S.
				Dec.				Inc.				Inc.				Dec.
1	11	56	47	7	11	57	22	9	12	3	18	11	12	5	46	4
2	11	56	40	7	11	57	31	9	12	3	29	11	12	5	42	5
3	11	56	33	6	11	57	40	10	12	3	40	11	12	5	37	5
4	11	56	27	6	11	57	50	10	12	3	51	11	12	5	32	6
5	11	56	21		11	58	0		12	4	2		12	5	26	
				5				11				10				6
6	11	56	16	4	11	58	11	11	12	4	12	10	12	5	20	7
7	11	56	12	4	11	58	22	11	12	4	22	9	12	5	13	8
8	11	56	8	4	11	58	33	11	12	4	31	9	12	5	5	8
9	11	56	4	3	11	58	44	12	12	4	40	8	12	4	57	9
10	11	56	1		11	58	56		12	4	48		12	4	48	
				2				12				8				9
11	11	55	59	1	11	59	8	12	12	4	56	8	12	4	39	10
12	11	55	58	1	11	59	20	12	12	5	4	7	12	4	29	10
13	11	55	57	Inc.	11	59	32	12	12	5	11	7	12	4	19	11
14	11	55	56	1	11	59	44	13	12	5	18	6	12	4	8	12
15	11	55	57		11	59	57		12	5	24		12	3	56	
				1				13				6				12
16	11	55	58	1	12	0	10	13	12	5	30	5	12	3	44	12
17	11	55	59	2	12	0	23	12	12	5	35	5	12	3	32	13
18	11	56	1	2	12	0	35	13	12	5	40	4	12	3	19	13
19	11	56	3	3	12	0	48	13	12	5	44	4	12	3	6	14
20	11	56	6		12	1	1		12	5	48		12	2	52	
				3				13				3				14
21	11	56	9	4	12	1	14	13	12	5	51	2	12	2	38	15
22	11	56	13	5	12	1	27	13	12	5	53	2	12	2	23	15
23	11	56	18	5	12	1	40	13	12	5	55	2	12	2	8	16
24	11	56	23	6	12	1	53	13	12	5	57	1	12	1	52	16
25	11	56	29		12	2	6		12	5	58		12	1	36	
				6				12				1				17
26	11	56	35	7	12	2	18	13	12	5	59	Dec.	12	1	19	17
27	11	56	42	7	12	2	31	12	12	5	58	1	12	1	2	17
28	11	56	49	7	12	2	43	12	12	5	57	2	12	0	45	17
29	11	56	56	8	12	2	55	12	12	5	55	2	12	0	28	18
30	11	57	4		12	3	7		12	5	53		12	0	10	
				9				11				3				18
31	11	57	13	9					12	5	50	4	11	59	52	19

May	June	July	Auguſt
Decr. 0′ 50″ Incr. 1 17	Incr. 5′ 45″	Incr. 2′ 41″ Decr. 0 8	Decr. 5′ 54″

A TABLE of the Equation of natural Days, ſhewing what Time it ought to be by the Clock when the Sun is on the Meridian.

The Biſſextile, or Leap-year.

Days	September			Dif.	October			Dif	November			Dif.	December			Dif.
	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S.	S.
				Dec.				Dec.				Dec.				Inc.
1	11	59	33	19	11	49	28	18	11	43	49	1	11	49	42	24
2	11	59	14	19	11	49	10	18	11	43	48	Inc.	11	50	6	24
3	11	58	55	19	11	48	52	18	11	43	49	1	11	50	30	25
4	11	58	36	19	11	48	34	18	11	43	50	2	11	50	54	25
5	11	58	17	20	11	48	16	17	11	43	52	3	11	51	20	26
6	11	57	57	20	11	47	59	17	11	43	55	4	11	51	46	26
7	11	57	37	20	11	47	42	16	11	43	59	5	11	52	12	26
8	11	57	17	20	11	47	26	15	11	44	4	6	11	52	38	27
9	11	56	57	21	11	47	11	15	11	44	10	6	11	53	5	28
10	11	56	36	21	11	46	56	15	11	44	16	7	11	53	33	28
11	11	56	15	21	11	46	41	15	11	44	23	8	11	54	1	29
12	11	55	54	21	11	46	26	14	11	44	31	9	11	54	30	29
13	11	55	33	21	11	46	12	13	11	44	40	10	11	54	59	29
14	11	55	12	21	11	45	59	13	11	44	50	11	11	55	28	29
15	11	54	51	21	11	45	46	12	11	45	1	12	11	55	57	29
16	11	54	30	20	11	45	34	11	11	45	13	13	11	56	26	30
17	11	54	10	21	11	45	23	11	11	45	26	13	11	56	56	30
18	11	53	49	21	11	45	12	11	11	45	39	14	11	57	26	30
19	11	53	28	21	11	45	1	10	11	45	53	15	11	57	56	30
20	11	53	7	21	11	44	51	9	11	46	8	16	11	58	26	30
21	11	52	46	21	11	44	42	9	11	46	24	16	11	58	56	30
22	11	52	25	20	11	44	33	8	11	46	40	17	11	59	26	30
23	11	52	5	20	11	44	25	7	11	46	57	18	11	59	56	30
24	11	51	45	20	11	44	18	7	11	47	15	19	12	0	26	30
25	11	51	25	20	11	44	11	6	11	47	34	20	12	0	56	30
26	11	51	5	20	11	44	5	5	11	47	54	20	12	1	26	30
27	11	50	45	20	11	44	0	4	11	48	14	21	12	1	56	29
28	11	50	25	19	11	43	56	3	11	48	35	22	12	2	25	29
29	11	50	6	19	11	43	53	2	11	48	57	22	12	2	54	29
30	11	49	47	19	11	43	51	1	11	49	19	23	12	3	23	29
31					11	43	50	1					12	3	52	
	Decr. 9′ 46″				Decr. 5′ 38″				Decr. 0′ 1″ Incr. 5 30				Incr. 14′ 10″			

A TABLE

A TABLE of the Equation of natural Days, ſhewing what Time it ought to be by the Clock when the Sun is on the Meridian.

The firſt after Leap-year.

Days	January			Dif.	February			Dif.	March			Dif.	April			Dif.
	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S	S.	H.	M.	S.	S.
				Inc.				Inc.				Dec.				Dec.
1	12	4	21	28	12	14	11	7	12	12	39	13	12	3	52	18
2	12	4	49	27	12	14	18	6	12	12	26	13	12	3	34	18
3	12	5	1	27	12	14	24	5	12	12	13	13	12	3	16	18
4	12	5	43	27	12	14	29	5	12	12	0	14	12	2	58	18
5	12	6	10		12	14	34		12	11	46		12	2	40	
				27				4				14				18
6	12	6	37	26	12	14	38	3	12	11	32	15	12	2	22	18
7	12	7	3	25	12	14	41	2	12	11	17	15	12	2	4	17
8	12	7	28	25	12	14	43	1	12	11	2	16	12	1	47	17
9	12	7	53	24	12	14	44	0	12	10	46	16	12	1	30	17
10	12	8	1		12	14	44		12	10	30		12	1	13	
				24				Dec.				17				16
11	12	8	4	23	12	14	44	1	12	10	14	17	12	0	57	16
12	12	9	4	22	12	14	43	2	12	9	57	17	12	0	41	16
13	12	9	26	22	12	14	41	3	12	9	40	17	12	0	25	16
14	12	9	48	21	12	14	38	3	12	9	23	17	12	0	9	15
15	12	10	9		12	14	35		12	9	6		11	59	54	
				21				4				18				15
16	12	10	30	20	12	14	31	5	12	8	48	18	11	59	39	14
17	12	10	50	19	12	14	26	6	12	8	30	18	11	59	25	14
18	12	11	9	18	12	14	20	6	12	8	12	18	11	59	11	14
19	12	11	27	17	12	14	14	7	12	7	54	18	11	58	57	13
20	12	11	44		12	14	7		12	7	36		11	58	44	
				17				7				18				13
21	12	12	1	16	12	14	0	8	12	7	18	19	11	58	31	12
22	12	12	17	15	12	13	52	9	12	6	59	19	11	58	19	12
23	12	12	32	14	12	13	43	9	12	6	40	19	11	58	7	12
24	12	12	46	13	12	13	34	10	12	6	21	19	11	57	55	11
25	12	12	59		12	13	24		12	6	2		11	57	44	
				13				10				19				10
26	12	13	12	12	12	13	14	11	12	5	43	19	11	57	34	10
27	12	13	23	11	12	13	3	12	12	5	24	19	11	57	24	10
28	12	13	34	10	12	12	51	12	12	5	5	19	11	57	14	9
29	12	13	44	9					12	4	46	18	11	57	5	8
30	12	13	53						12	4	28		11	56	57	
				9								18				8
31	12	14	3	8					12	4	10	18				

Incr. 9′ 42″	Incr. 0′ 33″ Decr. 1 53	Decr. 8′ 29″	Decr. 6′ 55″

A TABLE

A TABLE of the Equation of natural Days, ſhewing what Time it ought to be by the Clock when the Sun is on the Meridian.

The firſt after Leap-year.

Days	May			Dif.	June			Dif	July			Dif	Auguſt			Dif.
	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S.	S.
				Dec.				Inc.				Inc.				Dec.
1	11	56	49	8	11	57	18	9	12	3	15	12	12	5	48	4
2	11	56	41	7	11	57	27	9	12	3	27	11	12	5	44	5
3	11	56	34	6	11	57	36	10	12	3	38	11	12	5	39	5
4	11	56	28	6	11	57	46	10	12	3	49	10	12	5	34	6
5	11	56	22		11	57	56		12	3	59		12	5	28	
				5				10				10				6
6	11	56	17	4	11	58	6	11	12	4	9	10	12	5	22	7
7	11	56	13	4	11	58	17	11	12	4	19	10	12	5	15	7
8	11	56	9	4	11	58	28	12	12	4	29	9	12	5	8	8
9	11	56	5	3	11	58	40	12	12	4	38	8	12	5	0	9
10	11	56	2		11	58	52		12	4	46		12	4	51	
				2				12				8				9
11	11	56	0	2	11	59	4	12	12	4	54	8	12	4	42	10
12	11	55	58	1	11	59	16	12	12	5	2	8	12	4	32	10
13	11	55	57	1	11	59	28	12	12	5	10	7	12	4	22	11
14	11	55	56	Inc.	11	59	40	13	12	5	17	6	12	4	11	11
15	11	55	56		11	59	53		12	5	23		12	4	0	
				1				13				6				12
16	11	55	57	1	12	0	6	13	12	5	29	5	12	3	48	12
17	11	55	58	2	12	0	19	13	12	5	34	5	12	3	36	13
18	11	56	0	2	12	0	32	13	12	5	39	4	12	3	23	13
19	11	56	2	3	12	0	45	13	12	5	43	4	12	3	10	14
20	11	56	5		12	0	58		12	5	47		12	2	56	
				3				13				4				14
21	11	56	8	4	12	1	11	13	12	5	51	3	12	2	42	15
22	11	56	12	4	12	1	24	13	12	5	54	2	12	2	17	15
23	11	56	16	5	12	1	37	13	12	5	56	1	12	2	12	16
24	11	56	21	6	12	1	50	13	12	5	57	1	12	1	56	16
25	11	56	27		12	2	3		12	5	58		12	1	40	
				6				13				Dec.				16
26	11	56	33	6	12	2	16	12	12	5	59	1	12	1	24	17
27	11	56	39	7	12	2	28	12	12	5	58	1	12	1	7	17
28	11	56	46	7	12	2	40	12	12	5	57	2	12	1	50	18
29	11	56	53	8	12	2	52	12	12	5	55	2	12	0	32	18
30	11	57	1		12	3	4		12	5	53		12	0	14	
				8				11				2				18
31	11	57	9	9					12	5	51	3	11	59	56	19

May	June	July	Auguſt
Decr. 0′ 53″ Incr. 1 12	Incr. 5′ 46″	Incr. 2′ 43″ Decr. 0 8	Decr. 5′ 52″

A TABLE of the Equation of natural Days, ſhewing what Time it ought to be by the Clock when the Sun is on the Meridian.

The firſt after Leap-year.

Days	September			Dif.	October			Dif.	November			Dif.	December			Dif.
	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S.	S.
				Dec.				Dec.				Dec.				Inc.
1	11	59	38	19	11	49	33	19	11	43	49	0	11	49	36	24
2	11	59	19	19	11	49	14	19	11	43	49	Inc.	11	50	0	24
3	11	59	0	19	11	48	5	18	11	43	49	1	11	50	24	25
4	11	58	41	20	11	48	37	17	11	43	50	2	11	50	49	25
5	11	58	21		11	48	20		11	43	52		11	51	14	
—				20				17				3				26
6	11	58	1	20	11	48	3	17	11	43	55	3	11	51	40	26
7	11	57	41	20	11	47	46	17	11	43	58	4	11	52	6	27
8	11	57	21	20	11	47	29	16	11	44	2	5	11	52	33	27
9	11	57	1	20	11	47	13	15	11	44	7	6	11	53	0	27
10	11	56	41		11	46	58		11	44	13		11	53	27	
—				20				15				7				28
11	11	56	21	21	11	46	43	14	11	44	20	8	11	53	35	28
12	11	56	0	21	11	46	29	13	11	44	28	9	11	54	23	29
13	11	55	39	21	11	46	16	13	11	44	37	10	11	54	52	29
14	11	55	18	21	11	46	3	13	11	44	47	11	11	55	21	29
15	11	54	57		11	45	50		11	44	58		11	55	50	
—				21				13				12				30
16	11	54	36	21	11	45	37	12	11	45	10	13	11	56	19	30
17	11	54	15	21	11	45	25	11	11	45	23	13	11	56	49	30
18	11	53	54	21	11	45	14	11	11	45	36	14	11	57	19	30
19	11	53	33	21	11	45	3	10	11	45	50	14	11	57	49	30
20	11	53	12		11	44	53		11	46	4		11	58	19	
—				21				10				15				30
21	11	52	51	20	11	44	43	9	11	46	19	16	11	58	49	30
22	11	52	31	20	11	44	34	8	11	46	35	17	11	59	19	30
23	11	52	11	21	11	44	26	7	11	46	52	18	11	59	49	30
24	11	51	50	21	11	44	19	6	11	47	10	19	12	0	10	30
25	11	51	29		11	44	13		11	47	29		12	0	49	
—				20				6				19				30
26	11	51	9	20	11	44	7	5	11	47	48	20	12	1	19	30
27	11	50	49	19	11	44	2	4	11	48	8	21	12	1	49	29
28	11	50	39	19	11	43	58	3	11	48	29	22	12	2	18	29
29	11	50	11	19	11	43	55	3	11	48	51	22	12	2	47	29
30	11	49	52		11	43	52		11	49	13		12	3	16	
—				19				2				23				29
31					11	43	50	1					12	3	45	29
	Decr. 9′ 46″				Decr. 5′ 43″				Decr. 0′ 0″ Incr. 5 24				Incr. 14′ 9″			

A TABLE

A TABLE of the Equation of natural Days, ſhewing what Time it ought to be by the Clock when the Sun is on the Meridian.

The ſecond after Leap-year.

Days	January			Dif.	February			Dif.	March			Dif.	April			Dif.
	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S	S.
				Inc.				Dec.				Inc.				Dec.
1	12	4	14	28	12	14	9	7	12	12	42	13	12	3	56	18
2	12	4	42	28	12	14	16	6	12	12	29	13	12	3	38	18
3	12	5	10	27	12	14	22	5	12	12	16	13	12	3	20	18
4	12	5	37	27	12	14	27	5	12	12	3	14	12	3	2	18
5	12	6	4	27	12	14	32	4	12	11	49	14	12	2	44	18
6	12	6	30	26	12	14	36	3	12	11	35	15	12	2	26	17
7	12	6	56	26	12	14	39	2	12	11	20	15	12	2	9	17
8	12	7	22	25	12	14	41	2	12	11	5	15	12	1	52	17
9	12	7	47	24	12	14	43	1	12	10	50	16	12	1	35	17
10	12	8	11	24	12	14	44	Dec.	12	10	34	16	12	1	18	17
11	12	8	35	23	12	14	44	1	12	10	18	17	12	1	1	16
12	12	8	58	22	12	14	43	2	12	10	1	17	12	0	45	16
13	12	9	20	22	12	14	41	3	12	9	44	17	12	0	29	16
14	12	9	42	21	12	14	38	3	12	9	27	17	12	0	13	15
15	12	10	3	21	12	14	35	4	12	9	10	18	11	59	58	15
16	12	10	24	20	12	14	31	4	12	8	52	18	11	59	43	14
17	12	10	44	19	12	14	27	5	12	8	34	18	11	59	29	14
18	12	11	3	18	12	14	22	6	12	8	16	18	11	59	15	14
19	12	11	21	18	12	14	16	7	12	7	58	18	11	59	1	14
20	12	11	39	17	12	14	9	7	12	7	40	18	11	58	47	13
21	12	11	56	16	12	14	2	8	12	7	22	18	11	58	34	12
22	12	12	12	15	12	13	54	9	12	7	4	19	11	58	22	12
23	12	12	27	15	12	13	45	9	12	6	45	19	11	58	10	12
24	12	12	42	14	12	13	36	10	12	6	26	19	11	57	58	11
25	12	12	56	13	12	13	26	10	12	6	7	19	11	57	47	11
26	12	13	9	12	12	13	16	11	12	5	48	19	11	57	36	10
27	12	13	21	11	12	13	5	11	12	5	29	19	11	57	26	10
28	12	13	32	10	12	12	54	12	12	5	10	19	11	57	16	9
29	12	13	42	10					12	4	51	18	11	57	7	9
30	12	13	52	9					12	4	33	18	11	56	58	8
31	12	14	1	8					12	4	15	18				
	Incr. 9′ 47″				Incr. 0′ 35″ Decr. 1 50				Decr. 8′ 27″				Decr. 6′ 58″			

A TABLE of the Equation of natural Days, ſhewing what Time it ought to be by the Clock when the Sun is on the Meridian.

The ſecond after Leap-year.

Days	May			Dif.	June			Dif.	July			Dif.	Auguſt			Dif.
	H.	M.	S	S.	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S.	S.
				Dec				Inc.				Inc.				Dec.
1	11	56	50	8	11	57	16	9	12	3	12	12	12	5	48	4
2	11	56	42	7	11	57	25	10	12	3	24	11	12	5	44	4
3	11	56	35	6	11	57	35	10	12	3	35	11	12	5	40	5
4	11	56	29	6	11	57	45	10	12	3	46	11	12	5	35	5
5	11	56	23		11	57	55		12	3	57		12	5	30	
				5				10				10				6
6	11	56	19	5	11	58	5	11	12	4	7	10	12	5	24	7
7	11	56	13	4	11	58	16	11	12	4	17	9	12	5	17	7
8	11	56	9	3	11	58	27	11	12	4	26	9	12	5	10	8
9	11	56	6	3	11	58	38	12	12	4	35	9	12	5	2	9
10	11	56	3		11	58	50		12	4	44		12	4	53	
				2				12				8				9
11	11	56	1	2	11	59	2	12	12	4	52	8	12	4	44	9
12	11	55	59	2	11	59	14	12	12	5	0	8	12	4	35	10
13	11	55	57	1	11	59	26	12	12	5	8	7	12	4	25	11
14	11	55	56	Inc.	11	59	38	12	12	5	15	6	12	4	14	11
15	11	55	56		11	59	50		12	5	21		12	4	3	
				1				13				6				12
16	11	55	57	1	12	0	3	13	12	5	27	6	12	3	51	12
17	11	55	58	2	12	0	16	13	12	5	33	5	12	3	39	12
18	11	56	0	2	12	0	29	13	12	5	38	4	12	3	27	13
19	11	56	2	3	12	0	42	13	12	5	42	4	12	3	14	14
20	11	56	5		12	0	55		12	5	46		12	3	0	
				3				13				3				14
21	11	56	8	3	12	1	8	13	12	5	49	3	12	2	46	15
22	11	56	11	4	12	1	21	13	12	5	52	2	12	2	31	15
23	11	56	15	5	12	1	34	13	12	5	54	2	12	2	16	15
24	11	56	20	6	12	1	47	12	12	5	56	2	12	2	1	16
25	11	56	26		12	1	59		12	5	58		12	1	45	
				6				13				1				16
26	11	56	32	6	12	2	12	13	12	5	59	Dec	12	1	29	17
27	11	56	38	7	12	2	25	12	12	5	58	1	12	1	12	17
28	11	56	45	7	12	2	37	12	12	5	57	1	12	0	55	18
29	11	56	52	8	12	2	49	12	12	5	56	2	12	0	37	18
30	11	57	0		12	3	1		12	5	54		12	0	19	
				8				11				3				18
31	11	57	8	8					12	5	51	3	12	0	1	18

May	June	July	Auguſt
Decr. 0′ 54″ Incr. 1 12	Incr. 5′ 45″	Incr. 2′ 46″ Decr. 0 8	Decr. 5′ 47″

A TABLE of the Equation of natural Days, ſhewing what Time it ought to be by the Clock when the Sun is on the Meridian.

The ſecond after Leap-year.

Days	September			Dif.	October			Dif.	November			Dif.	December			Dif.
	H.	M.	S.	S.	H.	M.	S	S.	H.	M.	S.	S.	H.	M.	S.	S.
				Dec.				Dec.				Dec.				Inc
1	11	59	43	19	11	49	37	19	11	43	49	1	11	49	30	23
2	11	59	24	19	11	49	19	18	11	43	48	Inc	11	49	53	24
3	11	59	5	19	11	49	0	18	11	43	49	1	11	50	17	25
4	11	58	46	20	11	48	42	18	11	43	50	2	11	50	42	25
5	11	58	26		11	48	24		11	43	52		11	51	7	
				20				17				3				25
6	11	58	6	20	11	48	7	17	11	43	55	3	11	51	33	26
7	11	57	46	20	11	47	50	17	11	43	58	4	11	51	59	26
8	11	57	26	21	11	47	33	16	11	44	2	5	11	52	25	27
9	11	57	5	20	11	47	17	16	11	44	7	6	11	52	52	28
10	11	56	45		11	47	1		11	44	13		11	53	20	
				21				15				7				28
11	11	56	24	21	11	46	46	14	11	44	20	8	11	53	48	28
12	11	56	3	21	11	46	32	14	11	44	28	9	11	54	16	28
13	11	55	42	20	11	46	18	13	11	44	37	9	11	54	44	29
14	11	55	22	20	11	46	5	13	11	44	46	10	11	54	13	29
15	11	55	2		11	45	52		11	44	56		11	55	42	
				21				13				11				29
16	11	54	41	21	11	45	39	12	11	45	7	12	11	56	11	30
17	11	54	20	21	11	45	27	11	11	45	19	13	11	56	41	30
18	11	53	59	20	11	45	16	10	11	45	32	14	11	57	11	30
19	11	53	39	21	11	45	6	10	11	45	46	15	11	57	41	30
20	11	53	18		11	44	56		11	46	1		11	58	11	
				21				10				15				30
21	11	52	57	20	11	44	46	9	11	46	16	16	11	58	41	30
22	11	52	37	21	11	44	37	8	11	46	32	17	11	59	11	30
23	11	52	16	21	11	44	29	7	11	46	49	18	11	59	41	30
24	11	51	55	21	11	44	22	7	11	47	7	18	12	0	11	30
25	11	51	34		11	44	15		11	47	25		12	0	41	
				20				6				19				30
26	11	51	14	20	11	44	9	5	11	47	44	20	12	1	11	30
27	11	50	54	20	11	44	4	5	11	48	4	21	12	1	41	30
28	11	50	34	19	11	43	59	4	11	48	25	21	12	2	11	29
29	11	50	15	19	11	43	55	3	11	48	46	22	12	2	40	29
30	11	49	56		11	43	52		11	49	8		12	3	9	
				19				2				22				29
31					11	43	50	1					12	3	38	29

Decr. 9′ 47″ Decr. 5′ 47″ Decr. 0′ 1″ Incr. 14′ 8″
Incr. 5 19

A TABLE

A TABLE of the Equation of natural Days, ſhewing what Time it ought to be by the Clock when the Sun is on the Meridian.

The third after Leap-year.

Days	January			Dif	February			Dif.	March			Dif.	April			Dif.
	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S.	S.
				Inc.				Inc.				Dec.				Dec.
1	12	4	7	28	12	14	6	7	12	12	44	12	12	4	1	18
2	12	4	35	28	12	14	13	7	12	12	32	13	12	3	43	18
3	12	5	3	27	12	14	20	6	12	12	19	13	12	3	25	18
4	12	5	30	27	12	14	26	5	12	12	6	14	12	3	7	18
5	12	5	57		12	14	31		12	11	52		12	2	49	
				27				4				14				18
6	12	6	24	26	12	14	35	3	12	11	38	14	12	2	31	18
7	12	6	50	25	12	14	38	2	12	11	24	15	12	2	13	18
8	12	7	15	25	12	14	41	1	12	11	9	16	12	1	55	17
9	12	7	40	25	12	14	43	1	12	10	53	16	12	1	38	17
10	12	8	5		12	14	44		12	10	37		12	1	21	
				24				Dec.				16				16
11	12	8	59	23	12	14	44	1	12	10	21	16	12	1	5	16
12	12	8	52	23	12	14	43	2	12	10	5	17	12	0	49	16
13	12	9	15	22	12	14	41	2	12	10	48	17	12	0	33	16
14	12	9	37	21	12	14	39	3	12	9	31	17	12	0	17	15
15	12	9	58		12	14	36		12	9	14		12	0	2	
				21				4				17				15
16	12	10	19	20	12	14	32	4	12	8	57	18	11	59	47	15
17	12	10	39	19	12	14	28	5	12	8	39	18	11	59	32	14
18	12	10	58	18	12	14	23	6	12	8	21	18	11	59	18	14
19	12	11	16	18	12	14	17	7	12	8	3	18	11	59	4	14
20	12	11	34		12	14	10		12	7	45		11	58	50	
				17				7				18				13
21	12	11	51	16	12	14	3	8	12	7	27	19	11	58	37	13
22	12	12	7	16	12	13	55	8	12	7	8	19	11	58	24	12
23	12	12	23	15	12	13	47	9	12	6	49	19	11	58	12	12
24	12	12	38	14	12	13	38	9	12	6	30	19	11	58	0	11
25	12	12	52		12	13	29		12	6	11		11	57	49	
				13				10				18				11
26	12	13	5	12	12	13	19	11	12	5	53	19	11	57	38	10
27	12	13	17	11	12	13	8	12	12	5	34	19	11	57	28	10
28	12	13	28	11	12	12	56	12	12	5	15	18	11	57	18	9
29	12	13	39	10					12	4	57	19	11	57	9	9
30	12	13	49						12	4	38		11	57	0	
				9								19				8
31	12	13	58	8					12	4	19	18				

Incr. 9′ 51″

Incr. 0′ 38″
Decr. 1 48

Decr. 8′ 25″

Decr. 7′ 1″

A TABLE

A TABLE of the Equation of natural Days, ſhewing what Time it ought to be by the Clock when the Sun is on the Meridian.

The third after Leap-year.

Days	May			Dif	June			Dif	July			Dif.	Auguſt			Dif.
	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S.	S.
				Dec.				Inc.				Inc.				Dec.
1	11	56	52	8	11	57	15	9	12	3	10	11	12	5	49	4
2	11	56	44	7	11	57	24	9	12	3	21	11	12	5	45	4
3	11	56	37	7	11	57	33	9	12	3	32	11	12	5	41	5
4	11	56	30	6	11	57	42	10	12	3	43	11	12	5	36	5
5	11	56	24		11	57	52		12	3	54		12	5	31	
				5				10				10				6
6	11	56	19	5	11	58	2	11	12	4	4	10	12	5	25	7
7	11	56	14	4	11	58	13	11	12	4	14	10	12	5	18	7
8	11	56	10	4	11	58	24	11	12	4	24	9	12	5	11	7
9	11	56	6	3	11	58	35	11	12	4	33	9	12	5	4	8
10	11	56	3		11	58	46		12	4	42		12	4	56	
				2				12				8				9
11	11	56	1	2	11	58	58	12	12	4	50	8	12	4	47	9
12	11	55	59	2	11	59	10	12	12	4	58	8	12	4	37	10
13	11	55	57	1	11	59	22	12	12	5	6	7	12	4	27	10
14	11	55	56	Inc.	11	59	34	13	12	5	13	6	12	4	17	11
15	11	55	56		11	59	47		12	5	19		12	4	6	
				1				13				6				12
16	11	55	57	1	12	0	0	13	12	5	25	6	12	3	54	12
17	11	55	58	1	12	0	13	13	12	5	31	5	12	3	42	13
18	11	55	59	2	12	0	26	13	12	5	36	5	12	3	29	13
19	11	56	1	2	12	0	39	13	12	5	41	4	12	3	16	13
20	11	56	3		12	0	52		12	5	45		12	3	3	
				3				13				4				14
21	11	56	6	4	12	1	5	12	12	5	49	3	12	2	49	15
22	11	56	10	4	12	1	17	13	12	5	52	3	12	2	34	15
23	11	56	14	5	12	1	30	13	12	5	55	2	12	2	19	15
24	11	56	19	5	12	1	43	13	12	5	57	1	12	2	4	16
25	11	56	24		12	1	56		12	5	58		12	1	48	
				6				13				1				16
26	11	56	30	6	12	2	9	13	12	5	59	Dec.	12	1	32	16
27	11	56	36	7	12	2	22	12	12	5	58	1	12	1	16	17
28	11	56	43	7	12	2	34	12	12	5	57	1	12	0	59	17
29	11	56	50	8	12	2	46	12	12	5	56	2	12	0	42	18
30	11	56	58		12	2	58		12	5	54		12	0	24	
				8				12				2				18
31	11	57	6	9					12	5	52	3	12	0	6	19

May	June	July	Auguſt
Decr. 0′ 56″ Incr. 1 10	Incr. 5′ 43″	Incr. 2′ 48″ Decr. 0 7	Incr. 5′ 43″

A TABLE

A TABLE of the Equation of natural Days, ſhewing what Time it ought to be by the Clock when the Sun is on the Meridian.

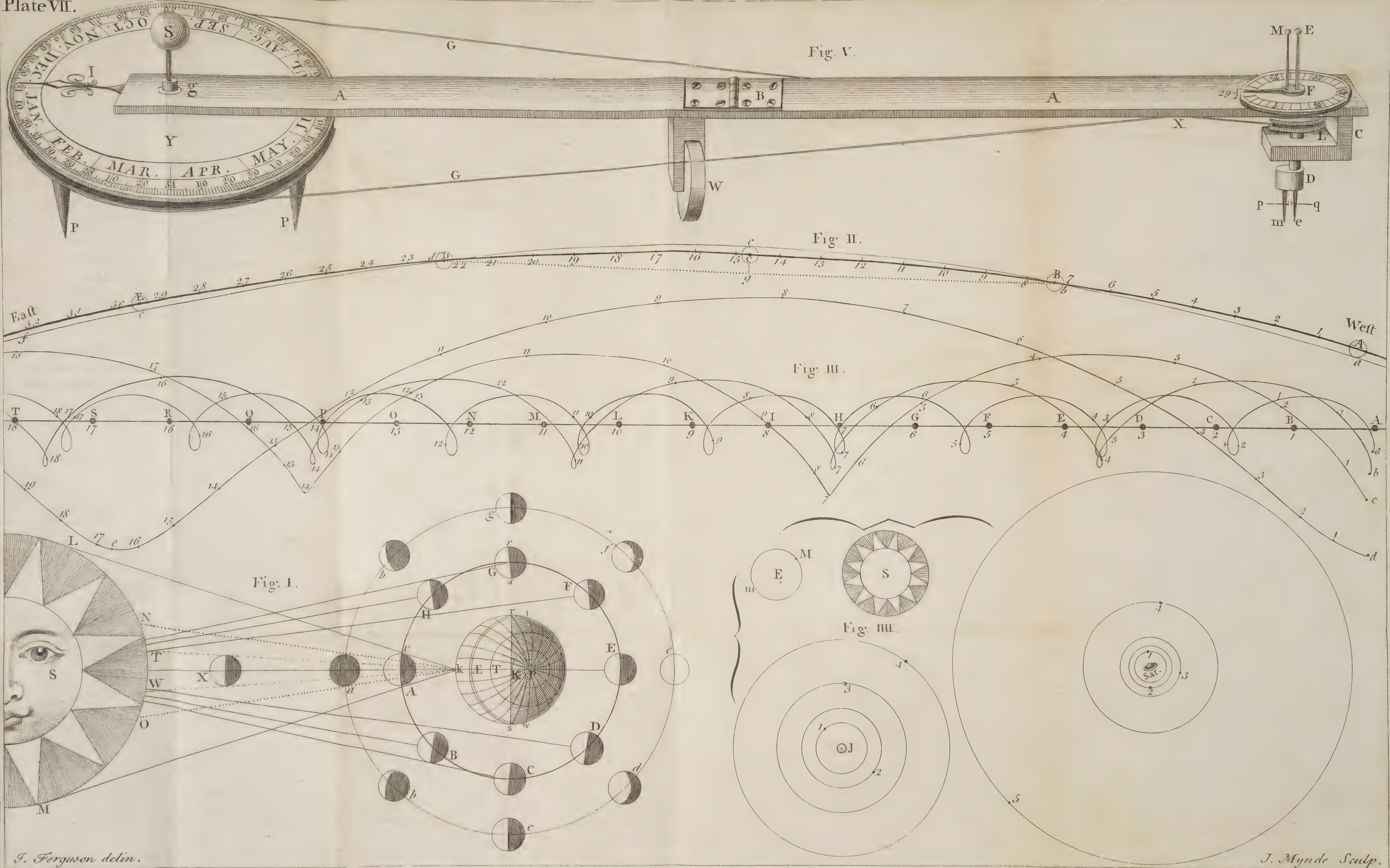
The third after Leap-year.

Days	September			Dif.	October			Dif.	November			Dif.	December			Dif.
	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S.	S.	H.	M.	S.	S.
				Dec.				Dec.				Dec.				Inc.
1	11	59	47	19	11	49	42	18	11	43	49	1	11	49	25	23
2	11	59	28	19	11	49	24	18	11	43	48	Inc	11	49	48	24
3	11	59	9	19	11	49	6	18	11	43	48	1	11	50	12	24
4	11	58	50	19	11	48	48	18	11	43	49	2	11	50	36	25
5	11	58	31		11	48	30		11	43	51		11	51	1	
				20				18				2				25
6	11	58	11	20	11	48	12	17	11	43	53	3	11	51	26	26
7	11	57	51	20	11	47	55	16	11	43	56	4	11	51	52	27
8	11	57	31	20	11	47	39	16	11	44	0	5	11	52	19	27
9	11	57	11	20	11	47	23	16	11	44	5	6	11	52	46	27
10	11	56	51		11	47	7		11	44	11		11	53	13	
				20				15				7				28
11	11	56	31	21	11	46	52	15	11	44	18	8	11	53	41	28
12	11	56	10	21	11	46	37	14	11	44	26	8	11	54	8	28
13	11	55	49	21	11	46	23	14	11	44	34	9	11	54	37	29
14	11	55	28	21	11	46	9	13	11	44	43	10	11	55	6	30
15	11	55	7		11	45	56		11	44	53		11	55	36	
				20				12				11				29
16	11	54	47	21	11	45	44	12	11	45	4	12	11	56	6	30
17	11	54	26	21	11	45	32	12	11	45	16	13	11	56	36	30
18	11	54	5	21	11	45	20	11	11	45	29	14	11	57	6	29
19	11	53	44	21	11	45	9	10	11	45	43	14	11	57	35	30
20	11	53	23		11	44	59		11	45	57		11	58	5	
				20				9				15				30
21	11	53	3	21	11	44	50	9	11	46	12	16	11	58	34	30
22	11	52	42	21	11	44	41	9	11	46	28	17	11	59	4	30
23	11	52	21	20	11	44	32	8	11	46	45	17	11	59	31	30
24	11	52	1	21	11	44	24	7	11	47	2	18	12	0	4	30
25	11	51	40		11	44	17		11	47	20		12	0	34	
				20				6				19				30
26	11	51	20	20	11	44	11	5	11	47	39	20	12	1	4	30
27	11	51	0	20	11	44	6	5	11	47	59	20	12	1	34	30
28	11	50	40	20	11	44	1	4	11	48	19	21	12	2	4	29
29	11	50	20	19	11	43	57	3	11	48	40	22	12	2	33	29
30	11	50	1		11	43	54		11	49	2		12	3	2	
				19				3				23				29
31					11	43	51	2					12	3	31	29

September	October	November	December
Decr. 9′ 46″	Decr. 5′ 51″	Decr. 0′ 1″ Incr. 5 14	Incr. 14′ 6″

CHAP.

Plate VII.



J. Ferguson delin.

J. Mynde Sculp.

CHAP. XV.

The Moon's ſurface mountainous: Her Phaſes deſcribed: Her path, and the paths of Jupiter's Moons delineated: The proportions of the Diameters of their Orbits, and thoſe of Saturn's Moons, to each other; and to the Diameter of the Sun.

PLATE VII.

252. BY looking at the Moon with an ordinary teleſcope, we perceive that her ſurface is diverſified with long tracts of prodigious high mountains and deep cavities. Some of her mountains, by comparing their height with her diameter (which is 2180 miles) are found to be three times higher than the higheſt hills on our Earth. This ruggedneſs of the Moon's ſurface is of great uſe to us, by reflecting the Sun's light to all ſides: for if the Moon were ſmooth and poliſhed like a looking-glaſs, or covered with water, ſhe could never diſtribute the Sun's light all round; only in ſome poſitions ſhe would ſhew us his image, no bigger than a point, but with ſuch a luſtre as would be hurtful to our eyes.

The Moon's ſurface mountainous.

253. The Moon's ſurface being ſo uneven, many have wondered why her edge appears not jagged, as well as the curve bounding the light and dark places. But if we conſider, that what we call the edge of the Moon's Diſc is not a ſingle line ſet round with mountains, in which caſe it would appear irregularly indented, but a large Zone having many mountains lying behind one another from the obſerver's eye, we ſhall find that the mountains in ſome rows will be oppoſite to the vales in others; and ſo fill up the inequalities as to make her appear quite round: juſt as when one looks at an orange, although it's roughneſs be very diſcernible on the ſide next the eye, eſpecially if the Sun or a Candle ſhines obliquely on that ſide, yet the line terminating

Why no hills appear on her edge.

PLATE VII. terminating the viſible part ſtill appears ſmooth and even.

The Moon has no twilight. 254. As the Sun can only enlighten that half of the Earth which is at any moment turned towards him, and being withdrawn from the oppoſite half, leaves it in darkneſs; ſo he likewiſe doth to the Moon: only with this difference, that the Earth being ſurrounded by an Atmoſphere, and the Moon having none, we have twilight after the Sun ſets; but the Lunar inhabitants have an immediate tranſition from the brighteſt Sun-ſhine to the blackeſt darkneſs, § 177. Fig. I. For, let *t r k s w* be the Earth, and *A*,*B*,*C*,*D*,*E*,*F*,*G*,*H* the Moon in eight different parts of her Orbit. As the Earth turns round its Axis, from weſt to eaſt, when any place comes to *t* the twilight begins there, and when it revolves from thence to *r* the Sun *S* riſes; when the place comes to *s* the Sun ſets, and when it comes to *w* the twilight ends. But as the Moon turns round her Axis, which is only once a month, the moment that any point of her ſurface comes to *r* (ſee the Moon at *G*) the Sun riſes there without any previous warning by twilight; and when the ſame point comes to *s* the Sun ſets, and that point goes into darkneſs as black as at midnight.

The Moon's Phaſes. 255. The Moon being an opaque ſpherical body (for her hills take off no more from her roundneſs than the inequalities on the ſurface of an orange takes off from it's roundneſs) we can only ſee that part of the enlightened half of her which is towards the Earth. And therefore, when the Moon is at *A*, in conjunction with the Sun *S*, her dark half is towards the Earth, and ſhe diſappears, as at *a*, there being no light on that half to render it viſible. When ſhe comes to her firſt Octant at *B*, or has gone an eighth part of her Orbit from her Conjunction, a quarter of her enlightened ſide is towards the Earth, and ſhe appears horned, as at *b*. When ſhe has gone a quarter of her Orbit from between the Earth and Sun to *C*, ſhe ſhews us one half of her enlightened ſide, as at *c*, and we ſay, ſhe is a quarter old. At *D* ſhe is in her ſecond Octant, and by ſhewing us more of her enlightened ſide ſhe appears gibbous, as at *d*. At *E* her whole enlightened ſide is towards the Earth, and therefore ſhe appears round, as at *e*, when we ſay, It is full Moon. In her third Octant at *F*, part of her dark ſide being towards the Earth, ſhe again appears gibbous, and is on the decreaſe, as at *f*. At *G* we ſee juſt one half of her enlightened ſide, and ſhe appears half decreaſed, or in her third Quarter, as at *g*. At *H* we only ſee a quarter of her enlightened ſide, being in her fourth Octant, where ſhe appears horned, as at *h*. And at *A*, having compleated her courſe from the Sun to the Sun again, ſhe diſappears; and we ſay, it is New Moon. Thus in going from *A* to *E* the Moon ſeems continually to increaſe; and in going from *E* to *A*, to decreaſe in the ſame proportion; having like Phaſes at equal diſtances from *A* or *E*, but as ſeen from the Sun *S*, ſhe is always Full.

The Moon's Diſc not always quite round when full.

256. The Moon appears not perfectly round when ſhe is Full in the higheſt or loweſt part of her Orbit, becauſe we have not a full view of her enlightened ſide at that time. When Full in the higheſt part of her Orbit, a ſmall deficiency appears on her lower edge; and the contrary when Full in the loweſt part of her Orbit.

The Phaſes of the Earth and Moon contrary.

257. It is plain by the Figure, that when the Moon changes to the Earth, the Earth appears Full to the Moon; and *vice verſa*. For when the Moon is at *A*, *New* to the Earth, the whole enlightened ſide of the Earth is towards the Moon: and when the Moon is at *E*, *Full* to the Earth, it's dark ſide is towards her. Hence a *New Moon* anſwers to a *Full Earth*, and a *Full Moon* to a *New Earth*. The *Quarters* are alſo reverſed to each other.

An agreeable Phenomenon.

258. Between the third Quarter and Change, the Moon is frequently viſible in the forenoon, even

when the Sun ſhines; and then ſhe affords us an opportunity of ſeeing a very agreeable appearance, wherever we find a globular ſtone above the level of the eye, as ſuppoſe on the top of a gate. For, if the Sun ſhines on the ſtone, and we place ourſelves ſo as the upper part of the ſtone may juſt ſeem to touch the point of the Moon's lowermoſt horn, we ſhall then ſee the enlightened part of the ſtone exactly of the ſame ſhape with the Moon; horned as ſhe is, and inclining the ſame way to the Horizon. The reaſon is plain; for the Sun enlightens the ſtone the ſame way as he does the Moon: and both being Globes, when we put ourſelves into the above ſituation, the Moon and ſtone have the ſame poſition to our eyes; and therefore we muſt ſee as much of the illuminated part of the one as of the other.

The Nonageſimal Degree, what.

259. The poſition of the Moon's Cuſps, or a right line touching the points of her horns, is very differently inclined to the Horizon at different hours of the ſame days of her age. Sometimes ſhe ſtands, as it were, upright on her lower horn, and then ſuch a line is perpendicular to the Horizon: when this happens, ſhe is in what the Aſtronomers call *the Nonageſimal Degree*; which is the higheſt point of the Ecliptic above the Horizon at that time, and is 90 degrees from both ſides of the Horizon where it is then cut by the Ecliptic. But this never happens when the Moon is on the Meridian, except when ſhe is at the very beginning of Cancer or Capricorn.

How the inclination of the Ecliptic may be found by the poſition of the Moon's horns.

260. The inclination of that part of the Ecliptic to the Horizon in which the Moon is at any time when horned, may be known by the poſition of her horns; for a right line touching their points is perpendicular to the Ecliptic. And as the angle that the Moon's Orbit makes with the Ecliptic can never raiſe her above, nor depreſs her below the Ecliptic, more than two minutes of a degree, as ſeen from the Sun; it can have no

ſenſible effect upon the poſition of her horns. Therefore, if a Quadrant be held up, ſo as one of it's edges may ſeem to touch the Moon's horns, the graduated ſide being kept towards the eye, and as far from the eye as it can be conveniently held, the arc between the Plumb-line and that edge of the Quadrant which ſeems to touch the Moon's horns will ſhew the inclination of that part of the Ecliptic to the Horizon. And the arc between the other edge of the Quadrant and Plumb-line will ſhew the inclination of the Moon's horns to the Horizon.

Fig. I. Why the Moon appears as big as the Sun.

261. The Moon generally appears as large as the Sun; for the Angle *v k A*, under which the Moon is ſeen from the Earth, is the ſame with the Angle *LkM*, under which the Sun is ſeen from it. And therefore the Moon may hide the Sun's whole Diſc from us, as ſhe ſometimes does in ſolar Eclipſes. The reaſon why ſhe does not eclipſe the Sun at every Change ſhall be explained afterwards. If the Moon were farther from the Earth, as at *a*, ſhe could never hide the whole of the Sun from us; for then ſhe would appear under the Angle *NkO*, eclipſing only that part of the Sun which lies between *N* and *O*: were ſhe ſtill further from the Earth, as at *X*, ſhe would appear under the ſmall angle *TkW*, like a ſpot on the Sun, hiding only the part *TW* from our ſight.

A proof of the Moon's turning round her Axis.

262. The Moon turns round her Axis in the time that ſhe goes round her Orbit; which is evident from hence, that a ſpectator at reſt, without the periphery of the Moon's Orbit, would ſee all her ſides turned regularly towards him in that time. She turns round her Axis from any Star to the ſame Star again in 27 days 8 hours; from the Sun to the Sun again in $29\frac{1}{2}$ days: the former is the length of her ſydereal day, and the latter the length of her ſolar day. A body moving round the Sun would have a ſolar day in every revolution, without turning on it's Axis; the ſame as if it

had kept all the while at reſt, and the Sun moved round it: but without turning round it's Axis it could never have one ſydereal day, becauſe it would always keep the ſame ſide towards any given Star.

Her periodical and ſynodical Revolution.

263. If the Earth had no annual motion, the Moon would go round it ſo as to compleat a Lunation, a ſydereal, and a ſolar day, all in the ſame time. But, becauſe the Earth goes forward in it's Orbit while the Moon goes round the Earth in her Orbit, the Moon muſt go as much more than round her Orbit from Change to Change in compleating a ſolar day, as the Earth has gone forward in it's Orbit during that time, *i. e.* almoſt a twelfth part of a Circle.

Familiarly repreſented.

264. The Moon's periodical and ſynodical revolution may be familiarly repreſented by the motions of the hour and minute hands of a watch round it's dial-plate, which is divided into 12 equal parts or hours, as the Ecliptic is divided into 12 Signs, and the year into 12 months. Let us ſuppoſe theſe 12 hours to be 12 Signs, the hour-hand the Sun, and the minute-hand the Moon; then the former will go round once in a year, and the latter once in a month; but the Moon, or minute-hand, muſt go more than round from any point

A Table ſhewing the times that the hour and minute hands of a watch are in conjunction.

Conj.	H.	M.	S.	$'''$	$''''$	v p^{ts}.
1	I	5	27	16	21	$49\frac{1}{11}$
2	II	10	54	32	43	$38\frac{2}{11}$
3	III	16	21	49	5	$27\frac{3}{11}$
4	IIII	21	49	5	27	$16\frac{4}{11}$
5	V	27	16	21	49	$5\frac{5}{11}$
6	VI	32	43	38	10	$54\frac{6}{11}$
7	VII	38	10	54	32	$43\frac{7}{11}$
8	VIII	43	38	10	54	$32\frac{8}{11}$
9	IX	49	5	27	16	$21\frac{9}{11}$
10	X	54	32	43	38	$10\frac{10}{11}$
11	XII	0	0	0	0	0

point of the Circle where it was laſt conjoined with the Sun, or hour-hand, to overtake it again: for the hour-hand being in motion, can never be overtaken by the minute-hand at that point from which they ſtarted at their laſt conjunction. The firſt column of the preceding Table ſhews the number of conjunctions which the hour and minute-hand make whilſt the hour-hand goes once round the dial-plate; and the other columns ſhew the times when the two hands meet at every conjunction. Thus, ſuppoſe the two hands to be in conjunction at XII, as they always are; then, at the firſt following conjunction it is 5 minutes 27 ſeconds 16 thirds 21 fourths $49\frac{1}{11}$ fifths paſt I where they meet; at the ſecond conjunction it is 10 minutes 54 ſeconds 32 thirds 43 fourths $38\frac{2}{11}$ fifths paſt II; and ſo on. This, though an eaſy illuſtration of the motions of the Sun and Moon, is not preciſe as to the times of their conjunctions; becauſe, while the Sun goes round the Ecliptic, the Moon makes $12\frac{1}{3}$ conjunctions with him; but the minute-hand of a watch or clock makes only 11 conjunctions with the hour-hand in one period round the dial-plate. But if, inſtead of the common wheel-work at the back of the dial-plate, the Axis of the minute-hand had a pinion of 6 leaves turning a wheel of 74, and this laſt turning the hour-hand, in every revolution it makes round the dial-plate, the minute-hand would make $12\frac{1}{3}$ conjunctions with it; and ſo would be a pretty device for ſhewing the motions of the Sun and Moon; eſpecially, as the ſloweſt moving hand might have a little Sun fixed on it's point, and the quickeſt a little Moon. Beſides, the plate, inſtead of hours and quarters, might have a Circle of months, with the 12 Signs and their Degrees; and if a plate of $29\frac{1}{2}$ equal parts for the days of the Moon's age were fixed to the Axis of the Sun-hand, and below it, ſo as the Sun always kept at the half day of that plate, the Moon-hand would ſhew the Moon's

A machine for ſhewing the motions of the Sun and Moon.

age upon that plate for every day pointed out by the Sun-hand in the Circle of months; and both Sun and Moon would ſhew their places in the Ecliptic: for the Sun would go round the Ecliptic in 365 Days; and the Moon in $27\frac{1}{3}$ days, which is her periodical revolution; but from the Sun to the Sun again, or from Change to Change, in $29\frac{1}{2}$ days, which is her ſynodical revolution.

The Moon's motion through open ſpace deſcribed.

265. If the Earth had no annual motion, the Moon's motion round the Earth, and her track in abſolute ſpace, would be always the ſame *. But as the Earth and Moon move round the Sun, the Moon's real path in the Heavens is very different from her viſible path round the Earth: the latter being in a progreſſive Circle, and the former in a curve of different degrees of concavity, which would always be the ſame in the ſame parts of the Heavens, if the Moon performed a compleat number of Lunations in a year without any thing over.

An idea of the Earth's path and the Moon's.

266. Let a nail in the end of the axle of a chariot-wheel repreſent the Earth, and a pin in the nave the Moon; if the body of the chariot be propped up ſo as to keep that wheel from touching the ground, and the wheel be then turned round by hand, the pin will deſcribe a Circle both round the nail and in the ſpace it moves through. But if the props be taken away, the horſes put to, and the chariot driven over a piece of ground which is circularly convex; the nail in the axle will deſcribe a circular curve, and the pin in the nave will ſtill deſcribe a circle round the progreſſive nail in the axle, but not in the ſpace through which it moves. In this caſe, the curve deſcribed by the nail will reſemble in miniature as much of

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* In this place, we may conſider the Orbits of all the Satellites as circular, with reſpect to their primary Planets; becauſe the excentricities of their Orbits are too ſmall to affect the Phenomena here deſcribed.

the Earth's annual path round the Sun, as it deſcribes whilſt the Moon goes as often round the Earth as the pin does round the nail: and the curve deſcribed by the nail will have ſome reſemblance of the Moon's path during ſo many Lunations. PLATE VII.

Let us now ſuppoſe that the radius of the circular curve deſcribed by the nail in the axle is to the radius of the circle which the pin in the nave deſcribes round the axle as $337\frac{1}{2}$ to 1; which is the proportion of the radius or ſemidiameter of the Earth's Orbit to that of the Moon's; or of the circular curve *A* 1 2 3 4 5 6 7 *B* &c. to the little circle *a*; and then, whilſt the progreſſive nail deſcribes the ſaid curve from *A* to *E*, the pin will go once round the nail with regard to the center of it's path, and in doing ſo, will deſcribe the curve *a b c d e*. The former will be a true repreſentation of the Earth's path for one Lunation, and the latter of the Moon's for that time. Here we may ſet aſide the inequalities of the Moon's motion, and alſo the Earth's moving round it's common center of gravity and the Moon's: all which, if they were truly copied in this experiment, would not ſenſibly alter the figure of the paths deſcribed by the nail and pin, even though they ſhould rub againſt a plain upright ſurface all the way, and leave their tracks viſible upon it. And if the chariot was driven forward on ſuch a convex piece of ground, ſo as to turn the wheel ſeveral times round, the track of the pin in the nave would ſtill be concave toward the center of the circular curve deſcribed by the pin in the axle; as the Moon's path is always concave to the Sun in the center of the Earth's annual Orbit. Fig. II.

In this Diagram, the thickeſt curve line *ABCDE*, with the numeral figures ſet to it, repreſents as much of the Earth's annual Orbit as it deſcribes in 32 days from weſt to eaſt; the little circles at *a*, *b*, *c*, *d*, *e* ſhew the Moon's Orbit in due propor-

tion

PLATE VII. tion to the Earth's; and the ſmalleſt curve *a b c d e f* repreſents the line of the Moon's path in the Heavens for 32 days, accounted from any particular New Moon at *a*. The Machine, Fig. 5th, is for delineating the Moon's path, and will be deſcribed, with the reſt of my Aſtronomical machinery, in the laſt Chapter. The Sun is ſuppoſed to be in the center of the curve *A* 1 2 3 4 5 6 7 *B* &c. and the ſmall dotted circles upon it repreſent the Moon's Orbit, of which the radius is in the ſame proportion to the Earth's path in this ſcheme, that the radius of the Moon's Orbit in the Heavens bears to the radius of the Earth's annual path round the Sun; that is, as 240,000 to 81,000,000, or as 1 to 337½.

Proportion of the Moon's Orbit to the Earth's.

Fig. II. When the Earth is at *A*, the New Moon is at *a*; and in the ſeven days that the Earth deſcribes the curve 1 2 3 4 5 6 7, the Moon in accompanying the Earth deſcribes the curve *a b*; and is in her firſt Quarter at *b* when the Earth is at *B*. As the Earth deſcribes the curve *B* 8 9 10 11 12 13 14, the Moon deſcribes the curve *b c*; and is at *c*, oppoſite to the Sun, when the Earth is at *C*. Whilſt the Earth deſcribes the curve *C* 15 16 17 18 19 20 21 22, the Moon deſcribes the curve *c d*; and is in her third Quarter at *d* when the Earth is at *D*. Once more, whilſt the Earth deſcribes the curve *D* 23 24 25 26 27 28 29, the Moon deſcribes the curve *d e*; and is again in conjuction at *e* with the Sun when the Earth is at *E*, between the 29th and 30th day of the Moon's age, accounted by the numeral Figures from the New Moon at *A*. In deſcribing the curve *a b c d e*, the Moon goes round the progreſſive Earth as really as if ſhe had kept in the dotted Circle *A*, and the Earth continued immoveable in the center of that Circle.

The Moon's motion always concave towards the Sun. And thus we ſee, that although the Moon goes round the Earth in a Circle, with reſpect to the Earth's center, her real path in the Heavens is not very different in appearance from the Earth's path.

To ſhew that the Moon's path is concave to the Sun, even at the time of Change, it is carried on a little farther into a ſecond Lunation, as to *f*.

267. The Moon's abſolute motion from her Change to her firſt Quarter, or from *a* to *b*, is ſo much ſlower than the Earth's, that ſhe falls 240 thouſand miles (equal to the ſemidiameter of her Orbit) behind the Earth at her firſt Quarter in *b*, when the Earth is in *B*; that is, ſhe falls back a ſpace equal to her diſtance from the Earth. From that time her motion is gradually accelerated to her Oppoſition or Full at *c*, and then ſhe is come up as far as the Earth, having regained what ſhe loſt in her firſt Quarter from *a* to *b*. From the Full to the laſt Quarter at *d* her motion continues accelerated, ſo as to be juſt as far before the Earth at *D*, as ſhe was behind it at her firſt Quarter in *b*. But, from *d* to *e* her motion is retarded ſo, that ſhe loſes as much with reſpect to the Earth as is equal to her diſtance from it, or to the ſemidiameter of her Orbit; and by that means ſhe comes to *e*, and is then in conjunction with the Sun as ſeen from the Earth at *E*. Hence we find, that the Moon's abſolute motion is ſlower than the Earth's from her third Quarter to her firſt; and ſwifter than the Earth's from her firſt Quarter to her third: her path being leſs curved than the Earth's in the former caſe, and more in the latter. Yet it is ſtill bent the ſame way towards the Sun; for if we imagine the concavity of the Earth's Orbit to be meaſured by the length of a perpendicular line *C g*, let down from the Earth's place upon the ſtraight line *b g d* at the Full of the Moon, and connecting the places of the Earth at the end of the Moon's firſt and third Quarters, that length will be about 640 thouſand miles; and the Moon when New only approaching nearer to the Sun by 240 thouſand miles than the Earth is, the length of the perpendicular let down from her place at that time upon the ſame ſtraight line, and

How her motion is alternately retarded and accelerated.

which ſhews the concavity of that part of her path, will be about 400 thouſand miles.

A difficulty removed.

268. The Moon's path being concave to the Sun throughout, demonſtrates that her gravity towards the Sun, at her Conjunction, exceeds her gravity towards the Earth. And if we conſider that the quantity of matter in the Sun is almoſt 230 thouſand times as great as the quantity of matter in the Earth, and that the attraction of each body diminiſhes as the ſquare of the diſtance from it increaſes, we ſhall ſoon find, that the point of equal attraction between the Earth and the Sun, is about 70 thouſand miles nearer the Earth than the Moon is at her Change. It may now appear ſurpriſing that the Moon does not abandon the Earth when ſhe is between it and the Sun, becauſe ſhe is conſiderably more attracted by the Sun than by the Earth at that time. But this difficulty vaniſhes when we conſider, that a common impulſe on any ſyſtem of bodies affects not their relative motions; but that they will continue to attract, impel, or circulate round one another, in the ſame manner as if there was no ſuch impulſe. The Moon is ſo near the Earth, and both of them ſo far from the Sun, that the attractive power of the Sun may be conſidered as equal on both: and therefore the Moon will continue to circulate round the Earth in the ſame manner as if the Sun did not attract them at all: like bodies in the cabbin of a ſhip, which move round or impel one another in the ſame manner when the ſhip is under ſail, as when it is at reſt; becauſe they are all equally affected by the common motion of the ſhip. If by any other cauſe, ſuch as the near approach of a Comet, the Moon's diſtance from the Earth ſhould happen to be ſo much increaſed, that the difference of their gravitating forces towards the Sun ſhould exceed that of the Moon towards the Earth; in that caſe, the Moon, when in conjunction,

tion, would abandon the Earth, and be either drawn into the Sun, or Comet, or circulate round about it.

269. The curves which Jupiter's Satellites deſcribe, are all of different ſorts from the path deſcribed by our Moon, although theſe Satellites go round Jupiter, as the Moon goes round the Earth. Let *A B C D E* &c. be as much of Jupiter's Orbit as he deſcribes in 18 days from *A* to *T*; and the curves *a*, *b*, *c*, *d* will be the paths of his four Moons going round him in his progreſſive motion.

Fig. III.

The abſolute Path of Jupiter and his Satellites delineated.

Now let us ſuppoſe all theſe Moons to ſet out from a conjunction with the Sun, as ſeen from Jupiter at *A*; then, his firſt or neareſt Moon will be at *a*, his ſecond at *b*, his third at *c*, and his fourth at *d*. At the end of 24 terreſtrial hours after this conjunction, Jupiter has moved to *B*, his firſt Moon or Satellite has deſcribed the curve *a* 1, his ſecond the curve *b* 1, his third *c* 1, and his fourth *d* 1. The next day, when Jupiter is at *C*, his firſt Satellite has deſcribed the curve *a* 2, from its conjunction, his ſecond the curve *b* 2, his third the curve *c* 2, and his fourth the curve *d* 2, and ſo on. The numeral Figures under the capital letters ſhew Jupiter's place in his path every day for 18 days, accounted from *A* to *T*; and the like Figures ſet to the paths of his Satellites, ſhew where they are at the like times. The firſt Satellite, almoſt under *C*, is ſtationary at + as ſeen from the Sun; and retrograde from + to 2: at 2 it appears ſtationary again, and thence it moves forward until it has paſt 3, and is twice ſtationary, and once retrograde, between 3 and 4. The path of this Satellite interſects itſelf every 42½ hours, making ſuch loops as in the Diagram at 2. 3. 5. 7. 9. 10. 12. 14. 16. 18, a little after every Conjunction. The ſecond Satellite *b*, moving ſlower, barely croſſes it's path every 3 days 13 hours; as at 4. 7. 11. 14. 18, making

PLATE VII.

making only five loops and as many conjunctions in the time that the firſt makes ten. The third Satellite *c* moving ſtill ſlower, and having deſcribed the curve *c* 1. 2. 3. 4. 5. 6. 7, comes to an angle at 7 in conjunction with the Sun at the end of 7 days four hours; and ſo goes on to deſcribe ſuch another curve 7. 8. 9. 10. 11. 12. 13. 14, and is at 14 in it's next conjunction. The fourth Satellite *d* is always progreſſive, making neither loops nor angles in the Heavens; but comes to it's next conjunction at *e* between the numeral figures 16 and 17, or in 16 days 18 hours. In order to have a tolerably good figure of the paths of theſe Satellites, I took the following method. Fig. III.

Fig. IV.

How to delineate the paths of Jupiter's Moon.

Having drawn their Orbits on a Card, in proportion to their relative diſtances from Jupiter, I meaſured the radius of the Orbit of the fourth Satellite, which was an inch and $\frac{14}{100}$ parts of an inch; then multiplied this by 424 for the radius of Jupiter's Orbit, becauſe Jupiter is 424 times as far from the Sun's center as his fourth Satellite is from his center; and the product thence ariſing was $483\frac{36}{100}$ inches. Then taking a ſmall cord of this length, and fixing one end of it to the floor of a long room by a nail, with a black-lead pencil at the other end I drew the curve *ABCD* &c. and ſet off a degree and a half thereon, from *A* to *T*; becauſe Jupiter moves only ſo much, whilſt his outermoſt Satellite goes once round him, and ſomewhat more; ſo that this ſmall portion of ſo large a circle differs but very little from a ſtraight line. This done, I divided the ſpace *AT* into 18 equal parts, as *AB*, *BC*, &c. for the daily progreſs of Jupiter; and each part into 24 for his hourly progreſs. The Orbit of each Satellite was alſo divided into as many equal parts as the Satellite is hours in finiſhing it's ſynodical period round Jupiter. Then drawing a right line through the center of the Card, as a diameter to all the four Orbits upon it, I put the card upon the line of Jupiter's

PLATE VII.

Jupiter's motion, and transferred it to every horary diviſion thereon, keeping always the ſaid diameter-line on the line of Jupiter's path; and running a pin through each horary diviſion in the Orbit of each Satellite as the card was gradually transferred along the line *A B C D* &c. of Jupiter's motion, I marked points for every hour through the Card for the Curves deſcribed by the Satellites, as the primary Planet in the center of the Card was carried forward on the line: and ſo finiſhed the Figure, by drawing the lines of each Satellite's motion through thoſe (almoſt innumerable) points: by which means, this is perhaps as true a Figure of the paths of theſe Satellites as can be deſired. And in the ſame manner might thoſe for Saturn's Satellites be delineated.

And Saturn's.

The grand Period of Jupiter's Moons.

270. It appears by the ſcheme, that the three firſt Satellites come almoſt into the ſame line or poſition every ſeventh day; the firſt being only a little behind with the ſecond, and the ſecond behind with the third. But the period of the fourth Satellite is ſo incommenſurate to the periods of the other three, that it cannot be gueſſed at by the diagram when it would fall again into a line of conjunction with them, between Jupiter and the Sun. And no wonder; for ſuppoſing them all to have been once in conjunction, it will require 3,087,043,493,260 years to bring them in conjunction again. See § 73.

Fig. IV. The proportions of the Orbits of the Planets and Satellites.

271. In Fig. 4th we have the proportions of the Orbits of Saturn's five Satellites, and of Jupiter's four, to one another, to our Moon's Orbit, and to the Diſc of the Sun. *S* is the Sun; *M m* the Moon's Orbit (the Earth ſuppoſed to be at *E*;) *J* Jupiter; 1. 2. 3. 4 the Orbits of his four Moons or Satellites; *Sat* Saturn; and 1. 2. 3. 4. 5 the Orbits of his five Moons. Hence it appears, that the Sun would much more than fill the whole Orbit of the Moon; for the Sun's diameter is 763,000 miles, and the diameter of the Moon's

Orbit only 480,000. In proportion to all theſe Orbits of the Satellites, the radius of Saturn's annual Orbit would be $21\frac{1}{4}$ yards, of Jupiter's Orbit $11\frac{2}{3}$, and of the Earth's $2\frac{1}{4}$, taking them in round numbers.

272. The annexed table ſhews at once what proportion the Orbits, Revolutions, and Velocities, of all the Satellites bear to thoſe of their primary Planets, and what ſort of curves the ſeveral Satellites deſcribe. For, thoſe Satellites whoſe velocities round their Primaries are greater than the velocities of their Primaries in open ſpace, make loops at their conjunctions, § 269; appearing retrograde as ſeen from the Sun whilſt they deſcribe the inferior parts of their Orbits, and direct whilſt they deſcribe the ſuperior. This is the caſe with Jupiter's firſt and ſecond Satellites, and with Saturn's firſt. But thoſe Satellites, whoſe velocities are leſs than the velocities of their primary Planets, move direct in their whole circumvolutions; which is the caſe of the third and fourth Satellites of Jupiter, and of the ſecond, third, fourth, and fifth Satellites of Saturn, as well as of our Satellite the Moon: But the Moon is the only Satellite whoſe motion is always concave to the Sun. There is a table

The Satellites		Proportion of the Radius of the Planet's Orbit to the Radius of the Orbit of each Satellite.	Proportion of the Time of the Planet's Revolution to the Revolution of each Satellite.	Proportion of the Velocity of each Satellite to the Velocity of it's primary Planet.
of Saturn	1	As 5322 to 1	As 5738 to 1	As 5738 to 5322
	2	4155 1	3912 1	3912 4155
	3	2954 1	2347 1	2347 2954
	4	1295 1	674 1	674 1295
	5	432 1	134 1	134 432
of Jupiter	1	As 1851 to 1	As 2445 to 1	As 2445 to 1851
	2	1165 1	1219 1	1219 1165
	3	731 1	604 1	604 731
	4	424 1	258 1	258 424
The Moon		As $337\frac{1}{2}$ to 1	As $12\frac{1}{3}$ to 1	As $12\frac{1}{13}$ to $337\frac{1}{2}$

table of this ſort in *De la Caille*'s Aſtronomy, but it is very different from the above, which I have computed from our *Engliſh* accounts of the periods and diſtances of theſe Planets and Satellites.

CHAP. XVI.

The Phenomena of the Harveſt-Moon explained by a common Globe: The years in which the Harveſt-Moons are leaſt and moſt beneficial from 1751, *to* 1861. *The long duration of Moon-light at the Poles in winter.*

No Harveſt-Moon at the Equator.

273. IT is generally believed that the Moon riſes about 50 minutes later every day than on the preceding; but this is true only with regard to places on the Equator. In places of conſiderable Latitude there is a remarkable difference, eſpecially in the harveſt time; with which Farmers were better acquainted than Aſtronomers till of late; and gratefully aſcribed the early riſing of the Full Moon at that time of the year to the goodneſs of God, not doubting that he had ordered it ſo on purpoſe to give them an immediate ſupply of Moon-light after ſun-ſet for their greater conveniency in reaping the fruits of the Earth.

In this inſtance of the Harveſt-Moon, as in many others diſcoverable by Aſtronomy, the wiſdom and beneficence of the Deity is conſpicuous, who really ordered the courſe of the Moon ſo, as to beſtow more or leſs light on all parts of the Earth as their ſeveral circumſtances and ſeaſons render it more or leſs ſerviceable. About the Equator, where there is no variety of ſeaſons, and the weather changes ſeldom, and at ſtated times, Moon-light is not neceſſary for gathering in the produce of the ground; and there the Moon riſes about 50 minutes later every day or night than on the former. At conſiderable diſtances from the Equator, where the weather and ſeaſons are more uncertain, the autumnal Full Moons riſe very ſoon after ſun-ſet for ſeveral evenings together. At the polar circles, where the mild ſeaſon is of very ſhort duration, the autumnal Full Moon riſes at ſun-ſet from the firſt to the third quarter. And at the Poles, where the Sun is for half a year abſent, the winter Full Moons ſhine conſtantly without ſetting from the firſt to the third quarter.

But remarkable according to the diſtance of places from it.

The reaſon of this.

It is ſoon ſaid that all theſe Phenomena are owing to the different Angles made by the Horizon and different parts of the Moon's Orbit; and that the Moon can be full but once or twice in a year in thoſe parts of her Orbit which riſe with the leaſt angles. But to explain this ſubject intelligibly, we muſt dwell much longer upon it.

274. The * plane of the Equinoctial is perpendicular to the Earth's Axis: and therefore, as the Earth turns round it's Axis, all parts of the Equinoctial make equal Angles with the Horizon both at riſing and ſetting; ſo that equal portions of it always riſe or ſet in equal times. Conſequently, if the Moon's motion were equable, and in the Equinoctial, at the rate of 12 degrees 11 min. from the Sun every day, as it is in her Orbit, ſhe would riſe and ſet 50 minutes later every day than on the preceding: for 12 deg. 11 min. of the Equinoctial riſe or ſet in 50 minutes of time in all Latitudes.

275. But the Moon's motion is ſo nearly in the Ecliptic, that we may conſider her at preſent as moving in it. Now the different parts of the Ecliptic, on account of it's obliquity to the Earth's Axis, make very different Angles with the Horizon as they riſe or ſet. Thoſe parts or Signs which riſe with the ſmalleſt Angles ſet with the greateſt, and *vice verſâ*. In equal times, whenever this Angle is leaſt, a greater portion of the Ecliptic riſes than when the Angle is larger; as may be ſeen by elevating the pole of a Globe to any con-

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* If a Globe be cut quite through upon any Circle, the flat ſurface where it is ſo divided, is the plane of that Circle.

ſiderable Latitude, and then turning it round it's Axis in the Horizon. Conſequently, when the Moon is in thoſe Signs which riſe or ſet with the ſmalleſt Angles, ſhe riſes or ſets with the leaſt difference of time; and with the greateſt difference in thoſe Signs which riſe or ſet with the greateſt Angles. PLATE III.

Fig. III.

But, becauſe all who read this Treatiſe may not be provided with Globes, though in this caſe it is requiſite to know how to uſe them, we ſhall ſubſtitute the Figure of a globe; in which *FUP* is the Axis, ♋ *TR* the Tropic of Cancer, *Lt* ♑ the Tropic of Capricorn, ♋ *EU* ♑ the Ecliptic touching both the Tropics, which are 47 degrees from each other, and *AB* the Horizon. The Equator, being in the middle between the Tropics, is cut by the Ecliptic in two oppoſite points, which are the beginnings of ♈ Aries and ♎ Libra, *K* is the Hour-circle with its Index, *F* the North Pole of the Globe elevated to a conſiderable Latitude, ſuppoſe 40 degrees above the Horizon; and *P* the South Pole depreſſed as much below it. Fig. III. Becauſe of the oblique poſition of the Sphere in this Latitude, the Ecliptic has the high elevation *N* ♋ above the Horizon, making the Angle *NU* ♋ of 73½ degrees with it when ♋ Cancer is on the Meridian, at which time ♎ Libra riſes in the Eaſt. But let the Globe be turned half round it's Axis, till ♑ Capricorn comes to the Meridian and ♈ Aries riſes in the Eaſt, and then the Ecliptic will have the low elevation *NL* above the Horizon, making only an Angle *NUL* of 26½ degrees with it; which is 47 degrees leſs than the former Angle, equal to the diſtance between the Tropics.

The different Angles made by the Ecliptic and Horizon.

276. In northern Latitudes, the ſmalleſt Angle made by the Ecliptic and Horizon is when Aries riſes, at which time Libra ſets: the greateſt when Libra riſes, at which time Aries ſets. From the riſing of Aries to the riſing of Libra (which is

Leaſt and greateſt, when.

twelve * Sydereal hours) the angle increaſes; and from the riſing of Libra to the riſing of Aries it decreaſes in the ſame proportion. By this article and the preceding, it appears that the Ecliptic riſes faſteſt about Aries, and ſloweſt about Libra.

Reſult of the quantity of this Angle at London.

277. On the Parallel of *London*, as much of the Ecliptic riſes about Piſces and Aries in two hours as the Moon goes through in ſix days; and therefore whilſt the Moon is in theſe Signs, ſhe differs but two hours in riſing for ſix days together; that is, about 20 minutes later every day or night than on the preceding, at a mean rate. But in fourteen days afterwards, the Moon comes to Virgo and Libra, which are the oppoſite Signs to Piſces and Aries; and then ſhe differs almoſt four times as much in riſing; namely, one hour and about fifteen minutes later every day or night than the former, whilſt ſhe is in theſe Signs. The annexed Table ſhews the daily mean difference of the Moon's

Days	Signs	Degrees	Riſing Diff.		Setting Diff.	
			H.	M.	H.	M.
1	♋	13	1	5	0	50
2		26	1	10	0	43
3	♌	10	1	14	0	37
4		23	1	17	0	32
5	♍	6	1	16	0	28
6		19	1	15	0	24
7	♎	2	1	15	0	20
8		15	1	15	0	18
9		28	1	15	0	17
10	♏	12	1	15	0	22
11		25	1	14	0	30
12	♐	8	1	13	0	39
13		21	1	10	0	47
14	♑	4	1	4	0	56
15		17	0	46	1	5
16	♒	1	0	40	1	8
17		14	0	35	1	12
18		27	0	30	1	15
19	♓	10	0	25	1	16
20		23	0	20	1	17
21	♈	7	0	17	1	16
22		20	0	17	1	15
23	♉	3	0	20	1	15
24		16	0	24	1	15
25		29	0	30	1	14
26	♊	13	0	40	1	13
27		26	0	56	1	7
28	♋	9	1	0	1	58

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* The Ecliptic, together with the fixed Stars, make 366¼ apparent diurnal revolutions about the Earth in a year; the Sun only 365¼. Therefore the Stars gain 3 minutes 56 ſeconds upon the Sun every day: ſo that a Sydereal day contains only 23 hours 56 minutes of mean Solar time; and a natural or Solar day 24 hours. Hence 12 Sydereal hours are 1 minute 58 ſeconds ſhorter than 12 Solar.

riſing and ſetting on the Parallel of *London*, for PLATE III
28 days; in which time the Moon finiſhes her period round the Ecliptic, and gets 9 degrees into the ſame Sign from the beginning of which ſhe ſet out. So it appears by the Table, that when the Moon is in ♍ and ♎ ſhe riſes an hour and a quarter later every day than ſhe roſe on the former; and differs only 28, 24, 20, 18 or 17 minutes in ſetting. But, when ſhe comes to ♓ and ♈, ſhe is only 20 or 17 minutes later in riſing; and an hour and a quarter later in ſetting.

278. All theſe things will be made plain by putting ſmall patches on the Ecliptic of a Globe, as far from one another as the Moon moves from any Point of the celeſtial Ecliptic in 24 hours, which at a mean rate is * 13$\frac{1}{6}$ degrees; and then in turning the Globe round, obſerve the riſing and ſetting of the patches in the Horizon, as the Index points out the different times in the hour-circle. A few of theſe patches are repreſented by dots at 0 1 2 3 &c. on the Ecliptic, which has the poſi- Fig. III.
tion *LUI* when Aries riſes in the Eaſt; and by the dots 0 1 2 3 &c. when Libra riſes in the Eaſt, at which time the Ecliptic has the poſition *EU* ♑: making an angle of 62 degrees with the Horizon in the latter caſe, and an angle of no more than 15 degrees with it in the former; ſuppoſing the Globe rectified to the Latitude of *London.*

279. Having rectified the Globe, turn it until the patch at 0, about the beginning of ♓ Piſces in the half *LUI* of the Ecliptic, comes to the Eaſtern ſide of the Horizon; and then keeping the ball ſteady, ſet the hour-index to XII, becauſe *that* hour may perhaps be more eaſily remembered than any other. Then, turn the Globe round weſt-

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* The Sun advances almoſt a degree in the Ecliptic in 24 hours, the ſame way that the Moon moves: and therefore, the Moon by advancing 13$\frac{1}{7}$ degrees in that time goes little more than 12 degrees farther from the Sun than ſhe was on the day before.

ward, and in that time, ſuppoſe the patch 0 to have moved thence to 1, $13\frac{1}{6}$ degrees, whilſt the Earth turns once round it's Axis, and you will ſee that 1 riſes only about 20 minutes later than 0 did on the day before. Turn the Globe round again, and in that time ſuppoſe the ſame patch to have moved from 1 to 2; and it will riſe only 20 minutes later by the hour-index than it did at 1 on the day or turn before. At the end of the next turn, ſuppoſe the patch to have gone from 2 to 3 at *U*, and it will riſe 20 minutes later than it did at 2. And ſo on for ſix turns, in which time there will ſcarce be two hours difference: nor would there have been ſo much if the 6 degrees of the Sun's motion in that time had been allowed for. At the firſt Turn the patch riſes ſouth of the Eaſt, at the middle Turn due Eaſt, and at the laſt Turn north of the Eaſt. But theſe patches will be 9 hours of ſetting on the weſtern ſide of the Horizon, which ſhews that the Moon will be ſo much later of ſetting in that week in which ſhe moves through theſe two Signs. The cauſe of this difference is evident; for Piſces and Aries make only an Angle of 15 degrees with the Horizon when they riſe; but they make an Angle of 62 degrees with it when they ſet. As the Signs Taurus, Gemini, Cancer, Leo, Virgo, and Libra, riſe ſucceſſively, the Angle increaſes gradually which they make with the Horizon; and decreaſes in the ſame proportion as they ſet. And for that reaſon, the Moon differs gradually more in the time of her riſing every day whilſt ſhe is in theſe Signs, and leſs in her ſetting: after which, through the other ſix Signs, *viz.* Scorpio, Sagittary, Capricorn, Aquarius, Piſces, and Aries, the riſing difference becomes leſs every day, until it be at the leaſt of all, namely, in Piſces and Aries.

280. The Moon goes round the Ecliptic in 27 days 8 hours; but not from Change to Change in leſs than 29 days 12 hours: ſo that ſhe is in Piſces

and Aries at leaſt once in every Lunation, and in ſome Lunations twice.

Why the Moon is always Full in different Signs.

281. If the Earth had no annual motion, the Sun would never appear to ſhift his place in the Ecliptic. And then every New Moon would fall in the ſame ſign and degree of the Ecliptic, and every Full Moon in the oppoſite: for the Moon would go preciſely round the Ecliptic from Change to Change. So that if the Moon was once Full in Piſces, or Aries, ſhe would always be Full when ſhe came round to the ſame Sign and Degree again. And as the Full Moon riſes at Sun-ſet (becauſe when any point of the Ecliptic ſets, the oppoſite point riſes) ſhe would conſtantly riſe within two hours of Sun-ſet, on the parallel of *London*, during the week in which ſhe were Full. But in the time that the Moon goes round the Ecliptic from any conjunction or oppoſition, the Earth goes almoſt a Sign forward; and therefore the Sun will ſeem to go as far forward in that time, namely, $27\frac{1}{2}$ degrees; ſo that the Moon muſt go $27\frac{1}{2}$ degrees more than round, and as much farther as the Sun advances in that interval, which is $2\frac{1}{15}$ degrees, before ſhe can be in conjunction with, or oppoſite to, the Sun again. Hence it is evident, that there can be but one conjunction or oppoſition of the Sun and Moon in a year in any particular part of the Ecliptic. This may be familiarly exemplified by the hour and minute hands of a watch, which are never in conjunction or oppoſition in that part of the dial-plate where they were ſo laſt before. And indeed if we compare the twelve hours on the dial-plate to the twelve ſigns of the Ecliptic, the hour-hand to the Sun and the minute-hand to the Moon, we ſhall have a tolerably near reſemblance in miniature to the motions of our great celeſtial Luminaries. The only difference is, that whilſt the Sun goes once round the Ecliptic, the Moon makes $12\frac{1}{3}$ conjunctions with him: but whilſt the hour-hand goes round the

Her periodical and ſynodical Revolution exemplified.

dial-plate, the minute-hand makes only 11 conjunctions with it; becauſe the minute-hand moves ſlower in reſpect of the hour-hand than the Moon does with regard to the Sun.

The Harveſt and Hunter's Moon.

282. As the Moon can never be full but when ſhe is oppoſite to the Sun, and the Sun is never in Virgo and Libra but in our autumnal months, it is plain that the Moon is never full in the oppoſite Signs, Piſces and Aries, but in theſe two months. And therefore we can have only two Full Moons in the year, which riſe ſo near the time of Sun-ſet for a week together, as above-mentioned. The former of theſe is called the *Harveſt Moon*, and the latter the *Hunter's Moon*.

Why the Moon's regular riſing is never perceived but in Harveſt.

283. Here it will probably be aſked, why we never obſerve this remarkable riſing of the Moon but in harveſt, ſince ſhe is in Piſces and Aries twelve times in the year beſides; and muſt then riſe with as little difference of time as in harveſt? The anſwer is plain: for in winter theſe Signs riſe at noon; and being then only a Quarter of a Circle diſtant from the Sun, the Moon in them is in her firſt Quarter: but when the Sun is above the Horizon, the Moon's riſing is neither regarded nor perceived. In ſpring theſe Signs riſe with the Sun, becauſe he is then in them; and as the Moon changeth in them at that time of the year, ſhe is quite inviſible. In ſummer they riſe about midnight, and the Sun being then three Signs, or a Quarter of a Circle before them, the Moon is in them about her third Quarter; when riſing ſo late, and giving but very little light, her riſing paſſes unobſerved. And in autumn, theſe Signs being oppoſite to the Sun, riſe when he ſets, with the Moon in oppoſition, or at the Full, which makes her riſing very conſpicuous.

284. At the Equator, the North and South Poles lie in the Horizon; and therefore the Ecliptic makes the ſame Angle ſouthward with the Ho-

rizon when Aries riſes, as it does northward when Libra riſes. Conſequently, as the Moon at all the fore-mentioned patches riſes and ſets nearly at equal Angles with the Horizon all the year round, and about 50 minutes later every day or night than on the preceding, there can be no particular Harveſt-Moon at the Equator.

285. The farther that any place is from the Equator, if it be not beyond the Polar Circle, the Angle gradually diminiſhes which the Ecliptic and Horizon make when Piſces and Aries riſe: and therefore when the Moon is in theſe Signs ſhe riſes with a nearly proportionable difference later every day than on the former; and is for that reaſon the more remarkable about the Full, until we come to the Polar Circles, or 66 degrees from the Equator; in which Latitude the Ecliptic and Horizon become coincident every day for a moment, at the ſame ſydereal hour (or 3 minutes 56 ſeconds ſooner every day than the former) and the very next moment one half of the Ecliptic containing Capricorn, Aquarius, Piſces, Aries, Taurus, and Gemini, riſes, and the oppoſite half ſets. Therefore, whilſt the Moon is going from the beginning of Capricorn to the beginning of Cancer, which is almoſt 14 days, ſhe riſes at the ſame ſydereal hour; and in autumn juſt at Sun-ſet, becauſe all that half of the Ecliptic, in which the Sun is at that time, ſets at the ſame ſydereal hour, and the oppoſite half riſes; that is, 3 minutes 56 ſeconds, of mean ſolar time, ſooner every day than on the day before. So whilſt the Moon is going from Capricorn to Cancer, ſhe riſes earlier every day than on the preceding; contrary to what ſhe does at all places between the polar Circles. But during the above fourteen days, the Moon is 24 ſydereal hours later in ſetting; for the ſix Signs which riſe all at once on the eaſtern ſide of the Horizon are 24 hours in ſetting on the weſtern ſide of it; as any one may ſee by making chalk-marks

at the beginning of Capricorn and of Cancer, and then, having elevated the Pole 66½ degrees, turn the Globe ſlowly round it's Axis, and obſerve the riſing and ſetting of the Ecliptic. As the beginning of Aries is equally diſtant from the beginning of Cancer and of Capricorn, it is in the middle of that half of the Ecliptic which riſes all at once. And when the Sun is at the beginning of Libra, he is in the middle of the other half. Therefore, when the Sun is in Libra, and the Moon in Capricorn, the Moon is a Quarter of a Circle before the Sun; oppoſite to him, and conſequently full in Aries, and a Quarter of a Circle behind him, when in Cancer. But when Libra riſes, Aries ſets, and all that half of the Ecliptic of which Aries is the middle, and therefore, at that time of the year, the Moon riſes at Sun-ſet from her firſt to her third Quarter.

The Harveſt-Moons regular on both ſides of the Equator.

286. In northern Latitudes, the autumnal Full Moons are in Piſces and Aries; and the vernal Full Moons in Virgo and Libra: in ſouthern Latitudes juſt the reverſe, becauſe the ſeaſons are contrary. But Virgo and Libra riſe at as ſmall Angles with the Horizon in ſouthern Latitudes, as Piſces and Aries do in the northern; and therefore the Harveſt-Moons are juſt as regular on one ſide of the Equator as on the other.

287. As theſe Signs, which riſe with the leaſt Angles, ſet with the greateſt, the vernal Full Moons differ as much in their times of riſing every night as the autumnal Full Moons differ in their times of ſetting; and ſet with as little difference as the autumnal Full Moons riſe: the one being in all caſes the reverſe of the other.

288. Hitherto, for the ſake of plainneſs, we have ſuppoſed the Moon to move in the Ecliptic, from which the Sun never deviates. But the Orbit in which the Moon really moves is different from the Ecliptic: one half being elevated 5⅓ degrees above it, and the other half as much depreſſed

preſſed below it. The Moon's Orbit therefore interſects the Ecliptic in two points diametrically oppoſite to each other; and theſe interſections are called the *Moon's Nodes.* So the Moon can never be in the Ecliptic but when ſhe is in either of her Nodes, which is at leaſt twice in every courſe from Change to Change, and ſometimes thrice. For, as the Moon goes almoſt a whole Sign more than round her Orbit from Change to Change; if ſhe paſſes by either Node about the time of Change, ſhe will paſs by the other in about fourteen days after, and come round to the former Node two days again before the next Change. That Node from which the Moon begins to aſcend northward, or above the Ecliptic, in northern Latitudes, is called the *Aſcending Node*; and the other the *Deſcending Node*, becauſe the Moon, when ſhe paſſes by it, deſcends below the Ecliptic ſouthward.

The Moon's Nodes.

289. The Moon's oblique motion with regard to the Ecliptic cauſes ſome difference in the times of her riſing and ſetting from what is already mentioned. For whilſt ſhe is northward of the Ecliptic, ſhe riſes ſooner and ſets later than if ſhe moved in the Ecliptic: and when ſhe is ſouthward of the Ecliptic, ſhe riſes later and ſets ſooner. This difference is variable, even in the ſame Signs, becauſe the Nodes ſhift backward about $19\frac{2}{3}$ degrees in the Ecliptic every year; and ſo go round it contrary to the order of Signs in 18 years 225 days.

290. When the Aſcending Node is in Aries, the ſouthern half of the Moon's Orbit makes an Angle of $5\frac{1}{3}$ degrees leſs with the Horizon than the Ecliptic does, when Aries riſes in northern Latitudes: for which reaſon the Moon riſes with leſs difference of time whilſt ſhe is in Piſces and Aries, than there would be if ſhe kept in the Ecliptic. But in 9 years and 112 days afterward, the Deſcending Node comes to Aries; and then the Moon's Orbit makes an Angle $5\frac{1}{3}$ degrees greater with the Horizon when Aries riſes, than the

Ecliptic does at that time; which cauſes the Moon to riſe with greater difference of time in Piſces and Aries than if ſhe moved in the Ecliptic.

291. To be a little more particular; when the Aſcending Node is in Aries, the Angle is only $9\frac{2}{3}$ degrees on the parallel of *London* when Aries riſes. But when the Deſcending Node comes to Aries, the Angle is $20\frac{1}{3}$ degrees; this occaſions as great a difference of the Moon's riſing in the ſame Signs every 9 years, as there would be on two parallels to $10\frac{2}{3}$ degrees from one another, if the Moon's courſe were in the Ecliptic. The following Table ſhews how much the obliquity of the Moon's Orbit affects her riſing and ſetting on the parallel of *London*, from the 12th to the 18th day of her age; ſuppoſing her to be Full at the autumnal Equinox: and then, either in the Aſcending Node, higheſt part of her Orbit, Deſcending Node, or loweſt part of her Orbit. *M* ſignifies morning, *A* afternoon; and the line at the foot of the Table ſhews a week's difference in riſing and ſetting.

Moon's Age.	Full in her Aſcending node.		In the higheſt part of her Orbit.		Full in her Deſcending node.		In the loweſt part of her Orbit.	
	Riſes at H. M.	Sets at H. M.	Riſes at H. M.	Sets at H. M.	Riſes at H. M.	Sets at H. M.	Riſes at H. M.	Sets at H. M.
12	5 *A* 15	3 *M* 20	4 *A* 30	3 *M* 15	4 *A* 32	3 *M* 40	5 *A* 16	3 *M* 0
13	5 32	4 25	4 50	4 45	5 15	4 20	6 0	4 15
14	5 48	5 30	5 10	6 0	5 45	5 40	6 20	5 28
15	6 5	7 0	5 42	7 20	6 15	6 56	6 45	6 32
16	6 20	8 15	6 2	8 35	6 46	8 0	7 8	7 45
17	6 36	9 12	6 26	9 45	7 18	9 15	7 30	9 15
18	6 54	10 30	7 0	10 40	8 0	10 20	7 52	10 0
Dif.	1 39	7 10	2 30	7 25	3 28	6 40	2 36	7 0

This Table was not computed, but only eſtimated as near as could be done from a common Globe, on which the Moon's Orbit was delineated with a black-lead pencil. It may at firſt ſight appear erroneous; ſince as we have ſuppoſed the Moon to be full in either Node at the autumnal Equinox, ſhe ought by the Table to riſe juſt at ſix o'clock or at Sun-ſet, on the 15th day of her age; being in the Ecliptic at that time. But it muſt be conſidered, that the Moon is only 14$\frac{3}{4}$ days old when ſhe is Full; and therefore in both caſes ſhe is a little paſt the Node on the 15th day, being above it at one time, and below it at the other.

The period of the Harveſt-Moon.

292. As there is a compleat revolution of the Nodes in 18$\frac{2}{3}$ years, there muſt be a regular period of all the Varieties which can happen in the riſing and ſetting of the Moon during that time. But this ſhifting of the Nodes never affects the Moon's riſing ſo much, even in her quickeſt deſcending Latitude, as not to allow us ſtill the benefit of her riſing nearer the time of Sun-ſet for a few days together about the Full in Harveſt, than when ſhe is Full at any other time of the year. The following Table ſhews in what years the Harveſt-Moons are leaſt beneficial as to the times of their riſing, and in what years moſt, from 1751 to 1861. The column of years under the letter *L* are thoſe in which the Harveſt-Moons are leaſt of all beneficial, becauſe they fall about the Deſcending Node: and thoſe under *M* are the moſt of all beneficial, becauſe they fall about the Aſcending Node. In all the columns from *N* to *S* the Harveſt-Moons deſcend gradually in the Lunar Orbit, and riſe to leſs heights above the Horizon. From *S* to *N* they aſcend in the ſame proportion, and riſe to greater heights above the Horizon. In both the columns under *S* the Harveſt-Moons are in the loweſt part of the Moon's Orbit, that is, fartheſt South of the Ecliptic; and therefore ſtay ſhorteſt of all above the Horizon: in the columns under *N* juſt the reverſe. And in both caſes, their riſing, though not at the ſame times, are nearly the ſame with regard to difference of time, as if the Moon's Orbit were coincident with the Ecliptic.

Years in which the Harveſt-Moons are leaſt beneficial.

N				L				S	
1751	1752	1753	1754	1755	1756	1757	1758	1759	
1770	1771	1772	1773	1774	1775	1776	1777	1778	
1788	1789	1790	1791	1792	1793	1794	1795	1796	1797
1807	1808	1809	1810	1811	1812	1813	1814	1815	
1826	1827	1828	1829	1830	1831	1832	1833	1834	
1844	1845	1846	1847	1848	1849	1850	1851	1852	

Years in which they are moſt beneficial.

S				M				N	
1760	1761	1762	1763	1764	1765	1766	1767	1768	1769
1779	1780	1781	1782	1783	1784	1785	1786	1787	
1798	1799	1800	1801	1802	1803	1804	1805	1806	
1816	1817	1818	1819	1820	1821	1822	1823	1824	1825
1835	1836	1837	1838	1839	1840	1841	1842	1843	
1853	1854	1855	1856	1857	1858	1859	1860	1861	

293. At the Polar Circles, when the Sun touches the Summer Tropic, he continues 24 hours above the Horizon; and 24 hours below it when he touches the Winter Tropic. For the ſame reaſon the Full Moon neither riſes in Summer, nor ſets in Winter, conſidering her as moving in the Ecliptic. For the Winter Full Moon being as high in the Ecliptic as the Summer Sun, muſt therefore continue as long above the Horizon; and the Summer Full Moon being as low in the Ecliptic as the Winter Sun, can no more riſe than he does. But theſe are only the two Full Moons which happen about the Tropics, for all the others riſe and ſet. In Summer the Full Moons are low, and their ſtay is ſhort above the Horizon, when the nights are ſhort, and we have leaſt occaſion for Moon-light: in Winter they go high, and ſtay long above the Horizon, when the nights are long, and we want the greateſt quantity of Moon-light.

The long continuance of Moon-light at the Poles.

294. At the Poles, one half of the Ecliptic never ſets, and the other half never riſes: and therefore, as the Sun is always half a year in deſcribing one half of the Ecliptic, and as long in going through the other half, it is natural to imagine

Plate VIII.

Fig. I.

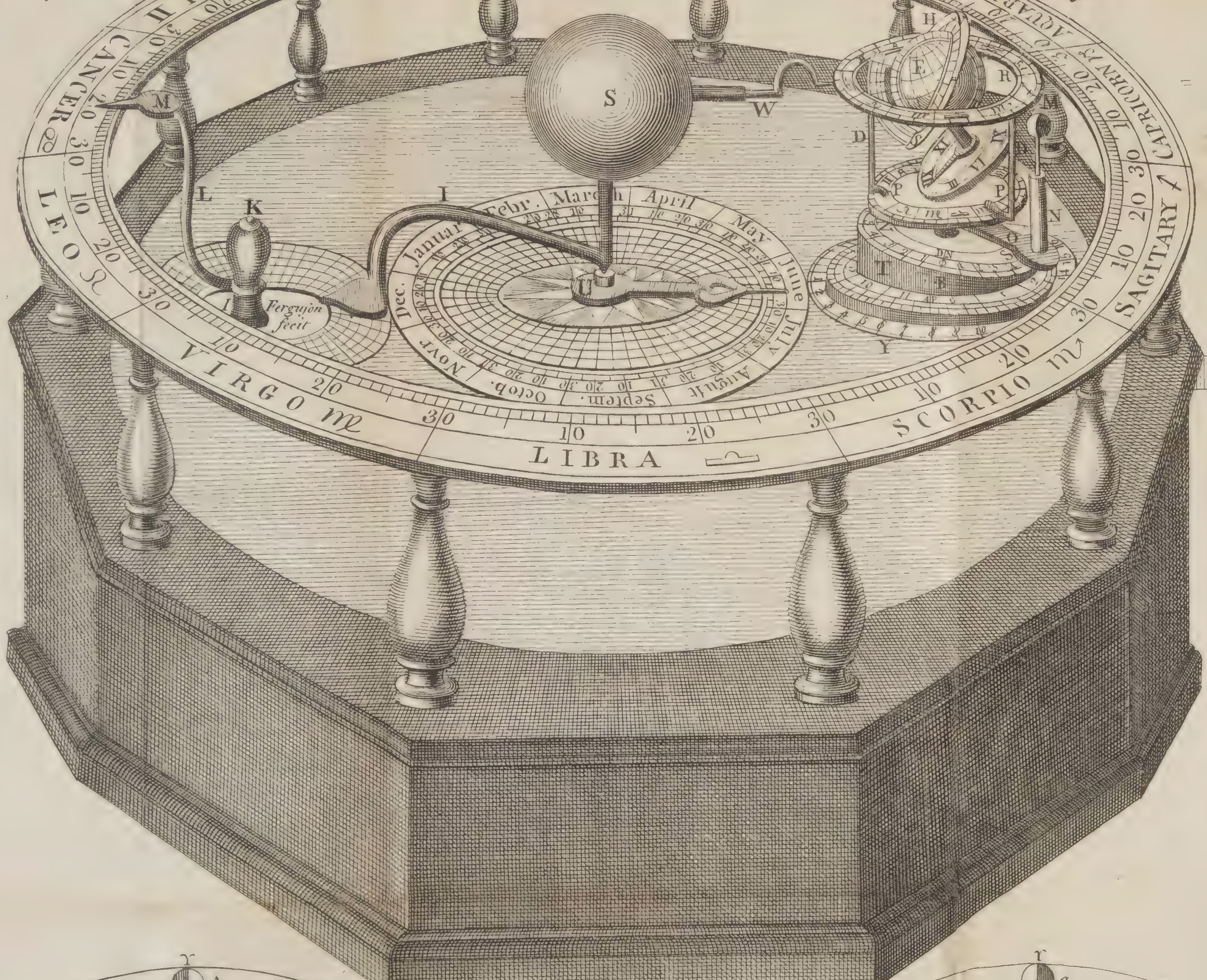


Fig. II.

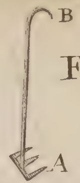


Fig. III.

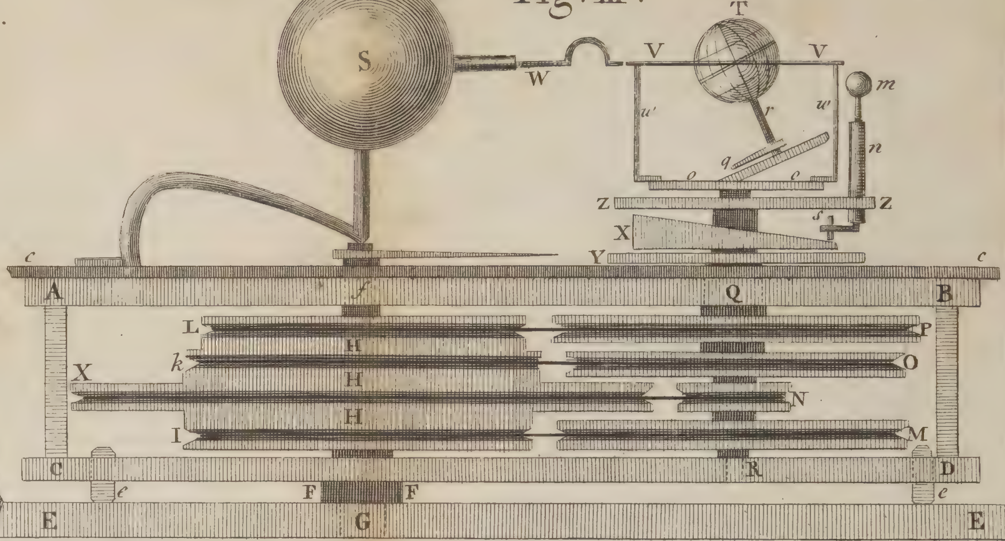


Fig. IIII.

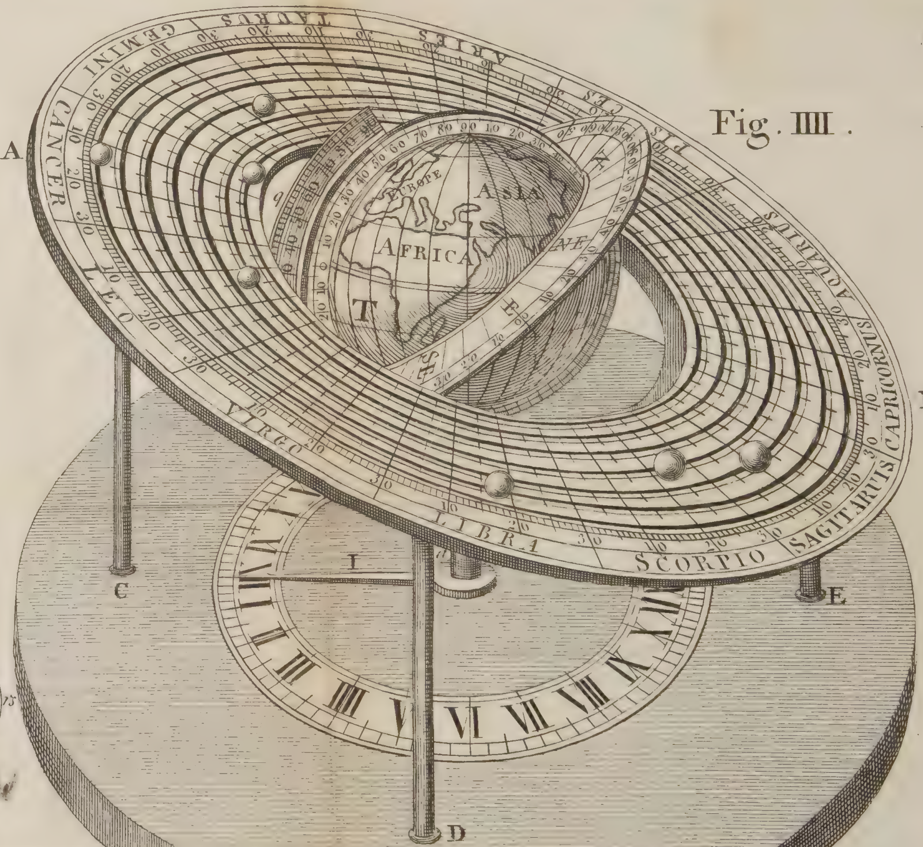
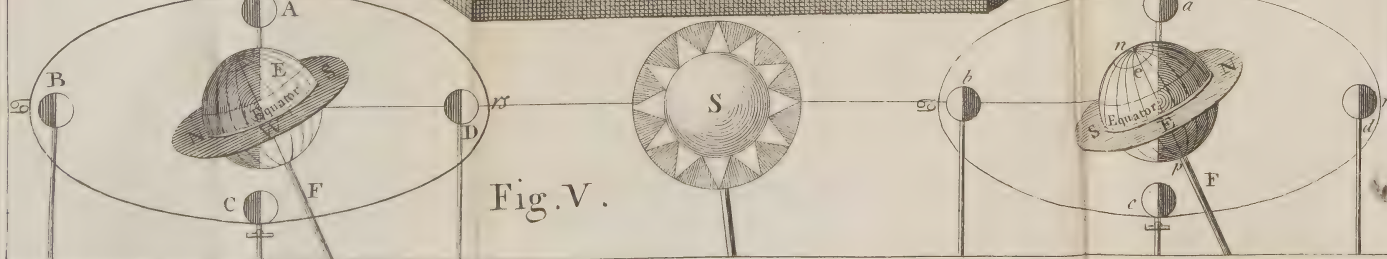


Fig. V.



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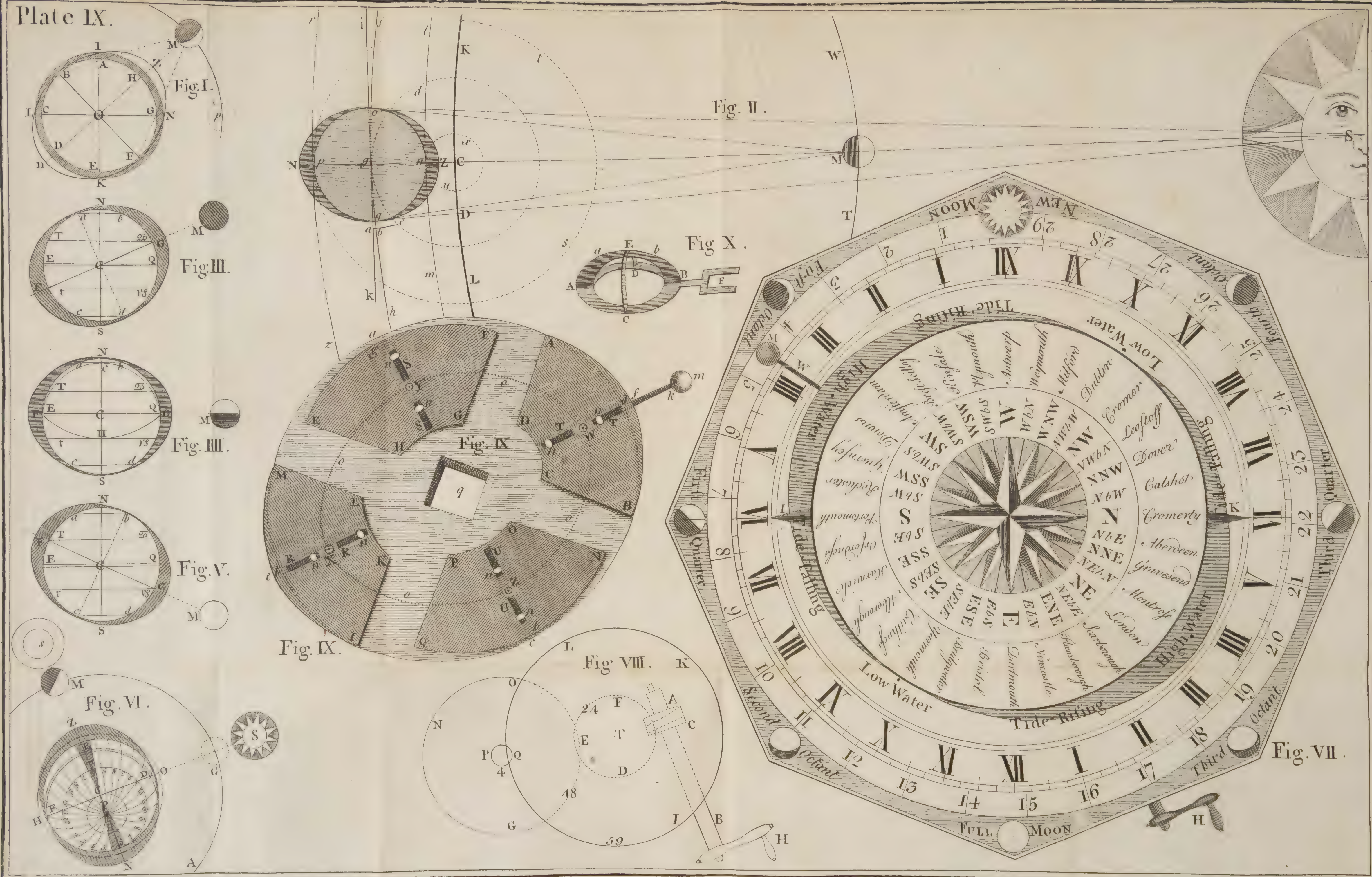
gine that the Sun continues half a year together above the Horizon of each Pole in it's turn, and as long below it; riſing to one Pole when he ſets to the other. This would be exactly the caſe if there were no refraction: but by the Atmoſphere's refracting the Sun's rays, he becomes viſible ſome days ſooner, § 183, and continues ſome days longer in ſight than he would otherwiſe do: ſo that he appears above the Horizon of either Pole before he has got below the Horizon of the other. And, as he never goes more than 23½ degrees below the Horizon of the Poles, they have very little dark night: it being twilight there as well as at all other places till the Sun be 18 degrees below the Horizon, § 177. The Full Moon being always oppoſite to the Sun, can never be ſeen while the Sun is above the Horizon, except when the Moon falls in the northern half of her Orbit; for whenever any point of the Ecliptic riſes, the oppoſite point ſets. Therefore, as the Sun is above the Horizon of the north Pole from the 20th of *March* till the 23d of *September*, it is plain that the Moon, when Full, being oppoſite to the Sun, muſt be below the Horizon during that half of the year. But when the Sun is in the ſouthern half of the Ecliptic, he never riſes to the north Pole, during which half of the year, every Full Moon happens in ſome part of the northern half of the Ecliptic, which never ſets. Conſequently, as the polar Inhabitants never ſee the Full Moon in Summer, they have her always in the Winter, before, at, and after the Full, ſhining for 14 of our days and nights. And when the Sun is at his greateſt depreſſion below the Horizon, being then in Capricorn, the Moon is at her Firſt Quarter in Aries, Full in Cancer, and at her Third Quarter in Libra. And as the beginning of Aries is the riſing point of the Ecliptic, Cancer the higheſt, and Libra the ſetting point, the Moon riſes at her firſt Quarter in Aries, is moſt elevated above the Horizon,

PLATE VIII. Horizon, and Full in Cancer, and ſets at the beginning of Libra in her Third Quarter, having continued viſible for 14 diurnal rotations of the Earth. Thus the Poles are ſupplied one half of the winter time with conſtant Moon-light in the Sun's abſence; and only loſe ſight of the Moon from her Third to her Firſt Quarter, while ſhe gives but very little light; and could be but of little, and ſometimes of no ſervice to them. A Fig. V. bare view of the Figure will make this plain; in which let *S* be the Sun, *e* the Earth in Summer when it's north Pole *n* inclines toward the Sun, and *E* the Earth in Winter, when it's north Pole declines from him. *S E N* and *N W S* is the Horizon of the north Pole, which is coincident with the Equator; and, in both theſe poſitions of the Earth, ♈ ♋ ♎ ♑ is the Moon's Orbit, in which ſhe goes round the Earth, according to the order of the letters *a b c d*, *A B C D*. When the Moon is at *a*, ſhe is in her Third Quarter to the Earth at *e*, and juſt riſing to the north Pole *n*; at *b* ſhe changes, and is at the greateſt height above the Horizon, as the Sun likewiſe is; at *c* ſhe is in her Firſt Quarter, ſetting below the Horizon; and is loweſt of all under it at *d*, when oppoſite to the Sun, and her enlightened ſide toward the Earth. But then ſhe is full in view to the ſouth Pole *p*; which is as much turned from the Sun as the north Pole inclines towards him. Thus in our Summer, the Moon is above the Horizon of the north Pole whilſt ſhe deſcribes the northern half of the Ecliptic ♈ ♋ ♎, or from her Third Quarter to her Firſt; and below the Horizon during her progreſs through the ſouthern half ♎ ♑ ♈; higheſt at the Change, moſt depreſſed at the Full. But in Winter, when the Earth is at *E*, and it's north Pole declines from the Sun, the New Moon at *D* is at her greateſt depreſſion below the Horizon *N W S*, and the Full Moon at *B* at her greateſt height above it; riſing at her Firſt Quarter *A*, and

Plate IX.



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and keeping above the Horizon till ſhe comes to her Third Quarter *C*. At a mean ſtate ſhe is $23\frac{1}{2}$ degrees above the Horizon at *B* and *b*, and as much below it at *D* and *d*, equal to the inclination of the Earth's Axis *F*. *S* ♋ and *S* ♑ are, as it were, a ray of light proceeding from the Sun to the Earth; and ſhews that when the Earth is at *e*, the Sun is above the Horizon, vertical to the Tropic of Cancer; and when the Earth is at *E*, he is below the Horizon, vertical to the Tropic of Capricorn.

CHAP. XVII.

Of the Ebbing and Flowing of the Sea.

295. THE cauſe of the Tides was diſcovered by KEPLER, who, in his *Introduction to the Phyſics of the Heavens*, thus explains it: "The Orb of the attracting power, which is in the Moon, is extended as far as the Earth; and draws the waters under the torrid Zone, acting upon places where it is vertical, inſenſibly on confined ſeas and bays, but ſenſibly on the ocean whoſe beds are large, and the waters have the liberty of reciprocation; that is, of riſing and falling." And in the 70th page of his *Lunar Aſtronomy*—— "But the cauſe of the Tides of the Sea appears to be the bodies of the Sun and Moon drawing the waters of the Sea." This hint being given, the immortal Sir ISAAC NEWTON improved it, and wrote ſo amply on the ſubject, as to make the Theory of the Tides in a manner quite his own; by diſcovering the cauſe of their riſing on the ſide of the Earth oppoſite to the Moon. For KEPLER believed, that the preſence of the Moon occaſioned an impulſe which cauſed another in her abſence.

The cauſe of the Tides diſcovered by KEPLER.

Their Theory improved by Sir ISAAC NEWTON.

296. It has been already ſhewn, § 106, that the power of gravity diminiſhes as the ſquare of the diſtance increaſes; and therefore the waters at *Z* on

Explained on the Newtonian principles.

PLATE IX. Fig. I. on the ſide of the Earth *A B C D E F G H* next the Moon *M* are more attracted than the central parts of the Earth *O* by the Moon, and the central parts are more attracted by her than the waters on the oppoſite ſide of the Earth at *n*: and therefore the diſtance between the Earth's center and the waters on it's ſurface under and oppoſite to the Moon will be increaſed. For, let there be three bodies at *H*, *O*, and *D*: if they are all equally attracted by the body *M*, they will all move equally faſt toward it, their mutual diſtances from each other continuing the ſame. If the attraction of *M* is unequal, then that body which is moſt ſtrongly attracted will move faſteſt, and this will increaſe it's diſtance from the other body. Therefore, by the law of gravitation, *M* will attract *H* more ſtrongly than it does *O*, by which, the diſtance between *H* and *O* will be increaſed: and a ſpectator on *O* will perceive *H* riſing higher toward *Z*. In like manner, *O* being more ſtrongly attracted than *D*, it will move farther towards *M* than *D* does: conſequently, the diſtance between *O* and *D* will be increaſed; and a ſpectator on *O*, not perceiving his own motion, will ſee *D* receding farther from him towards *n*: all effects and appearances being the ſame, whether *D* recedes from *O*, or *O* from *D*.

297. Suppoſe now there is a number of bodies, as *A*,*B*,*C*,*D*,*E*,*F*,*G*,*H* placed round *O*, ſo as to form a flexible or fluid ring: then, as the whole is attracted towards *M*, the parts at *H* and *D* will have their diſtance from *O* increaſed; whilſt the parts at *B* and *F*, being nearly at the ſame diſtance from *M* as *O* is, theſe parts will not recede from one another; but rather, by the oblique attraction of *M*, they will approach nearer to *O*. Hence, the fluid ring will form itſelf into an ellipſe *Z I B L n K F N Z*, whoſe longer Axis *n O Z* produced will paſs through *M*, and it's ſhorter Axis *B O F* will terminate in *B* and *F*. Let the ring be

filled with fluid particles, ſo as to form a ſphere round *O*; then, as the whole moves toward *M*, the fluid ſphere being lengthened at *Z* and *n*, will aſſume an oblong or oval form. If *M* is the Moon, *O* the Earth's center, *ABCDEFGH* the Sea covering the Earth's ſurface, it is evident, by the above reaſoning, that whilſt the Earth by it's gravity falls toward the Moon, the Water directly below her at *B* will ſwell and riſe gradually towards her: alſo the Water at *D* will recede from the center [ſtrictly ſpeaking, the center recedes from *D*] and riſe on the oppoſite ſide of the Earth: whilſt the Water at *B* and *F* is depreſſed, and falls below the former level. Hence, as the Earth turns round it's Axis from the Moon to the Moon again in 24¾ hours, there will be two Tides of Flood and two of Ebb in that time, as we find by experience.

298. As this explanation of the ebbing and flowing of the Sea is deduced from the Earth's conſtantly falling toward the Moon by the power of gravity, ſome may find a difficulty in conceiving how this is poſſible, when the Moon is full, or in oppoſition to the Sun; ſince the Earth revolves about the Sun, and muſt continually fall towards it, and therefore cannot fall contrary ways at the ſame time: or if the Earth is conſtantly falling towards the Moon, they muſt come together at laſt. To remove this difficulty, let it be conſidered, that it is not the center of the Earth that deſcribes the annual Orbit round the Sun, but the * common center of gravity of the Earth and Moon together: and that whilſt the Earth is moving

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* This center is as much nearer the Earth's center than the Moon's as the Earth is heavier, or contains a greater quantity of matter than the Moon, namely, about 40 times. If both bodies were ſuſpended on it, they would hang in *equilibrio*. So that dividing 240,000 miles, the Moon's diſtance from the Earth's center, by 40, the exceſs of the Earth's weight above the Moon's, the quotient will be 6000 miles, which is the diſtance of the common center of gravity of the Earth and Moon from the Earth's center.

PLATE IX. moving round the Sun, it alſo deſcribes a Circle round that center of gravity; going as many times round it in one revolution about the Sun as there are lunations or courſes of the Moon round the Earth in a year: and therefore, the Earth is conſtantly falling towards the Moon from a tangent to the Circle it deſcribes round the ſaid common center of gravity. Fig. II. Let *M* be the Moon, *TW* part of the Moon's Orbit, and *C* the center of gravity of the Earth and Moon: whilſt the Moon goes round her Orbit, the center of the Earth deſcribes the Circle *e g d* round *C*, to which Circle *g a k* is a tangent: and therefore, when the Moon has gone from *M* to a little paſt *W*, the Earth has moved from *g* to *e*; and in that time has fallen towards the Moon, from the tangent at *a* to *e*; and ſo round the whole Circle.

299. The Sun's influence in raiſing the Tides is but ſmall in compariſon of the Moon's: For though the Earth's diameter bears a conſiderable proportion to it's diſtance from the Moon, it is next to nothing when compared with the diſtance of the Sun. And therefore, the difference of the Sun's attraction on the ſides of the Earth under and oppoſite to him, is much leſs than the difference of the Moon's attraction on the ſides of the Earth under and oppoſite to her: and therefore the Moon muſt raiſe the Tides much higher than they can be raiſed by the Sun.

Why the Tides are not higheſt when the Moon is on the Meridian.

300. On this Theory, ſo far as we have explained it, the Tides ought to be higheſt directly under and oppoſite to the Moon; that is, when the Moon is due north and ſouth. But we find, that in open Seas, where the water flows freely, the Moon *M* is generally paſt the north and ſouth Meridian, as at *p*, when it is high water at *Z* and at *n*. Fig. I. The reaſon is obvious; for though the Moon's attraction was to ceaſe altogether when ſhe was paſt the Meridian, yet the motion of aſcent

communicated to the water before that time would make it continue to riſe for ſome time after; much more muſt it do ſo when the attraction is only diminiſhed: as a little impulſe given to a moving ball will cauſe it ſtill to move farther than otherwiſe it could have done. And as experience ſhews, that the day is hotter about three in the afternoon, than when the Sun is on the Meridian, becauſe of the encreaſe made to the heat already imparted.

PLATE IX.

301. The Tides anſwer not always to the ſame diſtance of the Moon from the Meridian at the ſame places; but are variouſly affected by the action of the Sun, which brings them on ſooner when the Moon is in her firſt and third Quarters, and keeps them back later when ſhe is in her ſecond and fourth: becauſe, in the former caſe, the Tide raiſed by the Sun alone would be earlier than the Tide raiſed by the Moon; and in the latter caſe later.

Nor always anſwer to her being at the ſame diſtance from it.

302. The Moon goes round the Earth in an elliptic Orbit, and therefore, in every Lunar Month, ſhe approaches nearer to the Earth than her mean diſtance, and recedes farther from it. When ſhe is neareſt, ſhe attracts ſtrongeſt, and ſo raiſes the Tides moſt; the contrary happens when ſhe is fartheſt, becauſe of her weaker attraction. When both Luminaries are in the Equator, and the Moon in *Perigeo*, or at her leaſt diſtance from the Earth, ſhe raiſes the Tides higheſt of all, eſpecially at her Conjunction and Oppoſition; both becauſe the equatoreal parts have the greateſt centrifugal force from their deſcribing the largeſt Circle, and from the concurring actions of the Sun and Moon. At the Change, the attractive forces of the Sun and Moon being united, they diminiſh the gravity of the waters under the Moon, and their gravity on the oppoſite ſide is diminiſhed by means of a greater centrifugal force. At the Full, whilſt the Moon raiſes the Tide under and oppoſite to her, the Sun acting in the ſame line, raiſes the Tide

Spring and neap Tides.

Fig. VI.

under and oppoſite to him; whence their conjoint effect is the ſame as at the Change; and in both caſes, occaſion what we call *the Spring Tides.* But at the Quarters the Sun's action on the waters at O and *H* diminiſhes the effect of the Moon's action on the waters at *Z* and *N*; ſo that they riſe a little under and oppoſite to the Sun at *O* and *H*, and fall as much under and oppoſite to the Moon at *Z* and *N*; making what we call the *Neap Tides*, becauſe the Sun and Moon then act croſs-wiſe to each other. But, ſtrictly ſpeaking, theſe Tides happen not till ſome time after; becauſe in this, as in other caſes, § 300, the actions do not produce the greateſt effect when they are at the ſtrongeſt, but ſome time afterward.

Not greateſt at the Equinoxes, and why.

303. The Sun being nearer the Earth in Winter than in Summer, § 205, is of courſe nearer to it in *February* and *October* than in *March* and *September*; and therefore the greateſt Tides happen not till ſome time after the autumnal Equinox, and return a little before the vernal.

The Tides would not immediately ceaſe upon the annihilation of the Sun and Moon.

The Sea being thus put in motion, would continue to ebb and flow for ſeveral times, even though the Sun and Moon were annihilated, or their influence ſhould ceaſe: as if a baſon of water were agitated, the water would continue to move for ſome time after the baſon was left to ſtand ſtill. Or like a Pendulum, which having been put in motion by the hand, continues to make ſeveral vibrations without any new impulſe.

The lunar day, what. The Tides riſe to unequal heights in the ſame day, and why.

304. When the Moon is in the Equator, the Tides are equally high in both parts of the lunar day, or time of the Moon's revolving from the Meridian to the Meridian again, which is 24 hours 50 minutes. But as the Moon declines from the Equator towards either Pole, the Tides are alternately higher and lower at places having north or ſouth Latitude. For one of the higheſt elevations, which is that under the Moon, follows her towards

the Pole to which ſhe is neareſt, and the other declines towards the oppoſite Pole; each elevation deſcribing parallels as far diſtant from the Equator, on oppoſite ſides, as the Moon declines from it to either ſide; and conſequently, the parallels deſcribed by theſe elevations of the water are twice as many degrees from one another, as the Moon is from the Equator; increaſing their diſtance as the Moon increaſes her declination, till it be at the greateſt, when the ſaid parallels are, at a mean ſtate, 47 degrees from one another: and on that day, the Tides are moſt unequal in their heights. As the Moon returns toward the Equator, the parallels deſcribed by the oppoſite elevations approach towards each other, until the Moon comes to the Equator, and then they coincide. As the Moon declines toward the oppoſite Pole, at equal diſtances, each elevation deſcribes the ſame parallel in the other part of the lunar day, which it's oppoſite elevation deſcribed before. Whilſt the Moon has north declination, the greateſt Tides in the northern Hemiſphere are when ſhe is above the Horizon; and the reverſe whilſt her declination is ſouth. Let *N E S Q* be the Earth, *N C S* it's Axis, *E Q* the Equator, *T* ♋ the Tropic of Cancer, *t* ♑ the Tropic of Capricorn, *a b* the arctic Circle, *c d* the antarctic, *N* the north Pole, *S* the ſouth Pole, *M* the Moon, *F* and *G* the two eminences of water, whoſe loweſt parts are at *a* and *d* (Fig. III.) at *N* and *S* (Fig. IV.) and at *b* and *c* (Fig. V.) always 90 degrees from the higheſt. Now when the Moon is in her greateſt north declination at *M*, the higheſt elevation *G* under her, is on the Tropic of Cancer, *T* ♋, and the oppoſite elevation *F* on the Tropic of Capricorn *t* ♑; and theſe two elevations deſcribe the Tropics by the Earth's diurnal rotation. All places in the northern Hemiſphere *E N Q* have the higheſt Tides when they come into the poſition *b* ♋ *Q*, under the Moon; and the loweſt Tides when the Earth's diurnal

PLATE IX.

Fig. III, IV, V.

Fig. III.

rotation

PLATE IX.

rotation carries them into the poſition *a T E*, on the ſide oppoſite to the Moon; the reverſe happens at the ſame time in the ſouthern Hemiſphere *E S Q*, as is evident to ſight. The Axis of the Tides *a C d* has now it's Poles *a* and *d* (being always 90 degrees from the higheſt elevations) in the arctic and antarctic Circles; and therefore it is plain, that at theſe Circles there is but one Tide of Flood, and one of Ebb, in the lunar day. For, when the point *a* revolves half round to *b*, in 12 lunar hours, it has a Tide of Flood; but when it comes to the ſame point *a* again in 12 hours more, it has the loweſt Ebb. In ſeven days afterward, the Moon *M* comes to the equinoctial Circle, and is over the Equator *E Q*, when both elevations deſcribe the Equator; and in both Hemiſpheres, at equal diſtances from the Equator, the Tides are equally high in both parts of the lunar day. The whole Phenomena being reverſed, when the Moon has ſouth declination, to what they were when her declination was north, require no farther deſcription.

Fig. IV.

Fig. V.

305. In the three laſt-mentioned Figures, the Earth is orthographically projected on the plane of the Meridian; but in order to deſcribe a particular Phenomenon, we now project it on the plane of the Ecliptic. Let *H Z O N* be the Earth and Sea, *F E D* the Equator, *T* the Tropic of Cancer, *C* the arctic Circle, *P* the north Pole, and the Curves 1, 2, 3, *&c.* 24 Meridians, or Hour-circles, interſecting each other in the Poles; *A G M* is the Moon's Orbit, *S* the Sun, *M* the Moon, *Z* the Water elevated under the Moon, and *N* the oppoſite equal Elevation. As the loweſt parts of the Water are always 90 degrees from the higheſt, when the Moon is in either of the Tropics (as at *M*) the Elevation *Z* is on the Tropic of Capricorn, and the oppoſite Elevation *N* on the Tropic of Cancer, the low-water Circle *H C O* touches the polar Circles at *C*; and the high-water Circle

Fig. VI.

When both Tides are equally high in the ſame day, they arrive at unequal intervals of Time; and *vice verſâ.*

E T P 6

E T P 6 goes over the Poles at *P*, and divides every parallel of Latitude into two equal ſegments. In this caſe the Tides upon every parallel are alternately higher and lower; but they return in equal times: the point *T*, for example, on the Tropic of Cancer (where the depth of the Tide is repreſented by the breadth of the dark ſhade) has a ſhallower Tide of Flood at *T* than when it revolves half round from thence to 6, according to the order of the numeral Figures; but it revolves as ſoon from 6 to *T* as it did from *T* to 6. When the Moon is in the Equinoctial, the Elevations *Z* and *N* are transferred to the Equator at *O* and *H*, and the high and low-water Circles are got into each other's former places; in which caſe the Tides return in unequal times, but are equally high in both parts of the lunar day: for a place at 1 (under *D*) revolving as formerly, goes ſooner from 1 to 11 (under *F*) than from 11 to 1, becauſe the parallel it deſcribes is cut into unequal ſegments by the high-water Circle *H C O*: but the points 1 and 11 being equidiſtant from the Pole of the Tides at *C*, which is directly under the Pole of the Moon's Orbit *M G A*, the Elevations are equally high in both parts of the day.

306. And thus it appears, that as the Tides are governed by the Moon, they muſt turn on the Axis of the Moon's Orbit, which is inclined 23½ degrees to the Earth's Axis at a mean ſtate: and therefore the Poles of the Tides muſt be ſo many degrees from the Poles of the Earth, or in oppoſite points of the polar Circles, going round theſe Circles in every lunar day. It is true, that according to Fig. IV, when the Moon is vertical to the Equator *E C Q*, the Poles of the Tides ſeem to fall in with the Poles of the World *N* and *S*: but when we conſider that *F G H* is under the Moon's Orbit, it will appear, that when the Moon is over *H*, in the Tropic of Capricorn, the north Pole of

the Tides (which can be no more than 90 degrees from under the Moon) muſt be at *c* in the arctic Circle, not at *N*, the north Pole of the Earth; and as the Moon aſcends from *H* to *G* in her Orbit, the north Pole of the Tides muſt ſhift from *c* to *a* in the arctic Circle, and the ſouth Pole as much in the antarctic.

It is not to be doubted, but that the Earth's quick rotation brings the Poles of the Tides nearer to the Poles of the World, than they would be if the Earth were at reſt, and the Moon revolved about it only once a month; for otherwiſe the Tides would be more unequal in their heights, and times of their returns, than we find they are. But how near the Earth's rotation may bring the Poles of it's Axis and thoſe of the Tides together, or how far the preceding Tides may affect thoſe which follow, ſo as to make them keep up nearly to the ſame heights, and times of ebbing and flowing, is a problem more fit to be ſolved by obſervation than by theory.

To know at what times we may expect the greateſt and leaſt Tides.

307. Thoſe who have opportunity to make obſervations, and chooſe to ſatisfy themſelves whether the Tides are really affected in the above manner by the different poſitions of the Moon, eſpecially as to the unequal times of their returns, may take this general rule for knowing when they ought to be ſo affected. When the Earth's Axis inclines to the Moon, the northern Tides, if not retarded in their paſſage through Shoals and Channels, nor affected by the Winds, ought to be greateſt when the Moon is above the Horizon, leaſt when ſhe is below it; and quite the reverſe when the Earth's Axis declines from her: but in both caſes, at equal intervals of time. When the Earth's Axis inclines ſidewiſe to the Moon, both Tides are equally high, but they happen at unequal intervals of time. In every Lunation the Earth's Axis inclines once to the Moon, once from her,

and twice ſidewiſe to her, as it does to the Sun every year; becauſe the Moon goes round the Ecliptic every month, and the Sun but once in a year. In Summer, the Earth's Axis inclines towards the Moon when New; and therefore the day-tides in the north ought to be higheſt, and night-tides loweſt about the Change: at the Full the reverſe. At the Quarters they ought to be equally high, but unequal in their returns; becauſe the Earth's Axis then inclines ſidewiſe to the Moon. In Winter the Phenomena are the ſame at Full-Moon as in Summer at New. In Autumn the Earth's Axis inclines ſidewiſe to the Moon when New and Full; therefore the Tides ought to be equally high, and unequal in their returns at theſe times. At the firſt Quarter the Tides of Flood ſhould be leaſt when the Moon is above the Horizon, greateſt when ſhe is below it; and the reverſe at her third Quarter. In Spring, the Phenomena of the firſt Quarter anſwer to thoſe of the third Quarter in Autumn; and *vice verſâ*. The nearer any time is to either of theſe ſeaſons, the more the Tides partake of the Phenomena of theſe ſeaſons; and in the middle between any two of them the Tides are at a mean ſtate between thoſe of both.

Why the Tides riſe higher in Rivers than in the Sea.

308. In open Seas, the Tides riſe but to very ſmall heights in proportion to what they do in wide-mouthed rivers, opening in the Direction of the Stream of Tide. For, in Channels growing narrower gradually, the water is accumulated by the oppoſition of the contracting Bank. Like a gentle wind, little felt on an open plain, but ſtrong and briſk in a ſtreet; eſpecially if the wider end of the ſtreet be next the plain, and in the way of the wind.

The Tides happen at all diſtances of the Moon from the Meridian at different places, and why.

309. The Tides are ſo retarded in their paſſage through different Shoals and Channels, and otherwiſe ſo variouſly affected by ſtriking againſt Capes and Headlands, that to different places they happen at all diſtances of the Moon from the Meridian;

conſequently at all hours of the lunar day. The Tide propagated by the Moon in the *German* Ocean, when ſhe is three hours paſt the Meridian, takes 12 hours to come from thence to *London Bridge*; where it arrives by the time that a new Tide is raiſed in the Ocean. And therefore when the Moon has north declination, and we ſhould expect the Tide at *London* to be greateſt when the Moon is above the Horizon, we find it is leaſt; and the contrary when ſhe has ſouth declination. At ſeveral places it is high water three hours before the Moon comes to the Meridian; but that Tide which the Moon puſhes as it were before her, is only the Tide oppoſite to that which was raiſed by her when ſhe was nine hours paſt the oppoſite Meridian.

The Water never riſes in Lakes.

310. There are no Tides in Lakes, becauſe they are generally ſo ſmall, that when the Moon is vertical ſhe attracts every part of them alike, and therefore by rendering all the water equally light, no part of it can be raiſed higher than another. The *Mediterranean* and *Baltic* Seas ſuffer very ſmall elevations, becauſe the Inlets by which they communicate with the Ocean are ſo narrow, that they cannot, in ſo ſhort a time, receive or diſcharge enough to raiſe or ſink their ſurfaces ſenſibly.

The Moon raiſes Tides in the Air.

311. Air being lighter than Water, and the ſurface of the Atmoſphere being nearer to the Moon than the ſurface of the Sea, it cannot be doubted that the Moon raiſes much higher Tides in the Air than in the Sea. And therefore many have wondered why the Mercury does not ſink in the Barometer when the Moon's action on the particles of Air makes them lighter as ſhe paſſes over the Meridian. But we muſt conſider, that as theſe particles are rendered lighter, a greater number of them is accumulated, until the deficiency of gravity be made up by the height of the column; and then there is an *equilibrium*, and conſequently

Why the Mercury in the Barometer is not affected by the aerial Tides.

ſequently an equal preſſure upon the Mercury as before; ſo that it cannot be affected by the aerial Tides.

CHAP. XVIII.

Of Eclipſes: Their Number and Periods. A large Catalogue of Ancient and Modern Eclipſes.

312. EVERY Planet and Satellite is illuminated by the Sun; and caſts a ſhadow towards that point of the Heavens which is oppoſite to the Sun. This ſhadow is nothing but a privation of light in the ſpace hid from the Sun by the opake body that intercepts his rays. A ſhadow, what.

313. When the Sun's light is ſo intercepted by the Moon, that to any place of the Earth the Sun appears partly or wholly covered, he is ſaid to undergo an Eclipſe; though properly ſpeaking, it is only an Eclipſe of that part of the Earth where the Moon's ſhadow or * Penumbra falls. When the Earth comes between the Sun and Moon, the Moon falls into the Earth's ſhadow; and having no light of her own, ſhe ſuffers a real Eclipſe from the interception of the Sun's rays. When the Sun is eclipſed to us, the Moon's Inhabitants on the ſide next the Earth (if any ſuch there be) ſee her ſhadow like a dark ſpot travelling over the Earth, about twice as faſt as it's equatoreal parts move, and the ſame way as they move. When the Moon is in an Eclipſe, the Sun appears eclipſed to her, total to all thoſe parts on which the Earth's ſhadow falls, and of as long continuance as they are in the ſhadow. Eclipſes of the Sun and Moon, what.

314. That the Earth is ſpherical (for the hills take off no more from the roundneſs of the Earth, than grains of duſt do from the roundneſs of a common A proof that the Earth and Moon are globular bodies.

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* The Penumbra is a faint kind of ſhadow all around the perfect ſhadow of the Planet or Satellite, and will be more fully explained by and by.

common Globe) is evident from the figure of its ſhadow on the Moon; which is always bounded by a circular line, although the Earth is inceſſantly turning it's different ſides to the Moon, and very ſeldom ſhews the ſame ſide to her in different Eclipſes, becauſe they ſeldom happen at the ſame hours. Were the Earth ſhaped like a round flat plate, it's ſhadow would only be circular when either of it's ſides directly faced the Moon; and more or leſs elliptical as the Earth happened to be turned more or leſs obliquely towards the Moon when ſhe is eclipſed. The Moon's different Phaſes prove her to be round, § 254; for, as ſhe keeps ſtill the ſame ſide towards the Earth, if that ſide were flat, as it appears to be, ſhe would never be viſible from the third Quarter to the firſt; and from the firſt Quarter to the third, ſhe would appear as round as when we ſay ſhe is Full: becauſe at the end of her firſt Quarter the Sun's light would come as ſuddenly on all her ſide next the Earth, as it does on a flat wall, and go off as abruptly at the end of her third Quarter.

And that the Sun is much bigger than the Earth, and the Moon much leſs.

315. If the Earth and Sun were equally big, the Earth's ſhadow would be infinitely extended, and all of the ſame bulk; and the Planet Mars, in either of it's Nodes and oppoſite to the Sun, would be eclipſed in the Earth's ſhadow. Were the Earth bigger than the Sun, it's ſhadow would increaſe in bulk the farther it extended, and would eclipſe the great Planets Jupiter and Saturn, with all their Moons, when they were oppoſite to the Sun. But as Mars in oppoſition never falls into the Earth's ſhadow, although he is not then above 42 millions of miles from the Earth, it is plain that the Earth is much leſs than the Sun; for otherwiſe it's ſhadow could not end in a point at ſo ſmall a diſtance. If the Sun and Moon were equally big, the Moon's ſhadow would go on to the Earth with an equal breadth, and cover a portion of the Earth's ſurface more than 2000 miles

broad, even if it fell directly againſt the Earth's center, as ſeen from the Moon: and much more if it fell obliquely on the Earth: but the Moon's ſhadow is ſeldom 150 miles broad at the Earth, unleſs when it falls very obliquely on the Earth, in total Eclipſes of the Sun. In annular Eclipſes, the Moon's real ſhadow ends in a point at ſome diſtance from the Earth. The Moon's ſmall diſtance from the Earth, and the ſhortneſs of her ſhadow, prove her to be leſs than the Sun. And, as the Earth's ſhadow is large enough to cover the Moon, if her diameter were three times as large as it is (which is evident from her long continuance in the ſhadow when ſhe goes through it's center) it is plain, that the Earth is much bigger than the Moon.

The primary Planets never eclipſe one another.

316. Though all opake bodies on which the Sun ſhines have their ſhadows, yet ſuch is the bulk of the Sun, and the diſtances of the Planets, that the primary Planets can never eclipſe one another. A Primary can eclipſe only it's Secondary, or be eclipſed by it; and never but when in oppoſition or conjunction with the Sun. The primary Planets are very ſeldom in theſe poſitions, but the Sun and Moon are ſo every month: whence one may imagine that theſe two Luminaries ſhould be eclipſed every month. But there are few Eclipſes in reſpect of the number of New and Full Moons; the reaſon of which we ſhall now explain.

Why there are ſo few Eclipſes.

317. If the Moon's Orbit were coincident with the Plane of the Ecliptic, in which the Earth always moves and the Sun appears to move, the Moon's ſhadow would fall upon the Earth at every Change, and eclipſe the Sun to ſome parts of the Earth. In like manner the Moon would go through the middle of the Earth's ſhadow, and be eclipſed at every Full; but with this difference, that ſhe would be totally darkened for above an hour and half; whereas the Sun never was above four minutes totally eclipſed by the interpoſition of

The Moon's Nodes. of the Moon. But one half of the Moon's Orbit is elevated $5\frac{1}{3}$ degrees above the Ecliptic, and the other half as much depreſſed below it: conſequently, the Moon's Orbit interſects the Ecliptic in two oppoſite points called *the Moon's Nodes*, as has been already taken notice of, § 288. When theſe points are in a right line with the center of the Sun at New or Full Moon, the Sun, Moon and Earth, are all in a right line; and if the Moon be then New, her ſhadow falls upon the Earth; if Full, the Earth's ſhadow falls upon her. When Limits of Eclipſes. the Sun and Moon are more than 17 degrees from either of the Nodes at the time of Conjunction, the Moon is then generally too high or too low in her Orbit to caſt any part of her ſhadow upon the Earth. And when the Sun is more than 12 degrees from either of the Nodes at the time of Full Moon, the Moon is generally too high or too low in her Orbit to go through any part of the Earth's ſhadow: and in both theſe caſes there will be no Eclipſe. But when the Moon is leſs than 17 degrees from either Node at the time of Conjunction, her ſhadow or Penumbra falls more or leſs upon the Earth, as ſhe is more or leſs within this limit *. And when ſhe is leſs than 12 degrees from either Node at the time of Oppoſition, ſhe goes through a greater or leſs portion of the Earth's ſhadow, as ſhe is more or leſs within this limit. Her Orbit contains 360 degrees; of which 17, the limit of ſolar Eclipſes on either ſide of the Nodes, and 12, the limit of lunar Eclipſes, are but ſmall portions: and as the Sun commonly paſſes by the Nodes but twice in a year, it is no wonder that

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* This admits of ſome variation: for, in apogeal Eclipſes, the ſolar limit is but $16\frac{1}{2}$ degrees; and in perigeal Eclipſes it is $18\frac{1}{3}$.——When the Full Moon is in her Apogee, ſhe will be eclipſed if ſhe be within $10\frac{1}{2}$ degrees of the Node; and when ſhe is full in her Perigee, ſhe will be eclipſed if ſhe be within $12\frac{1}{30}$ degrees of the Node.

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Plate X.

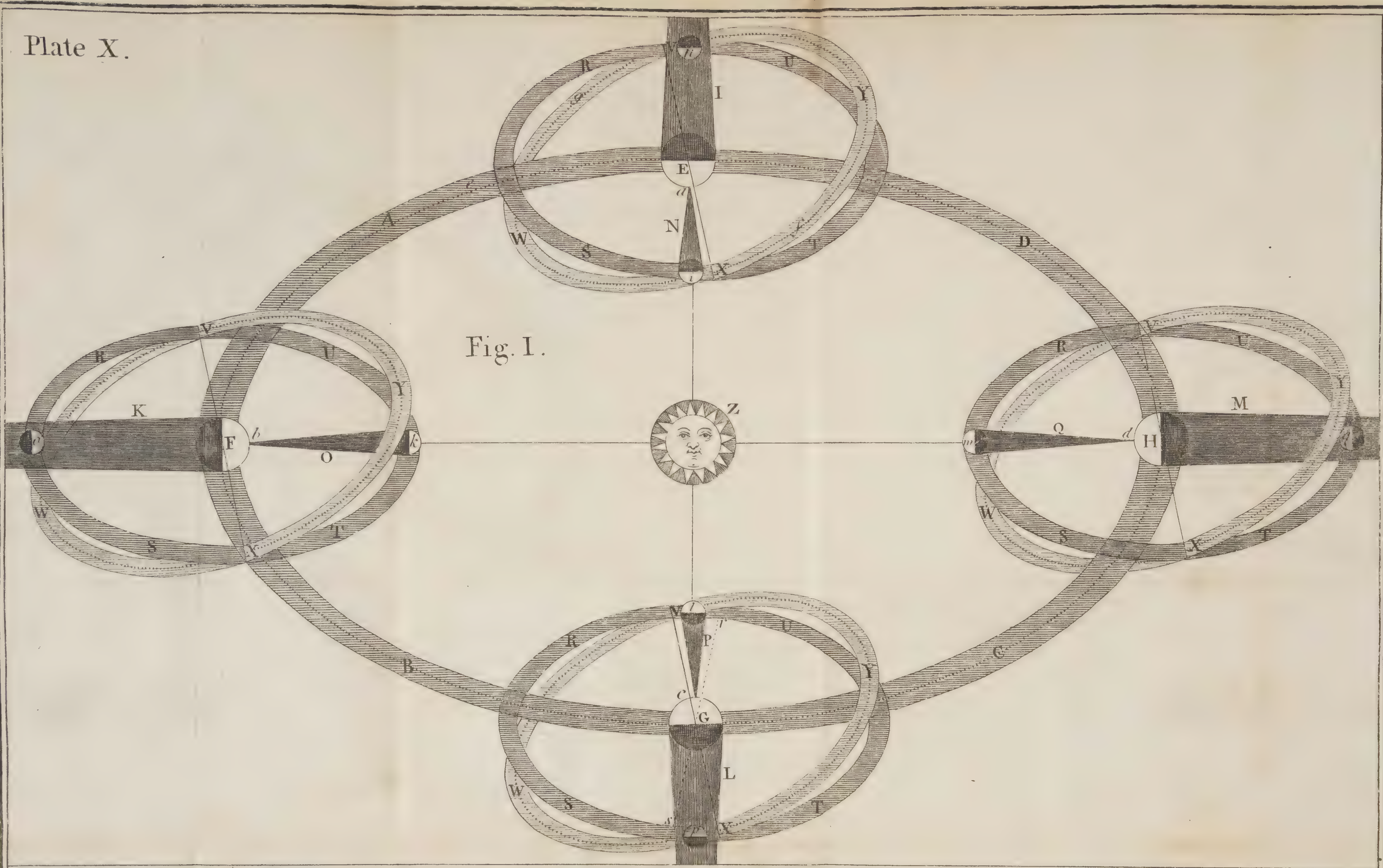

Fig. I.

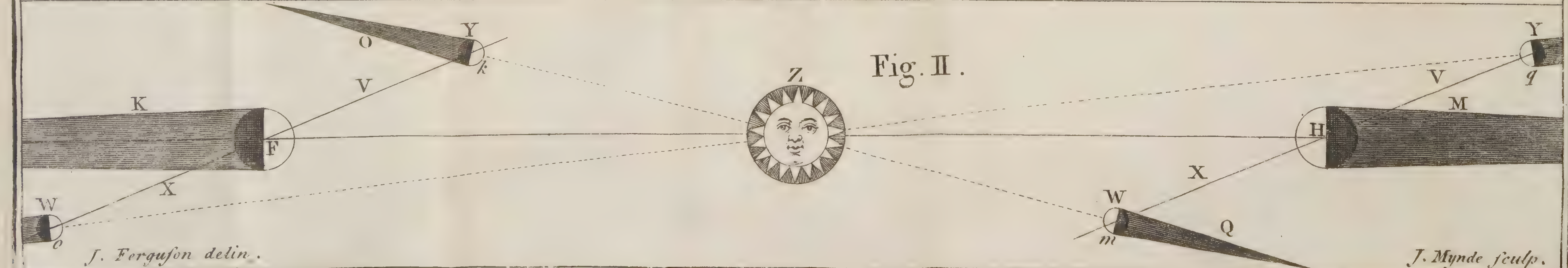

Fig. II.

J. Ferguson delin. J. Mynde ſculp.

we have ſo many New and Full Moons without Eclipſes. PLATE X.

To illuſtrate this, let *ABCD* be the *Ecliptic*, *RSTU* a Circle lying in the ſame Plane with the Ecliptic, and *VWXY* the *Moon's Orbit*, all thrown into an oblique view, which gives them an elliptical ſhape to the eye. One half of the Moon's Orbit, as *VWX*, is always below the Ecliptic, and the other half *XYV* above it. The points *V* and *X*, where the Moon's Orbit interſects the Circle *RSTU*, which lies even with the Ecliptic, are the *Moon's Nodes*; and a right line, as *XEV*, drawn from one to the other, through the Earth's center, is called the *Line of the Nodes*, which is carried almoſt parallel to itſelf round the Sun in a year. Fig. I. Line of the Nodes.

If the Moon moved round the Earth in the Orbit *RSTU*, which is coincident with the Plane of the Ecliptic, her ſhadow would fall upon the Earth every time ſhe is in conjunction with the Sun, and at every oppoſition ſhe would go through the Earth's ſhadow. Were this the caſe, the Sun would be eclipſed at every Change, and the Moon at every Full, as already mentioned.

But although the Moon's ſhadow *N* muſt fall upon the Earth at *a*, when the Earth is at *E*, and the Moon in conjunction with the Sun at *i*, becauſe ſhe is then very near one of her Nodes; and at her oppoſition *n* ſhe muſt go through the Earth's ſhadow *I*, becauſe ſhe is then near the other Node; yet, in the time that ſhe goes round the Earth to her next Change, according to the order of the letters *XYVW*, the Earth advances from *E* to *e*, according to the order of the letters *EFGH*, and the line of the Nodes *VEX* being carried nearly parallel to itſelf, brings the point *f* of the Moon's Orbit in conjunction with the Sun at that next Change; and then the Moon being at *f*, is too high above the Ecliptic to caſt her ſhadow on the Earth: and as the Earth is ſtill moving forward, the Moon at her next oppoſition will be at *g*, too

PLATE X. far below the Ecliptic to go through any part of the Earth's ſhadow; for by that time the point *g* will be at a conſiderable diſtance from the Earth as ſeen from the Sun.

When the Earth comes to *F*, the Moon in conjunction with the Sun *Z* is not at *k*, in a Plane coincident with the Ecliptic, but above it at *Y* in the higheſt part of her Orbit: and then the point *b* of her ſhadow *O* goes far above the Earth (as in Fig. II, which is an edge view of Fig. I.) The Moon at her next oppoſition is not at *o* (Fig. I.) but at *W*, where the Earth's ſhadow goes far above her (as in Fig. II.) In both theſe caſes the line of the Nodes *V F X* (Fig. I.) is about 90 degrees from the Sun, and both Luminaries are as far as poſſible from the limits of Eclipſes. Fig. I. and II.

When the Earth has gone half round the Ecliptic from *E* to *G*, the line of the Nodes *V G X* is nearly, if not exactly, directed towards the Sun at *Z*; and then the New Moon *l* caſts her ſhadow *P* on the Earth *G*; and the Full Moon *p* goes through the Earth's ſhadow *L*; which brings on Eclipſes again, as when the Earth was at *E*.

When the Earth comes to *H*, the New Moon falls not at *m* in a plane coincident with the Ecliptic *C D*, but at *W* in her Orbit below it: and then her ſhadow *Q* (ſee Fig. II.) goes far below the Earth. At the next Full ſhe is not at *q* (Fig. I.) but at *Y* in her Orbit $5\frac{1}{3}$ degrees above *q*, and at her greateſt height above the Ecliptic *C D*; being then as far as poſſible, at any oppoſition, from the Earth's ſhadow *M* (as in Fig. II.)

So, when the Earth is at *E* and *G*, the Moon is about her Nodes at New and Full; and in her greateſt *North* and *South Declination* (or Latitude as it is generally called) from the Ecliptic at her Quarters: but when the Earth is at *F* or *H*, the Moon is in her greateſt *North* and *South Declination* from the Ecliptic at New and Full, and in the *Nodes* about her Quarters.

PLATE X. The Moon's aſcending and deſcending Node.

Her North and South Latitude.

318. The point *X* where the Moon's Orbit croſſes the Ecliptic is called *the Aſcending Node*, becauſe the Moon aſcends from it above the Ecliptic: and the oppoſite point of interſection *V* is called *the Deſcending Node*, becauſe the Moon deſcends from it below the Ecliptic. When the Moon is at *Y* in the higheſt point of her Orbit, ſhe is in her greateſt *North Latitude*; and when ſhe is at *W* in the loweſt point of her Orbit, ſhe is in her greateſt *South Latitude.*

The Nodes have a retrograde motion.

Fig. I.

Which brings on the Eclipſes ſooner every year than they would be if the Nodes had not ſuch a motion.

319. If the line of the Nodes, like the Earth's Axis, was carried parallel to itſelf round the Sun, there would be juſt half a year between the conjunctions of the Sun and Nodes. But the Nodes ſhift backward, or contrary to the Earth's annual motion, $19\frac{1}{3}$ degrees every year; and therefore the ſame Node comes round to the Sun 19 days ſooner every year than on the year before. Conſequently, from the time that the aſcending Node *X* (when the Earth is at *E*) paſſes by the Sun as ſeen from the Earth, it is only 173 days (not half a year) till the deſcending Node *V* paſſes by him. Therefore, in whatever time of the year we have Eclipſes of the Luminaries about either Node, we may be ſure that in 173 days afterward we ſhall have Eclipſes about the other Node. And when at any time of the year the line of the Nodes is in the ſituation *V G X*, at the ſame time next year it will be in the ſituation *r G s*; the aſcending Node having gone backward, that is, contrary to the order of Signs, from *X* to *s*, and the deſcending Node from *V* to *r*; each $19\frac{1}{3}$ degrees. At this rate the Nodes ſhift through all the ſigns and degrees of the Ecliptic in 18 years and 225 days; in which time there would always be a regular period of Eclipſes, if any compleat number of Lunations were finiſhed without a fraction. But this never happens; for if both the Sun and Moon ſhould ſtart from a line of conjunction with either of the Nodes in any point of the Ecliptic, the Sun would

perform 18 annual revolutions and 222 degrees over and above, and the Moon 230 Lunations and 85 degrees of the 231ſt, by the time the Node came round to the ſame point of the Ecliptic again: ſo that the Sun would then be 138 degrees from the Node, and the Moon 85 degrees from the Sun.

A period of Eclipſes.

320. But, in 223 mean Lunations, after the Sun, Moon, and Nodes, have been once in a line of conjunction, they return ſo nearly to the ſame ſtate again, as that the ſame Node, which was in conjunction with the Sun and Moon at the beginning of the firſt of theſe Lunations, will be within 28′ 12″ of a degree of a line of conjunction with the Sun and Moon again, when the laſt of theſe Lunations is compleated. And therefore, in that time, there will be a regular period of Eclipſes, or return of the ſame Eclipſe, for many ages.—In this period (which was firſt diſcovered by the *Chaldeans)* there are 18 *Julian* years 11 days 7 hours 43 minutes 20 ſeconds, when the laſt day of *February* in Leap-years is four times included: but when it is five times included, the period conſiſts of only 18 years 10 days 7 hours 43 minutes 20 ſeconds. Conſequently, if to the mean time of any Eclipſe, either of the Sun or Moon, you add 18 *Julian* years 11 days 7 hours 43 minutes 20 ſeconds, when the laſt day of *February* in Leap-years comes in four times, or a day leſs when it comes in five times, you will have the mean time of the return of the ſame Eclipſe.

But the falling back of the line of conjunctions or oppoſitions of the Sun and Moon 28′ 12″ with reſpect to the line of the Nodes in every period, will wear it out in proceſs of time; and after that, it will not return again in leſs than 12492 years.—Theſe Eclipſes of the Sun, which happen about the Aſcending Node, and begin to come in at the North Pole of the Earth, will go a little ſoutherly at each return, till they go quite off the Earth at the South Pole; and thoſe which happen about the Deſcending Node, and begin to come in at the South Pole of the Earth, will go a little northerly at each return, till at laſt they quite leave the Earth at the North Pole.

To exemplify this matter, we ſhall firſt conſider the Sun's Eclipſe, *March* 21ſt Old Stile (*April* 1ſt New Stile) A. D. 1764, according to it's mean revolutions, without equating the times, or the Sun's diſtance from the Node; and then according to it's true equated times.

This Eclipſe fell in the open ſpace at each return, quite clear of the Earth, ever ſince the creation till A. D. 1295, *June* 13th Old Stile, at 12 h. 52 m. 59 ſec. *poſt meridiem*, when the Moon's ſhadow firſt touched the Earth at the North Pole; the Sun being then 17° 48′ 27″ from the Aſcending Node.—In each period ſince that time, the Sun has come 28′ 12″ nearer and nearer the ſame Node, and the Moon's ſhadow has therefore gone more and more ſoutherly.—In the year 1962, *July* 18th Old Stile, at 10 h. 36 m. 21 ſec. *p. m.* when the ſame Eclipſe will have returned 38 times, the Sun will be only 24′ 45″ from the Aſcending Node, and the center of the Moon's ſhadow will fall a little northward of the Earth's center.—At the end of the next following period, A. D. 1980, *July* 28th Old Stile, at 18 h. 19 m. 41 ſec. *p. m.* the Sun will have receded back 3′ 27″ from the Aſcending Node, and the Moon will have a very ſmall degree of ſouthern Latitude, which will cauſe the center of her ſhadow to paſs a very ſmall matter ſouth of the Earth's center.—After which, in every following period, the Sun will be 28′ 12″ farther back from the Aſcending Node than in the period laſt before; and the Moon's ſhadow will go ſtill farther and farther ſouthward, until *September* 12th Old Stile, at 23 h. 46 m. 22 ſec. *p. m.* A. D. 2665; when the Eclipſe will have compleated it's 77th periodical return, and will go quite off the Earth at the South Pole (the Sun being then 17° 55′ 22″ back from the Node) and it cannot come in at the North Pole, ſo as to begin the ſame Courſe over again, in leſs then 12492 years afterward.—And ſuch will be the caſe of every other Eclipſe of the Sun: for, as there is about 18 degrees on each ſide of the Node within which there is a poſſibility of Eclipſes, their whole revolution goes through 36 degrees about that Node, which taken from 360 degrees, leaves remaining 324 degrees for the Eclipſes to travel *in expanſum.* And as this 36 degrees is not gone through in leſs than 77 periods, which takes up 1388 years, the remaining 324 degrees cannot be ſo gone through in leſs than 12492 years. For, as 36 is to 1388, ſo is 324 to 12492.

321. In order to ſhew both the mean and true times of the returns of this Eclipſe, through all it's periods, together with the mean Anomalies of the Sun and Moon, at each return, and the mean and true diſtances of the Sun from the Moon's Aſcending Node, and the Moon's true Latitude at the true time of each New Moon, I have calculated the following Tables for the ſake of thoſe who may chooſe to project this Eclipſe at any of it's returns, according to the rules laid down in the 15th Chapter; and have thereby taken by much the greateſt part of the trouble off their hands.—All the times are according to the Old Stile, for the ſake of a regularity which, with reſpect to the nominal days of the Months, does not take place in the New: but by adding the days difference of Stiles, they are reduced to the times which agree with the New Stile.

According to the mean (or ſuppoſed equable) motions of the Sun, Moon, and Nodes, the Moon's ſhadow in this Eclipſe would have firſt touched the Earth at the North Pole, on the 13th of *June*, A. D. 1295, at 12 h. 52 m. 59 ſec. paſt Noon on the meridian of *London*; and would quite leave the

Earth at the South Pole, on the 12th of *September*, A. D. 2665, at 23 h. 46 m. 22 ſec. paſt Noon, at the completion of it's 77th period; as ſhewn by the firſt and ſecond Tables.

But, on account of the true (or unequable) motions of the Sun, Moon, and Nodes, the firſt coming-in of this Eclipſe, at the North Pole of the Earth, was on the 24th of *June*, A. D. 1313, at 3 h. 57 m. 3 ſec. paſt Noon; and it will finally leave the Earth at the South Pole, on the 31ſt of *July*, A. D. 2593, at 10 h. 25 m. 31 ſec. paſt Noon, at the completion of it's 72d period; as ſhewn by the third and fourth Tables.—So that, the true motions do not only alter the true times from the mean, but they alſo cut off five periods from thoſe of the mean returns of this Eclipſe.

TABLE I. *The mean Time of New Moon, with the mean Anomalies of the Sun and Moon, and the Sun's mean Diſtance from the Moon's Aſcending Node, at the mean Time of each periodical Return of the Sun's Eclipſe,* March *21ſt,* 1764, *from it's firſt coming upon the Earth ſince the Creation, till it falls right againſt the Earth's center, according to the Old Stile.*

Periodical Returns.	Years of Chriſt.	Mean Time of New Moon.					Sun's mean Anomaly.				Moon's mean Anomaly.				Sun's mean Diſt. from the Node.			
		Month.	D.	H.	M.	S.	s	°	′	″	s	°	′	″	s	°	′	″
0	1277	June	2	5	9	39	11	17	57	41	1	26	31	42	0	18	16	40
1	1295	June	13	12	52	59	1	28	27	38	1	23	40	19	0	17	48	27
2	1313	June	23	20	35	19	0	8	57	35	1	20	48	56	0	17	20	15
3	1331	July	5	4	19	39	0	19	27	32	1	17	57	33	0	16	52	2
4	1349	July	15	12	2	59	0	29	57	29	1	15	6	10	0	16	23	50
5	1367	July	25	19	46	19	1	10	27	2	1	12	14	47	0	15	55	37
6	1385	Aug.	6	3	29	39	1	20	57	23	1	9	23	24	0	15	27	25
7	1403	Aug.	17	11	12	59	2	1	27	20	1	6	32	1	0	14	59	12
8	1421	Aug.	27	18	56	19	2	11	57	17	1	3	40	38	0	14	31	0
9	1439	Sept.	8	2	39	39	2	22	27	14	1	0	49	15	0	14	2	47
10	1457	Sept.	18	10	2	59	3	2	57	11	0	27	57	52	0	13	34	35
11	1475	Sept.	29	18	6	19	3	13	27	8	0	25	6	29	0	13	6	22
12	1493	Oct.	10	1	49	39	3	23	57	5	0	22	15	6	0	12	38	10
13	1511	Oct.	21	9	32	59	4	4	27	2	0	19	23	43	0	12	9	57
14	1529	Oct.	31	17	16	19	4	14	56	59	0	16	32	20	0	11	41	45
15	1547	Nov.	12	0	59	40	4	25	26	56	0	13	40	57	0	11	13	32
16.	1565	Nov.	22	8	43	0	5	5	56	53	0	10	49	34	0	10	45	20
17	1583	Dec.	3	16	26	20	5	16	26	50	0	7	58	9	0	10	17	7
18	1601	Dec.	14	0	9	40	5	26	56	47	0	5	6	48	0	9	48	55
19	1619	Dec.	25	7	53	0	6	7	26	44	0	2	15	25	0	9	20	42
20	1638	Jan.	4	15	36	20	6	17	56	41	11	29	24	2	0	8	52	30
21	1656	Jan.	15	23	19	40	6	28	26	38	11	26	32	39	0	8	24	17
22	1674	Jan.	26	7	3	0	7	8	56	35	11	23	41	16	0	7	56	5
23	1692	Feb.	6	14	46	20	7	19	26	32	11	20	49	53	0	7	27	52
24	1710	Feb.	16	22	29	40	7	29	56	29	11	17	58	30	0	6	59	40
25	1728	Feb.	28	6	13	0	8	10	26	26	11	15	7	7	0	6	31	27
26	1746	Mar.	10	13	56	20	8	20	56	23	11	12	15	44	0	6	3	15
27	1764	Mar.	20	21	39	40	9	1	26	20	11	9	24	21	0	5	35	2
28	1782	April	1	5	23	0	9	11	56	17	11	6	32	58	0	5	6	50
29	1800	April	11	13	6	20	9	22	26	14	11	3	41	35	0	4	38	37
30	1818	April	22	20	49	40	10	2	56	11	11	0	50	12	0	4	10	25
31	1836	May	3	4	33	0	10	13	26	8	10	27	58	49	0	3	42	12
32	1854	May	14	12	16	20	10	23	56	5	10	25	7	26	0	3	14	0
33	1872	May	24	19	59	40	11	4	26	2	10	22	16	3	0	2	45	47
34	1890	June	5	3	43	0	11	14	55	59	10	19	24	40	0	2	17	35
35	1908	June	15	11	26	20	11	25	25	56	10	16	33	17	0	1	49	22
36	1926	June	26	19	9	40	0	5	55	53	10	13	41	54	0	1	21	10
37	1944	July	7	2	53	0	0	16	25	50	10	10	50	31	0	0	52	57
38	[illegible]	July	18	10	36	21	0	26	55	47	10	7	59	8	0	0	24	45

TABLE II. *The mean Time of New Moon, with the mean Anomalies of the Sun and Moon, and the Sun's mean Diſtance from the Moon's Aſcending Node, at the mean Time of each periodical Return of the Sun's Eclipſe,* March 21*ſt*, 1764, *from the mean Time of it's falling right againſt the Earth's center, till it finally leaves the Earth, according to the Julian or Old Stile.*

Periodical Returns.	Years of Chriſt.	Mean Time of New Moon.					Sun's mean Anomaly.				Moon's mean Anomaly.				Sun's mean Diſt. from the Node.			
		Month.	D.	H.	M.	S.	s	°	′	″	s	°	′	″	s	°	′	″
39	1980	July	28	18	19	41	1	7	25	44	10	5	7	45	11	29	56	33
40	1998	Aug.	9	2	3	1	1	17	55	41	10	2	16	22	11	29	28	20
41	2016	Aug.	19	9	46	21	1	28	25	38	9	29	24	59	11	29	0	8
42	2034	Aug.	30	17	29	41	2	8	55	36	9	26	33	36	11	28	31	55
43	2052	Sept.	10	1	13	1	2	19	25	33	9	23	42	13	11	28	3	43
44	2070	Sept.	21	8	56	21	2	29	55	32	9	20	50	50	11	27	35	30
45	2088	Oct.	1	16	39	41	3	10	25	27	9	17	59	27	11	27	7	18
46	2106	Oct.	13	0	23	1	3	20	55	24	9	15	8	4	11	26	39	5
47	2124	Oct.	23	8	6	21	4	1	25	21	9	12	16	41	11	26	10	53
48	2142	Nov.	3	15	49	41	4	11	55	18	9	9	25	18	11	25	42	40
49	2160	Nov.	13	23	31	1	4	22	25	15	9	6	33	56	11	25	14	28
50	2178	Nov.	25	7	16	21	5	2	55	12	9	3	42	33	11	24	46	15
51	2196	Dec.	5	14	59	41	5	13	25	9	9	0	51	10	11	24	18	3
52	2214	Dec.	16	22	43	1	5	23	55	7	8	27	59	47	11	23	49	50
53	2232	Dec.	27	6	26	21	6	4	25	4	8	25	8	24	11	23	21	38
54	2251	Jan.	7	14	9	41	6	14	55	1	8	22	17	1	11	22	53	25
55	2269	Jan.	17	21	53	1	6	25	24	58	8	19	25	38	11	22	15	13
56	2287	Jan.	29	5	36	21	7	5	54	55	8	16	31	15	11	21	57	0
57	2305	Feb.	8	13	19	41	7	16	24	52	8	13	42	52	11	21	28	48
58	2323	Feb.	19	21	3	1	7	26	54	49	8	10	51	29	11	21	0	35
59	2341	Mar.	2	4	46	21	8	7	24	46	8	8	0	6	11	20	32	23
60	2359	Mar.	13	12	29	42	8	17	54	43	8	5	8	43	11	20	4	10
61	2377	Mar.	23	20	13	2	8	28	24	40	8	2	17	20	11	19	35	58
62	2395	Apr.	4	3	56	22	9	8	54	37	7	29	25	57	11	19	7	45
63	2413	Apr.	14	11	39	42	9	19	24	34	7	26	34	34	11	18	39	33
64	2431	Apr.	25	19	23	2	9	29	54	31	7	23	43	11	11	18	11	20
65	2449	May	6	3	6	22	10	10	24	28	7	20	51	48	11	17	43	8
66	2467	May	17	10	49	42	10	20	54	25	7	18	0	25	11	17	14	54
67	2485	May	27	18	33	2	11	1	24	22	7	15	9	2	11	16	46	43
68	2503	June	8	2	16	22	11	11	54	19	7	12	17	39	11	16	18	31
69	2521	June	18	9	59	42	11	22	24	16	7	9	26	16	11	15	50	18
70	2539	June	29	17	43	2	0	2	54	14	7	6	34	53	11	15	22	6
71	2557	July	10	1	26	22	0	13	24	11	7	3	43	30	11	14	53	54
72	2575	July	21	9	9	42	0	23	54	8	7	0	52	7	11	14	25	41
73	2593	July	31	16	53	2	1	4	24	5	6	28	0	44	11	13	57	28
74	2611	Aug.	12	0	36	22	1	14	54	2	6	25	9	21	11	13	29	16
75	2629	Aug.	22	8	19	42	1	25	23	59	6	22	17	58	11	13	1	3
76	2647	Sept.	2	15	3	2	2	5	53	56	6	19	26	35	11	12	32	51
77	2665	Sept.	12	23	46	22	2	16	23	53	6	16	35	12	11	12	4	38

TABLE III. *The true Time of New Moon, with the Sun's true Diſtance from the Moon's Aſcending Node, and the Moon's true Latitude, at the true Time of each periodical Return of the Sun's Eclipſe, March 21ſt, Old Stile, A. D. 17[illegible], from the Time of it's firſt coming upon the Earth ſince the Creation till it falls right againſt the Earth's center.*

Periodical Returns.	Years of Chriſt.	True Time of New Moon					Sun's true Diſtance from the Node.				Moon's true Latitude, North.			
		Month.	D	H.	M.	S.	s	°	′	″	°	′	″	Nor.
	1295	June	13	21	54	32	0	18	40	54	1	33	45	N. A.
1	1313	June	24	3	57	3	0	17	20	22	1	29	34	N. A.
2	1331	July	5	10	42	8	0	16	29	35	1	25	20	N. A.
3	1349	July	15	17	14	15	0	15	34	18	1	20	45	N. A.
4	1367	July	26	23	9	21	0	14	46	8	1	16	39	N. A.
5	1385	Aug.	6	6	41	17	0	13	59	43	1	12	43	N. A.
6	1403	Aug	17	13	32	19	0	13	16	44	1	9	3	N. A.
7	1421	Aug	27	20	30	17	0	12	37	4	1	5	42	N. A.
8	143[illegible]	Sept.	8	3	51	46	0	12	1	54	1	2	41	N. A.
9	1457	Sept	18	10	23	11	0	11	30	27	0	58	53	N. A
10	1475	Sept.	29	17	57	7	0	11	3	56	0	57	43	N. A.
11	1493	Oct.	10	1	44	3	0	10	41	55	0	55	49	N. A.
12	1511	Oct.	21	9	29	53	0	10	25	11	0	54	28	N. A.
13	1[illegible]29	Oct.	31	17	9	18	0	10	11	27	0	53	12	N. A.
14	1547	Nov.	12	0	51	25	0	10	1	10	0	52	19	N. A.
15	1565	Nov.	22	8	54	5[illegible]	0	9	52	49	0	51	46	N. A.
16	1583	Dec.	3	16	46	1[illegible]	0	9	48	4	0	51	11	N. A.
17	1601	Dec	14	0	51	[illegible]	0	9	43	42	0	50	49	N A.
[illegible]	1619	Dec.	25	8	5[illegible]	59	0	9	40	23	0	50	31	N. A.
[illegible]9	1637	Jan.	4	1[illegible]	5[illegible]	1	0	9	34	57	0	50	3	N. A.
[illegible]	16[illegible]	Jan.	16	0	54	41	0	9	29	24	0	49	57	N. A.
[illegible]	1673	Jan.	2[illegible]	8	48	24	0	9	19	44	0	48	44	N. A.
22	1692	Feb.	6	16	36	23	0	9	8	58	0	47	49	N. A.
23	1710	Feb.	17	0	8	37	0	8	54	20	0	46	44	N. A.
[illegible]4	[illegible]2	Feb.	28	7	43	40	0	8	34	53	0	44	52	N. A.
25	1[illegible]	Mar.	10	15	14	33	0	8	10	38	0	42	46	N. A
[illegible]	17[illegible]	Mar.	2[illegible]	22	30	2[illegible]	0	7	42	14	0	40	18	N. A.
[illegible]	1782	Apr.	1	5	37	[illegible]	0	7	9	27	0	37	28	N. A.
28	180[illegible]	Apr.	11	12	36	[illegible]	0	6	35	30	0	34	31	N. A.
29	1818	Apr.	22	19	27	34	0	5	51	48	0	30	43	N. A.
30	1836	May	3	2	12	7	0	5	5	5	0	26	40	N. A.
31	1854	May	14	8	50	4	0	4	19	45	0	22	42	N. A.
[illegible]2	1872	May	24	15	28	1[illegible]	0	3	26	3	0	18	1	N. A.
33	1890	June	[illegible]	22	8	[illegible]	0	2	35	5	0	13	34	N. A.
[illegible]	19[illegible]	June	15	4	38	23	0	1	41	43	0	8	54	N. A.
	19[illegible]6	June	26	11	13	[illegible]	0	0	47	28	0	4	10	N. A.

On account of the differences between the mean and true New Moons, and between the Sun's mean and true Diſtances from the Node, the Moon's ſhadow falls even with the Earth's center two periods ſooner in this Table than in the firſt.

TABLE IV. *The true Time of New Moon, with the Sun's true Diſtanc from the Moon's Aſcending Node, and the Moon's true Latitude, at each periodical Return of the Sun's Eclipſe,* March 21*ſt*, Old Stile, A. D. 1764, *from it's falling right againſt the Earth's center, till it finally leaves the Earth.*

Periodical Returns.	Years of Chriſt.	True Time of New Moon.					Sun's true Diſtance from the Node.				Moon's true Latitude, South.			
		Month.	D.	H.	M.	S.	s	o	′	″	o	′	″	South
36	1944	July	6	17	50	35	11	29	55	28	0	0	24	S. A.
37	1962	July	18	0	31	38	11	29	2	35	0	5	2	S. A.
38	1980	July	28	7	1[illegible]	53	11	28	11	32	0	9	29	S. A.
39	1998	Aug.	8	14	12	22	11	27	26	41	0	13	25	S. A.
40	2016	Aug.	18	21	14	53	11	26	42	16	0	17	18	S. A.
41	2034	Aug.	30	4	25	45	11	26	2	0	0	20	48	S. A.
42	2052	Sept.	9	11	45	17	11	25	25	46	0	23	53	S. A.
43	2070	Sept.	20	19	17	26	11	24	55	4	0	26	39	S. A.
44	2088	Oct.	1	2	57	8	11	24	27	43	0	28	58	S. A.
45	2106	Oct.	12	10	47	39	11	24	4	38	0	31	2	S. A.
46	2124	Oct.	22	18	37	40	11	23	48	28	0	32	20	S. A.
47	2142	Nov.	3	2	56	19	11	23	35	11	0	33	53	S. A.
48	2160	Nov.	13	11	11	20	11	23	22	22	0	34	42	S. A.
49	2178	Nov.	24	19	30	14	11	23	18	57	0	35	0	S. A.
50	2196	Dec	5	4	4	9	11	23	14	40	0	35	22	S. A.
51	2214	Dec.	16	12	35	48	11	23	10	43	0	35	43	S. A.
52	2232	Dec.	26	20	29	9	11	23	6	47	0	36	1	S. A.
53	2251	Jan.	7	5	42	9	11	23	4	27	0	36	16	S. A.
54	2269	Jan.	17	14	14	8	11	23	0	41	0	36	35	S. A.
55	2287	Jan.	28	22	43	34	11	22	53	58	0	37	10	S. A.
56	2305	Feb.	8	7	8	30	11	22	44	44	0	37	59	S. A.
57	2323	Feb.	19	15	7	10	11	22	31	1	0	39	8	S. A.
58	2341	Mar.	2	0	6	5	11	22	17	46	0	40	28	S. A.
59	2359	Mar.	13	7	59	17	11	21	55	29	0	42	9	S. A.
60	2377	Mar.	23	15	51	59	11	21	39	40	0	43	41	S. A.
61	2395	Apr.	3	23	45	7	11	21	0	53	0	46	58	S. A.
62	2413	Apr.	14	7	32	40	11	20	26	22	0	49	48	S. A.
63	2431	Apr.	25	15	12	5[illegible]	11	19	47	34	0	53	17	S A
64	2449	May	5	22	45	14	11	19	6	22	0	56	50	S. A.
65	2467	May	17	6	17	30	11	18	21	16	1	0	40	S A.
66	2485	May	27	13	40	2[illegible]	11	7	34	20	1	4	42	S. A.
67	2503	June	7	21	10	31	11	16	43	17	1	9	3	S. A.
68	2521	June	18	4	24	42	11	15	51	48	1	13	26	S. A.
69	2539	June	29	11	58	46	11	15	1	12	1	17	43	S. A.
70	2557	July	9	19	24	7	11	14	9	13	1	22	0	S. A.
71	2575	July	21	2	52	34	11	13	19	22	1	26	16	S. A.
72	2593	July	31	10	25	31	11	12	13	43	1	31	44	S. A.
0	2611	Aug.	11	17	58	39	11	11	45	13	1	36	13	S. A.

By the true Motions of the Sun, Moon, and Nodes, this Eclipſe goes off the Earth four Periods ſooner than it would have done by mean equable Motions.

From Mr. G. SMITH's diſſertation on Eclipſes, printed at *London*, by E. CAVE, in the year 1748.

“ To illuſtrate this a little farther, we ſhall exa-
“ mine ſome of the moſt remarkable circumſtances
“ of the returns of the Eclipſe which happened
“ *July* 14, 1748, about noon. This Eclipſe, after
“ traverſing the voids of ſpace from the Creation,
“ at laſt began to enter the *Terra Auſtralis Incog-*
“ *nita*, about 88 years after the Conqueſt, which
“ was the laſt of King STEPHEN's reign; every
“ * *Chaldean* period it has crept more northerly,
“ but was ſtill inviſible in *Britain* before the year
“ 1622; when on the 30th of *April* it began to
“ touch the ſouth parts of *England* about 2 in the
“ afternoon; it's central appearance riſing in the
“ *American* South Seas, and traverſing *Peru* and
“ the *Amazon*'s country, through the *Atlantic* ocean
“ into *Africa*, and ſetting in the *Æthiopian* conti-
“ nent, not far from the beginning of the Red Sea.

“ It's next viſible period was after three *Chaldean*
“ revolutions in 1676, on the firſt of *June*, riſing
“ central in the *Atlantic* ocean, paſſing us about
“ 9 in the morning, with four † Digits eclipſed on
“ the under limb; and ſetting in the gulph of
“ *Cochinchina* in the *Eaſt-Indies*.

“ It being now near the Solſtice, this Eclipſe
“ was viſible the very next return in 1694, in the
“ evening; and in two periods more, which was
“ in 1730, on the 4th of *July*, was ſeen above half
“ eclipſed juſt after Sun-riſe, and obſerved both
“ at *Wirtemberg* in *Germany*, and *Pekin* in *China*,
“ ſoon after which it went off.

“ Eighteen years more afforded us the Eclipſe
“ which fell on the 14th of *July* 1748.

“ The next viſible return will happen on *July*
“ 25, 1766, in the evening, about four Digits
“ eclipſed; and after two periods more, on *Auguſt*

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* The above period of 18 years 11 days 7 hours 43 minutes 20 ſeconds, which was found out by the *Chaldeans*, and by them called *Saros*.

† A Digit is a twelfth part of the diameter of the Sun or Moon.

“ 16th, 1802, early in the morning, about five
“ Digits, the center coming from the north frozen
“ continent, by the capes of *Norway*, through
“ *Tartary*, *China*, and *Japan*, to the *Ladrone* iſlands,
“ where it goes off.

“ Again, in 1820, *Auguſt* 26, betwixt one and
“ two, there will be another great Eclipſe at *London*,
“ about 10 Digits; but happening ſo near the
“ Equinox, the center will leave every part of
“ *Britain* to the Weſt, and enter *Germany* at *Embden*,
“ paſſing by *Venice*, *Naples*, *Grand Cairo*, and
“ ſet in the gulf of *Baſſora* near that city.

“ It will be no more viſible till 1874, when five
“ Digits will be obſcured (the center being now
“ about to leave the Earth) on *September* 28. In
“ 1892 the Sun will go down eclipſed at *London*,
“ and again in 1928 the paſſage of the center will
“ be in the *expanſum*, though there will be two
“ Digits eclipſed at *London*, *October* the 31ſt of
“ that year; and about the year 2090 the whole
“ Penumbra will be wore off; whence no more
“ returns of this Eclipſe can happen till after a revolution
“ of 10 thouſand years.

“ From theſe remarks on the intire revolution
“ of this Eclipſe, we may gather, that a thouſand
“ years, more or leſs (for there are ſome irregularities
“ that may protract or lengthen this period
“ 100 years) complete the whole terreſtrial Phenomena
“ of any ſingle Eclipſe: and ſince 20 periods
“ of 54 years each, and about 33 days, comprehend
“ the intire extent of their revolution, it
“ is evident that the times of the returns will paſs
“ through a circuit of one year and ten Months,
“ every *Chaldean* period being ten or eleven days
“ later, and of the equable appearances about 32
“ or 33 days. Thus, though this Eclipſe happens
“ about the middle of *July*, no other ſubſequent
“ Eclipſe of this period will return to the middle
“ of the ſame month again; but wear conſtantly
“ each period 10 or 11 days forward; and at laſt

"appear in Winter, but then it begins to ceaſe from "affecting us.

"Another concluſion from this revolution may "be drawn, that there will ſeldom be any more "than two great Eclipſes of the Sun in the interval "of this period, and theſe follow ſometimes next "return, and often at greater diſtances. That of "1715 returned again in 1733 very great; but "this preſent Eclipſe will not be great till the "arrival of 1820, which is a revolution of four "*Chaldean* periods: ſo that the irregularities of "their circuits muſt undergo new computations to "aſſign them exactly.

"Nor do all Eclipſes come in at the ſouth Pole: "*that* depends altogether on the poſition of the "lunar Nodes, which will bring in as many from "the *expanſum* one way as the other; and ſuch "Eclipſes will wear more ſoutherly by degrees, "contrary to what happens in the preſent caſe.

"The Eclipſe, for example, of 1736, in *Sep-* "*tember*, had it's center in the *expanſum*, and ſet "about the middle of it's obſcurity in *Britain*; it "will wear in at the north Pole, and in the year "2600, or thereabouts, go off in the *expanſum* on "the ſouth ſide of the Earth.

"The Eclipſes therefore which happened about "the Creation are little more than half way yet "of their ethereal circuit; and will be 4000 years "before they enter the Earth any more. This "grand revolution ſeems to have been entirely "unknown to the antients.

Why our preſent Tables agree not with antient obſervations.

322. "It is particularly to be noted, that Eclipſes "which have happened many centuries ago, will "not be found by our preſent Tables to agree ex- "actly with antient obſervations, by reaſon of the "great Anomalies in the lunar motions; which "appears an inconteſtable demonſtration of the "non-eternity of the Univerſe. For it ſeems con- "firmed by undeniable proofs, that the Moon now "finiſhes her period in leſs time than formerly,

“and will continue by the centripetal law to approach nearer and nearer the Earth, and to go ſooner and ſooner round it: nor will the centrifugal power be ſufficient to compenſate the different gravitations of ſuch an aſſemblage of bodies as conſtitute the ſolar ſyſtem, which would come to ruin of itſelf, without ſome new regulation and adjuſtment of their original motions*.

THALES's Eclipſe.

323. “We are credibly informed from the teſtimony of the antients, that there was a total Eclipſe of the Sun predicted by THALES to happen in the fourth year of the 48th † *Olympiad*,

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* There are two antient Eclipſes of the Moon, recorded by *Ptolemy* from *Hipparchus*, which afford an undeniable proof of the Moon's acceleration. The firſt of theſe was obſerved at *Babylon*, *December* the 22d, in the year before CHRIST 383: when the Moon began to be eclipſed about half an hour before the Sun roſe, and the Eclipſe was not over before the Moon ſet: but by moſt of our Aſtronomical Tables, the Moon was ſet at *Babylon* half an hour before the Eclipſe began; in which caſe, there could have been no poſſibility of obſerving it. The ſecond Eclipſe was obſerved at *Alexandria*, *September* the 22d, the year before CHRIST 201; where the Moon roſe ſo much eclipſed, that the Eclipſe muſt have begun about half an hour before ſhe roſe: whereas, by moſt of our Tables, the beginning of this Eclipſe was not till about 10 minutes after the Moon roſe at *Alexandria*. Had theſe Eclipſes began and ended while the Sun was below the Horizon, we might have imagined, that as the antients had no certain way of meaſuring time, they might have been ſo far miſtaken in the hours, that we could not have laid any ſtreſs on the accounts given by them. But, as in the firſt Eclipſe the Moon was ſet, and conſequently the Sun riſen, before it was over; and in the ſecond Eclipſe the Sun was ſet and the Moon not riſen, till ſome time after it began; theſe are ſuch circumſtances as the obſervers could not poſſibly be miſtaken in Mr. *Struyk*, in the following Catalogue, notwithſtanding the expreſs words of *Ptolemy*, puts down theſe two Eclipſes as obſerved at *Athens*; where they might have been ſeen as above, without any acceleration of the Moon's motion: *Athens* being 20 degrees Weſt of *Babylon*, and 7 degrees Weſt of *Alexandria*.

† Each *Olympiad* began at the time of Full Moon next after the Summer Solſtice, and laſted four years, which were of unequal lengths, becauſe the time of Full Moon differs 11 days every year: ſo that they might ſometimes begin on the next day

“ either at *Sardis* or *Miletus* in *Aſia*, where THALES
“ then reſided. That year correſponds to the
“ 585th year before CHRIST; when accordingly
“ there happened a very ſignal eclipſe of the Sun,
“ on the 28th of *May*, anſwering to the preſent
“ 10th of that month*, central through *North*
“ *America*, the ſouth parts of *France*, *Italy*, &c. as
“ far as *Athens*, or the Iſles in the *Ægean* Sea;
“ which is the fartheſt that even the *Caroline* Tables
“ carry it; and conſequently make it inviſible to
“ any part of *Aſia*, in the total character; though
“ I have good reaſons to believe that it extended
“ to *Babylon*, and went down central over that city.
“ We are not however to imagine, that it was ſet

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day after the Solſtice, and at other times not till four weeks after it. The firſt *Olympiad* began in the year of the Julian Period 3938, which was 776 years before the firſt year of CHRIST, or 775 before the year of his birth; and the laſt *Olympiad*, which was the 293d, began *A. D.* 393. At the expiration of each *Olympiad*, the *Olympic Games* were celebrated in the *Elean* fields, near the river *Alpheus* in the *Peloponneſus* (now *Morea*) in honour of JUPITER OLYMPUS. See STRAUCHIUS's *Breviarium Chronologium*, p. 247—251.

* The reader may probably find it difficult to underſtand why Mr. SMITH ſhould reckon this Eclipſe to have been in the 4th year of the 48th *Olympiad*, as it was only in the end of the third year: and alſo why the 28th of *May*, in the 585th year before CHRIST, ſhould anſwer to the preſent 10th of that Month. But we hope the following explanation will remove theſe difficulties.

The month of *May* (when the Sun was eclipſed) in the 585th year before the firſt year of CHRIST, which was a leap-year, fell in the latter end of the third year of the 48th *Olympiad*; and the fourth year of that *Olympiad* began at the Summer Solſtice following: but perhaps Mr. SMITH begins the years of the *Olympiad* from *January*, in order to make them correſpond more readily with *Julian* years; and ſo reckons the month of *May*, when the Eclipſe happened, to be in the fourth year of that *Olympiad*.

The Place or Longitude of the Sun at that time was ♉ 29° 43′ 17″, to which ſame place the Sun returned (after 2300 years, *viz.*) *A. D.* 1716, on *May*, 9^{d} 5^{h} 6^{m} after noon: ſo that, with reſpect to the Sun's place, the 9th of *May*, 1716, anſwers to the 28th of *May* in the 58 th year before the firſt year of CHRIST; that is, the Sun had the ſame Longitude on both thoſe days.

"before it paſt *Sardis* and the *Aſiatic* towns, "where the predictor lived; becauſe an inviſible "Eclipſe could have been of no ſervice to demonſtrate his ability in Aſtronomical Sciences to his "countrymen, as it could give no proof of it's "reality.

324. "For a farther illuſtration, THUCYDIDES "relates, that a ſolar Eclipſe happened on a Summer's day in the afternoon, in the firſt year of "the *Peloponneſian* war, ſo great, that the Stars appeared. RHODIUS was victor in the *Olympic* "games the fourth year of the ſaid war, being alſo "the fourth of the 87th *Olympiad*, on the 428th "year before CHRIST. So that the Eclipſe muſt "have happened in the 431ſt year before CHRIST; "and by computation it appears, that on the 3d "of *Auguſt* there was a ſignal Eclipſe which would "have paſt over *Athens*, central about 6 in the "evening, but which our preſent Tables bring no "farther than the antient *Syrtes* on the *African* "coaſt, above 400 miles from *Athens*; which "ſuffering in that caſe but 9 Digits, could by no "means exhibit the remarkable darkneſs recited "by this hiſtorian; the center therefore ſeems to "have paſt *Athens* about 6 in the evening, and "probably might go down about *Jeruſalem*, or "near it, contrary to the conſtruction of the preſent Tables. I have only obviated theſe things "by way of caution to the preſent Aſtronomers, "in re-computing antient Eclipſes; and refer them "to examine the Eclipſe of *Nicias*, ſo fatal to the "*Athenian* fleet*; that which overthrew the *Macedonian* Army†, *&c.*" So far Mr. SMITH.

THUCYDIDES's Eclipſe.

325. In any year, the number of Eclipſes of both Luminaries cannot be leſs than two, nor more than ſeven; the moſt uſual number is four, and it is very rare to have more than ſix. For the Sun paſſes by both the Nodes but once a year, unleſs he

The number of Eclipſes.

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* Before CHRIST 413, *Auguſt* 27.

† Before CHRIST 168, *June* 21.

he paſſes by one of them in the beginning of the year; and if he does, he will paſs by the ſame Node again a little before the year be finiſhed; becauſe, as theſe points move $19\frac{1}{3}$ degrees backward every year, the Sun will come to either of them 173 days after the other, § 319. And when either Node is within 17 degrees of the Sun at the time of New Moon, the Sun will be eclipſed. At the ſubſequent oppoſition, the Moon will be eclipſed in the other Node; and come round to the next conjunction again ere the former Node be 17 degrees paſt the Sun, and will therefore eclipſe him again. When three Eclipſes fall about either Node, the like number generally falls about the oppoſite; as the Sun comes to it in 173 days afterwards: and ſix Lunations contain but four days more. Thus, there may be two Eclipſes of the Sun and one of the Moon about each of her Nodes. But when the Moon changes in either of the Nodes, ſhe cannot be near enough the other Node at the next Full to be eclipſed; and in ſix lunar months afterward ſhe will change near the other Node: in theſe caſes there can be but two Eclipſes in a year, and they are both of the Sun.

326. A longer period than the above-mentioned, § 320, for comparing and examining Eclipſes which happen at long intervals of time, is 557 years 21 days 18 hours 30 minutes 11 ſeconds; in which time there are 6890 mean Lunations; and the Sun and Node meet again ſo nearly as to be but 11 ſeconds diſtant: but then it is not the ſame Eclipſe that returns, as in the ſhorter period above-mentioned.

327. We ſhall ſubjoin a Catalogue of Eclipſes recorded in hiſtory, from 721 years before CHRIST to *A. D.* 1485; of computed Eclipſes from 1485 to 1700; and of all the Eclipſes viſible in *Europe* from 1700 to 1800. From the beginning of the Catalogue to *A D.* 1485 the Eclipſes are taken from STRUYK's *Introduction to univerſal Geography*, as

An account of the following Catalogue of Eclipſes.

as that indefatigable author has, with much labour, collected them from *Ptolemy*, *Thucydides*, *Plutarch*, *Calviſius*, *Xenophon*, *Diodorus Siculus*, *Juſtin*, *Polybius*, *Titus Livius*, *Cicero*, *Lucanus*, *Theophanes*, *Dion. Caſſius*, and many others. From 1485 to 1700 the Eclipſes are taken from *Ricciolus's Almageſt:* and from 1700 to 1800 from *L'Art de verifier les Dates.* Thoſe from *Struyk* have all the places mentioned where they were obſerved: Thoſe from the *French* authors, *viz.* the religious *Benedictines* of the Congregation of *St. Maur*, are fitted to the Meridian of *Paris:* And concerning thoſe from *Ricciolus*, that author gives the following account.

" Becauſe it is of great uſe for fixing the Cycles or Revolutions of Eclipſes, to have at hand, without the trouble of calculation, a liſt of ſucceſſive Eclipſes for many years, computed by authors of *Ephemerides*, although from Tables not perfect in all reſpects, I ſhall for the benefit of Aſtronomers give a ſummary collection of ſuch. The authors I extract from are, an anonymous one who publiſhed *Ephemerides* from 1484 to 1506 incluſive: *Jacobus Pilaumen* and *Jo. Stæſlerinus*, to the Meridian of *Ulm*, from 1507 to 1534: *Lucas Gauricus*, to the Latitude of 45 degrees, from 1534 to 1551: *Peter Appian*, to the Meridian of *Leyſing*, from 1538 to 1578: *Jo. Stæſlerus*, to the Meridian of *Tubing*, from 1543 to 1554: *Petrus Pitatus*, to the Meridian of *Venice*, from 1544 to 1556: *Georgius-Joachimus Rheticus*, for the year 1551: *Nicholaus Simus*, to the Meridian of *Bologna*, from 1552 to 1568: *Michael Mæſtlin*, to the Meridian of *Tubing*, from 1557 to 1590: *Jo. Stadius*, to the Meridian of *Antwerp*, from 1554 to 1574: *Jo. Antoninus Maginus*, to the Meridian of *Venice*, from 1581 to 1630: *David Origan*, to the Meridian of *Franckfort* on the *Oder*, from 1595 to 1664: *Andrew Argol*, to the Meridian of *Rome*, from 1630 to 1700: *Franciſcus Montebrunus*, to the Meridian of *Bologna*, from 1461 to 1660: Among which, *Stadius*, *Mæſtlin*, and *Maginus*,

ginus, uſed the *Prutenic* Tables; *Origan* the *Prutenic* and *Tychonic*; *Montebrunus* the *Lanſbergian*, as likewiſe thoſe of *Duret*. Almoſt all the reſt the *Alphonſine*.

But, that the places may readily be known for which theſe Eclipſes were computed, and from what Tables, conſult the following Liſt, in which the years *incluſive* are alſo ſet down.

From	To	
1485	1506	The place and author unknown.
1507	1553	*Ulm* in *Suabia*, from the *Alphonſine*.
1554	1576	*Antwerp*, from the *Prutenic*.
1577	1585	*Tubing*, from the *Prutenic*.
1586	1594	*Venice*, from the *Prutenic*.
1595	1600	*Franckfort* on the *Oder*, from the *Prutenic*.
1601	1640	*Franckfort* on the *Oder*, from the *Tychonic*.
1641	1660	*Bologna*, from the *Lanſbergian*.
1661	1700	*Rome*, from the *Tychonic*."

So far RICCIOLUS.

N. B. The Eclipſes marked with an Aſteriſk are not in RICCIOLUS's Catalogue, but are ſupplied from *L'Art de verifier les Dates*.

From the beginning of the Catalogue to *A. D.* 1700, the time is reckoned from the noon of the day mentioned to the noon of the following day: but from 1700 to 1800 the time is ſet down according to our common way of reckoning. Thoſe marked *Pekin* and *Canton* are Eclipſes from the *Chineſe* chronology according to STRUYK; and throughout the Table this mark ☉ ſignifies *Sun*, and this ☽ *Moon*.

STRUYK's Catalogue of ECLIPSES.

Bef. Chr.	Eclipſes of the Sun and Moon ſeen at		M. & D.		Middle H.	M.	Digits eclipſed	
721	Babylon	☽	Mar.	19	10	34	Total	
720	Babylon	☽	Mar.	8	11	56	1	5
720	Babylon	☽	Sept.	1	10	18	5	4
621	Babylon	☽	Apr.	21	18	22	2	36
523	Babylon	☽	July	16	12	47	7	24
502	Babylon	☽	Nov.	19	12	21	1	52
491	Babylon	☽	Apr.	25	12	12	1	44
431	Athens	☼	Aug.	3	6	35	11	0
425	Athens	☽	Oct.	9	6	45	Total	
424	Athens	☼	Mar.	20	20	17	9	0
413	Athens	☽	Aug.	27	10	15	Total	
406	Athens	☽	Apr.	15	8	50	Total	
404	Athens	☼	Sept.	2	21	12	8	40
403	Pekin	☼	Aug.	28	5	53	10	40
394	Gnide	☼	Aug.	13	22	17	11	0
383	Athens	☽	Dec.	22	19	6	2	1
382	Athens	☽	June	18	8	54	6	15
382	Athens	☽	Dec.	12	10	21	Total	
364	Thebes	☼	July	12	23	51	6	10
357	Syracuſe	☼	Feb.	28	22	—	3	33
357	Zant	☽	Aug.	29	7	29	4	21
340	Zant	☼	Sept.	14	18	—	9	0
331	Arbela	☽	Sept.	20	10	9	Total	
310	Sicily Iſland	☼	Aug.	14	20	5	10	22
219	Myſia	☽	Mar.	19	14	5	Total	
218	Pergamos	☽	Sept.	1	riſing		Total	
217	Sardinia	☼	Feb.	11	1	57	9	6
203	Fruſini	☼	May	6	2	52	5	40
202	Cumis	☼	Oct.	18	22	24	1	0
201	Athens	☽	Sept.	22	7	14	8	58
200	Athens	☽	Mar.	19	13	9	Total	
200	Athens	☽	Sept.	11	14	48	Total	
198	Rome	☼	Aug.	6	—		—	
190	Rome	☼	Mar.	13	18	—	11	0
188	Rome	☼	July	16	20	38	10	48
174	Athens	☽	Apr.	30	14	33	7	1
168	Macedonia	☽	June	21	8	2	Total	
141	Rhodes	☽	Jan.	27	10	8	3	26
104	Rome	☼	July	18	22	0	11	52
63	Rome	☽	Oct.	27	6	22	Total	
60	Gibraltar	☼	Mar.	16	ſetting		Central	
54	Canton	☼	May	9	3	41	Total	
51	Rome	☼	Mar.	7	2	12	9	0
48	Rome	☽	Jan.	18	10	0	Total	
45	Rome	☽	Nov.	6	14	—	Total	
36	Rome	☼	May	19	3	52	6	47

STRUYK's Catalogue of ECLIPSES.

Bef. Chr.	Eclipſes of the Sun and Moon ſeen at		M. & D.		Middle H.	M.	Digits eclipſed	
31	Rome	☉	Aug.	20	ſetting		Gr. Ecl.	
29	Canton	☉	Jan.	5	4	2	11	0
28	Pekin	☉	June	18	23	48	Total	
26	Canton	☉	Oct.	23	4	16	11	15
24	Pekin	☉	April	7	4	11	2	0
16	Pekin	☉	Nov.	1	5	13	2	8
2	Canton	☉	Feb.	1	20	8	11	42
Aft. Chr.								
1	Pekin	☉	June	10	1	10	11	43
5	Rome	☉	Mar.	28	4	13	4	45
14	Panonia	☽	Sept.	26	17	15	Total	
27	Canton	☉	July	22	8	56	Total	
30	Canton	☉	Nov.	13	19	20	10	30
40	Pekin	☉	Apr.	30	5	50	7	34
45	Rome	☉	July	31	22	1	5	17
46	Pekin	☉	July	21	22	25	2	10
46	Rome	☽	Dec.	31	9	52	Total	
49	Pekin	☉	May	20	7	16	10	8
53	Canton	☉	Mar.	8	20	42	11	6
55	Pekin	☉	July	12	21	50	6	40
56	Canton	☉	Dec.	25	0	28	9	20
59	Rome	☉	Apr.	30	3	8	10	38
60	Canton	☉	Oct.	13	3	31	10	30
65	Canton	☉	Dec.	15	21	50	10	23
69	Rome	☽	Oct.	18	10	43	10	49
70	Canton	☉	Sept.	22	21	13	8	26
71	Rome	☽	Mar.	4	8	32	6	0
95	Epheſus	☉	May	21	——		1	0
125	Alexandria	☽	April	5	9	16	1	44
133	Alexandria	☽	May	6	11	44	Total	
134	Alexandria	☽	Oct.	20	11	5	10	19
136	Alexandria	☽	March	5	15	56	5	17
237	Bologna	☉	April	12	——		Total	
238	Rome	☉	April	1	20	20	8	45
290	Carthage	☉	May	15	3	20	11	20
304	Rome	☽	Aug.	31	9	36	Total	
316	Conſtantinople	☉	Dec.	30	19	53	2	18
334	Toledo	☉	July	17	at noon		Central	
348	Conſtantinople	☉	Oct.	8	19	24	8	0
360	Iſpahan	☉	Aug.	27	18	0	Central	
364	Alexandria	☽	Nov.	25	15	24	Total	
401	Rome	☽	June	11	——		Total	
401	Rome	☽	Dec.	6	12	15	Total	
402	Rome	☽	June	1	8	43	10	2

STRUYK's Catalogue of ECLIPSES.

Aft. Chr.	Eclipſes of the Sun and Moon ſeen at		M. & D.		Middle H.	M.	Digits eclipſed	
402	Rome	☼	Nov.	10	20	33	10	30
447	Compoſtello	☼	Dec.	23	0	46	1	—
451	Compoſtello	☽	April	1	16	34	19	52
451	Compoſtello	☽	Sept.	26	6	30	0	2
458	Chaves	☼	May	27	23	16	18	53
462	Compoſtello	☽	March	1	13	2	11	11
464	Chaves	☼	July	19	19	1	10	15
484	Conſtantinople	☼	Jan.	13	19	53	10	0
486	Conſtantinople	☼	May	19	1	10	5	15
497	Conſtantinople	☼	April	18	6	5	17	57
512	Conſtantinople	☼	June	28	23	8	1	50
538	England	☼	Feb.	14	19	—	8	23
540	London	☼	June	19	20	15	8	—
577	Tours	☽	Dec.	10	17	28	6	46
581	Paris	☽	April	4	13	33	6	42
582	Paris	☽	Sept.	17	12	41	Total	
590	Paris	☽	Oct.	18	6	30	9	25
592	Conſtantinople	☼	March	18	22	6	10	0
603	Paris	☼	Aug.	12	3	3	11	20
622	Conſtantinople	☽	Feb.	1	11	28	Total	
644	Paris	☼	Nov.	5	0	30	9	53
680	Paris	☽	June	17	12	30	Total	
683	Paris	☽	April	16	11	30	Total	
693	Conſtantinople	☼	Oct.	4	23	54	11	54
716	Conſtantinople	☽	Jan.	13	7	—	Total	
718	Conſtantinople	☼	June	3	1	15	Total	
733	England	☼	Aug.	13	20	—	11	1
734	England	☽	Jan.	23	14	—	Total	
752	England	☽	July	30	13	—	Total	
753	England	☼	June	8	22	—	10	35
753	England	☽	Jan.	23	13	—	Total	
760	England	☼	Aug.	15	4	—	8	15
760	London	☽	Aug.	30	5	50	10	40
764	England	☼	June	4	at noon		7	15
770	London	☽	Feb.	14	7	12	Total	
774	Rome	☽	Nov.	22	14	37	11	58
784	London	☽	Nov.	1	14	2	Total	
787	Conſtantinople	☼	Sept.	14	20	43	9	47
796	Conſtantinople	☽	March	27	16	22	Total	
800	Rome	☽	Jan.	15	9	0	10	17
807	Angouleſme	☼	Feb.	10	21	24	9	42
807	Paris	☽	Feb.	25	13	43	Total	
807	Paris	☽	Aug.	21	10	20	Total	
809	Paris	☼	July	15	21	33	8	8
809	Paris	☽	Dec.	25	8	—	Total	
810	Paris	☽	June	20	8	—	Total	

STRUYK's Catalogue of ECLIPSES.

Aft. Chr.	Eclipſes of the Sun and Moon ſeen at		M. & D.		Middle H.	M.	Digits eclipſed	
810	Paris	☉	Nov.	30	0	12	Total	
810	Paris	☽	Dec.	14	8	—	Total	
812	Conſtantinople	☉	May	14	2	13	9	—
813	Cappadocia	☉	May	3	17	5	10	35
817	Paris	☽	Feb.	5	5	42	Total	
818	Paris	☉	July	6	18	—	6	35
820	Paris	☽	Nov.	23	6	26	Total	
824	Paris	☽	March	18	7	55	Total	
828	Paris	☽	June	30	15	—	Total	
828	Paris	☽	Dec.	24	13	45	Total	
831	Paris	☽	April	30	6	19	11	8
831	Paris	☉	May	15	23	—	4	24
831	Paris	☽	Oct.	24	11	18	Total	
832	Fulda	☽	April	18	9	0	Total	
840	Paris	☉	May	4	23	22	9	20
841	Paris	☉	Oct.	17	18	58	5	24
842	Paris	☽	March	29	14	38	Total	
843	Paris	☽	March	19	7	1	Total	
861	Paris	☽	March	29	15	7	Total	
878	Paris	☽	Oct.	14	16	—	Total	
878	Paris	☉	Oct.	29	1	—	11	14
883	Arracta	☽	July	23	7	44	11	—
889	Conſtantinople	☉	April	3	17	52	9	23
891	Conſtantinople	☉	Aug.	7	23	48	10	30
901	Arracta	☽	Aug.	2	15	7	Total	
904	London	☽	May	31	11	47	Total	
904	London	☽	Nov.	25	9	0	Total	
912	London	☽	Jan.	6	15	12	Total	
925	Paris	☽	March	31	15	17	Total	
934	Paris	☉	April	16	4	30	11	36
939	Paris	☉	July	18	19	45	10	7
955	Paris	☽	Sept.	4	11	18	Total	
961	Rhemes	☉	May	16	20	13	9	18
970	Conſtantinople	☉	May	7	18	38	11	22
976	London	☽	July	13	15	7	Total	
985	Meſſina	☉	July	20	3	52	4	10
989	Conſtantinople	☉	May	28	6	54	8	40
990	Fulda	☽	April	12	10	22	9	5
990	Fulda	☽	Oct.	6	15	4	11	10
990	Conſtantinople	☉	Oct.	21	0	45	10	5
995	Augſburgh	☽	July	14	11	27	Total	
1009	Ferrara	☽	Oct.	6	11	38	Total	
1010	Meſſina	☉	March	18	5	41	9	12
1016	Nimeguen	☽	Nov.	16	16	39	Total	
1017	Nimeguen	☉	Oct.	22	2	8	6	—
1020	Cologne	☽	Sept.	4	11	38	Total	

STRUYK's Catalogue of ECLIPSES.

Aft. Chr.	Eclipſes of the Sun and Moon ſeen at		M. & D.		Middle H.	M.	Digits eclipſed
1023	London	☉	Jan.	23	23	29	11 —
1030	Rome	☽	Feb.	20	11	43	Total
1031	Paris	☽	Feb.	9	11	51	Total
1033	Paris	☽	Dec.	8	11	11	9 17
1034	Milan	☽	June	4	9	8	Total
1037	Paris	☉	April	17	20	45	10 45
1039	Auxerre	☉	Aug.	21	23	40	11 5
1042	Rome	☽	Jan.	8	16	39	Total
1044	Auxerre	☽	Nov.	7	16	12	10 1
1044	Cluny	☉	Nov.	21	22	12	11 —
1056	Nuremburg	☽	April	2	12	9	Total
1063	Rome	☽	Nov.	8	12	16	Total
1074	Augſburgh	☽	Oct.	7	10	13	Total
1080	Conſtantinople	☽	Nov.	29	11	12	9 36
1082	London	☽	May	14	10	32	10 2
1086	Conſtantinople	☉	Feb.	16	4	7	Total
1089	Naples	☽	June	25	6	6	Total
1093	Augſburgh	☉	Sept.	22	22	35	10 12
1096	Gembluors	☽	Feb.	10	16	4	Total
1096	Augſburgh	☽	Aug.	6	8	21	Total
1098	Augſburgh	☉	Dec.	25	1	25	10 12
1099	Naples	☽	Nov.	30	4	58	Total
1103	Rome	☽	Sept.	17	10	18	Total
1106	Erfurd	☽	July	17	11	28	11 54
1107	Naples	☽	Jan.	10	13	16	Total
1109	Erfurd	☉	May	31	1	30	10 20
1110	London	☽	May	5	10	51	Total
1113	Jeruſalem	☉	Mar.	18	19	0	9 12
1114	London	☽	Aug.	17	15	5	Total
1117	Trier	☽	June	15	13	26	Total
1117	Trier	☽	Dec.	10	12	51	Total
1118	Naples	☽	Nov.	29	15	46	4 11
1121	Triers	☽	Sept.	27	16	47	Total
1122	Prague	☽	March	24	11	20	3 49
1124	Erfurd	☽	Feb.	1	6	43	8 39
1124	London	☉	Auguſt	10	23	29	9 58
1132	Erfurd	☽	March	3	8	14	Total
1133	Prague	☽	Feb.	20	16	41	3 23
113[illegible]	London	☽	Dec.	22	20	11	Total
1142	Rome	☽	Feb.	11	14	17	8 30
1143	Rome	☽	Feb.	1	6	36	Total
1147	Auranches	☉	Oct.	25	22	38	7 20
1149	Bary	☽	March	25	13	54	5 29
1151	Eimbeck	☽	Auguſt	28	12	4	4 29
1153	Augſburgh	☉	Jan.	26	0	42	11 —
1154	Paris	☽	June	26	16	1	Total

STRUYK's Catalogue of ECLIPSES.

Aft. Chr.	Eclipſes of the Sun and Moon ſeen at		M. & D.		Middle H.	M.	Digits eclipſed	
1154	Paris	☽	Dec.	21	8	30	4	42
1155	Auranches	☽	June	16	8	45	0	53
1160	Rome	☽	Auguſt	18	7	53	6	49
1161	Rome	☽	Auguſt	7	8	15	Total	
1162	Erfurd	☽	Feb.	1	6	40	5	56
1162	Erfurd	☽	July	27	12	30	4	11
1163	Mont Caſſin.	☼	July	3	7	40	2	0
1164	Milan	☽	June	6	10	0	Total	
1168	London	☽	Sept.	18	14	0	Total	
1172	Cologne	☽	Jan.	11	13	31	Total	
1176	Auranches	☽	April	25	7	2	8	6
1176	Auranches	☽	Oct.	19	11	20	8	53
1178	Cologne	☽	March	5	ſetting		7	52
1178	Auranches	☽	Auguſt	29	13	52	5	31
1178	Cologne	☼	Sept.	12	—		10	51
1179	Cologne	☽	Auguſt	18	14	28	Total	
1180	Auranches	☼	Jan.	28	4	14	10	34
1181	Auranches	☼	July	13	3	15	3	48
1181	Auranches	☽	Dec.	22	8	58	4	40
1185	Rhemes	☼	May	1	1	53	9	0
1186	Cologne	☽	April	5	6	—	Total	
1186	Franckfort	☼	April	20	7	19	4	0
1187	Paris	☽	March	25	16	17	8	42
1187	England	☼	Sept.	3	21	54	8	6
1189	England	☽	Feb.	2	10	—	9	—
1191	England	☼	June	23	0	20	11	32
1192	France	☽	Nov.	20	14	—	6	—
1193	France	☽	Nov.	10	5	27	Total	
1194	London	☼	April	22	2	15	6	49
1200	London	☽	Jan.	2	17	2	4	35
1201	London	☽	June	17	15	4	Total	
1204	England	☽	April	15	12	39	Total	
1204	Saltzburg	☽	Oct.	10	6	32	Total	
1207	Rhemes	☼	Feb.	27	10	50	10	20
1208	Rhemes	☽	Feb.	2	5	10	Total	
1211	Vienna	☽	Nov.	21	13	57	Total	
1215	Cologne	☽	March	16	15	35	Total	
121	Acre	☼	Feb.	18	21	15	11	36
1216	Acre	☽	March	5	9	38	7	4
1218	Damiétta	☽	July	9	9	46	11	31
1222	Rome	☽	Oct.	22	14	28	Total	
1223	Colmar	☽	April	16	8	13	11	0
1228	Naples	☼	Dec.	27	9	55	9	19
1230	Naples	☼	May	13	17	—	Total	
1230	London	☽	Nov.	21	13	21	9	34
1232	Rhemes	☼	Oct.	15	4	29	4	25

STRUYK's Catalogue of ECLIPSES.

Aft. Chr.	Eclipſes of the Sun and Moon ſeen at		M. & D.	Middle H.	M.	Digits eclipſed
1245	Rhemes	☉	July 24	17	47	6 —
1248	London	☽	June 7	8	49	Total
1255	London	☽	July 20	9	47	Total
1255	Conſtantinople	☉	Dec. 30	2	52	Annul.
1258	Augſburgh	☽	May 18	11	17	Total
1261	Vienna	☉	March 31	22	40	9 8
1262	Vienna	☽	March 7	5	50	Total
1262	Vienna	☽	Auguſt 30	14	39	Total
1263	Vienna	☽	Feb. 24	6	52	6 29
1263	Augſburgh	☉	Auguſt 5	3	24	11 17
1263	Vienna	☽	Auguſt 20	7	35	9 7
1265	Vienna	☽	Dec. 23	16	25	Total
1267	Conſtantinople	☉	May 24	23	11	11 40
1270	Vienna	☉	March 22	18	47	10 40
1272	Vienna	☽	Auguſt 10	7	27	8 53
1274	Vienna	☽	Jan. 23	10	39	9 25
1275	Lauben	☽	Dec. 4	6	20	4 29
1276	Vienna	☽	Nov. 22	15	—	Total
1277	Vienna	☽	May 18	—		Total
1279	Franckfort	☉	April 12	6	55	10 6
1280	London	☽	March 17	12	12	Total
1284	Reggio	☽	Dec. 23	16	11	9 13
1290	Wittemburg	☉	Sept. 4	19	37	10 30
1291	London	☽	Feb. 14	10	2	Total
1302	Conſtantinople	☽	Jan. 14	10	25	Total
1307	Ferrara	☉	April 2	22	18	0 54
1309	London	☽	Feb. 24	17	44	Total
1309	Lucca	☽	Auguſt 21	10	32	Total
1310	Wittemburg	☉	Jan. 31	2	2	10 10
1310	Torcello	☽	Feb. 14	4	8	10 20
1310	Torcello	☽	Auguſt 10	15	33	7 16
1312	Wittemburg	☉	July 4	19	49	3 23
1312	Plaiſance	☽	Dec. 14	7	19	Total
1313	Torcello	☽	Dec. 3	8	58	9 34
1316	Modena	☽	Oct. 1	14	55	Total
1321	Wittemburg	☉	June 25	18	1	11 17
1323	Florence	☽	May 20	15	24	Total
1324	Florence	☽	May 9	6	3	Total
1324	Wittemburg	☉	April 23	6	35	8 8
1327	Conſtantinople	☽	Auguſt 31	18	26	Total
1328	Conſtantinople	☽	Feb. 25	13	47	11 —
1330	Florence	☽	June 30	15	10	7 34
1330	Conſtantinople	☉	July 16	4	5	10 43
1330	Prague	☽	Dec. 25	15	49	Total
1331	Prague	☉	Nov. 29	20	26	7 41
1331	Prague	☽	Dec. 14	18	—	11 —

STRUYK's Catalogue of ECLIPSES.

Aft. Chr.	Eclipſes of the Sun and Moon ſeen at		M. & D.		Middle H.	M.	Digits eclipſed	
1333	Wittemburg	☼	May	14	3	—	10	18
1334	Ceſena	☽	April	19	10	33	Total	
1341	Conſtantinople	☽	Nov.	23	12	23	Total	
1341	Conſtantinople	☼	Dec.	8	22	15	6	30
1342	Conſtantinople	☽	May	20	14	27	Total	
1344	Alexandria	☼	Oct.	6	18	40	8	55
1349	Wittemburg	☽	June	30	12	20	Total	
1354	Wittemburg	☼	Sept.	16	20	45	8	43
1356	Florence	☽	Feb.	16	11	43	Total	
1361	Conſtantinople	☼	May	4	22	15	8	54
1367	Sienna	☽	Jan.	16	8	27	Total	
1389	Eugibio	☽	Nov.	3	17	5	Total	
1396	Augſburg	☼	Jan.	11	0	16	6	22
1396	Augſburg	☽	June	21	11	10	Total	
1399	Forli	☼	Oct.	29	0	43	9	—
1406	Conſtantinople	☽	June	1	13	—	10	31
1406	Conſtantinople	☼	June	15	18	1	11	38
1408	Forli	☼	Oct.	18	21	47	9	32
1409	Conſtantinople	☼	April	15	3	1	10	48
1410	Vienna	☽	March	20	13	13	Total	
1415	Wittemburg	☼	June	6	6	43	Total	
1419	Franckfort	☼	March	25	22	5	1	45
1421	Forli	☽	Feb.	17	8	2	Total	
1422	Forli	☽	Feb.	6	8	26	11	7
1424	Wittemburg	☼	June	26	3	57	11	20
1431	Forli	☼	Feb.	12	2	4	1	39
1433	Wittemburg	☼	June	17	5	—	Total	
1438	Wittemburg	☼	Sept.	18	20	59	8	7
1442	Rome	☽	Dec.	17	3	56	Total	
1448	Tubing	☼	Auguſt	28	22	23	8	53
1450	Conſtantinople	☽	July	24	7	19	Total	
1457	Vienna	☽	Sept.	3	11	17	Total	
1460	Auſtria	☽	July	3	7	31	5	23
1460	Auſtria	☼	July	17	17	32	11	19
1460	Vienna	☽	Dec.	27	13	30	Total	
1461	Vienna	☽	June	22	11	50	Total	
1461	Rome	☽	Dec.	17	—		Total	
1462	Viterbo	☽	June	11	15	—	7	38
1462	Viterbo	☼	Nov.	21	0	10	2	6
1464	Padua	☽	April	21	12	43	Total	
1465	Rome	☼	Sept.	20	5	15	8	46
1465	Rome	☽	Oct.	4	5	12	Total	
1469	Rome	☽	Jan.	27	7	9	Total	
1485	Norimburg	☼	March	1	3	53	11	—

All the following ECLIPSES are taken from Ricciolus, except thoſe marked with an Aſteriſk, which are from *L'Art de verifier les Dates.*

Aft. Chr.		M.&D.	Middle H.	M.	Digits eclipſed
1486	☽	Feb. 18	5	41	Total
1486	☼	Mar. 5	17	43	9 0
1487	☽	Feb. 7	15	49	Total
1487	☼	July 20	2	6	7 0
1488	☽	Jan. 28	6	—	*
1488	☼	July 8	17	30	4 0
1489	☽	Dec. 7	17	41	Total
1490	☼	May 19	Noon		*
1490	☽	June 2	10	6	Total
1490	☽	Nov. 26	18	25	Total
1491	☼	Mar. 8	2	19	9
1491	☽	Nov. 15	18	—	*
1492	☼	Apr. 26	7	—	*
1492	☼	Oct. 20	23	—	*
1493	☽	April 1	14	0	Total
1493	☼	Oct. 10	2	40	8 0
1494	☼	Mar. 7	4	12	4 0
1494	☽	Mar. 21	14	38	Total
1494	☽	Sept. 14	19	45	Total
1495	☽	Mar. 10	16	—	*
1495	☼	Aug. 19	17	—	*
1496	☽	Jan. 29	14	—	*
1497	☽	Jan. 18	6	38	Total
1497	☼	July 29	3	2	3 0
1499	☽	June 22	17	—	*
1499	☼	Aug. 23	18	—	*
1499	☽	Nov. 17	10	—	*
1500	☼	Mar. 27	In the		Night
1500	☽	Apr. 11		At	Noon
1500	☽	Oct. 5	14	2	10 0
1501	☽	May 2	17	49	Total
1502	☼	Sept. 30	19	45	10 0
1502	☽	Oct. 15	12	20	2 0
1503	☽	Mar. 12	9	—	*
1503	☼	Sept. 19	22	—	*
1504	☽	Feb. 29	13	36	Total
1504	☼	Mar. 16	3	—	*
1505	☽	Aug. 14	8	18	Total
1506	☽	Feb. 7	15	—	*
1507	☼	July 20	3	11	2 0
1506	☽	Aug. 3	10	—	*
1507	☼	Jan. 12	19	—	*
1508	☼	Jan. 2	4	—	*
1508	☼	May 29	6	—	*
1508	☽	June 12	17	40	Total
1509	☽	June 2	11	11	7 0
1509	☼	Nov. 11	22	—	*
1510	☽	Oct. 16	19	—	*
1511	☽	Oct. 6	11	50	Total
1512	☽	Sept. 25	3	56	Total
1513	☼	Mar. 7	0	30	6 0
1513	☼	July 30	1	—	*
1515	☽	Jan. 29	15	18	Total
1516	☽	Jan. 19	6	0	Total
1516	☽	July 13	11	37	Total
1516	☼	Dec. 23	3	47	3 0
1517	☼	June 18	16	—	*
1517	☽	Nov. 27	19	—	*
1518	☽	May 24	11	19	9 11
1518	☼	June 7	17	56	11 0
1519	☼	May 28	1	—	*
1519	☼	Oct. 23	4	33	6 0
1519	☽	Nov. 6	6	24	Total
1520	☽	May 2	7	—	*
1520	☼	Oct. 11	5	22	3
1520	☽	Oct. 25	19	—	*
1520	☽	Mar. 21	17	—	*
1521	☼	April 6	19	—	*
1521	☼	Sept. 30	3	—	*
1522	☽	Sept. 5	12	17	Total
1523	☽	Mar. 1	8	26	Total
1523	☽	Aug 25	15	24	Total
1524	☼	Feb. 4	1	—	*
1524	☽	Aug. 16	16	—	*
1525	☼	Jan. 23	4	—	*
1525	☽	July 4	10	10	Total
1525	☽	Dec. 29	10	46	Total
1526	☽	Dec. 18	10	30	Total
1527	☼	Jan. 2	3	—	*
1527	☽	Dec 7	10	—	*
1528	☼	May 17	20	—	*
1529	☽	Oct. 16	20	23	11 55
1530	☼	Mar. 28	18	23	8 24
1530	☽	Oct. 6	12	11	Total
1531	☽	April 1	7	—	*
1532	☼	Aug. 30	0	49	3 35

RICCIOLUS's Catalogue of ECLIPSES.

Aft. Chr.		M.&D.	Middle H.	M.	Digits eclipſed
1533	☽	Aug. 4	11	50	Total
1533	☼	Aug. 19	17	—	*
1534	☼	Jan. 14	1	42	5 45
1534	☽	Jan. 29	14	25	Total
1535	☼	June 30	Noon		*
1535	☽	July 14	8	—	*
1535	☼	Dec. 24	2	—	*
1536	☼	June 18	2	2	8 0
1536	☽	Nov. 27	6	21	10 15
1537	☽	May 24	8	3	Total
1537	☼	June 7	8	—	*
1537	☽	Nov. 16	14	56	Total
1538	☽	May 13	14	24	3 0
1538	☽	Nov. 6	5	31	3 37
1539	☼	April 8	4	33	9 0
1540	☼	April 6	17	15	Total
1541	☽	Mar. 11	16	34	Total
1541	☼	Aug. 21	0	56	3
1542	☽	Mar. 1	8	46	1 38
1542	☼	Aug 10	17	—	*
1543	☽	July 15	16	—	*
1544	☽	Jan. 9	18	13	Total
1544	☼	Jan. 23	21	16	11 17
1544	☽	July 4	8	31	Total
1544	☽	Dec. 28	18	27	Total
1545	☼	June 8	20	48	3 45
1545	☽	Dec. 17	18	—	*
1546	☼	May 30	5	—	*
1546	☼	Nov. 22	23	—	*
1547	☽	May 4	10	27	8 0
1547	☽	Oct. 28	4	56	11 34
1547	☼	Nov. 12	2	9	9 30
1548	☼	April 8	3	—	*
1548	☽	Apr. 22	11	24	Total
1549	☽	Apr. 11	15	19	2 0
1549	☽	Oct. 6	6	—	*
1550	☼	Mar. 16	20	—	*
1551	☽	Feb. 20	8	21	Total
1551	☼	Aug. 31	2	0	1 52
1553	☼	Jan. 12	22	54	1 22
1553	☼	July 10	7	—	*
1553	☽	July 24	16	0	0 31
1554	☼	June 29	6	—	*
1554	☽	Dec. 8	13	7	10 12
1555	☽	June 4	15	0	Total
1555	☼	Nov. 13	19	—	*
1556	☼	Nov. 1	18	0	9 41
1556	☽	Nov. 16	12	44	6 55
1557	☼	Oct. 20	20	—	*
1558	☽	April 2	11	0	9 50
1558	☼	Apr. 18	1	—	*
1559	☽	Apr. 16	4	50	Total
1560	☽	Mar. 11	15	40	4 13
1560	☼	Aug. 21	1	0	6 22
1560	☽	Sept. 4	7	—	*
1561	☼	Feb. 13	19	—	*
1562	☼	Feb. 3	5	—	*
1562	☽	July 15	15	50	Total
1563	☼	Jan. 22	19	—	*
1563	☼	June 20	4	50	8 38
1563	☽	July 5	8	4	11 34
1565	☼	Mar. 7	12	53	—
1565	☽	May 14	16	—	*
1565	☽	Nov. 7	12	46	11 46
1566	☽	Oct 28	5	38	Total
1567	☼	April 8	23	4	9 34
1567	☽	Oct. 17	13	43	2 40
1568	☼	Mar. 28	5	—	*
1569	☽	Mar. 2	15	18	Total
1570	☽	Feb. 20	5	46	Total
1570	☽	Aug. 15	9	17	Total
1571	☼	Jan. 25	4	—	*
1572	☼	Jan. 14	19	—	*
1572	☽	June 25	9	0	5 26
1573	☼	June 28	18	—	*
1573	☼	Nov. 24	4	—	*
1573	☽	Dec. 8	6	51	Total
1574	☼	Nov. 13	3	50	5 21
1575	☼	May 19	8	—	*
1575	☼	Nov. 2	5	—	*
1576	☽	Oct 7	9	45	—
1577	☽	April 2	8	33	Total
1577	☽	Sept. 26	13	4	Total
1578	☽	Sept. 15	13	4	2 20
1579	☼	Feb. 15	5	41	8 36
1579	☼	Aug. 20	19	0	*
1580	☽	Jan. 31	10	7	Total
1581	☽	Jan. 19	9	22	Total
1581	☽	July 15	17	51	Total
1582	☽	Jan. 8	10	29	0 53
1582	☼	June 9	17	5	7 5
1583	☽	Nov. 25	21	51	Total

RICCIOLUS's Catalogue of ECLIPSES.

Aft. Chr.		M.&D.	Middle H.	M.	Digits eclipſed	
1584	☉	May 9	18	20	3	36
1584	☽	Nov.17	14	15	Total	
1585	☉	Apr.29	7	53	11	7
1585	☽	May 13	5	9	6	54
1586	☽	Sept.27	8	—	*	
1586	☉	Oct. 12	Noon		*	
1587	☽	Sept.16	9	28	10	2
1588	☉	Feb. 26	1	23	1	3
1588	☽	Mar.12	14	14	Total	
1588	☽	Sept. 4	17	30	Total	
1589	☉	Aug.10	18	—	*	
1589	☽	Aug.25	8	1	3	54
1590	☉	Feb. 4	5	—	*	
1590	☽	July 16	17	4	3	54
1590	☉	July 30	19	57	10	27
1591	☽	Jan. 9	6	21	9	40
1591	☽	July 6	5	8	Total	
1591	☉	July 20	4	2	1	0
1591	☽	Dec.29	16	11	Total	
1592	☽	June24	10	13	8	58
1592	☽	Dec.18	7	24	5	54
1593	☉	May 30	2	30	2	38
1594	☉	May 19	14	58	10	23
1594	☽	Oct. 28	19	15	9	40
1595	☉	April 9	Ter. de		Fuego	
1595	☽	Apr.24	4	12	Total	
1595	☉	May 7	22	—	*	
1595	☉	Oct. 3	2	4	5	18
1595	☽	Oct. 18	20	47	Total	
1596	☉	Mar.28		In	Chili	
1596	☽	Apr.12	8	52	6	4
1596	☉	Sept.21		In	China	
1596	☽	Oct. 6	21	15	3	33
1597	☉	Mar.17	St. Pet.		Iſle	
1597	☉	Sept.11	Picora		9	49
1598	☽	Feb. 20	18	12	10	55
1598	☉	Mar. 6	22	12	11	57
1598	☽	Aug.16	8	15	Total	
1598	☉	Aug.31	Magel.		8	34
1599	☽	Feb. 10	17	21	Total	
1599	☉	July 22	4	31	4	18
1599	☽	Aug. 6	—	—	Total	
1600	☉	Jan. 15	Java		11	48
1600	☽	Jan. 30	6	40	2	58
1600	☉	July 10	2	10	5	39
1601	☉	Jan 4	Ethiop.		9	40
1601	☽	June 15	6	18	4	52
1601	☉	June 29	China		4	29
1601	☽	Dec. 9	7	6	10	53
1601	☉	Dec. 24	2	46	9	52
1602	☉	May 21	Greenl.		2	41
1602	☽	June 4	7	18	Total	
1602	☉	June 19	N.Gra.		5	43
1602	☉	Nov.13	Magel.		3	—
1602	☽	Nov.28	10	2	Total	
1603	☉	May 10	China		11	21
1603	☽	May 24	11	41	7	59
1603	☉	Nov. 3	Rom. I.		11	17
1603	☽	Nov.18	7	31	3	26
1604	☉	Apr.20	Arabia		9	32
1604	☉	Oct. 22	Peru		6	49
1605	☽	April 3	9	19	11	49
1605	☉	Apr. 18	Madag.		5	31
1605	☽	Sept.27	4	27	9	26
1605	☉	Oct. 12	2	32	9	24
1606	☉	Mar. 8	Mexico		6	0
1606	☽	Mar.24	11	17	Total	
1606	☉	Sept. 2	Magel.		6	40
1606	☉	Sept. 2	Magel.		6	40
1606	☽	Sept.16	15	6	Total	
1607	☉	Feb. 25	21	48	1	13
1607	☽	Mar.13	6	36	1	22
1607	☉	Sept. 5	15	40	4	7
1608	☉	Feb. 15	at the		Antipo	
1608	☽	July 27	0	30	1	53
1608	☉	Aug. 9	4	39	0	40
1609	☽	Jan. 19	15	21	10	32
1609	☉	Feb. 4	Fuego		5	22
1609	☽	July 16	12	8	Total	
1609	☉	July 30	Canada		4	10
1609	☉	Dec.26	19	—	5	50
1610	☽	Jan. 9	1	31	Total	
1610	☉	June 20	Java		10	46
1610	☽	July 5	16	58	11	13
1610	☉	Dec. 15	Cyprus		4	50
1610	☽	Dec. 29	16	47	4	23
1611	☉	June 10	Califor.		11	30
1612	☽	May 14	10	38	7	22
1612	☉	May 29	23	38	7	14
1612	☽	Nov. 8	3	22	9	49
1612	☉	Nov.22	Magel.		9	0
1613	☉	Apr. 20	Magel		lanica	

RICCIOLUS's Catalogue of ECLIPSES.

Aft. Chr.		M.&D.	Middle H. M.	Digits eclipſed	Aft. Chr.		M.&D.	Middle H. M.	Digits eclipſed
1613	☽	May 4	0 35	Total	1625	☼	Mar. 8	Florida	
1613	☼	May 19	Eaſt	Tartary	1625	☽	Mar. 23	14 11	2 11
1613	☼	Oct. 13	South	Amer.	1625	☼	Sept. 1	St. Pe	ter's Iſl.
1613	☽	Oct. 28	4 19	Total	1625	☽	Sept. 16	11 41	5 6
1614	☼	April 8	N.Gui.	8 44	1626	☼	Feb. 25	Madag.	8 27
1614	☽	Apr. 23	17 36	5 25	1626	☽	Aug. 7	7 48	0 25
1614	☼	Oct. 3	0 57	5 2	1626	☼	Aug. 21	In	Mexico
1614	☽	Oct. 17	4 38	4 56	1627	☽	Jan. 30	11 38	10 21
1615	☼	Mar. 29	Goa	10 38	1627	☼	Feb. 15	Magel	lanica
1615	☼	Sept. 22	Salom	Iſle	1627	☽	July 27	9 4	Total
1616	☽	Mar. 3	1 58	Total	1627	☼	Aug. 11	Tenduc	10 0
1616	☼	Mar. 17	Mexico	6 47	1628	☼	Jan. 6	Tenduc	5 40
1616	☽	Aug. 26	15 33	Total	1628	☽	Jan. 20	10 11	Total
1616	☽	Sept. 10	Magel	10 33	1628	☼	July 1	C Good	Hope
1617	☼	Feb. 5	Magel	lanica	1628	☽	July 16	11 26	Total
1617	☽	Feb. 20	1 49	Total	1628	☼	Dec. 25	In Eng	land
1617	☼	Mar. 6	22 —		1629	☽	Jan. 9	1 36	4 27
1617	☼	Aug. 1	Biarmia	*	1629	☼	June 11	Ganges	11 25
1617	☽	Aug. 16	8 22	Total	1629	☼	Dec. 14	Peru	10 14
1618	☼	Jan. 26	Magel	lanica	1630	☽	May 25	17 56	6 0
1618	☽	Feb. 9	3 29	2 57	1630	☼	June 10	7 47	9 8
1618	☼	July 21	Mexico	———	1630	☽	Nov. 19	11 24	9 27
1619	☼	Jan. 15	Califor	nia	1630	☼	Dec. 3	N.Gui.	10 10
1619	☽	June 26	12 43	3 10	1631	☼	Apr. 30	Antar.	Circle
1619	☼	July 11	Africa	11 39	1631	☽	May 15	8 15	Total
1619	☽	Dec. 20	15 53	10 47	1631	☼	Oct. 24	C Good	Hope
1620	☼	May 31	Arctic	Circle	1631	☽	Nov. 8	12 0	Total
1620	☽	June 14	13 47	Total	1632	☼	Apr. 19	C Good	Hope
1620	☼	June 29	Magel.	7 20	1632	☽	May 4	1 24	6 35
1620	☽	Dec. 9	6 39	Total	1632	☼	Oct. 13	Mexico	8 37
1620	☼	Dec. 23	Magel	lanica	1632	☽	Oct. 27	12 23	5 31
1621	☼	May 20	14 54	10 44	1633	☼	April 8	5 14	4 30
1621	☽	June 3	19 42	9 53	1633	☼	Oct. 3	Maldiv.	Total
1621	☼	Nov. 13	Magel	lanica	1634	☽	Mar. 14	9 35	11 18
1621	☽	Nov. 28	15 43	3 38	1634	☼	Mar. 28	Japan	10 19
1632	☼	May 10	C. Verd	11 52	1634	☽	Sept. 7	5 0	Total
1622	☼	Nov. 2	Malac	ca In.	1634	☼	Sept. 22	C.G.H.	9 54
1623	☽	Apr. 14	7 19	10 54	1635	☼	Feb. 17	Antar.	Circle
1623	☼	Apr. 29	———	———	1635	☽	Mar. 3	9 25	Total
1623	☽	Oct. 8	0 22	8 35	1635	☼	Mar. 18	Mexico	0 16
1623	☼	Oct. 23	Califor.	10 46	1635	☼	Aug. 12	Iceland	5 0
1624	☼	May 18	N. Zem.	6 0	1635	☽	Aug. 27	16 4	Total
1624	☽	April 3	7 9	Total	1636	☼	Feb. 6	In	Peru
1624	☼	Apr. 17	Antar.	Circle	1636	☽	Feb. 20	11 34	3 23
1624	☼	Sept. 12	Magel	lanica	1636	☼	Aug. 1	Tartary	11 20
1624	☽	Sept. 26	8 55	Total	1626	☽	Aug. 16	4 34	1 25

RICCIOLUS's Catalogue of ECLIPSES.

Aft. Chr.		M.&D.	Middle H. M.	Digits eclipſed
1637	☼	Jan. 25	Cam	boya
1637	☼	July 21	Jucutan	
1637	☽	Dec. 31	0 44	10 45
1638	☼	Jan. 14	Perſia	9 45
1638	☽	June 25	20 17	Total
1638	☼	July 11	Mag-	9 5
1638	☼	Dec. 5	ellan.	2 10
1638	☽	Dec. 20	15 16	Total
1639	☼	Jan. 4	Tartary	0 30
1639	☼	June 1	5 59	10 40
1639	☽	June 15	2 41	11 9
1639	☼	Nov. 24	Magel.	11 0
1639	☽	Dec. 9	11 57	3 46
1640	☼	May 20	N. Spa.	10 30
1640	☼	Nov. 13	Peru	10 36
1641	☽	Apr. 25	1 2	9 49
1641	☼	May 9	Peru	10 16
1641	☽	Oct. 18	8 19	6 31
1641	☼	Nov. 2	18 46	——
1642	☼	Mar. 30	Eſtotl.	4 0
1642	☽	Apr. 14	14 31	Total
1642	☼	Sept. 25	Magel	lanica
1642	☽	Oct. 7	16 45	Total
1643	☼	Mar. 19	13 53	——
1643	☽	April 3	21 10	3 9
1643	☼	Sept. 12	17 0	——
1643	☽	Sept. 27	7 38	6 0
1644	☼	Mar. 8	6 20	——
1644	☼	Aug. 31	18 10	——
1645	☽	Feb. 10	7 45	8 52
1645	☼	Feb. 26	Rom. I.	10 46
1645	☽	Aug. 7	2 4	Total
1645	☼	Aug. 21	0 35	4 40
1646	☼	Jan. 16	Str. of	Anian
1646	☽	Jan. 30	18 11	Total
1646	☼	July 12	6 57	——
1646	☽	July 27	6 2	Total
1647	☼	Jan. 5	12 10	——
1647	☽	Jan. 20	9 43	4 47
1647	☼	July 2	0 9	——
1647	☼	Dec. 25	13 38	——
1648	☽	June 5	0 55	4 28
1648	☼	June 20	13 28	——
1648	☽	Nov. 29	19 17	7 40
1648	☼	Dec. 13	21 48	——
[illegible]	☽	May 25	15 20	Total

Aft. Chr.		M.&D.	Middle H. M.	Digits eclipſed
1649	☼	June 9	Arct. C.	4
1649	☼	Nov. 4	2 10	5 1
1649	☽	Nov. 18	19 56	Total
1650	☼	Apr. 30	5 54	——
1650	☽	May 15	8 37	7 57
1650	☼	Oct. 24	17 17	——
1650	☽	Nov. 7	20 29	5 3
1651	☼	Apr. 19	Tuber.	——
1651	☼	Oct. 14	2 15	——
1652	☽	Mar. 24	16 52	8 50
1652	☼	April 7	22 40	9 59
1652	☽	Sept. 17	7 27	9 49
1652	☼	Oct. 2	5 2	——
1653	☼	Feb. 27	——	——
1653	☽	Mar. 13	17 9	Total
1653	☼	Aug. 22	——	——
1653	☽	Sept. 6	23 45	Total
1654	☼	Feb. 16	9 10	——
1654	☽	Mar. 2	19 25	3 14
1654	☼	Aug. 11	22 24	2 28
1654	☽	Aug. 27	11 49	1 53
1655	☼	Feb. 6	2 37	4 20
1655	☼	Aug. 1	14 19	——
1655	☽	Aug. 16	16 —	*
1656	☽	Jan. 11	9 4	10 0
1656	☽	July 6	3 17	Total
1656	☼	July 21	11 48	——
1656	☽	Dec. 30	23 30	Total
1657	☼	June 11	11 20	——
1657	☽	June 25	9 35	Total
1657	☼	Dec. 4	20 0	——
1657	☽	Dec. 20	7 47	3 9
1658	☼	May 31	16 0	——
1658	☽	June 14	22 58	——
1658	☽	Nov. 9	13 56	0 10
1658	☼	Nov. 24	11 36	——
1659	☽	May 6	8 34	8 5
1659	☼	May 20	17 4	——
1659	☽	Oct. 29	16 16	5 52
1659	☼	Nov. 14	4 25	9 51
1660	☽	Apr. 24	21 58	Total
1660	☼	Oct. 3	22 34	——
1660	☽	Oct. 18	0 32	Total
1660	☼	Nov. 2	13 48	——
1661	☼	Mar. 29	22 32	——
1661	☽	Apr. 14	4 28	——

Ricciolus's Catalogue of ECLIPSES.

Aft. Chr.		M.&D.	Middle H.	M.	Digits eclipſed	
1661	☉	Sept.23	1	36	11	19
1661	☽	Oct. 7	14	51	7	4
1662	☉	Mar.19	15	8	———	
1662	☉	Apr.12	1	8	———	
1663	☽	Feb. 21	16	11	3	14
1663	☉	Mar. 9	5	47	———	
1663	☽	Aug.18	8	45	Total	
1663	☉	Sept. 1	8	8	———	
1664	☉	Jan. 27	20	40	———	
1664	☽	Feb. 11	3	16	———	
1664	☉	July 22	14	48	———	
1664	☉	Aug.20	22	10	———	
1665	☽	Jan. 30	18	47	4	34
1665	☉	July 12	7	48	———	
1665	☽	July 26	13	31	0	10
1666	☉	Jan. 4	21	33	———	
1666	☉	July 1	19	0	11	10
1667	☽	June 5	Noon		———	
1667	☉	July 21	2	32	———	
1667	☉	Nov.15	11	30	———	
1668	☉	May 10	Setting		———	
1668	☽	May 25	16	26	9	32
1663	☉	Nov. 4	2	53	9	50
1668	☽	Nov.18	3	54	6	45
1669	☉	Apr. 29	18	18	———	
1669	☉	Oct. 24	10	13	———	
1670	☉	Apr. 19	7	0	———	
1670	☉	Sept.10	19	0	———	
1670	☽	Sept.28	15	43	9	7
1670	☉	Oct. 13	12	5	———	
1671	☉	Apr. 8	23	29	———	
1671	☉	Sept. 2	21	25	———	
1671	☽	Sept.18	7	44	Total	
1672	☉	Feb. 28	3	38	———	
1672	☽	Mar.13	3	17	———	
1672	☉	Aug.22	6	43	———	
1672	☽	Sept. 6	18	54	———	
1673	☉	Feb. 16	7	29	———	
1673	☉	Aug.11	21	44	———	
1674	☽	Jan. 21	18	22	11	21
1674	☉	Feb. 5	9	4	———	
1674	☽	July 17	9	40	Total	
1675	☽	Jan. 11	8	29	Total	
1675	☉	Jan. 25	10	36	———	
1675	☽	July 6	16	31	Total	
1676	☉	June 10	21	26	4	34
1676	☽	June 25	6	26	———	
1676	☉	Dec. 4	20	52	———	
1677	☉	Nov.24	12	5	———	
1677	☽	May 16	16	25	8	15
1678	☽	May 6	5	30	———	
1678	☽	Oct. 29	9	17	Total	
1679	☉	Apr. 10	21	0	———	
1679	☽	May 25	11	53	5	47
1680	☉	Mar.29	23	22	———	
1980	☉	Sept.22	7	57	———	
1681	☽	Mar. 4	Noon		———	
1681	☉	Mar.19	13	43	———	
1681	☽	Aug.28	15	22	10	35
1681	☉	Sept.11	15	43	———	
1682	☽	Feb. 21	12	28	Total	
1682	☽	Aug.17	18	56	Total	
1683	☉	Jan. 27	1	35	10	30
1683	☽	Feb. 9	3	39	———	
1683	☽	Aug. 6	20	36	———	
1684	☉	Jan. 16	6	34	———	
1684	☽	June 26	15	18	1	35
1684	☉	July 12	3	26	Total	
1684	☽	Dec. 21	11	18	9	45
1685	☉	Jan. 4	16	0	———	
1685	☽	June 16	6	0	———	
1685	☽	Dec. 10	11	26	Total	
1686	☉	May 21	17	9	———	
1686	☽	June 6	Noon		———	
1686	☽	Nov.29	12	22	Total	
1687	☉	May 11	1	—	*	
1687	☽	May 26	14	—	*	
1687	☽	Apr. 15	7	4	6	49
1688	☉	Apr. 29	16	27	———	
1688	☽	Oct. 9	Noon		———	
1688	☉	Oct. 25	19	40	———	
1689	☽	Apr. 4	7	42	Total	
1689	☽	Sept.28	15	46	Total	
1690	☉	Mar.10	———		———	
1690	☽	Mar.24	11	14	5	43
1690	☉	Sept. 3	———		———	
1690	☽	Sept.18	2	42	———	
1691	☉	Feb. 27	17	30	———	
1691	☉	Aug.23	5	51	———	
1692	☽	Feb. 2	3	20	———	
1692	☉	Feb. 16	17	31	———	
1692	☽	July 27	16	9	Total	

RICCIOLUS's Catalogue of ECLIPSES.

Aft. Chr.		M.&D.	Middle H. M.	Digits eclipſed	Aft. Chr.		M.&D.	Middl H. M.	Digits eclipſed
1693	☽	Jan. 21	17 25	Total	1696	☼	Nov. 23	17 32	—
1693	☽	July 17	Noon	—	1697	☼	Apr. 20	14 32	—
1694	☽	Jan. 11	Noon	—	1697	☽	May 5	18 27	—
1694	☼	June 22	4 22	6 22	1697	☽	Oct. 29	8 44	8 54
1694	☽	July 6	13 51	0 47	1698	☼	Apr. 10	9 13	—
1695	☼	May 11	6 3	—	1698	☼	Oct. 3	15 29	—
1695	☽	May 28	Noon	—	1699	☽	Mar. 15	8 14	9 7
1695	☽	Nov. 20	8 0	6 55	1699	☼	Mar. 30	22 0	—
1695	☼	Dec. 5	17 7	—	1699	☽	Sept. 8	23 22	—
1696	☽	May 16	12 45	Total	1699	☼	Sept. 23	22 38	9 58
1696	☼	May 30	12 56	—	1700	☽	Mar. 4	20 11	—
1696	☽	Nov 8	17 30	Total	1700	☽	Aug. 29	1 42	—

The Eclipſes from STRUYK were obſerved; thoſe from RICCIOLUS calculated: the following from *L'Art de verifier les Dates*, are only thoſe which are viſible in *Europe* for the preſent century: thoſe which are total are marked with a *T*; and *M* ſignifies Morning, *A* Afternoon.

Viſible ECLIPSES from 1700 to 1800.

Aft. Chr.		Months and Days.	Time of the Day or Night.	Aft. Chr.		Months and Days.	Time of the Day or Night.
1701	☽	Feb. 22	11 A.	1715	☼	May 3	9 M. *T.*
1703	☽	Jan. 3	7 M.	1715	☽	Nov. 11	5 M.
1703	☽	June 29	1 M. *T.*	1717	☽	Mar. 27	3 M.
1703	☽	Dec. 23	7 M. *T.*	1717	☽	May 20	6 A.
1704	☽	Dec. 11	7 M.	1718	☽	Sept. 9	8 A. *T.*
1706	☽	Apr. 28	2 M.	1719	☽	Aug. 29	9 A.
1706	☼	May 12	10 M.	1721	☽	Jan. 13	3 A.
1706	☽	Oct. 21	7 A.	1722	☽	June 29	3 M.
1707	☽	Apr. 17	2 M. *T.*	1722	☼	Dec. 8	3 A.
1708	☽	Apr. 5	6 M.	1722	☽	Dec. 22	4 A.
1708	☼	Dec. 14	8 M.	1724	☼	May 22	7 A. *T.*
1708	☽	Sept. 29	9 A.	1724	☽	Nov. 1	4 M.
1709	☼	Mar. 11	2 A.	1725	☽	Oct. 21	7 A.
1710	☽	Feb. 13	11 A.	1726	☼	Sept. 25	6 A.
1710	☼	Feb. 28	1 A.	1726	☽	Oct. 11	5 M.
1711	☼	July 15	8 A.	1727	☼	Sept. 15	7 M.
1711	☽	July 29	6 A. *T.*	1729	☽	Feb. 13	9 A. *T.*
1712	☽	Jan. 23	8 A.	1729	☽	Aug. 9	1 M.
1713	☽	June 8	6 A.	1730	☽	Feb. 4	4 M.
1713	☽	Dec. 2	4 M.	1731	☽	June 20	2 M.

Viſible ECLIPSES from 1700 to 1800.

Aft. Chr.		Months and Days.	Time of the Day or Night.	Aft. Chr.		Months and Days.	Time of the Day or Night.
1732	☽	Dec. 1	10 A. *T.*	1764	☼	Apr. 1	10 M.
1733	☼	May 13	7 A.	1764	☽	Apr. 16	1 M.
1733	☽	May 28	7 A.	1765	☼	Mar. 21	2 A.
1735	☽	Oct. 2	1 M.	1765	☼	Aug. 16	5 A.
1736	☽	Mar. 26	12 A. *T.*	1766	☽	Feb. 24	7 A.
1736	☽	Sept. 20	3 M. *T.*	1766	☼	Aug. 5	7 A.
1736	☼	Oct. 4	6 A.	1768	☽	Jan. 4	5 M.
1737	☼	Mar. 1	4 A.	1768	☽	June 30	4 M. *T.*
1737	☽	Sept. 9	4 M.	1768	☽	Dec. 23	4 A. *T.*
1738	☼	Aug. 15	11 M.	1769	☼	June 4	8 M.
1739	☽	Jan. 24	11 A.	1769	☽	Dec. 13	7 M.
1739	☼	Aug. 4	5 A.	1770	☼	Nov. 17	10 M.
1739	☼	Dec. 30	9 M.	1771	☽	Apr. 28	2 M.
1740	☽	Jan. 13	11 A. *T.*	1771	☽	Oct. 23	5 A.
1741	☽	Jan. 1	12 A.	1772	☽	Oct. 11	6 A. *T.*
1743	☽	Nov. 2	3 M. *T.*	1772	☼	Oct. 26	10 M.
1744	☽	Aug. 26	9 A.	1773	☼	Mar. 23	5 M.
1746	☽	Aug. 30	12 A.	1773	☽	Sept. 30	7 A.
1747	☽	Feb. 14	5 M. *T.*	1774	☼	Mar. 12	10 M.
1748	☼	July 25	11 M.	1776	☽	July 31	1 M. *T.*
1748	☽	Aug. 8	12 A.	1776	☼	Aug. 14	5 M.
1749	☽	Dec. 23	8 A.	1777	☼	Jan. 9	5 A.
1750	☼	Jan. 8	9 M.	1778	☼	June 24	4 A.
1750	☽	June 19	9 A. *T.*	1778	☽	Dec. 4	6 M.
1750	☽	Dec. 13	7 M.	1779	☽	May 30	5 M. *T.*
1751	☽	June 9	2 M.	1779	☼	June 14	8 M.
1751	☽	Dec. 2	10 A.	1779	☽	Nov. 23	8 A.
1752	☼	May 13	8 A.	1780	☼	Oct. 27	6 A.
1753	☽	Apr. 17	7 A.	1780	☽	Nov. 12	4 M.
1753	☼	Oct. 26	10 M.	1781	☼	Apr. 23	6 A.
1755	☽	Mar. 28	1 M.	1781	☼	Oct. 17	8 M.
1757	☽	Feb. 4	6 M.	1782	☽	Apr. 12	7 A.
1757	☽	July 30	12 A.	1783	☽	Mar. 18	9 A. *T.*
1758	☽	Jan. 24	7 M. *T.*	1783	☽	Sept. 10	11 A. *T.*
1758	☼	Dec. 30	7 M.	1784	☽	Mar. 7	3 M.
1759	☼	June 24	7 A.	1785	☼	Feb. 9	1 A.
1759	☼	Dec. 19	2 A.	1787	☽	Jan. 3	12 A. *T.*
1760	☽	May 29	9 A.	1787	☼	Jan. 19	10 M.
1760	☼	June 13	7 M.	1787	☼	June 15	5 A.
1760	☽	Nov. 22	9 A.	1787	☽	Dec. 24	3 A.
1761	☽	May 18	11 A. *T.*	1788	☼	June 4	9 M.
1762	☽	May 8	4 M.	1789	☽	Nov. 2	12 A.
1762	☼	Oct. 17	8 M.	1790	☽	Apr. 28	12 A. *T.*
1762	☽	Nov. 1	8 A.	1790	☽	Oct 23	1 M. *T.*
1763	☼	Apr. 13	8 M.	1791	☼	Apr. 3	1 A.

Viſible ECLIPSES from 1700 to 1800.

Aft. Chr.		Months and Days	Time of the Day or Night.	Aft. Chr.		Months and Days.	Time of the Day or Night.
1791	☽	Oct. 12	3 M.	1795	☽	Feb. 4	1 M.
1792	☼	Sept. 16	11 M.	1795	☼	July 16	9 M.
1793	☽	Feb. 25	10 A.	1795	☽	July 31	8 A.
1793	☼	Sept. 5	3 A.	1797	☼	June 25	8 A.
1794	☼	Jan. 31	4 A.	1797	☽	Dec. 4	6 M.
1794	☽	Feb. 14	11 A. *T.*	1798	☽	May 27	7 A. *T.*
1794	☼	Aug. 25	5 A.	1800	☽	Oct. 2	11 A.

328. *A Liſt of Eclipſes, and hiſtorical Events, which happened about the ſame Times, from* RICCIOLUS.

Before CHRIST.

754	*July*	5	But according to an old Calendar, this Eclipſe of the Sun was on the 21ſt of *April*, on which day the Foundations of *Rome* were laid; if we may believe *Taruntius Firmanus*.
721	*March*	19	A total Eclipſe of the Moon. The *Aſſyrian* Empire at an end; the *Babylonian* eſtabliſhed.
585	*May*	28	An Eclipſe of the Sun foretold by THALLS, by which a peace was brought about between the *Medes* and *Lydians*. Hiſtorical Eclipſe.
523	*July*	16	An Eclipſe of the Moon, which was followed by the death of CAMBYSES.
502	*Nov.*	19	An Eclipſe of the Moon, which was followed by the ſlaughter of the *Sabines*, and death of *Valerius Publicola*.
463	*April*	30	An Eclipſe of the Sun. The *Perſian* war, and the falling off of the *Perſians* from the *Egyptians*.

Before CHRIST.

431	*April* 25	An Eclipſe of the Moon, which was followed by a great famine at *Rome*; and the beginning of the *Peloponneſian* war.
431	*Auguſt* 3	A total Eclipſe of the Sun. A Comet and Plague at *Athens* *.
413	*Auguſt* 27	A total Eclipſe of the Moon. *Nicias* with his ſhip deſtroyed at *Syracuſe*.
394	*Auguſt* 14	An Eclipſe of the Sun. The *Perſians* beat by *Conon* in a ſea engagement.
168	*June* 21	A total Eclipſe of the Moon. The next day *Perſeus* King of *Macedonia* was conquered by *Paulus Emilius*.

After CHRIST.

59	*April* 30	An Eclipſe of the Sun. This is reckoned among the prodigies, on account of the murder of *Agrippinus* by *Nero*.
237	*April* 12	A total Eclipſe of the Sun. A ſign that the reign of the *Gordiani* would not continue long. A ſixth perſecution of the Chriſtians.
306	*July* 27	An Eclipſe of the Sun. The Stars were ſeen, and the Emperor *Conſtantius* died.
840	*May* 4	A dreadful Eclipſe of the Sun. And *Lewis* the Pious died within ſix months after it.
1009	———	An Eclipſe of the Sun. And *Jeruſalem* taken by the *Saracens*.
1133	*Auguſt* 2	A terrible Eclipſe of the Sun. The Stars were ſeen. A ſchiſm in the church, occaſioned by there being three Popes at once.

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* This Eclipſe happened in the firſt year of the *Peloponneſian* war.

329. I have not cited one half of RICCIOLUS's liſt of portentous Eclipſes; and for the ſame reaſon that he declines giving any more of them than what that liſt contains; namely, that it is moſt diſagreeable to dwell any longer on ſuch nonſenſe, and as much as poſſible to avoid tiring the reader: the ſuperſtition of the antients may be ſeen by the few here copied. My author farther ſays, that there were treatiſes written to ſhew againſt what regions the malevolent effects of any particular Eclipſe was aimed: and the writers affirmed, that the effects of an Eclipſe of the Sun continued as many years as the Eclipſe laſted hours; and that of the Moon as many months.

The ſuperſtitious notions of the antients with regard to Eclipſes.

330. Yet ſuch idle notions were once of no ſmall advantage to CHRISTOPHER COLUMBUS; who, in the year 1493, was driven on the iſland of *Jamaica*, where he was in the greateſt diſtreſs for want of proviſions, and was moreover refuſed any aſſiſtance from the inhabitants; on which he threatened them with a plague, and told them, that in token of it, there ſhould be an Eclipſe: which accordingly fell on the day he had foretold, and ſo terrified the Barbarians, that they ſtrove who ſhould be firſt in bringing him all ſorts of proviſions; throwing them at his feet, and imploring his forgiveneſs. RICCIOLUS's *Almageſt*, Vol. I. l. v. c. ii.

Very fortunate once for CHRISTOPHER COLUMBUS.

331. Eclipſes of the Sun are more frequent than of the Moon, becauſe the Sun's ecliptic limits are greater than the Moon's, § 317: yet we have more viſible Eclipſes of the Moon than of the Sun, becauſe Eclipſes of the Moon are ſeen from all parts of that Hemiſphere of the Earth which is next her, and are equally great to each of thoſe parts; but the Sun's Eclipſes are viſible only to that ſmall portion of the Hemiſphere next him whereon the Moon's ſhadow falls; as ſhall be explained by and by at large.

Why there are more viſible Eclipſes of the Moon than of the Sun.

332. The Moon's Orbit being elliptical, and the Earth in one of it's focuſes, ſhe is once at her

leaſt

PLATE XI. Fig. I.

Total and annular Eclipſes of the Sun.

leaſt diſtance from the Earth, and once at her greateſt, in every Lunation. When the Moon changes at her leaſt diſtance from the Earth, and ſo near the Node that her dark ſhadow falls upon the Earth, ſhe appears big enough to cover the whole * Diſc of the Sun from that part on which her ſhadow falls; and the Sun appears totally eclipſed there, as at *A*, for ſome minutes: but when the Moon changes at her greateſt diſtance from the Earth, and ſo near the Node that her dark ſhadow is directed towards the Earth, her diameter ſubtends a leſs angle than the Sun's; and therefore ſhe cannot hide his whole Diſc from any part of the Earth, nor does her ſhadow reach it at that time; and to the place over which the point of her ſhadow hangs, the Eclipſe is annular, as at *B*; the Sun's edge appearing like a luminous ring all around the body of the Moon. When the Change happens within 17 degrees of the Node, and the Moon at her mean diſtance from the Earth, the point of her ſhadow juſt touches the Earth, and ſhe eclipſeth the Sun totally to that ſmall ſpot whereon her ſhadow falls; but the darkneſs is not of a moment's continuance.

The longeſt duration of total Eclipſes of the Sun.

333. The Moon's apparent diameter when largeſt exceeds the Sun's when leaſt, only 1 minute 38 ſeconds of a degree: and in the greateſt Eclipſe of the Sun that can happen at any time and place, the total darkneſs continues no longer than whilſt the Moon is going 1 minute 38 ſeconds from the Sun in her Orbit; which is about 3 minutes and 13 ſeconds of an hour.

To how much of the Earth the Sun may be totally or partially eclipſed at once.

334. The Moon's dark ſhadow covers only a ſpot on the Earth's ſurface, about 180 *Engliſh* miles broad, when the Moon's diameter appears largeſt

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* Although the Sun and Moon are ſpherical bodies, as ſeen from the Earth they appear to be circular planes; and ſo would the Earth do, if it were ſeen from the Moon. The apparently flat ſurfaces of the Sun and Moon are called their *Diſcs* by Aſtronomers.

Plate XI.

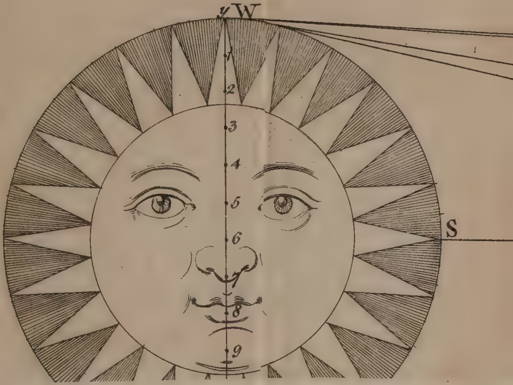

Plate XI.

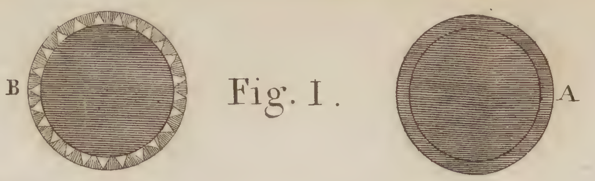

Fig. I.

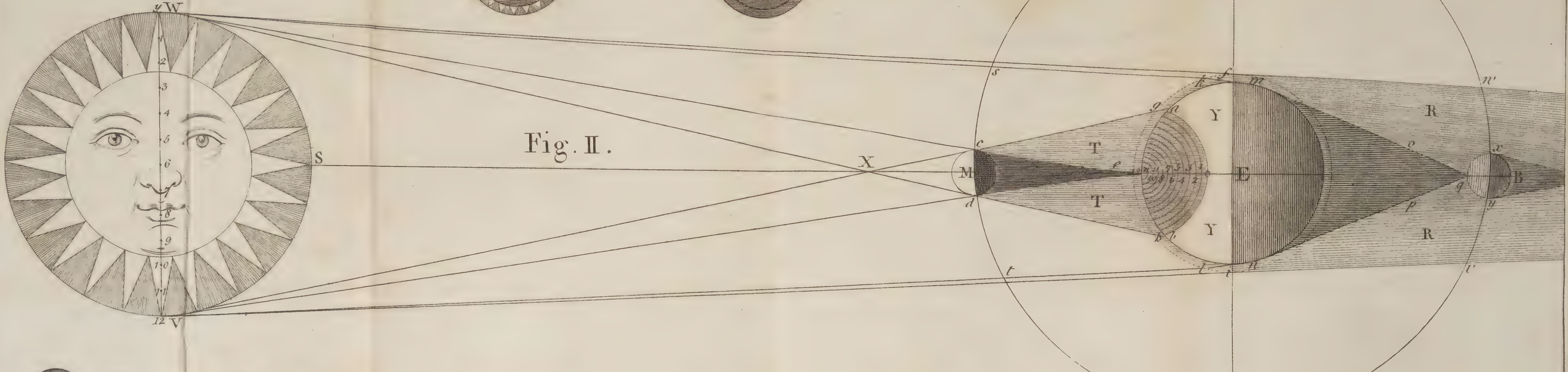

Fig. II.

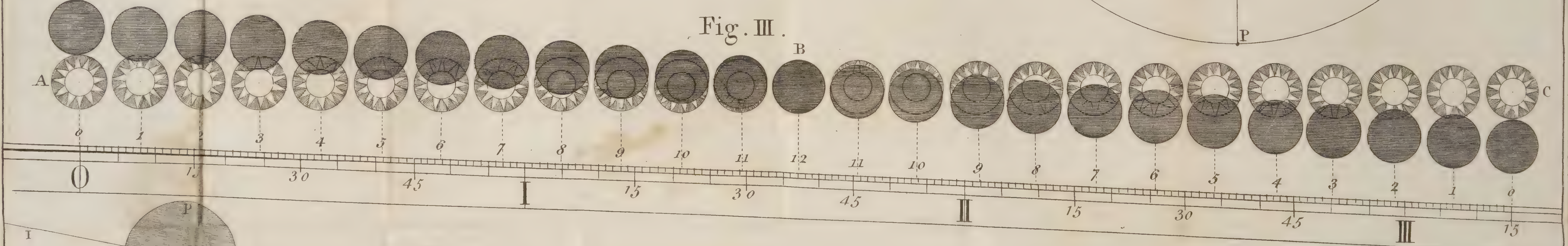

Fig. III.

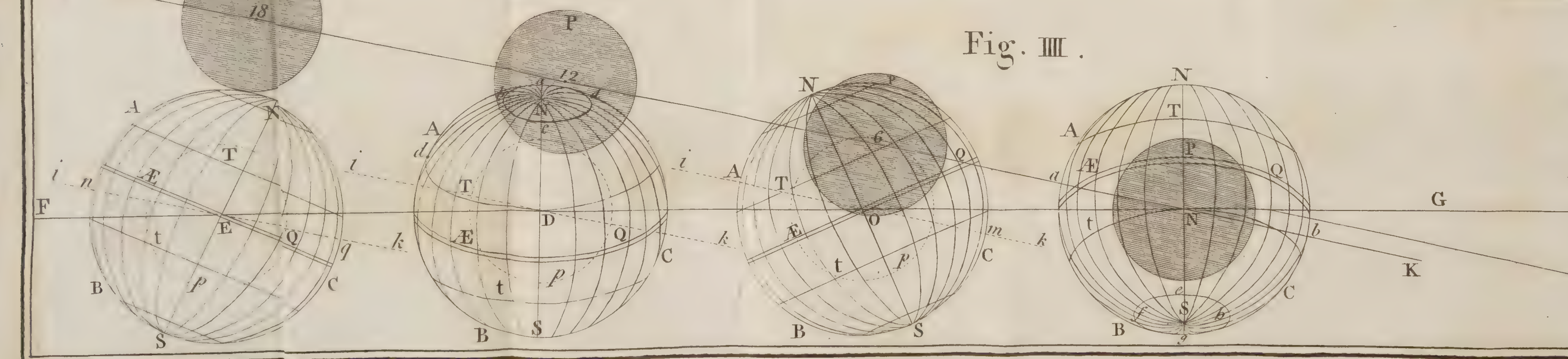

Fig. IIII.

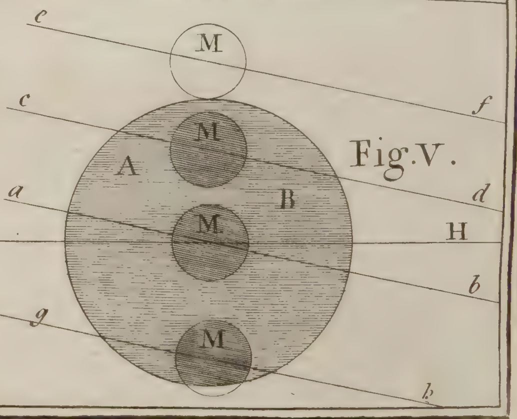

Fig. V.

J. Ferguson delin.
J. Mynde sculp.

PLATE XI.

and the Sun's leaſt; and the total darkneſs can extend no farther than the dark ſhadow covers. Yet the Moon's partial Shadow or Penumbra may then cover a circular ſpace 4900 miles diameter, within all which the Sun is more or leſs eclipſed, as the places are leſs or more diſtant from the Center of the Penumbra. When the Moon changes exactly in the Node, the Penumbra is circular on the Earth at the middle of the general Eclipſe; becauſe at that time it falls perpendicularly on the Earth's ſurface: but at every other moment it falls obliquely, and will therefore be elliptical; and the more ſo, as the time is longer before or after the middle of the general Eclipſe; and then, much greater portions of the Earth's ſurface are involved in the Penumbra.

Duration of general and particular Eclipſes.

335. When the Penumbra firſt touches the Earth, the general Eclipſe begins: when it leaves the Earth, the general Eclipſe ends: from the beginning to the end the Sun appears eclipſed in ſome part of the Earth or other. When the Penumbra touches any place, the Eclipſe begins at that place, and ends when the Penumbra leaves it. When the Moon changes in the Node, the Penumbra goes over the center of the Earth's Diſc as ſeen from the Moon; and conſequently, by deſcribing the longeſt line poſſible on the Earth, continues the longeſt upon it; namely, at a mean rate, 5 hours 50 minutes: more, if the Moon be at her greateſt diſtance from the Earth, becauſe ſhe then moves ſloweſt; leſs, if ſhe be at her leaſt diſtance, becauſe of her quicker motion.

Fig. II.

336. To make the laſt five articles and ſeveral other Phenomena plainer, let *S* be the Sun, *E* the Earth, *M* the Moon, and *A M P* the Moon's Orbit. Draw the right line *W c* 12 from the weſtern ſide of the Sun at *W*, touching the weſtern ſide of the Moon at *c*, and the Earth at 12: draw alſo the right line *V d* 12 from the eaſtern ſide of the Sun at *V*, touching the eaſtern ſide of the Moon at *d*,

the Earth at 12: the dark ſpace *c e* 12 *d* included between thoſe lines is the Moon's ſhadow, ending in a point at 12, where it touches the Earth; becauſe in this caſe the Moon is ſuppoſed to change at *M* in the middle between *A* the Apogee, or fartheſt point of her Orbit from the Earth, and *P* the Perigree, or neareſt point to it. For, had the point *P* been at *M*, the Moon had been nearer the Earth; and her dark ſhadow at *e* would have covered a ſpace upon it about 180 miles broad, and the Sun would have been totally darkened, as at *A* (Fig. I.) with ſome continuance: but had the point *A* (Fig. II.) been at *M*, the Moon would have been farther from the Earth, and her ſhadow would have ended in a point about *e*, and therefore the Sun would have appeared, as at *B* (Fig. I.) like a luminous ring all around the Moon. Draw the right lines *W X d b* and *V X c g*, touching the contrary ſides of the Sun and Moon, and ending on the Earth at *a* and *b*: draw alſo the right line *S X M* 12, from the center of the Sun's Diſc, through the Moon's center, to the Earth at 12; and ſuppoſe the two former lines *W X d b* and *V X c g* to revolve on the line *S X M* 12 as an Axis, and their points *a* and *b* will deſcribe the limits of the Penumbra *T T* on the Earth's ſurface, including the large ſpace *a* o *b* 12 *a*; within which the Sun appears more or leſs eclipſed, as the places are more or leſs diſtant from the verge of the Penumbra *a* o *b*.

The Moon's dark ſhadow, and Penumbra.

Digits, what.

Draw the right line *y* 12 acroſs the Sun's Diſc, perpendicular to *S X M* the Axis of the Penumbra: then, divide the line *y* 12 into twelve equal parts, as in the Figure, for the twelve * Digits of the Sun's diameter: and, at equal diſtances from the center of the Penumbra at 12 (on the Earth's ſurface *Y Y*) to it's edge *a* o *b*, draw twelve concentric Circles, as marked with the numeral Figures 1 2 3 4, &c. and remember that the Moon's motion

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* A Digit is a twelfth part of the diameter of the Sun and Moon.

tion in her Orbit *AMP* is from weſt to eaſt, as from *s* to *t*. Then,

PLATE XI. The different Phaſes of a ſolar Eclipſe.

To an obſerver on the Earth at *b*, the eaſtern limb of the Moon at *d* ſeems to touch the weſtern limb of the Sun at *W*, when the Moon is at *M*; and the Sun's Eclipſe begins at *b*, appearing as at *A* in Fig. III. at the left hand; but, at the ſame moment of abſolute time to an obſerver at *a* in Fig. II. the weſtern edge of the Moon at *c* leaves the eaſtern edge of the Sun at *V*, and the Eclipſe ends, as at the right hand *C* of Fig III. At the very ſame inſtant, to all thoſe who live on the Circle marked 1 on the Earth *E* in Fig. II, the Moon *M* cuts off or darkens a twelfth part of the Sun *S*, and eclipſes him one Digit, as at 1 in Fig. III: to thoſe who live on the Circle marked 2 in Fig. II, the Moon cuts off two twelfth parts of the Sun, as at 2 in Fig. III: to thoſe on the Circle 3, three parts; and ſo on to the center at 12 in Fig. II, where the Sun is centrally eclipſed, as at *B* in the middle of Fig. III; under which Figure there is a ſcale of hours and minutes, to ſhew at a mean rate how long it is from the beginning to the end of a central Eclipſe of the Sun on the parallel of *London*; and how many Digits are eclipſed at any particular time from the beginning at *A* to the middle at *B*, or the end at *C*. Thus, in 16 minutes from the beginning, the Sun is two Digits eclipſed; in an hour and five minutes, eight Digits; and in an hour and thirty-ſeven minutes, 12 Digits. Fig. III.

337. By Fig II. it is plain, that the Sun is totally or centrally eclipſed but to a ſmall part of the Earth at any time; becauſe the dark conical ſhadow *e* of the Moon *M* falls but on a ſmall part of the Earth: and that the partial Eclipſe is confined at that time to the ſpace included by the Circle *a o b*, of which only one half can be projected in the Figure, the other half being ſuppoſed to be hid by the convexity of the Earth *E*: and likewiſe, that no part of the Sun is eclipſed to the large ſpace *YY* Fig. II.

PLATE XI.

The Velocity of the Moon's ſhadow on the Earth.

of the Earth, becauſe the Moon is not between the Sun and any of that part of the Earth: and therefore to all that part the Eclipſe is inviſible. The Earth turns eaſtward on it's Axis, as from *g* to *h*, which is the ſame way that the Moon's ſhadow moves; but the Moon's motion is much ſwifter in her Orbit from *s* to *t*: and therefore, although Eclipſes of the Sun are of longer duration on account of the Earth's motion on it's Axis than they would be if that motion was ſtopt, yet in four minutes of time at moſt, the Moon's ſwifter motion carries her dark ſhadow quite over any place that it's center touches at the time of greateſt obſcuration. The motion of the ſhadow on the Earth's Diſc is equal to the Moon's motion from the Sun, which is about 30½ minutes of a degree every hour at a mean rate; but ſo much of the Moon's Orbit is equal to 30½ degrees of a great Circle on the Earth, § 320; and therefore the Moon's ſhadow goes 30½ degrees or 1830 geographical miles on the Earth in an hour, or 30½ miles in a minute, which is almoſt four times as ſwift as the motion of a cannon-ball.

Fig. IV.

Phenomena of the Earth as ſeen from the Sun or New Moon at different times of the year.

338. As ſeen from the Sun or Moon, the Earth's Axis appears differently inclined every day of the year, on account of keeping it's paralleliſm throughout it's annual courſe. Let *E*, *D*, *O*, *N* be the Earth at the two Equinoxes and the two Solſtices, *N S* it's Axis, *N* the North Pole, *S* the South Pole, *Æ Q* the Equator, *T* the tropic of Cancer, *t* the tropic of Capricorn, and *A B C* the Circumference of the Earth's enlightened Diſc as ſeen from the Sun or New Moon at theſe times. The Earth's Axis has the poſition *N E S* at the vernal Equinox, lying towards the right hand, as ſeen from the Sun or New Moon; it's Poles *N* and *S* being then in the Circumference of the Diſc; and the Equator and all it's parallels ſeem to be ſtraight lines, becauſe their planes paſs through the obſerver's eye looking down upon the Earth from the Sun or

Moon directly over *E*, where the Ecliptic *FG* interſects the Equator *Æ*. At the Summer Solſtice, the Earth's Axis has the poſition *N D S*; and that part of the Ecliptic *F G*, in which the Moon is then New, touches the Tropic of Cancer *T* at *D*. The North Pole *N* at that time inclining 23½ degrees towards the Sun, falls ſo many degrees within the Earth's enlightened Diſc, becauſe the Sun is then vertical to *D*, 23½ degrees north of the Equator *Æ Q*; and the Equator with all it's parallels ſeem elliptic curves bending downward, or towards the South Pole, as ſeen from the Sun: which Pole, together with 23½ degrees all round it, is hid behind the Diſc in the dark Hemiſphere of the Earth. At the autumnal Equinox, the Earth's Axis has the poſition *N O S*, lying to the left hand as ſeen from the Sun or New Moon, which are then vertical to *O*, where the Ecliptic cuts the Equator *Æ Q*. Both Poles now lie in the circumference of the Diſc, the North Pole juſt going to diſappear behind it, and the South Pole juſt entering into it; and the Equator with all it's parallels ſeem to be ſtraight lines, becauſe their planes paſs through the obſerver's eye, as ſeen from the Sun, and very nearly ſo as ſeen from the Moon. At the Winter Solſtice, the Earth's Axis has the poſition *N N S*; when it's South Pole *S* inclining 23½ degrees towards the Sun, falls 23½ degrees within the enlightened Diſc, as ſeen from the Sun or New Moon, which are then vertical to the Tropic of Capricorn *t*, 23½ degrees ſouth of the Equator *Æ Q*; and the Equator with all it's parallels ſeem elliptic curves bending upward; the North Pole being as far behind the Diſc in the dark Hemiſphere, as the South Pole is come into the light. The nearer that any time of the year is to the Equinoxes or Solſtices, the more it partakes of the Phenomena relating to them.

339. Thus it appears, that from the vernal equinox to the autumnal, the North Pole is enlightened;

PLATE XI.

Various poſitions of the Earth's Axis, as ſeen from the Sun at different times of the year.

ed; and the Equator and all it's parallels appear elliptical as ſeen from the Sun, more or leſs curved as the time is nearer to or farther from the Summer Solſtice; and bending downwards, or towards the South Pole; the reverſe of which happens from the autumnal Equinox to the vernal. A little conſideration will be ſufficient to convince the reader, that the Earth's Axis inclines towards the Sun at the Summer Solſtice; from the Sun at the Winter Solſtice; and ſidewiſe to the Sun at the Equinoxes; but towards the right hand, as ſeen from the Sun at the vernal Equinox; and towards the left hand at the autumnal. From the Winter to the Summer Solſtice, the Earth's Axis inclines more or leſs to the right hand, as ſeen from the Sun; and the contrary from the Summer to the Winter Solſtice.

How theſe poſitions affect ſolar Eclipſes.

340. The different poſitions of the Earth's Axis, as ſeen from the Sun at different times of the year, affect ſolar Eclipſes greatly with regard to particular places; yea ſo far as would make central Eclipſes which fall at one time of the year inviſible if they had fallen at another, even though the Moon ſhould always change in the Nodes, and at the ſame hour of the day: of which indefinitely various affections, we ſhall only give Examples for the times of the Equinoxes and Solſtices.

Fig. IV.

In the ſame Diagram, let *FG* be part of the Ecliptic, and *IK*, *ik*, *ik*, *ik* part of the Moon's Orbit; both ſeen edgewiſe, and therefore projected into right lines; and let the interſections *N*, *O*, *D*, *E* be one and the ſame Node at the above times, when the Earth has the forementioned different poſitions; and let the ſpace included by the Circles *P*, *p*, *p*, *p* be the Penumbra at theſe times, as it's center is paſſing over the center of the Earth's Diſc. At the Winter Solſtice, when the Earth's Axis has the poſition *NNS*, the center of the Penumbra *P* touches the Tropic of Capricorn *t* in *N* at the middle of the general Eclipſe; but no part of the Penumbra touches the Tropic of Cancer *T*. At the Summer Solſtice, when the Earth's Axis has the poſition *N D S* (*i D k* being then part of the Moon's Orbit, whoſe Node is at *D*) the Penumbra *p* has it's center at *D*, on the Tropic of Cancer *T*, at the middle of the general Eclipſe, and then no part of it touches the Tropic of Capricorn *t*. At the autumnal Equinox, the Earth's Axis has the poſition *N O S* (*i O k* being then part of the Moon's Orbit) and the Penumbra equally includes part of both Tropics *T* and *t* at the middle of the general Eclipſe: at the vernal Equinox it does the ſame, becauſe the Earth's Axis has the poſition *N E S*: but, in the former of theſe two laſt caſes, the Penumbra enters the Earth at *A*, north of the Tropic of Cancer *T*, and leaves it at *m*, ſouth of the Tropic of Capricorn *t*; having gone over the Earth obliquely ſouthward, as it's center deſcribed the line *AOm*: whereas, in the latter caſe, the Penumbra touches the Earth at *n*, ſouth of the Equator *Æ Q*, and deſcribing the line *n E q* (ſimilar to the former line *A O m* in open ſpace) goes obliquely northward over the Earth, and leaves it at *q*, north of the Equator.

In all theſe circumſtances, the Moon has been ſuppoſed to change at noon in her deſcending Node: had ſhe changed in her aſcending Node, the Phenomena would have been as various the contrary way, with reſpect to the Penumbra's going northward or ſouthward over the Earth. But becauſe the Moon changes at all hours, as often in one Node as in the other, and at all diſtances from them both at different times as it happens, the variety of the Phaſes of Eclipſes are almoſt innumerable, even at the ſame places; conſidering alſo how variouſly the ſame places are ſituated on the enlightened Diſc of the Earth, with reſpect to the Penumbra's motion, at the different hours when Eclipſes happen.

341. When

How much of the Penumbra falls on the Earth at different diſtances from the Nodes.

341. When the Moon changes 17 degrees ſhort of her deſcending Node, the Penumbra *P* 18 juſt touches the northern part of the Earth's Diſc, near the North Pole *N*; and, as ſeen from that place, the Moon appears to touch the Sun, but hides no part of him from ſight. Had the Change been as far ſhort of the aſcending Node, the Penumbra would have touched the ſouthern part of the Diſc near the South Pole *S*. When the Moon changes 12 degrees ſhort of the deſcending Node, more than a third part of the Penumbra *P* 12 falls on the northern parts of the Earth at the middle of the general Eclipſe: had ſhe changed as far paſt the ſame Node, as much of the other ſide of the Penumbra about *P* would have fallen on the ſouthern of the Earth; all the reſt in the *expanſum*, or open ſpace. When the Moon changes 6 degrees from the Node, almoſt the whole Penumbra *P* 6 falls on the Earth at the middle of the general Eclipſe. And laſtly, when the Moon changes in the Node at *N*, the Penumbra *P N* takes the longeſt courſe poſſible on the Earth's Diſc; it's center falling on the middle thereof, at the middle of the general Eclipſe. The farther the Moon changes from either Node, within 17 degrees of it, the ſhorter is the Penumbra's continuance on the Earth, becauſe it goes over a leſs portion of the Diſc, as is evident by the Figure.

The Earth's diurnal motion lengthens the duration of ſolar Eclipſes, which fall without the polar Circles.

342. The nearer that the Penumbra's center is to the Equator at the middle of the general Eclipſe, the longer is the duration of the Eclipſe at all thoſe places where it is central; becauſe, the nearer that any place is to the Equator, the greater is the Circle it deſcribes by the Earth's motion on it's Axis: and ſo, the place moving quicker, keeps longer in the Penumbra, whoſe motion is the ſame way with that of the place, though faſter, as has been already mentioned, § 337. Thus (ſee the Earth at *D* and the Penumbra at 12) whilſt the point *b* in the polar Circle *a b c d* is carried from *b*

to *c* by the Earth's diurnal motion, the point *d* on the Tropic of Cancer *T* is carried a much greater length from *d* to *D*: and therefore, if the Penumbra's center goes one time over *c* and another time over *D*, the Penumbra will be longer in paſſing over the moving place *d* than it was in paſſing over the moving place *b*. Conſequently, central Eclipſes about the Poles are of the ſhorteſt duration; and about the Equator the longeſt.

And ſhortens the duration of ſome which fall within theſe Circles.

343. In the middle of Summer, the whole frigid Zone included by the polar Circle *a b c d* is enlightened; and if it then happens that the Penumbra's center goes over the North Pole, the Sun will be eclipſed much the ſame number of Digits at *a* as at *c*; but whilſt the Penumbra moves eaſtward over *c*, it moves weſtward over *a*, becauſe, with reſpect to the Penumbra, the motions of *a* and *c* are contrary: for *c* moves the ſame way with the Penumbra towards *d*, but *a* moves the contrary way towards *b*; and therefore the Eclipſe will be of longer duration at *c* than at *a*. At *a* the Eclipſe begins on the Sun's eaſtern limb, but at *c* on his weſtern: at all places lying without the polar Circles, the Sun's Eclipſes begin on his weſtern limb, or near it, and end on or near his eaſtern. At thoſe places where the Penumbra touches the Earth, the Eclipſe begins with the riſing Sun, on the top of his weſtern or uppermoſt edge; and at thoſe places where the Penumbra leaves the Earth, the Eclipſe ends with the ſetting Sun, on the top of his eaſtern edge, which is then the uppermoſt, juſt at it's diſappearing in the Horizon.

The Moon has no Atmoſphere.

344. If the Moon were ſurrounded by an Atmoſphere of any conſiderable Denſity, it would ſeem to touch the Sun a little before the Moon made her appulſe to his edge, and we ſhould ſee a little faintneſs on that edge before it were eclipſed by the Moon: but as no ſuch faintneſs has been obſerved, at leaſt ſo far as I ever heard, it ſeems plain, that the Moon has no ſuch Atmoſphere as that

PLATE XI.

of the Earth. The faint ring of light ſurrounding the Sun in total Eclipſes, called by CASSINI *la Chevelure du Soleil*, ſeems to be the Atmoſphere of the Sun; becauſe it has been obſerved to move equally with the Sun, not with the Moon.

345. Having been ſo prolix concerning Eclipſes of the Sun, we ſhall drop that ſubject at preſent, and proceed to the doctrine of lunar Eclipſes; which, being more ſimple, may be explained in leſs time.

Eclipſes of the Moon.

That the Moon can never be eclipſed but at the time of her being Full, and the reaſon why ſhe is not eclipſed at every Full, has been ſhewn already, § 316, 317. Let *S* be the Sun, *E* the Earth, *R R* the Earth's ſhadow, and *B* the Moon in oppoſition to the Sun: in this ſituation the Earth intercepts the Sun's light in it's way to the Moon; and when the Moon touches the Earth's ſhadow at *v*, ſhe begins to be eclipſed on her eaſtern limb *x*, and continues eclipſed until her weſtern limb *y* leaves the ſhadow at *w*: at *B* ſhe is in the middle of the ſhadow, and conſequently in the middle of the Eclipſe.

Fig. II.

346. The Moon when totally eclipſed is not inviſible, if ſhe be above the Horizon and the Sky be clear; but appears generally of a duſky colour like tarniſhed copper, which ſome have thought to be the Moon's native light. But the true cauſe of her being viſible is the ſcattered beams of the Sun, bent into the Earth's ſhadow by going through the Atmoſphere; which, being more denſe near the Earth than at conſiderable heights above it, refracts or bends the Sun's rays more inward, § 179, the nearer they are paſſing by the Earth's ſurface, than thoſe rays which go through higher parts of the Atmoſphere, where it is leſs denſe according to it's height, until it be ſo thin or rare as to loſe it's refractive power. Let the Circle *f g h i*, concentric to the Earth, include the Atmoſphere whoſe refractive power vaniſhes at the heights *f*

Why the Moon is viſible in a total Eclipſe.

and

PLATE XI.

and *i*; ſo that the rays *Wfw* and *Viv* go on ſtraight without ſuffering the leaſt refraction: But all thoſe rays which enter the Atmoſphere between *f* and *k*, and between *i* and *l*, on oppoſite ſides of the Earth, are gradually more bent inward as they go through a greater portion of the Atmoſphere, until the rays *Wk* and *Vl* touching the Earth at *m* and *n*, are bent ſo much as to meet at *q*, a little ſhort of the Moon; and therefore the dark ſhadow of the Earth is contained in the ſpace *moqpn*, where none of the Sun's rays can enter: all the reſt *R R*, being mixed by the ſcattered rays which are refracted as above, is in ſome meaſure enlightened by them; and ſome of thoſe rays falling on the Moon, give her the colour of tarniſhed copper, or of iron almoſt red hot. So that if the Earth had no Atmoſphere, the Moon would be as inviſible in total Eclipſes as ſhe is when New. If the Moon were ſo near the Earth as to go into it's dark ſhadow, ſuppoſe about *po*, ſhe would be inviſible during her ſtay in it; but viſible before and after in the fainter ſhadow *R R*.

Why the Sun and Moon are ſometimes viſible when the Moon is totally eclipſed.

347. When the Moon goes through the center of the Earth's ſhadow, ſhe is directly oppoſite to the Sun: yet the Moon has been often ſeen totally eclipſed in the Horizon when the Sun was alſo viſible in the oppoſite part of it: for, the horizontal refraction being almoſt 34 minutes of a of a degree, § 181, and the diameter of the Sun and Moon being each at a mean ſtate but 32 minutes, the refraction cauſes both Luminaries to appear above the Horizon when they are really below it, § 179.

Fig. V.

348. When the Moon is Full at 12 degrees from either of her Nodes, ſhe juſt touches the Earth's ſhadow, but enters not into it. Let *G H* be the Ecliptic, *ef* the Moon's Orbit where ſhe is 12 degrees from the Node at her Full; *cd* her Orbit where ſhe is 6 degrees from the Node, *ab* her Orbit where ſhe is Full in the Node, *AB* the Earth's

Duration of central Eclipſes of the Moon.

Earth's ſhadow, and *M* the Moon. When the Moon deſcribes the line *e f*, ſhe juſt touches the ſhadow, but does not enter into it; when ſhe deſcribes the line *c d*, ſhe is totally though not centrally immerſed in the ſhadow; and when ſhe deſcribes the line *a b*, ſhe paſſes by the Node at *M* in the center of the ſhadow, and takes the longeſt line poſſible, which is a diameter, through it: and ſuch an Eclipſe being both total and central is of the longeſt duration, namely, 3 hours 57 minutes 6 ſeconds from the beginning to the end, if the Moon be at her greateſt diſtance from the Earth: and 3 hours 37 minutes 26 ſeconds, if ſhe be at her leaſt diſtance. The reaſon of this difference is, that when the Moon is fartheſt from the Earth, ſhe moves the ſloweſt; and when neareſt to it, quickeſt.

Digits.

349. The Moon's diameter, as well as the Sun's, is ſuppoſed to be divided into twelve equal parts, called *Digits*; and ſo many of theſe parts as are darkened by the Earth's ſhadow, ſo many Digits is the Moon eclipſed. All that the Moon is eclipſed above 12 Digits, ſhew how far the ſhadow of the Earth is over the body of the Moon, on that edge to which ſhe is neareſt at the middle of the Eclipſe.

Why the beginning and end of a lunar Eclipſe is ſo difficult to be determined by obſervation.

350. It is difficult to obſerve exactly either the beginning or ending of a lunar Eclipſe, even with a good Teleſcope; becauſe the Earth's ſhadow is ſo faint, and ill defined about the edges, that when the Moon is either juſt touching or leaving it, the obſcuration of her limb is ſcarce ſenſible; and therefore the niceſt obſervers can hardly be certain to four or five ſeconds of time. But both the beginning and ending of ſolar Eclipſes are viſibly inſtantaneous; for the moment that the edge of the Moon's Diſc touches the Sun's, his roundneſs ſeems a little broke on that part; and the moment ſhe leaves it, he appears perfectly round again.

351. In Aſtronomy, Eclipſes of the Moon are of great uſe for aſcertaining the periods of her motions; eſpecially ſuch Eclipſes as are obſerved to be alike in all circumſtances, and have long intervals of time between them. In Geography, the Longitudes of places are found by Eclipſes, as already ſhewn in the eleventh chapter: but for this purpoſe Eclipſes of the Moon are more uſeful than thoſe of the Sun, becauſe they are more frequently viſible, and the ſame lunar Eclipſe is of equal largeneſs and duration at all places where it is ſeen. In Chronology, both ſolar and lunar Eclipſes ſerve to determine exactly the time of any paſt event: for there are ſo many particulars obſervable in every Eclipſe, with reſpect to it's quantity, the places where it is viſible (if of the Sun) and the time of the day or night; that it is impoſſible there can be two ſolar Eclipſes in the courſe of many ages which are alike in all circumſtances.

The uſe of Eclipſes in Aſtronomy, Geography, and Chronology.

352. From the above explanation of the doctrine of Eclipſes it is evident, that the darkneſs at our SAVIOUR's crucifixion was ſupernatural. For he ſuffered on the day on which the Paſſover was eaten by the *Jews*, on which day it was impoſſible that the Moon's ſhadow could fall on the Earth; for the *Jews* kept the Paſſover at the time of Full Moon: nor does the darkneſs in total Eclipſes of the Sun laſt above four minutes in any place, § 333, whereas the darkneſs at the crucifixion laſted three hours, *Matt.* xxviii. 15. and overſpread at leaſt all the land of *Judea*.

The darkneſs at our SAVIOUR's crucifixion ſupernatural.

CHAP. XIX.

Shewing the Principles on which the following Aſtronomical Tables are conſtructed, and the Method of calculating the Times of New and Full Moons and Eclipſes by them.

353. THE nearer that any object is to the eye of an obſerver, the greater is the angle under which it appears: the farther from the eye, the leſs.

The diameters of the Sun and Moon ſubtend different angles at different times. And, at equal intervals of time, theſe angles are once at the greateſt, and once at the leaſt, in ſomewhat more than a compleat revolution of the Luminary through the Ecliptic, from any given fixed Star to the ſame Star again.—This proves that the Sun and Moon are conſtantly changing their diſtances from the Earth; and that they are once at their greateſt diſtance, and once at their leaſt, in little more than a compleat revolution.

The gradual differences of theſe angles are not what they would be, if the Luminaries moved in circular Orbits, the Earth being ſuppoſed to be placed at ſome diſtance from the center: but they agree perfectly with elliptic orbits, ſuppoſing the lower focus of each orbit to be at the center of the Earth.

The fartheſt point of each Orbit from the Earth's center is called the *Apogee*, and the neareſt point is called the *Perigee.*—Theſe points are directly oppoſite to each other.

Aſtronomers divide each Orbit into 12 equal parts, called *Signs*; each ſign into 30 equal parts, called *Degrees*; each degree into 60 equal parts, called *Minutes*; and every minute into 60 equal parts, called *Seconds*. The diſtance of the Sun or Moon from any given point of it's orbit, is reckoned in ſigns, degrees, minutes, and ſeconds. Here we mean the diſtance that the Luminary has moved through from any given point; not the ſpace it is ſhort thereof in coming round again, though ever ſo little.

The diſtance of the Sun or Moon from it's Apogee, at any given time, is called it's *mean Anomaly:* ſo that, in the Apogee, the anomaly is nothing; in the Perigee, it is ſix ſigns.

The motions of the Sun and Moon are obſerved to be continually accelerated from the Apogee to the Perigee, and as gradually retarded from the Perigee to the Apogee; being ſloweſt of all when the mean anomaly is nothing, and ſwifteſt of all when it is ſix ſigns.

When the Luminary is in it's Apogee or Perigee, it's place is the ſame as it would be, if it's motion were equable in all parts of it's Orbit.—The ſuppoſed equable motions are called *mean*; the unequable are juſtly called the *true*.

The mean place of the Sun or Moon, is always forwarder than the true place *, whilſt the Luminary is moving from it's Apogee to it's Perigee; and the true place is always forwarder than the mean, whilſt the Luminary is moving from it's Perigee to it's Apogee.—In the former caſe, the anomaly is always leſs than ſix ſigns; and in the latter caſe, more.

It has been found, by a long ſeries of obſervations, that the Sun goes through the Ecliptic, from the *Vernal Equinox* to the ſame Equinox again, in 365 days 5 hours 48 minutes 55 ſeconds: from the *firſt Star of Aries* to the ſame Star again, in 365 days 6 hours 9 minutes 24 ſeconds: and from his *Apogee* to the ſame again, in 365 days 6 hours 14 minutes 0 ſeconds.—The firſt of theſe is called the *Solar Year*, the ſecond the *Sydereal Year*, and the third the *Anomaliſtic Year*. So that the Solar Year is 20 minutes 29 ſeconds ſhorter than the Sydereal; and the Sydereal Year is 4 minutes 36 ſeconds ſhorter than the Anomaliſtic.—Hence it appears, that the *Equinoctial Point*, or interſection of the Ecliptic and Equator at the beginning of Aries, goes backward with reſpect to the fixed Stars, and that the Sun's Apogee goes forward.

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* The point of the Ecliptic in which the Sun or Moon is, at any given moment of time, is called the *place* of the Sun or Moon at that time.

It is alſo obſerved, that the Moon goes through her Orbit, from any given fixed Star to the ſame Star again, in 27 days 7 hours 43 minutes 4 ſeconds, at a mean rate: from her Apogee to her Apogee again, in 27 days, 13 hours 18 minutes 43 ſeconds: and from the Sun to the Sun again, in 29 days 12 hours 44 minutes $3\frac{1}{20}$ ſeconds.—This ſhews, that the Moon's Apogee moves forward in the Ecliptic, and *that* at a much quicker rate than the Sun's Apogee does; ſince the Moon is 5 hours 55 minutes 39 ſeconds longer in revolving from her Apogee to her Apogee again, than from any Star to the ſame Star again.

The Moon's Orbit croſſes the Ecliptic in two oppoſite points, which are called her *Nodes*: and it is obſerved that ſhe revolves ſooner from any Node to the ſame Node again, than from any Star to the ſame Star again, by 2 hours 38 minutes 27 ſeconds, which ſhews that her Nodes move backward, or contrary to the order of ſigns, in the Ecliptic.

The time in which the Moon revolves from the Sun to the Sun again (or from change to change) is called a *Lunation*; which, according to Dr. Pound's mean meaſures, would always conſiſt of 29 days 12 hours 44 minutes 3 ſeconds 2 thirds 58 fourths, if the motions of the Sun and Moon were always equable *.—Hence, 12 mean Lunations

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* We have thought proper to keep by Dr. *Pound*'s length of a mean Lunation, becauſe his numbers come nearer to the times of the antient Eclipſes, than *Meyer*'s do, without allowing for the Moon's acceleration.

tions contain 354 days 8 hours 48 minutes 36 ſeconds 35 thirds 40 fourths, which is 10 days 21 hours 11 minutes 23 ſeconds 24 thirds 20 fourths leſs than the length of a common *Julian year*, conſiſting of 365 days 6 hours: and 13 mean Lunations contain 383 days 21 hours 32 minutes 39 ſeconds 38 thirds 38 fourths, which exceeds the length of a common *Julian year*, by 18 days 15 hours 32 minutes 39 ſeconds 38 thirds 38 fourths.

The mean time of New Moon being found for any given year and month, as ſuppoſe for *March* 1700, Old Stile, if this mean New Moon falls later than the 11th day of *March*, then, 12 mean Lunations added to the time of this mean New Moon, will give the time of the mean New Moon in *March* 1701, after having thrown off 365 days.—But, when the mean New Moon happens to be before the 11th of *March*, we muſt add 13 mean Lunations, in order to have the time of mean New Moon in *March* the year following: always taking care to ſubtract 365 days in common years, and 366 days in leap-years, from the ſum of this addition.

Thus, *A. D.* 1700, Old Stile, the time of mean New Moon in *March* was the 8th day, at 16 hours 11 minutes 25 ſeconds after the noon of that day (*viz.* at 11 minutes 25 ſeconds paſt IV in the morning of the 9th day, according to common reckoning.) To this we muſt add 13 mean Lunations, or 383 days 21 hours 32 minutes 39 ſeconds 38 thirds 38 fourths, and the ſum will be 392 days 13 hours 44 minutes 4 ſeconds 38 thirds 38 fourths; from which ſubtract 365 days, becauſe the year 1701 is a common year, and there will remain 27 days 13 hours 44 minutes 4 ſeconds 38 thirds 38 fourths for the time of mean New Moon in *March*, *A. D.* 1701.

Carrying on this addition and ſubtraction till *A. D.* 1703, we find the time of mean New Moon in *March* that year, to be on the 6th day, at 7 hours 21 minutes 17 ſeconds 49 thirds 46 fourths paſt noon; to which add 13 mean Lunations, and the ſum will be 390 days 4 hours 53 minutes 57 ſeconds 28 thirds 20 fourths; from which ſubtract 366 days, becauſe the year 1704 is a leap-year, and there will remain 24 days 4 hours 53 minutes 57 ſeconds 28 thirds 20 fourths, for the time of mean New Moon in *March*, *A. D.* 1704.

In this manner was the firſt of the following Tables conſtructed to ſeconds, thirds and fourths; and then wrote out to the neareſt ſeconds.—The reaſon why we choſe to begin the year with *March*, was to avoid the inconvenience of adding a day to the tabular time in leap-years after *February*, or ſubtracting a day therefrom in *January* and *February* in thoſe years; to which all tables of this kind are ſubject, which begin the year with *January*, in calculating the times of New or Full Moons.

The mean anomalies of the Sun and Moon, and the Sun's mean motion from the aſcending Node of the Moon's Orbit, are ſet down in Table III. from one to 13 mean Lunations.—Theſe Numbers, for 13 Lunations, being added to the radical anomalies of the Sun and Moon, and to the Sun's mean diſtance from the aſcending Node, at the time of mean New Moon in *March* 1700, (Table I.) will give their mean anomalies, and the Sun's mean diſtance from the Node, at the time of mean New Moon in *March* 1701; and being added for 12 Lunations to thoſe for 1701, give them for the time of mean New Moon in *March* 1702. And ſo on, as far as you pleaſe to continue the Table (which is here carried on to the year 1800) always throwing off 12 ſigns when their ſum exceeds 12, and ſetting down the remainder as the proper quantity.

If the Numbers belonging to *A. D.* 1700 (in Table I.) be ſubtracted from thoſe belonging to 1800, we ſhall have their whole differences in 100 compleat Julian years; which accordingly we find to be 4 days 8 hours 10 minutes 52 ſeconds 15 thirds 40 fourths, with reſpect to the time of mean New Moon.—Theſe being added together 60 times (always taking care to throw off a whole Lunation when the days exceed 29½) making up 60 centuries, or 6000 years, as in Table VI, which was carried on to ſeconds, thirds, and fourths; and then wrote out to the neareſt ſeconds. In the ſame manner were the reſpective anomalies and the Sun's diſtance from the Node found, for theſe centurial years; and then (for want of room) wrote out only to the neareſt minutes, which is ſufficient in whole centuries.—By means of theſe two Tables, we may find the time of any mean New Moon in *March*, together with the anomalies of the Sun and Moon, and the Sun's diſtance from the Node, at theſe times, within the limits of 6000 years, either before or after any given year in the 18th century; and the mean time of any New or Full Moon in any given month after *March*, by means of the third and fourth Tables, within the ſame limits, as ſhewn in the precepts for calculation.

Thus it would be a very eaſy matter to calculate the time of any New or Full Moon, if the Sun and Moon moved equably in all parts of their Orbits.—But we have already ſhewn that their places are never the ſame as they would be by equable motions, except when they are in Apogee or Perigee; which is, when their mean anomalies are either nothing, or ſix ſigns: and that their mean places are always forwarder than their true places, whilſt the anomaly is leſs than ſix ſigns; and their true places are forwarder than the mean, whilſt the anomaly is more.

Hence it is evident, that whilſt the Sun's anomaly is leſs than ſix ſigns, the Moon will overtake him, or be oppoſite to him, ſooner than ſhe could if his motion were equable; and later whilſt his anomaly is more than ſix ſigns.—The greateſt difference that can poſſibly happen between the mean

and

and true time of New or Full Moon, on account of the inequality of the Sun's motion, is 3 hours 48 minutes 28 ſeconds: and that is, when the Sun's anomaly is either 3 ſigns 1 degree, or 8 ſigns 29 degrees; ſooner in the firſt caſe, and later in the laſt.—In all other ſigns and degrees of anomaly, the difference is gradually leſs, and vaniſhes when the anomaly is either nothing or ſix ſigns.

The Sun is in his Apogee on the 30th of *June*, and in his Perigee on the 30th of *December*, in the preſent age: ſo that he is nearer the Earth in our winter than in our ſummer.—The proportional difference of diſtance, deduced from the difference of the Sun's apparent diameter at theſe times, is as 983 to 1017.

The Moon's orbit is dilated in winter, and contracted in ſummer; therefore, the Lunations are longer in winter than in ſummer. The greateſt difference is found to be 22 minutes 29 ſeconds: the Lunations increaſing gradually in length whilſt the Sun is moving from his Apogee to his Perigee, and decreaſing in length whilſt he is moving from his Perigee to his Apogee.—On this account, the Moon will be later every time in coming to her conjunction with the Sun, or being in oppoſition to him, from *December* till *June*, and ſooner from *June* till *December*, than if her orbit had continued of the ſame ſize all the year round.

As both theſe differences depend on the Sun's anomaly, they may be fitly put together into one Table, and called *The annual, or firſt equation of the mean to the true* * *ſyzygy* (ſee Table VII.) This equational difference is to be ſubtracted from the time of the mean ſyzygy when the Sun's anomaly is leſs than ſix ſigns, and added when the anomaly is more.—At the greateſt, it is 4 hours 10 minutes 57 ſeconds, *viz.* 3 hours 48 minutes 28 ſeconds, on account of the Sun's unequal motion, and 22 minutes 29 ſeconds, on account of the dilatation of the Moon's orbit.

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* The word *ſyzygy* ſignifies both the conjunction and oppoſition of the Sun and Moon.

This compound equation would be ſufficient for reducing the mean time of New or Full Moon to the true time thereof, if the Moon's orbit were of a circular form, and her motion quite equable in it.—But the Moon's orbit is more elliptical than the Sun's, and her motion in it ſo much the more unequal. The difference is ſo great, that ſhe is ſometimes in conjunction with the Sun, or in oppoſition to him, ſooner by 9 hours 47 minutes 54 ſeconds, than ſhe would be if her motion were equable; and at other times as much later.—The former happens when her mean anomaly is 9 ſigns 4 degrees, and the latter when it is 2 ſigns 26 degrees. *See* Table IX.

At different diſtances of the Sun from the Moon's Apogee, the figure of the Moon's orbit becomes different.—It is longeſt of all, or moſt excentric, when the Sun is in the ſame ſign and degree either with the Moon's Apogee or Perigee; ſhorteſt of all, or leaſt excentric, when the Sun's diſtance from the Moon's Apogee is either three ſigns or nine ſigns; and at a mean ſtate when the diſtance is either 1 ſign 15 degrees, 4 ſigns 15 degrees, 7 ſigns 15 degrees, or 10 ſigns 15 degrees.—When the Moon's orbit is at it's greateſt excentricity, her apogeal diſtance from the Earth's center is to her perigeal diſtance therefrom, as 1067 is to 933; when leaſt excentric, as 1043 is to 957; and when at the mean ſtate, as 1055 is to 945.

But the Sun's diſtance from the Moon's Apogee is equal to the quantity of the Moon's mean anomaly at the time of New Moon, and by the addition of ſix ſigns, it becomes equal in quantity to the Moon's mean anomaly at the time of Full Moon.—Therefore, a table may be conſtructed ſo as to anſwer to all the various inequalities depending on the different excentricities of the Moon's orbit, in the ſyzygies; and called *The ſecond equation of the*

the mean to the true ſyzygy (ſee Table IX.) and the Moon's anomaly, when equated by Table VIII. may be made the proper argument for taking out this ſecond equation of time; which muſt be added to the former equated time, when the Moon's anomaly is leſs than ſix ſigns, and ſubtracted when the anomaly is more.

There are ſeveral other inequalities in the Moon's motion, which ſometimes bring on the true ſyzygy a little ſooner, and at other times keep it back a little later, than it would otherwiſe be: but they are ſo ſmall, that they may be all omitted except two; the former of which (*ſee* Table X.) depends on the difference between the anomalies of the Sun and Moon in the ſyzygies, and the latter (*ſee* Table XI.) depends on the Sun's diſtance from the Moon's Nodes at theſe times.—The greateſt difference ariſing from the former, is 4 minutes 58 ſeconds; and from the latter, 1 minute 34 ſeconds.

Having deſcribed the Phenomena ariſing from the inequalities of the Solar and Lunar Motions, we ſhall now ſhew the reaſons of theſe inequalities.

In all calculations relating to the Sun and Moon, we conſider the Sun as a moving body, and the Earth as a body at reſt; ſince all the appearances are the ſame, whether it be the Sun or the Earth that moves.—But the truth is, that the Sun is at reſt, and the Earth moves round him once a year, in the plane of the Ecliptic. Therefore, whatever ſign and degree of the Ecliptic the Earth is in, at any given time, the Sun will then appear to be in the oppoſite ſign and degree.

The nearer that any body is to the Sun, the more it is attracted by him; and this attraction increaſes as the ſquare of the diſtance diminiſhes; and *vice verſâ.*

The Earth's annual Orbit is elliptical, and the Sun is placed in one of it's focuſes. The remoteſt point of the Earth's orbit from the Sun, is called *The Earth's Aphelion*; and the neareſt point of the Earth's orbit to the Sun, is called *The Earth's Perihelion.*—When the Earth is in it's Aphelion, the Sun appears to be in it's Apogee; and when the Earth is in it's Perihelion, the Sun appears to be in it's Perigee.

As the Earth moves from it's Aphelion to it's Perihelion, it is conſtantly more and more attracted by the Sun; and this attraction, by conſpiring in ſome degree with the Earth's motion, muſt neceſſarily accelerate it. But as the Earth moves from it's Perihelion to it's Aphelion, it is continually leſs and leſs attracted by the Sun; and as this attraction acts then juſt as much againſt the Earth's motion, as it acted for it in the other half of the Orbit, it retards the motion in the like degree.—The faſter the Earth moves, the faſter will the Sun appear to move; the ſlower the Earth moves, the ſlower is the Sun's apparent motion.

The Moon's orbit is alſo elliptical, and the Earth keeps conſtantly in one of it's focuſes.—The Earth's attraction has the ſame kind of influence on the Moon's motion, as the Sun's attraction has on the motion of the Earth: and therefore, the Moon's motion muſt be continually accelerated whilſt ſhe is paſſing from her Apogee to her Perigee; and as gradually retarded in moving from her Perigee to her Apogee.

At the time of New Moon, the Moon is nearer the Sun than the Earth is at that time, by the whole ſemidiameter of the Moon's orbit; which, at a mean ſtate, is 240,000 miles: and at the Full, ſhe is as much farther from the Sun than the Earth then is.—Conſequently, the Sun attracts the Moon more than it attracts the Earth in the former caſe, and leſs in the latter. The difference is greateſt when the Earth is neareſt the Sun, and leaſt when it is fartheſt from him. The obvious reſult of this is, that as the Earth is neareſt to the Sun in winter, and fartheſt from him in ſummer, the Moon's orbit muſt be dilated in winter, and contracted in ſummer.

Theſe are the principal cauſes of the difference of time, that generally happens between the mean and true times of conjunction or oppoſition of the Sun and Moon. As to the other two differences, *viz.* thoſe which depend on the difference between the anomalies of the Sun and Moon, and upon the Sun's diſtance from the lunar Nodes, in the ſyzygies, they are owing to the different degrees of attraction of the Sun and Earth upon the Moon, at greater or leſs diſtances, according to their reſpective anomalies, and to the poſition of the Moon's Nodes with reſpect to the Sun.

If ever it ſhould happen, that the anomalies of both the Sun and Moon were either nothing or ſix ſigns, at the mean time of New or Full Moon, and the Sun ſhould then be in conjunction with either of the Moon's Nodes, all the above-mentioned equations would vaniſh, and the mean and true time of the ſyzygy would coincide. But if ever this circumſtance did happen, we cannot expect the like again in many ages afterward.

TABLE I. *The mean Time of New Moon in* March, *Old Stile; with the mean Anomalies of the Sun and Moon, and the Sun's mean Diſtance from the Moon's Aſcending Node, from* A. D. 1700 *to* A. D. 1800 *incluſive.*

Y. of Chr.	Mean New Moon in March.				Sun's mean Anomaly.				Moon's mean Anomaly.				Sun's mean Diſt. from the Node.			
	D.	H.	M.	S.	s	o	′	″	s	o	′	″	s	o	′	″
1700	8	16	11	2[illegible]	8	19	58	48	1	22	30	37	6	14	31	7
1701	27	13	44	5	9	8	20	59	0	28	7	42	7	23	14	8
1702	16	22	32	41	8	27	36	51	11	7	55	47	8	1	10	55
1703	6	7	21	18	8	16	52	43	9	17	43	52	8	9	19	42
1704	24	4	53	57	9	5	14	54	8	23	20	57	9	18	2	43
1705	13	13	42	34	8	24	30	4[illegible]	7	3	9	2	9	26	5	30
1706	2	22	31	11	8	13	46	39	5	12	57	7	10	4	8	17
1707	21	20	3	50	9	2	8	5[illegible]	4	18	34	13	11	12	51	18
1708	10	4	52	27	8	21	24	43	2	28	22	18	11	20	54	5
1709	29	2	25	7	9	9	46	54	2	3	59	24	0	29	37	6
1710	18	11	13	43	8	29	2	47	0	13	47	30	1	7	39	54
1711	7	20	2	20	8	18	18	39	10	23	35	36	1	15	42	41
1712	25	17	34	59	9	6	40	51	9	29	12	42	2	14	25	43
1713	15	2	23	36	8	25	56	43	8	9	0	47	3	2	28	30
1714	4	11	12	13	8	15	12	35	6	18	48	52	3	10	21	1
1715	23	8	44	52	9	3	34	47	5	24	25	57	4	19	14	18
1716	11	17	33	29	8	22	50	39	4	4	14	2	4	27	17	5
1717	1	2	22	5	8	12	6	3[illegible]	2	14	2	8	5	5	19	52
1718	19	23	54	45	9	0	28	44	1	19	39	13	6	14	2	5
1719	9	8	43	22	8	19	44	37	11	29	27	18	6	22	5	41
1720	27	6	16	1	9	8	6	49	11	5	4	24	8	0	48	42
1721	16	15	4	38	8	27	22	41	9	14	52	29	8	8	51	29
1722	5	23	53	14	8	16	38	35	7	24	40	34	8	16	54	16
1723	24	21	25	54	9	5	0	45	7	0	17	40	9	25	37	18
1724	13	6	14	31	8	24	16	37	5	10	5	45	10	3	40	5
1725	2	15	3	7	8	13	32	29	3	19	53	50	10	11	42	52
1726	21	12	35	47	9	1	54	41	2	25	30	56	11	20	25	5[illegible]
1727	10	21	24	23	8	21	10	34	1	5	19	1	11	28	28	41
1728	28	18	57	3	9	9	52	4	0	10	56	7	1	7	11	42
1729	18	3	45	40	8	28	48	39	10	20	44	12	1	15	14	29
1730	7	12	34	16	8	18	4	31	9	0	32	17	1	23	17	16
1731	26	10	6	56	9	6	26	42	8	6	9	23	3	2	0	17
1732	14	18	55	3[illegible]	8	25	42	34	6	15	57	[illegible]	3	10	3	4

TABLE

TABLE I. *continued. Old Stile.*

Y. of Chr.	Mean New Moon in March.				Sun's mean Anomaly.				Moon's mean Anomaly.				Sun's mean Diſt. from the Node.			
	D.	H.	M.	S.	s	°	′	″	s	°	′	″	s	°	′	
1733	4	3	44	9	8	14	58	26	4	25	45	33	3	18	5	5
1734	23	1	16	49	9	3	20	38	4	1	22	39	4	26	48	5
1735	12	10	5	25	8	22	36	30	2	11	10	44	5	4	51	4
1736	0	18	54	2	8	11	52	22	0	20	58	49	5	12	54	27
1737	19	16	26	42	9	0	14	34	11	26	35	55	6	21	37	2
1738	9	1	15	18	8	19	30	26	10	6	24	0	6	29	40	1
1739	27	22	47	58	9	7	52	38	9	12	1	6	8	8	23	1
1740	16	7	36	34	8	27	8	30	7	21	49	11	8	16	26	
1741	5	16	25	11	8	16	24	22	6	1	37	16	8	24	28	5
1742	24	13	57	52	9	4	46	34	5	7	14	22	10	3	11	54
1743	13	22	46	27	8	24	2	27	3	17	2	27	10	1	14	41
1744	2	7	35	4	8	13	18	20	1	26	50	32	10	19	17	2
1745	21	5	7	44	9	1	40	32	1	2	27	38	11	28	0	3
1746	10	13	56	20	8	20	56	24	11	12	15	43	0	6	3	17
1747	29	11	29	0	9	9	18	36	10	17	52	49	1	14	46	1
1748	17	20	17	36	8	28	34	28	8	27	40	54	1	22	49	5
1749	7	5	6	13	8	17	50	20	7	7	28	59	2	0	51	5
1750	26	2	38	53	9	6	12	32	6	13	6	5	3	9	34	53
1751	15	11	27	29	8	25	28	24	4	22	54	10	3	17	37	4
1752	3	20	16	6	8	14	44	16	3	2	42	15	3	25	40	27
1753	22	17	48	45	9	3	6	28	2	8	19	21	5	4	23	28
1754	12	2	37	22	8	22	22	20	0	18	7	26	5	12	26	15
1755	1	11	25	59	8	11	38	12	10	27	55	31	5	20	29	2
1756	19	8	58	38	9	0	0	24	10	3	32	37	6	29	12	3
1757	8	17	47	15	8	19	16	16	8	13	20	42	7	7	14	5
1758	27	15	19	54	9	7	38	28	7	18	57	48	8	15	57	5
1759	17	0	8	31	8	26	54	20	5	28	45	54	8	24	0	39
1760	5	8	57	8	8	16	10	12	4	8	34	0	9	2	3	26
1761	24	6	29	47	9	4	32	24	3	14	11	6	10	10	46	27
1762	13	15	18	24	8	23	48	16	1	23	59	11	10	18	49	14
1763	3	0	7	1	8	13	4	8	0	3	47	16	10	26	52	1
1764	20	21	39	40	9	1	26	20	11	9	24	21	0	5	35	2
1765	10	6	28	17	8	20	42	13	9	19	12	26	0	13	37	4
1766	29	4	0	56	9	9	4	20	8	24	49	32	1	22	20	5

TABL

TABLE I. *concluded.* *Old Stile.*

Y. of Chr.	Mean New Moon in March.				Sun's mean Anomaly.				Moon's mean Anomaly.				Sun's mean Diſt. from the Node.			
	D.	H.	M.	S.	s	°	′	″	s	°	′	″	s	°	′	″
1767	18	12	49	33	8	28	20	17	7	4	37	37	2	0	23	38
1768	6	21	38	10	8	17	36	9	5	14	25	42	2	8	26	25
1769	25	19	10	40	9	5	58	21	4	20	2	48	3	17	9	27
1770	15	3	59	26	8	25	14	13	2	29	50	53	3	25	12	14
1771	4	12	48	2	8	14	30	5	1	9	38	58	4	3	15	1
1772	22	10	20	4	9	2	52	17	0	15	16	4	5	11	58	3
1773	11	19	9	19	8	22	8	9	10	25	4	9	5	20	0	5
1774	1	3	57	55	8	11	24	1	9	4	52	14	5	28	3	37
1775	20	1	30	35	8	29	46	13	8	10	29	20	7	6	46	3
1776	8	10	19	12	8	19	2	5	6	20	17	25	7	14	49	2
1777	27	7	51	51	9	7	24	17	5	25	54	31	8	23	32	26
1778	16	16	40	28	8	26	40	9	4	5	42	36	9	1	35	13
1779	6	1	29	4	8	15	56	1	2	15	30	41	9	9	38	0
1780	23	23	1	44	9	4	18	13	1	21	7	47	10	18	21	1
1781	13	7	50	21	8	23	34	5	0	0	55	52	10	26	23	48
1782	2	16	38	57	8	12	49	58	10	10	43	5	11	4	26	35
1783	21	14	11	37	9	1	12	10	9	16	21	3	0	13	9	36
1784	9	23	0	13	8	20	28	3	7	26	9	8	0	21	12	23
1785	28	20	32	53	9	8	50	15	7	1	46	14	1	29	55	25
1786	18	5	21	30	8	28	6	7	5	11	34	19	2	7	58	12
787	7	14	10	6	8	17	21	59	3	21	22	24	2	16	0	59
788	25	11	42	46	9	5	44	11	2	26	59	30	3	24	44	1
789	14	20	31	23	8	25	0	3	1	6	47	35	4	2	46	48
790	4	5	19	59	8	14	15	55	11	16	35	40	4	10	49	35
791	23	2	52	39	9	2	38	7	10	22	12	46	5	19	32	37
792	11	11	41	15	8	21	53	59	9	2	0	52	5	27	35	24
793	30	9	13	55	9	10	16	11	8	7	37	58	7	6	18	26
794	19	18	2	32	8	29	32	3	6	17	26	4	7	14	21	13
795	9	2	51	8	8	18	47	55	4	27	14	9	7	22	24	0
796	27	0	23	48	9	7	10	7	4	2	51	14	9	1	7	1
797	16	9	12	24	8	26	25	59	2	12	39	19	9	9	9	48
798	5	18	1	1	8	15	41	51	0	22	27	25	9	17	12	35
799	24	15	33	41	9	4	4	3	11	28	4	31	10	25	55	37
800	13	0	22	17	8	23	19	55	10	7	52	36	11	3	58	[illegible]

TABLE II. *Mean New Moon, &c. in* March, *New Stile, from* A. D. 1752 *to* A. D. 1800.

Y. of Chr.	Mean New Moon in March.				Sun's mean Anomaly.				Moon's mean Anomaly.				Sun's mean Dist. from the Node.			
	D.	H.	M.	S.	s	°	'	"	s	°	'	"	s	°	'	"
1752	14	20	16	6	8	14	44	16	3	2	42	15	3	25	40	27
1753	4	5	4	42	8	4	0	8	1	12	30	20	4	3	43	14
1754	23	2	37	22	8	22	22	20	0	18	7	26	5	12	26	15
1755	12	11	25	59	8	11	38	12	10	27	55	31	5	20	29	2
1756	30	8	58	38	9	0	0	24	10	3	32	37	6	29	12	3
1757	19	17	47	15	8	19	16	16	8	13	20	42	7	7	14	50
1758	9	2	35	51	8	8	32	8	6	23	8	47	7	15	17	38
1759	28	0	8	31	8	26	54	20	5	28	45	54	8	24	0	39
1760	16	8	57	8	8	16	10	12	4	8	34	0	9	2	3	26
1761	5	17	45	44	8	5	26	4	2	18	22	5	9	10	6	13
1762	24	15	18	24	8	23	48	16	1	23	59	11	10	18	49	14
1763	14	0	7	1	8	13	4	8	0	3	47	16	10	26	52	1
1764	2	8	55	36	8	2	20	0	10	13	35	21	11	4	54	48
1765	21	6	28	17	8	20	42	13	9	19	12	26	0	13	37	49
1766	10	15	16	53	8	9	58	5	7	29	0	31	0	21	40	37
1767	29	12	49	33	8	28	20	17	7	4	37	37	2	0	23	38
1768	17	21	38	9	8	17	36	9	5	14	25	42	2	8	26	25
1769	7	6	26	46	8	6	52	1	3	24	13	47	2	16	29	13
1770	26	3	59	26	8	25	14	13	2	29	50	53	3	25	12	14
1771	15	12	48	2	8	14	30	5	1	9	38	58	5	3	15	1
1772	3	21	36	39	8	3	45	57	11	17	27	3	4	11	17	48
1773	22	19	9	19	8	22	8	9	10	25	4	9	5	20	0	50
1774	12	3	57	55	8	11	24	1	9	4	52	14	5	28	3	37
1775	1	12	46	31	8	0	39	53	7	14	40	19	6	6	6	24
1776	19	10	19	12	8	19	2	5	6	20	17	25	7	14	49	25
1777	8	19	7	48	8	8	17	57	5	0	5	30	7	22	52	12
1778	27	16	40	28	8	26	40	9	4	5	42	36	9	1	35	13
1779	17	1	29	4	8	15	56	1	2	15	30	41	9	9	38	0
1780	5	10	17	40	8	5	11	53	0	25	18	46	9	17	40	47
1781	24	7	50	21	8	23	34	5	0	0	55	52	10	26	23	48
1782	13	16	38	57	8	12	49	58	10	10	43	57	11	4	26	35
1783	3	1	27	33	8	2	5	50	8	20	32	2	11	12	29	22
1784	20	23	0	13	8	20	28	3	9	26	9	8	0	21	12	23
1785	10	7	48	50	8	9	43	55	6	5	57	13	0	29	15	10
1786	9	5	21	30	8	28	6	7	5	11	34	19	2	7	58	12

TABLE II. *concluded. New Stile.*

Y. of Chr.	Mean New Moon in March.				Sun's mean Anomaly.				Moon's mean Anomaly.				Sun's mean Diſt. from the Node.			
	D.	H.	M.	S.	s	o	′	″	s	o	′	″	s	o	′	″
1787	18	14	10	6	8	17	21	59	3	21	22	24	2	16	0	59
1788	6	22	58	42	8	6	37	51	2	1	10	29	2	24	3	46
1789	25	20	31	23	8	25	0	3	1	6	47	35	4	2	46	48
1790	15	5	19	59	8	14	15	55	11	16	35	40	4	10	49	35
1791	4	14	8	35	8	3	31	47	9	26	23	45	4	18	52	22
1792	22	11	41	15	8	21	53	59	9	2	0	52	5	27	35	24
1793	11	20	29	51	8	11	9	51	7	11	48	57	6	5	38	11
1794	30	18	2	32	8	29	32	3	6	17	26	4	7	14	21	13
1795	20	2	51	8	8	18	47	55	4	27	14	9	7	22	24	0
1796	8	11	39	44	8	8	3	47	3	7	2	14	8	0	26	47
1797	27	9	12	24	8	26	25	59	2	12	39	19	9	9	9	48
1798	16	18	1	1	8	15	41	51	0	22	27	25	9	17	12	35
1799	6	2	49	37	8	4	57	43	11	2	15	30	9	25	15	22
1800	25	0	22	17	8	23	19	55	10	7	52	36	11	3	58	24

TABLE III. *Mean Anomalies, and Sun's mean Diſtance from the Node, for* 13½ *mean Lunations.*

N°	Mean Lunations.				Sun's mean Anomaly.				Moon's mean Anomaly.				Sun's mean Diſt. from the Node.			
	D.	H.	M.	S.	s	o	′	″	s	o	′	″	s	o	′	″
1	29	12	44	3	0	29	6	19	0	25	49	0	1	0	40	14
2	59	1	28	6	1	28	12	39	1	21	38	1	2	1	20	28
3	88	14	12	9	2	27	18	58	2	17	27	1	3	2	0	42
4	118	2	56	12	3	26	25	17	3	13	16	2	4	2	40	56
5	147	15	40	15	4	25	31	37	4	9	5	2	5	3	21	10
6	177	4	24	18	5	24	37	56	5	4	54	3	6	4	1	24
7	206	17	8	21	6	23	44	15	6	0	43	3	7	4	41	38
8	236	5	52	24	7	22	50	35	6	26	32	3	8	5	21	52
9	265	18	36	27	8	21	56	54	7	22	21	4	9	6	2	6
10	295	7	20	30	9	21	3	14	8	18	10	4	10	6	42	20
11	324	20	4	33	10	20	9	33	9	13	59	5	11	7	22	34
12	354	8	48	36	11	19	15	52	10	9	48	5	0	8	2	47
13	383	21	32	40	0	18	22	12	11	5	37	6	1	8	43	1
½	14	18	22	2	0	14	33	10	6	12	54	20	0	15	20	7

TABLE IV. *The Days of the Year, reckoned from the beginning of* March.

Days.	March.	April.	May.	June.	July.	Auguſt.	September.	October.	November.	December.	January.	February.
1	1	32	62	93	123	154	185	215	246	276	307	338
2	2	33	63	94	124	155	186	216	247	277	308	339
3	3	34	64	95	125	156	187	217	248	278	309	340
4	4	35	65	96	126	157	188	218	249	279	310	341
5	5	36	66	97	127	158	189	219	250	280	311	342
6	6	37	67	98	128	159	190	220	251	281	312	343
7	7	38	68	99	129	160	191	221	252	282	13	344
8	8	39	69	100	130	161	192	222	253	283	314	345
9	9	40	70	101	131	162	193	223	254	284	315	346
10	10	41	71	102	132	163	194	224	255	285	316	347
11	11	42	72	103	133	164	195	225	256	286	317	348
12	12	43	73	104	134	165	196	226	257	287	318	349
13	13	44	74	105	135	166	197	227	258	288	319	350
14	14	45	75	106	136	167	198	228	259	289	320	351
15	15	46	76	107	137	168	199	229	260	290	321	352
16	16	47	77	108	138	169	200	230	261	291	322	353
17	17	48	78	109	139	170	201	231	262	292	323	354
18	18	49	79	110	140	171	202	232	263	293	324	355
19	19	50	80	111	141	172	203	233	264	294	325	356
20	20	51	81	112	142	173	204	234	265	295	326	357
21	21	52	82	113	143	174	205	235	266	296	327	358
22	22	53	83	114	144	175	206	236	267	297	328	359
23	23	54	84	115	145	176	207	237	268	298	329	360
24	24	55	85	116	146	177	208	238	269	299	330	361
25	25	56	86	117	147	178	209	239	270	300	331	362
26	26	57	87	118	148	179	210	240	271	301	332	363
27	27	58	88	119	149	180	211	241	272	302	333	364
28	28	59	89	120	150	181	212	242	273	303	334	365
29	29	60	90	121	151	182	213	243	274	304	335	366
30	30	61	91	122	152	183	214	244	275	305	336	
31	31		92		153	184		245		306	337	

TABLE V. *Mean Lunations from* 1 *to* 100000.

Lunat.	Days. Decimal Parts.	Days	Hou.	M.	S.	Th.	Fo.
1	29.530590851080	= 29	12	44	3	2	58
2	59.061181702160	59	1	28	6	5	57
3	88.591772553240	88	14	12	9	8	55
4	118.122363404320	118	2	56	12	11	53
5	147.652954255401	147	15	40	15	14	52
6	177.183545106481	177	4	24	18	17	50
7	206.714135957561	206	17	8	21	20	48
8	236.244726808641	236	5	52	24	23	47
9	265.775317659722	265	18	36	27	26	45
10	295.305908851080	295	7	20	30	29	43
20	590.61181702160	590	14	41	0	59	26
30	885.91772553240	885	22	1	31	29	10
40	1181.22363404320	1181	5	22	1	58	53
50	1476.52954255401	1476	12	42	32	28	36
60	1771.83545106481	1771	20	3	2	58	19
70	2067.14135957561	2067	3	23	33	28	2
80	2362.44726808641	2362	10	44	3	57	46
90	2657.75317659722	2657	18	4	34	27	29
100	2953.0590851080	2953	1	25	4	57	12
200	5906.1181702160	5906	2	50	9	54	24
300	8859.1772553240	8859	4	15	14	51	36
400	11812.2363404320	11812	5	40	19	48	48
500	14765.2954255401	14765	7	5	24	46	0
600	17718.3545106481	17718	8	30	29	43	12
700	20671.4135957561	20671	9	55	34	40	24
800	23624.4726808641	23624	11	20	39	37	36
900	26577.5317659722	26577	12	45	44	34	48
1000	29530.590851080	29530	14	10	49	32	0
2000	59061.181702160	59061	4	21	39	4	0
3000	88591.772553240	88591	18	32	28	36	0
4000	118122.363404320	118122	8	43	18	8	0
5000	147652.954255401	147652	22	54	7	40	0
6000	177183.545106481	177183	13	4	57	12	0
7000	206714.135957561	206714	3	15	46	44	0
8000	236244.726808641	236244	17	26	36	16	0
9000	265775.317659722	265775	7	37	25	48	0
10000	295305.90851080	295305	21	48	15	20	0
20000	590611.81702160	590611	19	36	30	40	0
30000	885917.72553240	885917	17	24	46	0	0
40000	1181223.63404320	1181223	15	13	1	20	0
50000	1476529.54255401	1476529	13	1	16	40	0
60000	1771835.45106481	1771835	10	49	32	0	0
70000	2067141.35957561	2067141	8	37	47	20	0
80000	2362447.26808641	2362447	6	25	2	40	0
90000	2657753.17659722	2657753	4	14	18	0	0
100000	2953059.0851080	2953059	2	2	33	20	0

TABLE VI. *The firſt mean New Moon, with the mean Anomalies of the Sun and Moon, and the Sun's mean Diſtance from the Aſcending Node, next after compleat Centuries of Julian years.*

Lunations.	Julian years.	Firſt New Moon.				Sun's mean Anomaly.			Moon's mean Anomaly.			Sun from Node.		
		D.	H.	M.	S.	s	°	′	s	°	′	s	°	′
1237	100	4	8	10	52	0	3	21	8	15	22	4	19	27
2474	200	8	16	21	44	0	6	42	5	0	44	9	8	55
3711	300	13	0	32	37	0	10	3	1	16	6	1	28	22
4948	400	17	8	43	29	0	13	24	10	1	28	6	17	49
6185	500	21	16	54	21	0	16	46	6	16	50	11	7	16
7422	600	26	1	5	14	0	20	7	3	2	12	3	26	44
8658	700	0	20	32	3	11	24	22	10	21	45	7	15	31
9895	800	5	4	42	55	11	27	43	7	7	7	0	4	58
11132	900	9	12	53	47	0	1	4	3	22	29	4	24	25
12369	1000	13	21	4	40	0	4	25	0	7	51	9	13	53
13606	1100	18	5	15	32	0	7	46	8	23	13	2	3	20
14843	1200	22	13	26	24	0	11	7	5	8	35	6	22	47
16080	1300	26	21	37	16	0	14	28	1	23	57	11	12	15
17316	1400	1	17	4	6	11	18	43	9	13	30	3	1	2
18553	1500	6	1	14	58	11	22	4	5	28	52	7	20	29
19790	1600	10	9	25	50	11	25	25	2	14	14	0	9	56
21027	1700	14	17	36	42	11	28	46	10	29	36	4	29	23
22264	1800	19	1	47	35	0	2	8	7	14	58	9	18	51
23501	1900	23	9	58	27	0	5	29	4	0	20	2	8	18
24738	2000	27	18	9	19	0	8	50	0	15	42	6	27	45
25974	2100	2	13	36	8	11	13	5	8	5	15	10	16	32
27211	2200	6	21	47	1	11	16	26	4	20	37	3	6	0
28448	2300	11	5	57	53	11	19	47	1	5	59	7	25	27
29685	2400	15	14	8	45	11	23	8	9	21	21	0	14	54
30922	2500	19	22	19	38	11	26	29	6	6	43	5	4	22
32159	2600	24	6	30	30	11	29	50	2	22	4	9	23	49
33396	2700	28	14	41	22	0	3	11	11	7	26	2	13	16
34632	2800	3	10	8	11	11	7	26	6	26	59	6	2	3
35869	2900	7	18	19	3	11	10	47	3	12	21	10	21	30
37106	3000	12	2	29	56	11	14	8	11	27	43	3	10	58
38343	3100	16	10	40	48	11	17	30	8	13	5	8	0	25
39580	3200	20	18	51	40	11	20	51	4	28	27	0	19	52

TABLE VI. *concluded.*

Lunations.	Julian years.	First New Moon.				Sun's mean Anomaly.			Moon's mean Anomaly.			Sun's mean Diſt from Node.		
		D.	H.	M.	S.	s	°	′	s	°	′	s	°	′
40817	3300	25	3	2	33	11	24	12	1	13	49	5	9	20
42054	3400	29	11	13	25	11	27	33	9	29	11	9	28	47
43290	3500	4	6	40	14	11	1	48	5	18	44	1	17	34
44527	3600	8	14	51	6	11	5	9	2	4	6	6	7	1
45764	3700	12	23	1	59	11	8	30	10	19	28	10	26	29
47001	3800	17	7	12	51	11	11	51	7	4	50	3	15	56
48238	3900	21	15	23	43	11	15	12	3	20	12	8	5	23
49475	4000	25	23	34	35	11	18	33	0	5	34	0	24	50
50711	4100	0	19	1	25	10	22	48	7	25	7	4	13	37
51948	4200	5	3	12	17	10	26	9	4	10	29	9	3	5
53185	4300	9	11	23	9	10	29	31	0	25	51	1	22	32
54422	4400	13	19	34	1	11	2	52	9	11	13	6	11	59
55659	4500	18	3	44	54	11	6	13	5	26	35	11	1	27
56896	4600	22	11	55	46	11	9	34	2	11	57	3	20	54
58133	4700	26	20	6	38	11	12	55	10	27	19	8	10	21
59369	4800	1	15	33	27	10	17	9	6	16	52	11	29	8
60606	4900	5	23	44	20	10	20	31	3	2	14	4	18	36
61843	5000	10	7	55	12	10	23	52	11	17	36	9	8	3
63080	5100	14	16	6	4	10	27	13	8	2	58	1	27	30
64317	5200	19	0	16	56	11	0	34	4	18	20	6	16	57
65554	5300	23	8	27	49	11	3	55	1	3	42	11	6	25
66791	5400	27	16	38	41	11	7	16	9	19	4	2	25	52
68028	5500	2	12	5	30	10	11	31	5	8	37	7	14	39
69265	5600	6	20	16	22	10	14	52	1	23	59	0	4	6
70502	5700	11	4	27	15	10	18	14	10	9	21	4	23	34
71739	5800	15	12	38	7	10	21	35	6	24	43	9	13	1
72976	5900	19	20	48	59	10	24	56	3	10	5	2	2	28
74212	6000	24	4	59	52	10	28	17	11	25	27	6	21	[illegible]

If Dr. *Pound*'s mean Lunation (which we have kept by in making theſe Tables) be added 74212 times to itſelf, the ſum will amount to the Julian years 24 days 4 hours 59 minutes 51 ſeconds 40 thirds; agreeing with the firſt part of the laſt line of this Table, within half a ſecond

TABLE VII. *The annual, or firſt Equation of the mean to the true Syzygy.*

Argument. Sun's mean Anomaly.

Subtract.

Degrees	0 Signs	1 Sign	2 Signs	3 Signs	4 Signs	5 Signs	Degrees
	H. M. S.	H. M. S.	H. M. S.	H. M. S.	H. M. S.	H. M. S.	
0	0 0 0	2 3 12	3 35 0	4 10 53	3 39 30	2 7 45	30
1	0 4 18	2 6 55	3 37 10	4 10 57	3 37 19	2 3 55	29
2	0 8 35	2 10 36	3 39 18	4 10 55	3 35 6	2 0 1	28
3	0 12 51	2 14 15	3 41 23	4 10 49	3 32 50	1 56 5	27
4	0 17 8	2 17 52	3 43 26	4 10 39	3 30 30	1 52 6	26
5	0 21 24	2 21 27	3 45 25	4 10 24	3 28 5	1 48 4	25
6	0 25 39	2 25 9	3 47 19	4 10 4	3 25 35	1 41 1	24
7	0 28 55	2 28 29	3 49 7	4 9 39	3 23 0	1 39 56	23
8	0 34 11	2 31 57	3 50 50	4 9 10	3 20 20	1 35 49	22
9	0 38 26	2 35 22	3 52 29	4 8 37	3 17 35	1 31 41	21
10	0 42 39	2 38 44	4 54 4	4 7 59	3 14 49	1 27 31	20
11	0 46 52	2 42 3	3 55 35	4 7 16	3 11 59	1 23 19	19
12	0 51 4	2 45 18	3 57 2	4 6 29	3 9 6	1 19 5	18
13	0 55 17	2 48 30	3 58 27	4 5 37	3 6 10	1 14 49	17
14	0 59 27	2 51 40	3 59 49	4 4 41	3 3 1	1 10 32	16
15	1 3 36	2 54 48	3 1 7	4 3 40	3 0 7	1 6 15	15
16	1 7 45	2 57 53	4 2 18	4 2 35	2 57 9	1 1 56	14
17	1 11 53	3 0 54	4 3 23	4 1 26	2 53 49	0 57 36	13
18	1 16 0	3 3 51	4 4 22	4 0 12	2 50 36	0 53 15	12
19	1 20 6	3 6 45	4 5 18	3 58 52	2 47 18	0 48 52	11
20	1 24 10	3 9 36	4 6 10	3 57 27	2 43 57	0 44 28	10
21	1 28 12	3 12 24	4 6 58	3 55 59	2 40 33	0 40 2	9
22	1 32 12	3 15 9	4 7 41	3 54 26	2 37 6	0 35 36	8
23	1 36 10	3 17 51	4 8 21	3 52 49	2 33 3	0 31 10	7
24	1 40 6	3 20 30	4 8 57	3 51 9	2 30 2	0 26 44	6
2	1 44 1	3 23 5	4 9 29	3 49 26	2 26 26	0 22 17	5
26	1 47 54	3 25 36	4 9 55	3 47 38	2 22 47	0 17 50	4
2	1 51 46	3 28 3	4 10 16	3 45 44	2 19 [illegible]	0 13 23	3
28	1 55 37	3 30 26	4 10 33	3 43 45	2 15 20	0 8 56	2
	1 59 26	3 32 45	4 10 45	3 41 40	2 11 35	0 4 29	1
0	2 3 12	3 35 0	4 10 53	3 39 30	2 7 45	0 0 0	0
	11 Signs	10 Signs	9 Signs	8 Signs	7 Signs	6 Signs	Deg

Add

TABLE

TABLE VIII. *Equation of the Moon's mean Anomaly.*

Argument. Sun's mean Anomaly.

Subtract

Degrees	0 Signs	1 Sign	2 Signs	3 Signs	4 Signs	5 Signs	Degrees
	° ′ ″	° ′ ″	° ′ ″	° ′ ″	° ′ ″	° ′ ″	
0	0 0 0	0 46 45	1 21 32	1 35 1	1 23 4	0 48 19	30
1	0 1 37	0 48 10	1 22 21	1 35 2	1 22 14	0 46 51	29
2	0 3 13	0 49 34	1 23 10	1 35 1	1 21 24	0 45 23	28
3	0 4 52	0 50 53	1 23 57	1 35 0	1 20 32	0 43 54	27
4	0 6 28	0 52 19	1 24 41	1 34 57	1 19 38	0 42 24	26
5	0 8 6	0 53 40	1 25 24	1 34 50	1 18 42	0 40 53	25
6	0 9 42	0 55 0	1 26 6	1 34 43	1 17 45	0 39 21	24
7	0 11 20	0 56 21	1 26 48	1 34 33	1 16 48	0 37 49	23
8	0 12 56	0 57 38	1 27 28	1 34 22	1 15 47	0 36 15	22
9	0 14 3[illegible]	0 58 56	1 28 6	1 34 9	1 14 44	0 34 40	21
10	0 16 10	1 0 13	1 28 43	1 33 53	1 13 41	0 33 5	20
11	0 17 47	1 1 29	1 29 17	1 33 37	1 12 37	0 31 31	19
12	0 19 23	1 2 43	1 29 51	1 33 20	1 11 33	0 29 54	18
13	0 20 59	1 3 56	1 30 22	1 33 0	1 10 26	0 28 18	17
14	0 22 35	1 5 8	1 30 50	1 32 38	1 9 17	0 26 40	16
15	0 24 10	1 6 18	1 31 19	1 32 14	1 8 8	0 25 3	15
16	0 25 45	1 7 27	1 31 45	1 31 50	1 6 58	0 23 23	14
17	0 27 19	1 8 36	1 32 12	1 31 23	1 5 40	0 21 45	13
18	0 28 52	1 9 42	1 32 34	1 30 55	1 4 32	0 20 7	12
19	0 30 25	1 10 49	1 32 57	1 30 25	1 3 19	0 18 28	11
20	0 31 57	1 11 54	1 33 17	1 29 54	1 2 1	0 16 48	10
21	0 33 2[illegible]	1 12 58	1 33 36	1 29 20	1 0 45	0 15 8	9
22	0 35 2	1 14 1	1 33 52	1 28 45	0 59 20	0 13 28	8
23	0 36 32	1 15 1	1 34 6	1 28 9	0 58 7	0 11 48	7
24	0 38 1	1 16 0	1 34 18	1 27 30	0 56 45	0 10 7	6
25	0 39 29	1 16 59	1 34 30	1 26 50	0 55 23	0 8 20	5
26	0 40 59	1 17 57	1 34 4[illegible]	1 26 27	0 54 1	0 6 44	4
27	0 42 26	1 18 52	1 34 48	1 25 5	0 52 37	0 5 3	3
28	0 43 54	1 19 47	1 34 54	1 24 39	0 51 12	0 3 21	2
29	0 45 19	1 20 40	1 34 58	1 23 52	0 49 45	0 1 40	1
30	0 46 45	1 21 32	1 35 1	1 23 4	0 48 19	0 0 0	0
Deg	11 Signs	10 Signs	9 Signs	8 Signs	7 Signs	6 Signs	Deg

Add

TABLE IX. *The ſecond Equation of the mean to the true Syzygy.*

Argument. Moon's equated Anomaly.

Add

Degrees	0 Signs	1 Sign	2 Signs	3 Signs	4 Signs	5 Signs	Degrees
	H. M. S.	H. M. S.	H. M. S.	H. M. S.	H. M. S.	H. M. S.	
0	0 0 0	5 12 48	8 47 8	9 46 44	8 8 59	4 34 33	30
1	0 10 58	5 21 56	8 51 45	9 45 3	8 3 12	4 26 1	29
2	0 21 56	5 30 57	8 56 10	9 45 12	7 57 23	4 17 25	28
3	0 32 54	5 39 51	9 0 25	9 44 11	7 51 33	4 8 47	27
4	0 43 52	5 48 37	9 4 31	9 42 59	7 45 46	4 0 7	26
5	0 54 50	5 57 17	9 8 25	9 41 36	7 39 46	3 51 23	25
6	1 5 48	6 5 51	9 12 9	9 40 3	7 33 36	3 42 32	24
7	1 16 46	6 14 19	9 15 43	9 38 19	7 27 22	3 33 38	23
8	1 27 44	6 22 41	9 19 5	9 36 24	7 21 2	3 24 42	22
9	1 38 40	6 30 57	9 22 14	9 34 18	7 14 30	3 15 44	21
10	1 49 33	6 39 4	9 25 12	9 32 1	7 7 50	3 6 45	20
11	2 0 23	6 47 0	9 27 54	9 29 33	7 1 2	2 57 43	19
12	2 11 10	6 54 46	9 30 32	9 26 54	6 54 8	2 48 39	18
13	2 21 54	7 2 24	9 32 58	9 24 4	6 47 9	2 39 34	17
14	2 32 34	7 9 52	9 35 12	9 21 3	6 40 6	2 30 28	16
15	2 43 9	7 17 9	9 37 14	9 17 51	6 32 56	2 21 19	15
16	2 53 38	7 24 19	9 39 8	9 14 28	6 25 40	2 12 8	14
17	3 4 3	7 31 18	9 40 51	9 10 54	6 18 18	2 2 53	13
18	3 14 24	7 38 9	9 42 21	9 7 9	6 10 49	1 53 36	12
19	3 24 42	7 44 51	9 43 42	9 3 13	6 3 16	1 44 16	11
20	3 34 58	7 51 24	9 44 53	8 59 6	5 55 38	1 34 54	10
21	3 45 11	7 57 45	9 45 52	8 54 50	5 47 54	1 25 31	8
22	3 55 21	8 3 56	9 46 38	8 50 24	5 40 4	1 16 7	9
23	4 5 20	8 9 57	9 47 13	8 45 48	5 32 9	1 6 41	7
24	4 15 26	8 15 46	9 47 36	8 41 2	5 24 9	0 57 13	6
25	4 25 20	8 21 24	9 47 49	8 36 6	5 16 5	0 47 44	5
26	4 35 6	8 26 53	9 47 54	8 31 0	5 7 56	0 38 13	4
27	4 44 42	8 32 11	9 47 46	8 25 44	4 59 42	0 28 41	3
28	4 54 11	8 37 19	9 47 33	8 20 18	4 51 15	0 19 8	2
29	5 3 33	8 42 18	9 47 14	8 14 33	4 43 2	0 9 34	1
30	5 12 48	8 47 8	9 46 44	8 8 59	4 34 33	0 0 0	0
Deg.	11 Signs	10 Signs	9 Signs	8 Signs	7 Signs	6 Signs	Deg.

Subtract

TABLE X. *The third Equation of the mean to the true Syzygy.*

Argument. Sun's Anomaly.—Moon's Anomaly.

Degrees	Signs 0 Sub. 6 Add		Signs 1 Sub. 7 Add		Signs 2 Sub. 8 Add		Degrees
	M.	S.	M.	S.	M.	S.	
0	0	0	2	22	4	12	30
1	0	5	2	26	4	15	29
2	0	10	2	30	4	18	28
3	0	15	2	34	4	21	27
4	0	20	2	38	4	24	26
5	0	25	2	42	4	27	25
6	0	30	2	46	4	30	24
7	0	35	2	50	4	32	23
8	0	40	2	54	4	34	22
9	0	45	2	58	4	36	21
10	0	50	3	2	4	38	20
11	0	55	3	6	4	40	19
12	1	0	3	10	4	42	18
13	1	5	3	14	4	44	17
14	1	10	3	18	4	46	16
15	1	15	3	22	4	48	15
16	1	20	3	26	4	50	14
17	1	25	3	30	4	51	13
18	1	30	3	34	4	52	12
19	1	35	3	38	4	53	11
20	1	40	3	42	4	54	10
21	1	45	3	45	4	55	9
22	1	49	3	48	4	56	8
23	1	52	3	51	4	57	7
24	1	56	3	54	4	57	6
25	2	0	3	57	4	57	5
26	2	4	4	0	4	58	4
27	2	9	4	3	4	58	3
28	2	13	4	6	4	58	2
29	2	18	4	9	4	58	1
30	2	22	4	12	4	58	0
Degrees	Signs 5 Sub. 11 Add		Signs 4 Sub. 10 Add		Signs 3 Sub. 9 Add		Degrees

TABLE XI. *The fourth Equation of the mean to the true Syzygy.*

Argument. Sun's mean Diſtance from the Node.

Degrees	Add 0, 6 Sig.		1, 7 Sig.		2, 8 Sig.		Degrees
	M.	S.	M.	S.	M.	S.	
0	0	0	1	22	1	22	30
1	0	4	1	23	1	21	29
2	0	7	1	24	1	20	28
3	0	10	1	25	1	18	27
4	0	13	1	26	1	16	26
5	0	16	1	27	1	14	25
6	0	20	1	28	1	12	24
7	0	23	1	29	1	10	23
8	0	26	1	30	1	8	22
9	0	29	1	31	1	6	21
10	0	32	1	32	1	3	20
11	0	35	1	33	1	0	19
12	0	38	1	33	0	57	18
13	0	41	1	34	0	54	17
14	0	44	1	34	0	51	16
15	0	47	1	34	0	49	15
16	0	50	1	34	0	45	14
17	0	52	1	34	0	41	13
18	0	54	1	34	0	37	12
19	0	57	1	33	0	34	11
20	1	0	1	33	0	31	10
21	1	2	1	32	0	28	9
22	1	5	1	31	0	25	8
23	1	8	1	30	0	22	7
24	1	10	1	29	0	19	6
25	1	12	1	28	0	16	5
26	1	14	1	27	0	13	4
27	1	16	1	26	0	10	3
28	1	18	1	25	0	6	2
29	1	20	1	24	0	3	1
30	1	22	1	22	0	0	0
Deg.	5, 11 Sig. Subtract		4, 10 Sig.		3, 9 Sig.		Deg.

TABLE XII. *The Sun's mean Longitude, Motion, and Anomaly: Old Stile.*

Years beginning	Sun's mean Longitude.				Sun's mean Anomaly.		
	s	°	'	"	s	°	'
1	9	7	53	10	6	28	48
201	9	9	23	50	6	26	57
301	9	10	9	10	6	25	1
401	9	10	54	30	6	25	5
501	9	11	39	50	6	24	9
1001	9	15	26	30	6	19	32
1101	9	16	11	50	6	18	36
1201	9	16	57	10	6	17	40
1301	9	17	42	30	6	16	44
1401	9	18	27	50	6	15	49
1501	9	19	13	10	6	14	53
1601	9	19	58	30	6	13	57
1701	9	20	43	50	6	13	1
1801	9	21	29	10	6	12	6

Years compleat	Sun's mean Motion.				Sun's mean Anomaly.		
	s	°	'	"	s	°	'
1	11	29	45	40	11	29	45
2	11	29	31	20	11	29	29
3	11	29	17	0	11	29	14
4	0	0	1	49	11	29	58
5	11	29	47	29	11	29	42
6	11	29	33	9	11	29	27
7	11	29	18	49	11	29	11
8	0	0	3	38	11	29	55
9	11	29	49	18	11	29	40
10	11	29	34	58	11	29	24
11	11	29	20	38	11	29	9
12	0	0	5	26	11	29	53
13	11	29	51	7	11	29	37
14	11	29	36	47	11	29	22
15	11	29	22	27	11	29	7
16	0	0	7	15	11	29	50
17	11	29	52	55	11	29	35
18	11	29	38	35	11	29	20

Years compleat	Sun's mean Motion.				Sun's mean Anomaly.		
	s	°	'	"	s	°	'
19	11	29	24	16	11	29	4
20	0	0	9	4	11	29	48
40	0	0	18	8	11	29	37
60	0	0	27	12	11	29	26
80	0	0	36	16	11	29	15
100	0	0	45	20	11	29	4
200	0	1	30	40	11	28	8
300	0	2	16	0	11	27	12
400	0	3	1	20	11	26	16
500	0	3	46	40	11	25	21
600	0	4	32	0	11	24	25
700	0	5	17	20	11	23	29
800	0	6	2	40	11	22	33
900	0	6	48	0	11	21	37
1000	0	7	33	20	11	20	41
2000	0	15	6	40	11	11	22
3000	0	22	40	0	11	2	[illegible]
4000	1	0	13	20	10	22	44
5000	1	7	46	40	10	13	25
6000	1	15	20	0	10	4	6

Months	Sun's mean Motion.				Sun's mean Anomaly.		
	s	°	'	"	s	°	'
Jan.	0	0	0	0	0	0	0
Feb.	1	0	33	18	1	0	33
Mar.	1	28	9	11	1	28	9
Apr.	2	28	42	30	2	28	42
May	3	28	16	40	3	28	17
June	4	28	49	58	4	28	50
July	5	28	24	8	5	28	24
Aug.	6	28	57	26	6	28	57
Sept.	7	29	30	44	7	29	30
Oct.	8	29	4	54	8	29	4
Nov.	9	29	38	12	9	29	37
Dec.	10	29	12	22	10	29	11

TABLE XII. *concluded.*

Days.	Sun's mean Motion and Anomaly.				Sun's mean Motion and Anomaly.				Sun's mean Diſt. from Node.			Sun's mean Motion and Anomaly.				Sun's mean Diſt. from Node.		
	s	°	′	″	H M S	° ′ ″	′ ″ ‴	″ ‴ ⁗	° ′ ″	′ ″ ‴	″ ‴ ⁗	H M S	° ′ ″	′ ″ ‴	″ ‴ ⁗	° ′ ″	′ ″ ‴	″ ‴ ⁗
1	0	0	59	8														
2	0	1	58	17	1	0	2	28	0	2	36	31	1	16	23	1	20	30
3	0	2	57	25	2	0	4	56	0	5	12	32	1	18	51	1	23	6
4	0	3	56	33	3	0	7	24	0	7	48	33	1	21	19	1	25	42
5	0	4	55	42	4	0	9	51	0	10	23	34	1	23	47	1	28	18
6	0	5	54	50	5	0	12	19	0	12	59	35	1	26	15	1	30	54
7	0	6	53	58	6	0	14	47	0	15	35	36	1	28	42	1	33	29
8	0	7	53	7	7	0	17	15	0	18	11	37	1	31	10	1	36	5
9	0	8	52	15	8	0	19	43	0	20	47	38	1	33	38	1	38	40
10	0	9	51	23	9	0	22	11	0	23	23	39	1	36	6	1	41	16
11	0	10	50	32	10	0	24	38	0	25	58	40	1	38	34	1	43	52
12	0	11	49	40	11	0	27	6	0	28	34	41	1	41	2	1	46	28
13	0	12	48	48	12	0	29	34	0	31	10	42	1	43	30	1	49	4
14	0	13	47	57	13	0	32	2	0	33	45	43	1	45	57	1	51	39
15	0	14	47	5	14	0	34	30	0	36	21	44	1	48	25	1	54	15
16	0	15	46	13	15	0	36	58	0	38	57	45	1	50	53	1	56	51
17	0	16	45	22	16	0	39	26	0	41	33	46	1	53	21	1	59	27
18	0	17	44	30	17	0	41	53	0	44	8	47	1	55	49	2	2	3
19	0	18	43	38	18	0	44	21	0	46	4	48	1	58	17	2	4	39
20	0	19	42	47	19	0	46	49	0	49	20	49	2	0	44	2	7	13
21	0	20	41	55	20	0	49	17	0	51	56	50	2	3	12	2	9	50
22	0	21	41	3	21	0	51	45	0	54	32	51	2	5	40	2	12	25
23	0	22	40	12	22	0	54	13	0	57	8	52	2	8	8	2	15	2
24	0	23	39	20	23	0	56	40	0	59	43	53	2	10	36	2	17	38
25	0	24	38	28	24	0	59	8	1	2	19	54	2	13	4	2	20	14
26	0	25	37	37	25	1	1	36	1	4	55	55	2	15	32	2	22	50
27	0	26	36	45	26	1	4	4	1	7	31	56	2	17	59	2	25	26
28	0	27	35	53	27	1	6	32	1	10	7	57	2	20	27	2	28	2
29	0	28	35	2	28	1	9	0	1	12	43	58	2	22	55	2	30	37
30	0	29	34	10	29	1	11	28	1	15	19	59	2	25	23	2	33	13
31	1	0	33	18	30	1	13	55	1	17	55	60	2	27	51	2	35	49

In Leap-years, after *February*, add one day, and one day's motion.

TABLE XIII. *Equation of the Sun's center, or the difference between his mean and true Place.*

Argument. Sun's mean Anomaly.

Subtract

Degrees	0 Signs	1 Sign	2 Signs	3 Signs	4 Signs	5 Signs	Degrees
	° ′ ″	° ′ ″	° ′ ″	° ′ ″	° ′ ″	° ′ ″	
0	0 0 0	0 56 47	1 39 6	1 55 37	1 41 12	0 58 33	30
1	0 1 59	0 58 30	1 40 7	1 55 39	1 40 12	0 57 7	29
2	0 3 57	1 0 12	1 41 6	1 55 38	1 39 10	0 55 19	28
3	0 5 56	1 1 53	1 42 3	1 55 36	1 38 6	0 53 30	27
4	0 7 54	1 3 33	1 42 59	1 55 31	1 37 0	0 51 40	26
5	0 9 52	1 5 12	1 43 52	1 55 24	1 35 52	0 49 49	25
6	0 11 50	1 6 50	1 44 44	1 55 15	1 34 43	0 47 57	24
7	0 13 48	1 8 27	1 45 34	1 55 3	1 33 32	0 46 5	23
8	0 15 46	1 10 2	1 46 22	1 54 50	1 32 19	0 44 11	22
9	0 17 43	1 11 36	1 47 8	1 54 35	1 31 4	0 42 16	21
10	0 19 40	1 13 9	1 47 53	1 54 17	1 29 47	0 40 21	20
11	0 21 37	1 14 41	1 48 35	1 53 57	1 28 29	0 38 25	19
12	0 23 33	1 16 11	1 49 15	1 53 36	1 27 9	0 36 28	18
13	0 25 29	1 17 40	1 49 54	1 53 12	1 25 48	0 34 30	17
14	0 27 25	1 19 8	1 50 30	1 52 46	1 24 25	0 32 32	16
15	0 29 20	1 20 34	1 51 5	1 52 18	1 23 0	0 30 33	15
16	0 31 15	1 21 59	1 51 37	1 51 48	1 21 34	0 28 33	14
17	0 33 9	1 23 22	1 52 8	1 51 15	1 20 6	0 26 33	13
18	0 35 2	1 24 44	1 52 36	1 50 41	1 18 36	0 24 33	12
19	0 36 55	1 26 5	1 53 3	1 50 5	1 17 5	0 22 32	11
20	0 38 47	1 27 24	1 53 27	1 49 26	1 15 33	0 20 30	10
21	0 40 39	1 28 41	1 53 50	1 48 46	1 13 59	0 18 28	9
22	0 42 30	1 29 57	1 54 10	1 48 3	1 12 24	0 16 26	8
23	0 44 20	1 31 11	1 54 28	1 47 19	1 10 47	0 14 24	7
24	0 46 9	1 32 25	1 54 44	1 46 32	1 9 9	0 12 21	6
25	0 47 57	1 33 35	1 54 58	1 45 44	1 7 29	0 10 18	5
26	0 49 45	1 34 45	1 55 10	1 44 53	1 5 49	0 8 14	4
27	0 51 32	1 35 53	1 55 20	1 44 1	1 4 7	0 6 11	3
28	0 53 18	1 36 59	1 55 28	1 43 7	1 2 24	0 4 7	2
29	0 55 3	1 38 3	1 55 34	1 42 10	1 0 39	0 2 4	1
30	0 56 47	1 39 6	1 55 37	1 41 12	0 58 53	0 0 0	0
Deg.	11 Signs	10 Signs	9 Signs	8 Signs	7 Signs	6 Signs	Deg.

Add

TABLE XIV. *The Sun's Declination.*

Argument. Sun's true Place.

Degrees	Signs.		Signs.		Signs.		Degrees
	0 *N.* 6 *S.*		1 *N.* 7 *S.*		2 *N.* 8 *S.*		
	°	′	°	′	°	′	
0	0	0	11	30	20	11	30
1	0	24	11	51	20	24	29
2	0	48	12	11	20	36	28
3	1	12	12	32	20	48	27
4	1	36	12	53	20	59	26
5	1	59	13	13	21	10	25
6	2	23	13	33	21	21	24
7	2	47	13	53	21	31	23
8	3	11	14	12	21	41	22
9	3	34	14	31	21	50	21
10	3	58	14	50	21	59	20
11	4	22	15	9	22	8	19
12	4	45	15	28	22	16	18
13	5	9	15	46	22	24	17
14	5	32	16	4	22	31	16
15	5	55	16	22	22	38	15
16	6	18	16	39	22	45	14
17	6	41	16	57	22	51	13
18	7	4	17	14	22	56	12
19	7	27	17	30	23	2	11
20	7	50	17	46	23	6	10
21	8	13	18	2	23	11	9
22	8	35	18	18	23	14	8
23	9	57	18	33	23	18	7
24	9	20	18	48	23	21	6
25	9	42	19	3	23	23	5
26	10	4	19	17	23	25	4
27	10	25	19	31	23	27	3
28	10	47	19	45	23	28	2
29	11	8	19	58	23	29	1
30	11	30	20	11	23	29	0
Degrees	Signs.		Signs.		Signs.		Degrees
	11 *S.* 5 *N*		10 *S.* 4 *N.*		9 *S.* 3 *N.*		

TABLE XV. *Equation of the Sun's mean Diſtance from the Node.*

Argument. Sun's mean Anomaly.

Subtract

Degrees	0 Signs.		1 Sign		2 Signs.		3 Signs.		4 Signs.		5 Signs.		Degrees
	°	′	°	′	°	′	°	′	°	′	°	′	
0	0	0	1	2	1	47	2	5	1	50	1	4	30
1	0	2	1	4	1	48	2	5	1	48	1	2	29
2	0	4	1	6	1	49	2	5	1	47	1	0	28
3	0	6	1	8	1	50	2	5	1	46	0	58	27
4	0	9	1	10	1	51	2	5	1	45	0	56	26
5	0	11	1	12	1	52	2	5	1	44	0	54	25
6	0	13	1	14	1	53	2	5	1	43	0	52	24
7	0	15	1	16	1	54	2	4	1	41	0	50	23
8	0	17	1	17	1	55	2	4	1	40	0	48	22
9	0	19	1	18	1	56	2	4	1	39	0	46	21
10	0	21	1	19	1	57	2	4	1	37	0	44	20
11	0	23	1	21	1	58	2	3	1	36	0	42	19
12	0	25	1	22	1	58	2	3	1	34	0	40	18
13	0	28	1	24	1	59	2	3	1	33	0	37	17
14	0	30	1	26	2	0	2	2	1	31	0	35	16
15	0	32	1	27	2	0	2	2	1	30	0	33	15
16	0	34	1	28	2	1	2	1	1	28	0	31	14
17	0	36	1	30	2	1	2	1	1	27	0	29	13
18	0	38	1	31	2	2	2	0	1	25	0	27	12
19	0	40	1	34	2	2	2	0	1	24	0	24	11
20	0	42	1	35	2	3	1	59	1	23	0	22	10
21	0	44	1	36	2	3	1	59	1	21	0	20	9
22	0	46	1	37	2	4	1	58	1	19	0	18	8
23	0	48	1	39	2	4	1	57	1	17	0	16	7
24	0	50	1	40	2	4	1	56	1	15	0	13	6
25	0	52	1	41	2	4	1	55	1	13	0	11	5
26	0	54	1	43	2	5	1	54	1	11	0	9	4
27	0	56	1	44	2	5	1	53	1	9	0	7	3
28	0	58	1	45	2	5	1	52	1	8	0	5	2
29	1	0	1	46	2	5	1	51	1	6	0	3	1
30	1	2	1	47	2	5	1	50	1	4	0	0	0
Deg	11 Signs.		10 Signs.		9 Signs.		8 Signs.		7 Signs.		6 Signs.		Deg.

Add

TABLE XVI. *The Moon's Latitude in Eclipſes.*

Argument Moon's equated Diſtance from the Node.

0 Signs. *North Aſcending.*

6 Signs. *South Deſcending.*

°	°	′	″	°
0	0	0	0	30
1	0	5	15	29
2	0	10	30	28
3	0	15	45	27
4	0	20	59	26
5	0	26	13	25
6	0	31	26	24
7	0	36	39	23
8	0	41	51	22
9	0	47	2	21
10	0	52	13	20
11	0	57	23	19
12	1	2	31	18
13	1	7	38	17
14	1	12	44	16
15	1	17	49	15
16	1	22	52	14
17	1	27	53	13
18	1	32	52	12
19	1	37	49	11

5 Signs. *North Deſcending*

11 Signs. *South Aſcending.*

This Table ſhews the Moon's Latitude a little beyond the utmoſt Limits of Eclipſes.

TABLE XVII. *The Moon's horizontal Parallax, wi the Semidiameters and true Horary Motions of the S and Moon, to every ſixth degree of their mean Anomalie the quantities for the intermediate degrees being eaſily pr portioned by ſight.*

Anomaly of Sun and Moon.		Moon's horizont. Parallax.		Sun's Semidiameter		Moon's Semidiameter.		Moon's Horary Motion.		Sun's Horary Motion.		of Sun and Moon.	
s	°	′	″	′	″	′	″	′	″	′	″	s	
0	0	54	29	15	50	14	54	30	10	2	23	12	
	6	54	31	15	50	14	55	30	12	2	23		2
	12	54	34	15	50	14	56	30	15	2	23		1
	18	54	40	15	51	14	57	30	19	2	23		1
	24	54	47	15	51	14	58	30	26	2	23		
1	0	54	56	15	52	14	59	30	34	2	24	11	
	6	55	6	15	53	15	1	30	44	2	24		2
	12	55	17	15	54	15	4	30	55	2	24		1
	18	55	29	15	55	15	8	31	9	2	24		1
	24	55	42	15	56	15	12	31	23	2	25		
2	0	55	56	15	58	15	17	31	40	2	25	10	
	6	56	12	15	59	15	22	31	56	2	26		2
	12	56	29	16	1	15	26	32	17	2	27		1
	18	56	48	16	2	15	30	32	39	2	27		1
	24	57	8	16	4	15	36	33	11	2	28		
3	0	57	30	16	6	15	41	33	23	2	28	9	
	6	57	52	16	8	15	46	33	47	2	29		2
	12	58	12	16	10	15	52	34	11	2	29		1
	18	58	31	16	11	15	58	34	34	2	29		1
	24	58	49	16	13	16	3	34	58	2	30		
4	0	59	6	16	14	16	9	35	22	2	30	8	
	6	59	21	16	15	16	14	35	45	2	31		2
	12	59	35	16	17	16	19	36	0	2	31		1
	18	59	48	16	19	16	24	36	20	2	32		1
	24	60	0	16	20	16	28	36	40	2	32		
5	0	60	11	16	21	16	31	37	0		32	7	
	6	60	21	16	21	16	34	37	10	2	33		2
	12	60	30	16	22	16	37	37	19	2	33		1
	18	60	38	16	2	16	38	37	28	2	33		1
	24	60	45	16	23	16	39	37	3[illegible]	2	33		
6	[illegible]	60	45	16	23	16	39	37	4[illegible]	2	33	6	

To calculate the true Time of New or full Moon.

PRECEPT I. If the required time be within the limits of the 18th century, write out the mean time of New Moon in *March*, for the propoſed year, from Table I. in the Old Stile, or from Table II. in the New; together with the mean Anomalies of the Sun and Moon, and the Sun's mean Diſtance from the Moon's aſcending Node.—If you want the time of full Moon in *March*, add the half Lunation at the foot of Table III, with it's Anomalies, &c. to the former numbers, if the New Moon falls before the 15th of *March*; but if it falls after, ſubtract the half Lunation, with the Anomalies, &c. belonging to it, from the former numbers, and write down the reſpective ſums or remainders.

II. In theſe additions or ſubtractions, obſerve, that 60 ſeconds make a minute, 60 minutes make a degree, 30 degrees make a ſign, and 12 ſigns make a circle.—When you exceed 12 ſigns in addition, reject 12, and ſet down the remainder.—When the number of ſigns to be ſubtracted is greater than the number you ſubtract from, add 12 ſigns to the leſſer number, and then you will have a remainder to ſet down.—In the Tables, ſigns are marked thus^s, degrees thus$^\circ$, minutes thus$'$, and ſeconds thus$''$.

III. When the required New or Full Moon is in any given month after *March*, write out as many Lunations, with their Anomalies, and the Sun's diſtance from the Node, from Table III, as the given month is after *March*; ſetting them in order below the numbers taken out for *March*.

IV. Add all theſe together, and they will give the mean time of the required New or Full Moon, with the mean Anomalies and Sun's mean diſtance from the aſcending Node, which are the Arguments for finding the proper Equations.

V. With the number of days added together, enter Table IV. under the given Month; and againſt that number you have the day of mean New or Full Moon in the left-hand column, which ſet before the hours, minutes, and ſeconds, already found.

But (as it will ſometimes happen) if the ſaid number of days falls ſhort of any in the column under the given month, add one Lunation and it's Anomalies, &c. (from Table III.) to the foreſaid ſums, and then you will have a new ſum of days wherewith to enter Table IV. under the given month, where you are ſure to find it the ſecond time, if the firſt falls ſhort.

VI. With the ſigns and degrees of the Sun's Anomaly, enter Table VII. and therewith take out the annual or firſt Equation for reducing the mean Syzygy to the true; taking care to make proportions in the Table for the odd minutes and ſeconds of Anomaly, as the Table gives the Equation only to whole degrees.

Obſerve, in this and every other caſe of finding Equations, that if the ſigns are at the head of the Table, their degrees are at the left hand, and are reckoned downwards; but if the ſigns are at the foot of the Table, their degrees are at the right hand, and are counted upward; the Equation being in the body of the Table, under or over the ſigns, in a collateral line with the degrees.—The titles *Add* or *Subtract* at the head or foot of the Tables where the ſigns are found, ſhew whether the Equation is to be added to the mean time of New or Full Moon, or to be ſubtracted from it. In this Table, the Equation is to be ſubtracted, if the ſigns of the Sun's Anomaly are found at the head of the Table; but it is to be added, if the ſigns are at the foot.

VII. With the ſigns and degrees of the Sun's mean Anomaly, enter Table VIII. and take out the Equation of the Moon's mean Anomaly; ſubtract

tract this Equation from her mean Anomaly, if the ſigns of the Sun's Anomaly be at the head of the Table, but add it if they are at the foot; the reſult will be the Moon's equated Anomaly, with which enter Table IX, and take out the ſecond Equation for reducing the mean to the true time of New or Full Moon; adding this Equation, if the ſigns of the Moon's Anomaly are at the head of the Table, but ſubtracting it if they are at the foot, and the reſult will give you the mean time of the required New or Full Moon twice equated, which will be ſufficiently near for common almanacks.—But when you want to calculate an Eclipſe, the following Equations muſt be uſed: thus,

VIII. Subtract the Moon's equated Anomaly from the Sun's mean Anomaly, and with the remainder in ſigns and degrees, enter Table X, and take out the third Equation, applying it to the former equated time, as the titles, *Add* or *Subtract*, do direct.

IX. With the Sun's mean diſtance from the aſcending Node enter Table XI, and take out the Equation anſwering to that argument, adding it to, or ſubtracting it from the former equated time, as the titles direct, and the reſult will give the time of New or Full Moon, agreeing with well-regulated clocks or watches, very near the truth. But, to make it agree with the ſolar, or apparent time, apply the Equation of natural days, for in the Tables (from page 161 to page 173) as it is Leap-year, or the firſt, ſecond, or third after.

The method of calculating the time of any New or Full Moon without the limits of the 18th century, will be ſhewn further on. And a few Examples compared with the Precepts, will make the whole work plain.

N. B. The Tables begin the day at noon, and reckon forward from thence to the noon following.—Thus, *March* the 31ſt, at 22 h. 30 min. 25 ſec. of tabular time, is *April* 1ſt (in common reckoning) at 30 min. 25 ſec. after 10 o'clock in the morning.

EXAMPLE I.

Required the true time of New Moon in April 1764, *New Stile?*

By the Precepts.	New Moon.	Sun's Anom.	Moon's Anom.	Sun fr. Node.
	D. H. M. S.	s ° ′ ″	s ° ′ ″	s ° ′ ″
March 1764,	2 8 55 36	8 2 20 0	10 13 35 21	11 4 54 48
Add 1 Lunation,	29 12 44 3	0 29 6 19	0 25 49 0	1 0 40 14
Mean New Moon,	31 21 39 39	9 1 26 19	11 9 24 21	0 5 35 2
First Equation,	+ 4 10 40	11 10 59 18	+ 1 34 57	Sun fr. Node,
Time once equated,	32 1 50 19	9 20 27 1	11 10 59 18	and Arg. 4th.
Second Equation,	− 3 24 49	Arg. 3d equat.	Arg. 2d equat	equation.
Time twice equat.	31 22 25 30			
Third Equation,	+ 4 37			
Time thrice equat.	31 22 30 7			
Fourth Equation,	+ 18			
True New Moon,	31 22 30 25			
Equation of days,	− 3 48			
Apparent time,	31 22 26 37			

So the true time is 22 h. 30 min. 25 ſec. after the noon of the 31ſt *March*; that is, *April* 1ſt, at 30 min. 25 ſec. after X in the morning. But the apparent time is 26 min. 37 ſec. after X in the morning.

EXAMPLE

EXAMPLE II.

Qu. *The true time of Full Moon in* May 1762, *New Stile?*

By the Precepts.	New Moon. D. H. M. S.	Sun's Anom. s ° ′ ″	Moon's Anom. s ° ′ ″	Sun fr. Node. s ° ′ ″
March 1762,	24 15 18 24	8 23 48 16	1 23 59 11	10 18 49 14
Add 2 Lunations,	59 1 28 6	1 28 12 39	1 21 38 1	2 1 20 28
New Moon, *May*,	22 16 45 30	10 22 0 55	3 15 37 12	0 20 9 42
Subt. ½ Lunation,	14 18 22 2	0 14 33 10	6 12 54 30	0 15 20 7
Full Moon, *May*,	7 22 24 28	10 7 27 45	9 2 42 42	0 4 49 35
First Equation,	+ 3 16 36	9 3 57 18	+ 1 14 36	Sun fr. Node, and Arg. 4th equation.
Time once equat.	8 1 41 4	1 3 30 27	9 3 57 18	
Second Equation,	− 9 47 53	Arg. 3d equat.	Arg. 2d equat	
Time twice equat.	7 15 53 11			
Third Equation,	− 2 36			
Time thrice equat.	7 15 50 35			
Fourth Equation,	+ 15			
The Full Moon,	7 15 50 50			

Anſ. *May* 7th at 15 h. 50 min. 50 ſec. paſt noon, viz. *May* 8th at III h. 50 min. 50 ſec. in the morning.

To calculate the time of New and Full Moon in a given year and month of any particular century, between the Chriſtian Æra and the 18th century.

Precept I. Find a year of the ſame number in the 18th century with that of the year in the century propoſed, and take out the mean Time of New Moon in *March*, Old Stile, for that year, with the mean Anomalies and Sun's mean Diſtance from the Node at that time, as already taught.

II. Take as many compleat centuries of years from Table VI. as, when ſubtracted from the abovesaid year in the 18th century, will anſwer to the given year; and take out the firſt mean new Moon and it's Anomalies, &c. belonging to the ſaid centuries, and ſet them below thoſe taken out for *March* in the 18th century.

III. Subtract the Numbers belonging to theſe centuries, from thoſe of the 18th century, and the remainders will be the mean Time and Anomalies, &c. of New Moon in *March*, in the given year of the century propoſed.—Then, work in all reſpects for the true time of New or Full Moon, as ſhewn in the above Precepts and Examples.

IV. If the days annexed to theſe centuries exceed the number of days from the beginning of *March* taken out in the 18th century, add a Lunation and it's Anomalies, &c. from Table III. to the Time and Anomalies of New Moon in *March*, and then proceed in all reſpects as above.—This circumſtance happens in Example V.

EXAMPLE III.

Required the true time of Full Moon in April, *Old Stile, A. D.* 30?

From 1730 ſubtract 1700 (or 17 centuries) and there remains 30.

By the Precepts.	New Moon.				Sun's Anom.				Moon's Anom.				Sun fr. Node.			
	D.	H.	M.	S.	s	°	′	″	s	°	′	″	s	°	′	″
March 1730,	7	12	34	16	8	18	4	31	9	0	32	17	1	23	17	16
Add ½ Lunation,	14	18	22	2	0	14	33	10	6	12	54	30	0	15	20	7
Full Moon,	22	6	56	18	9	2	37	41	3	13	26	47	2	8	37	23
1700 years ſubtr.	14	17	36	42	11	28	46	0	10	29	36	0	4	29	23	0
Full ☽ *Mar. A D.* 30,	7	13	19	36	9	3	51	41	4	13	50	47	9	9	14	23
Add 1 Lunation,	29	12	44	3	0	29	6	19	0	25	49	0	1	0	40	14
Full Moon, *April*,	6	2	3	39	10	2	58	0	5	9	39	47	10	9	54	37
Firſt Equation,	+	3	28	4	5	10	58	40	+	1	18	53	Sun fr. Node,			
Time once equat.	6	5	31	43	4	21	59	20	5	10	58	40	and Arg. fourth			
Second Equation,	+	2	57	48	Arg. 3d equat.				Arg. 2d equat.				equation.			
Time twice equat.	6	8	29	31												
Third Equation,		—	2	54												
Time thrice equat.	6	8	26	37												
Fourth Equation,		—	1	33												
Tr. Full Moon, *Apr.*	6	8	25	4												

Hence it appears, that the true time of Full Moon in *April, A. D.* 30, Old Stile, was on the 6th day, at 25 m. 4 ſ. paſt VIII in the evening.

To calculate the true time of New or Full Moon in any given year and month before the Chriſtian Æra.

Precept I. Find a year in the 18th century, which being added to the given number of years before Chriſt diminiſhed by one, ſhall make a number of compleat centuries.

II. Find this number of centuries in Table VI. and ſubtract the Time and Anomalies belonging to it from thoſe of the mean New Moon in *March*, the above-found year of the 18th century; and the remainder will denote the Time and Anomalies, &c. of mean New Moon in *March*, the given year before Chriſt.—Then, for the true time thereof in any month of that year, proceed as above taught.

EXAMPLE IV.

Required the true time of New Moon in May, *Old Stile, the year before Chriſt* 585?

The years 584 added to 1716, make 2300, or 23 centuries.

By the Precepts.	New Moon.				Sun's Anom.				Moon's Anom.				Sun fr. Node.			
	D.	H.	M.	S.	s	°	′	″	s	°	′	″	s	°	′	″
March 1716,	11	17	33	29	8	22	50	39	4	4	14	2	4	27	17	5
2300 years ſubt.	11	5	57	53	11	19	47	0	1	5	59	0	7	25	27	0
Mar. bef. Ch. 585,	0	11	35	36	9	3	3	39	2	28	15	2	9	1	50	5
Add 3 Lunations,	88	14	12	9	2	27	18	58	2	17	27	1	3	2	0	42
May bef. Ch. 585,	28	1	47	45	0	0	22	37	5	15	42	3	0	3	50	47
Firſt Equation,		—	1	37	5	15	41	17			—	46	Sun fr. Node, and Arg. fourth equation.			
Time once equat.	28	1	46	8	6	14	41	20	5	15	41	17				
Second Equation,	+	2	15	1	Arg. 3d equat.				Arg. 2d equat.							
Time twice equat.	28	4	1	9												
Third Equation,		+	1	9												
Time thrice equat.	28	4	2	18												
Fourth Equation,			+	12												
True New Moon,	28	4	2	30												

So the true time was *May* 28th, at 2 minutes 30 ſeconds paſt IV in the afternoon.

Theſe Tables are calculated for the meridian of *London*; but they will ſerve for any other place, by ſubtracting four minutes from the tabular time, for every degree that the meridian of the given place is weſtward of *London*, or adding four minutes for every degree that the meridian of the given place is eaſtward: as in

EXAMPLE V.

Required the true time of Full Moon at Alexandria *in* Egypt *in* September, *Old Stile, the year before Chriſt* 201?

The years 200 add to 1800, make 2000, or 20 centuries.

By the Precepts.	New Moon.	Sun's Anom.	Moon's Anom.	Sun fr. Node
	D. H. M. S.	s ° ′ ″	s ° ′ ″	s ° ′ ″
March 1800,	13 0 22 17	8 23 19 55	10 7 52 36	11 3 58 24
Add 1 Lunation,	29 12 44 3	0 29 6 19	0 25 49 0	1 0 40 14
From the ſum,	42 13 6 20	9 22 26 14	11 3 41 36	0 4 38 38
Subtr. 2000 years,	27 18 9 19	0 8 50 0	0 15 42 0	6 27 45 0
N.M. bef. Chr. 201,	14 18 57 1	9 13 36 14	10 17 59 36	5 6 53 38
Add 6 Lunations,	177 4 24 18	5 24 37 56	5 4 54 3	6 4 1 24
Add half Lunat.	14 18 22 2	0 14 33 10	6 12 54 30	0 15 20 7
Full Moon *Sept.*	22 17 43 21	3 22 47 20	10 5 48 9	11 26 15 9
Firſt Equation,	— 3 52 6	10 4 19 55	— 1 28 14	Sun fr. Node,
Time once equat.	22 13 51 15	5 18 27 25	10 4 19 55	and Arg. 4th
Second Equation,	— 8 25 4	Arg. 3d equat	Arg. 2d equat	equation.
Time twice equat.	22 5 26 11			
Third Equation,	— 58			
Time thrice equat.	22 5 25 13			
Fourth Equation,	— 12			
Tr. time at *London*,	22 5 25 1			
Add for *Alexandria*,	2 1 27			
True time there,	22 7 26 28			

Thus it appears, that the true time of Full Moon at *Alexandria*, in *September*, Old Stile, the year before Chriſt 201, was the 22d day, at 26 m. 28 ſ. after VII in the evening.

EXAMPLE VI.

Required the true time of Full Moon at Babylon *in* October, *Old Stile, the* 4008 *year before the first year of Christ, or* 4007 *before the year of his birth?*

The years 4007 added to 1793, make 5800, or 58 centuries.

By the Precepts.	New Moon.	Sun's Anom.	Moon's Anom.	Sun fr. Node.
	D. H. M. S.	s ° ′ ″	s ° ′ ″	s ° ′ ″
March 1793,	30 9 13 55	9 10 16 11	8 7 37 58	7 6 18 26
Subtr. 5800 years,	15 12 38 7	10 21 35 0	6 24 43 0	9 13 1 0
N.M.bef.Chr.4007,	14 20 35 48	10 18 41 11	1 12 54 58	9 23 17 26
Add { 7 Lunations,	206 17 8 21	6 23 44 15	6 0 43 3	7 4 41 38
Add { half Lunat.	14 18 22 2	0 14 33 10	6 12 54 30	0 15 20 7
Full Moon, *October*,	22 8 6 11	5 26 58 36	1 26 32 31	5 13 19 11
First Equation,	— 13 26	1 26 27 26	— 5 5	Sun fr Node,
Time once equat.	22 7 52 45	4 0 31 10	1 26 27 26	and Arg. 4th
Second Equation,	+ 8 29 21	Arg. 3d equat.	Arg. 2d equat.	equation.
Time twice equat.	22 16 22 6			
Third Equation,	— 4 10			
Time thrice equat.	22 16 17 56			
Fourth Equation,	— 51			
Full Moon at *London*,	22 16 17 5			
Add for *Babylon*,	2 25 41			
True time there,	22 18 42 46			

So that, on the meridian of *London*, the true time was *October* 23d, at 17 min. 5 ſec. paſt IV in the morning; but at *Babylon*, the true time was *October* 23d, at 42 min. 46 ſec. paſt VI in the morning.—This is ſuppoſed by ſome to have been the year of the Creation.

To calculate the true time of New or Full Moon in any given year and Month after the 18th century.

Precept I. Find a year of the ſame number in the 18th century with that of the year propoſed, and take out the mean Time and Anomalies, &c. of New Moon in *March*, Old Stile, for that year, in Table I.

II. Take ſo many years from Table VI. as when added to the above-mentioned year in the 18th century, will anſwer to the given year in which the New or Full Moon is required: and take out the firſt New Moon, with its Anomalies for theſe compleat centuries.

III. Add all theſe together, and then work in all reſpects as above ſhewn, only remember to ſubtract a Lunation and its Anomalies, when the abovefaid addition carries the New Moon beyond the 31ſt of *March*; as in the following example.

EXAMPLE VII.

Required the true time of New Moon in July, *Old Stile*, A. D. 2180?

Four centuries (or 400 years) added to *A. D.* 1780, make 2180.

By the Precepts.	New Moon.				Sun's Anom.				Moon's Anom.				Sun fr. Node			
	D.	H.	M.	S.	s	°	′	″	s	°	′	″	s	°	′	″
March 1780,	23	23	1	44	9	4	18	13	1	21	7	47	10	18	21	1
Add 400 years,	17	8	43	29	0	13	24	0	10	1	28	0	6	17	49	0
From the ſum	41	7	45	13	9	17	42	13	11	22	35	47	5	6	10	1
Subtr. 1 Lunation,	29	12	44	3	0	29	6	19	0	25	49	0	1	0	40	1
New ☽ *March* 2180,	11	19	1	10	8	18	35	54	10	26	46	47	4	5	29	47
Add 4 Lunations,	118	2	56	12	3	26	25	17	3	13	16	2	4	2	40	56
N. ☽ *July* 2180,	7	21	57	22	0	15	1	11	2	10	2	49	8	8	10	43
Firſt equation,	—	1	3	39	3	9	38	37		—	24	12	Sun fr. Node,			
Time once equat.	7	20	53	43	10	5	22	34	2	9	38	37	and Arg. 4th			
Second equation,	+	9	24	8	Arg 3d equat				Arg. 2d equat.				equation.			
Time twice equat.	8	6	17	51												
Third equation,		+	3	56												
Time thrice equat.	8	6	21	47												
Fourth equation,		+	1	8												
True time, *July*,	8	6	22	55												

True time, *July* 8, at 22 minutes 55 ſeconds paſt VI in the evening.

In keeping by the Old Style, we are always ſure to be right, by adding or ſubtracting whole hundreds of years to or from any given year in the 18th century. But in the New Stile we may be very apt to make miſtakes, on account of the Leap-year's not coming in regularly every fourth year:—And therefore, when we go without the limits of the 18th century, we had beſt keep to the Old Stile, and at the end of the calculation reduce the time to the New. Thus, in the 22d century, there will be 14 days difference between the Stiles; and therefore, the true time of New Moon in this laſt Example being reduced to the New Stile, will be the 22d of *July*, at 22 minutes 55 ſeconds paſt VI in the evening.

To calculate the true place of the Sun for any given moment of time.

Precept I. In Table XII. find the next leſſer year in number to that in which the Sun's place is ſought, and write out his mean Longitude and Anomaly anſwering thereto: to which add his mean Motion and Anomaly for the compleat reſidue of years, months, days, hours, minutes and ſeconds, down to the given time, and this will be the Sun's mean Place and Anomaly at that time, in the Old Stile, provided the ſaid time be in any year after the Chriſtian æra. *See the firſt following Example.*

II. Enter Table XIII with the Sun's mean anomaly, and making proportions for the odd minutes and ſeconds thereof, take out the Equation of the Sun's center; which, being applied to his mean Place as the title *Add* or *Subtract* directs, will give his true Place or Longitude from the Vernal Equinox, at the time for which it was required.

III. To calculate the Sun's place for any time in a given year before the Chriſtian æra, take out his mean Longitude and Anomaly for the firſt year thereof, and from theſe numbers, ſubtract the mean Motions and Anomalies for the compleat hundreds or thouſands next above the given year; and, to the remainders, add thoſe for the reſidue of years, months, &c. and then work in all reſpects as above. *See the ſecond Example following.*

EXAMPLE

EXAMPLE I.

Required the Sun's true place, March 20*th, Old Stile,* 1764, *at* 22 *hours* 30 *minutes* 25 *ſeconds paſt noon?—In common reckoning,* March 21*ſt, at* 10 *hours* 30 *minutes* 25 *ſeconds in the forenoon.*

		Sun's Longitude.				Sun's Anomaly.			
		s	°	'	"	s	°	'	"
To the radical year after Chriſt — — —	1701	9	20	43	50	6	13	1	0
Add compleat years — — — — — —	60	0	0	27	12	11	29	26	0
	3	11	29	17	0	11	29	14	0
	March	1	28	9	11	1	28	9	0
Biſſextile, Days — —	20		20	41	55		20	41	55
Hours — —	22			54	13			54	13
Minutes —	30			1	14			1	14
Seconds —	25				1				1
Sun's mean place at the given time — — — —		0	10	14	36	9	1	27	23
Equation of the Sun's center, add — — — —			1	55	36	Mean Anomaly.			
Sun's true place at the ſame time — — — —		0	12	10	12 or	♈	12	10	12

EXAMPLE

EXAMPLE II.

Required the Sun's true place, October 23*d, Old Stile, at* 16 *hours* 57 *minutes paſt noon, in the* 4008*th year before the year of Chriſt* 1; *which was the* 4007*th before the year of his birth, and the year of the* Julian *period* 706?

By the Precepts.

		Sun's Longitude.				Sun's Anomaly.			
		s	°	′	″	s	°	′	″
From the radical numbers after Chriſt — — —	1	9	7	53	10	6	28	48	0
Subtract thoſe for 5000 compleat years — — —		1	7	46	40	10	13	25	0
Remains, for a new radix		8	0	6	30	8	15	23	0
To which add, to bring it to the given time: compleat years — — —	900	0	6	48	0	11	21	37	0
	80	0	0	36	16	11	29	15	0
	12	0	0	5	26	11	29	53	0
	October	8	29	4	54	8	29	4	0
Days	23		22	40	12		22	40	12
Hours	16			39	26			39	26
Minutes	57			2	20			2	20
Sun's mean place at the given time — — — —		6	0	3	4	5	28	33	58
Equation of the Sun's center ſubtract — — — —				3	4	Sun's Anomaly.			
Sun's true place at the ſame time — — — —		6	0	0	0	or ♎	0	0	0

So that in the meridian of *London*, the Sun was then juſt entering the ſign ♎ *Libra*, and conſequently was upon the point of the Autumnal Equinox.

If to the above time of the Autumnal Equinox at *London*, we add 2 hours, 25 minutes 41 ſeconds for the longitude of *Babylon*, we ſhall have for the time of the ſame Equinox, at that place, *October* 23d, at 19 hours, 22 minutes 41 ſeconds; which in the common way of reckoning, is *October* 24th, at 22 minutes 41 ſeconds paſt VII in the morning*.

And it appears by Example VI. that in the ſame year, the true time of Full Moon at *Babylon* was *October* 23d, at 42 minutes 46 ſeconds after VI in the morning; ſo that the Autumnal Equinox was on the day next after the day of Full Moon.—The Dominical letter for that year was *G*, and conſequently the 24th of *October* was on a *Wedneſday*.

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* The reaſon why this calculation makes the Autumnal Equinox, in the year of the *Julian Period* 706, to be two days ſooner than the time of the ſame Equinox mentioned in page 153 is, that in *that* page, only the mean time is taken into the account, as if there was no Equation of the Sun's motion.

The Equation at the Autumnal Equinox then, did not exceed an hour and a quarter, when reduced to time.—But, in the year of Chriſt 1756 (which was 5763 years after) the Equation at the Autumnal Equinox amounted to 1 day 22 hours 24 minutes, by which quantity, the true time fell later than the mean.—So that, if we conſider the *true* time of this laſt-mentioned Equinox, only as *mean* time, the mean Motion of the Sun carried thence back to the Autumnal Equinox in the year of the *Julian Period* 706, will fix it to the 25th of *October* in that year.

To

To find the Sun's diſtance from the Moon's aſcending Node, at the time of any given New or Full Moon; and conſequently, to know whether there is an Eclipſe at that time, or not.

The Sun's diſtance from the Moon's aſcending Node is the argument for finding the Moon's fourth Equation in the Syzygies, and therefore it is taken into all the foregoing Examples in finding the times thereof.—Thus, at the time of mean New Moon in *April* 1764, the Sun's mean Diſtance from the aſcending Node, is $0^{s}\ 5^{\circ}\ 35'\ 2'$. *See Example* I. p. 306.

The deſcending Node is oppoſite to the aſcending one, and they are juſt ſix Signs diſtant from each other.

When the Sun is within 17 degrees of either of the Nodes at the time of New Moon, he will be eclipſed at that time: and when he is within 12 degrees of either of the Nodes at the time of Full Moon, the Moon will be then eclipſed.—Thus we find, that there will be an Eclipſe of the Sun at the time of New Moon in *April* 1764.

But the true time of that New Moon comes out by the Equations to be 50 minutes 46 ſeconds later than the mean Time thereof, by comparing theſe times in the above Example: and therefore, we muſt add the Sun's motion from the Node during that interval, to the above mean Diſtance $0^{s}\ 5^{\circ}\ 35'\ 2''$, which motion is found in Table XII. for 50 minutes 46 ſeconds, to be $2'\ 12''$. And to this we muſt apply the Equation of the Sun's mean Diſtance from the Node, in Table XV. found by the Sun's anomaly, which, at the mean time of New Moon in Example I. is $9^{s}\ 1^{\circ}\ 26'\ 19''$; and then we ſhall have the Sun's true Diſtance from the Node, at the true time of New Moon, as follows:

At

	Sun from Node			
	s	°	′	″
At the mean time of New Moon in *April* 1764 — — — —	0	5	35	2
Sun's motion from the Node for — — 50 minutes			2	10
46 ſeconds				2
Sun's mean Diſtance from Node at true New Moon — — —	0	5	37	14
Equation of mean Diſtance from Node, add — — — —		2	5	0
Sun's true Diſtance from the aſcending Node — — —	0	7	42	14

Which, being far within the above limit of 17 degrees, ſhews that the Sun muſt then be eclipſed.

And now we ſhall ſhew how to project this, or any other eclipſe, either of the Sun or Moon.

To project an Eclipſe of the Sun.

In order to this, we muſt find the ten following Elements, by means of the Tables.

1. The true time of conjunction of the Sun and Moon; and at that time, 2. The ſemidiameter of the Earth's diſc, as ſeen from the Moon, which is equal to the Moon's horizontal parallax. 3. The Sun's diſtance from the ſolſtitial Colure to which he is then neareſt. 4. The Sun's declination. 5. The angle of the Moon's viſible path with the Ecliptic. 6. The Moon's latitude. 7. The Moon's true horary motion from the Sun. 8. The Sun's ſemidiameter. 9. The Moon's. 10. The ſemidiameter of the Penumbra.

We ſhall now proceed to find theſe Elements for the Sun's Eclipſe in *April* 1764.

To find the true time of New Moon. This, by Example I. pag. 306, is found to be on the firſt day of the ſaid month, at 30 minutes 25 ſeconds after X in the morning.

2. *To find the Moon's horizontal parallax, or ſemi-diameter of the Earth's diſc, as ſeen from the Moon.* Enter Table XVII. with the ſigns and degrees of the Moon's anomaly (making proportions, becauſe the Anomaly is in the Table only to every 6th degree) and thereby take out the Moon's horizontal parallax; which, for the above time, anſwering to the Anomaly $11^s\ 9^\circ\ 24'\ 21''$, is $54'\ 53''$.

3. *To find the Sun's diſtance from the neareſt Solſtice, viz. the beginning of Cancer, which is 3^s or 90° from the beginning of Aries.* It appears by the Example on page 314 (where the Sun's place is calculated to the above time of New Moon) that the Sun's longitude from the beginning of Aries is then $0^s\ 12^\circ\ 10'\ 12''$: that is, the Sun's place at that time is ♈ Aries, 12° 10′ 12″.

	s	°	′	″
Therefore from — — — —	3	0	0	0
Subtract the Sun's longitude or place	0	12	10	12
Remains the Sun's diſtance from the Solſtice ♋ — — — =	2	17	49	48

Or 77° 49′ 48′; each ſign containing 30 degrees.

4. *To find the Sun's declination.* Enter Table XIV. with the ſigns and degrees of the Sun's true place, viz. $0^s\ 12^\circ$, and making proportions for the 10′ 12″, take out the Sun's declination anſwering to his true place, and it will be found to be 4° 49′ north.

5. *To find the Moon's latitude.* This depends on her diſtance from her aſcending Node, which is the ſame as the Sun's diſtance from it at the time of New Moon; and is thereby found in Table XVI.

But we have already found, that the Sun's equated diſtance from the aſcending Node, at the time of New Moon in *April* 1764, is $0^s\ 7^\circ\ 42'\ 14''$. *See the preceding page.*

Therefore, enter Table XVI. with 0 ſigns at the top, and 7 and 8 degrees at the left hand, and take out 36′ and 39″, the latitude for 7°; and

41′ 51″, the latitude for 8°: and by making proportions between theſe latitudes for the 42′ 14″, by which the Moon's diſtance from the Node exceeds 7 degrees; her true Latitude will be found to be 40′ 18″ north aſcending.

6. *To find the Moon's true horary motion from the Sun.* With the Moon's anomaly, viz. 11^{s} 9° 24′ 21″, enter Table XVII. and take out the Moon's horary motion; which, by making proportions in that Table, will be found to be 30′ 22″. Then, with the Sun's anomaly, 9^{s} 1° 26′ 19″, take out his horary motion 2′ 28″ from the ſame Table: and ſubtracting the latter from the former, there will remain 27′ 54″ for the Moon's true horary motion from the Sun.

7. *To find the angle of the Moon's viſible path with the Ecliptic.* This, in the projection of Eclipſes, may be always rated at 5° 35′, without any ſenſible error.

8, 9. *To find the ſemidiameters of the Sun and Moon.* Theſe are found in the ſame Table, and by the ſame Arguments, as their horary Motions. —In the preſent caſe, the Sun's anomaly gives his ſemidiameter 16′ 6″, and the Moon's anomaly gives her ſemidiameter 14′ 57″.

10. *To find the ſemidiameter of the Penumbra.* Add the Moon's ſemidiameter to the Sun's, and their ſum will be the ſemidiameter of the Penumbra, viz. 31′ 3″.

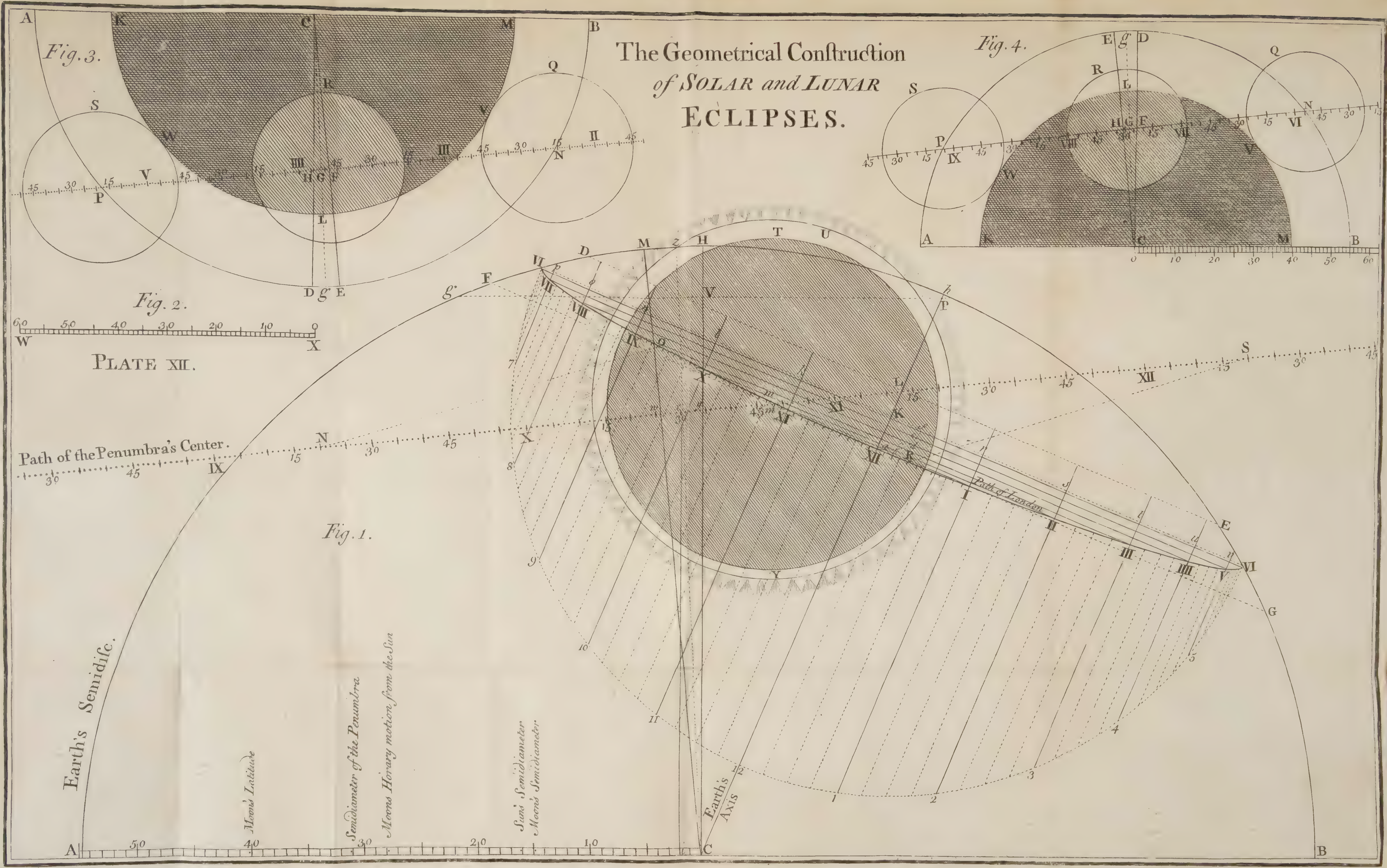
Now collect theſe Elements, that they may be found the more readily when they are wanted in the conſtruction of this Eclipſe.

1. True time of New Moon in *April*, 1764 — — — — } 1 10 30 25

	°	″	′
2. Semidiameter of the Earth's diſc	0	54	53
3. Sun's diſtance from the neareſt Solſt.	77	49	48
4. Sun's declination, north	4	49	0
5. Moon's latitude, north aſcending	0	40	18

6. Moon's

The Geometrical Conſtruction of SOLAR and LUNAR ECLIPSES.



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J. Mynd sc.

6.	Moon's horary motion from the Sun	0 27	54
7.	Angle of the Moon's viſible path with the Ecliptic —	5 35	0
8.	Sun's ſemidiameter	16	6
9.	Moon's ſemidiameter	14	57
10.	Semidiameter of the Penumbra	31	3

To project an Eclipſe of the Sun geometrically.

PLATE XII. Fig. I.

Make a ſcale of any convenient length, as *AC*, and divide it into as many equal parts as the Earth's ſemi-diſc contains minutes of a degree; which, at the time of the Eclipſe in *April* 1764, is 54′ 53″. Then, with the whole length of the ſcale as a radius, deſcribe the ſemicircle *AMB* upon the center *C*; which ſemicircle ſhall repreſent the northern half of the Earth's enlightened diſc, as ſeen from the Sun.

Upon the center *C* raiſe the ſtraight line *CH*, perpendicular to the diameter *ACB*; ſo *ACB* ſhall be a part of the Ecliptic, and *CH* its Axis.

Being provided with a good ſector, open it to the radius *CA* in the line of chords; and taking from thence the chord of 23½ degrees in your compaſſes, ſet it off both ways from *H*, to *g* and to *h*, in the periphery of the ſemi-diſc; and draw the ſtraight line *g V h*, in which the North Pole of the Diſc will be always found.

When the Sun is in Aries, Taurus, Gemini, Cancer, Leo, and Virgo, the North Pole of the Earth is enlightened by the Sun: but whilſt the Sun is in the other ſix Signs, the South Pole is enlightened, and the North Pole is in the dark.

And when the Sun is in Capricorn, Aquarius, Piſces, Aries, Taurus, and Gemini, the northern half of the Earth's axis *C* XII *P* lies to the right hand of the Axis of the Ecliptic, as ſeen from the Sun; and to the left hand, whilſt the Sun is in the other ſix Signs.

Open the ſector till the radius (or diſtance of the two 90's) of the ſines be equal to the length of *V h*, and take the ſine of the Sun's diſtance from the Solſtice (77° 49′ 48″) as nearly as you can gueſs, in your compaſſes, from the line of ſines, and ſet off that diſtance from *V* to *P* in the line *g V h*, becauſe the Earth's axis lies to the right hand of the Axis of the Ecliptic in this caſe, the Sun being in Aries; and draw the ſtraight line *C* XII *P* for the Earth's axis, of which *P* is the North Pole. If the Earth's axis had lain to the left hand from the axis of the Ecliptic, the diſtance *V P* would have been ſet off from *V* towards *g*.

To draw the Parallel of Latitude of any given place, as ſuppoſe *London*, or the path of that place on the Earth's enlightened diſc as ſeen from the Sun, from Sun-riſe till Sun-ſet, take the following method.

Subtract the Latitude of *London*, $51^\circ\frac{1}{2}$ from 90°, and the remainder $38^\circ\frac{1}{2}$ will be the co-latitude, which take in your compaſſes from the line of chords, making *C A* or *C B* the radius, and ſet it from *h* (where the Earth's axis meets the Periphery of the Diſc) to VI and VI, and draw the occult or dotted line VI *K* VI. Then, from the points where this line meets the Earth's diſc, ſet off the chord of the Sun's declination 4° 49′ to *D* and *F*, and to *E* and *G*, and connect theſe points by the two occult lines *F* XII *G* and *D L E*.

Biſect *L K* XII in *K*, and through the point *K* draw the black line VI *K* VI. Then making *C B* the radius of a line of ſines on the ſector, take the co-latitude of *London* $38^\circ\frac{1}{2}$ from the ſines in your compaſſes, and ſet it both ways from *K*, to VI and VI.—Theſe hours will be juſt in the edge of the Diſc at the Equinoxes, but at no other time in the whole year.

With the extent *K* VI taken into your compaſſes, ſet one foot in *K* (in the black line below the occult one) as a center, and with the other foot

deſcribe

diſcribe the ſemicircle VI 7 8 9 10, &c. and divide it into 12 equal parts. Then, from theſe points of diviſion, draw the occult lines 7 *p*, 8 *o*, 9 *n*, &c. parallel to the Earth's axis *C* XII *P*.

With the ſmall extent *K* XII as a radius, deſcribe the quadrantal Arc XII *f*, and divide it into ſix equal parts, as XII *a*, *a b*, *b c*, *c d*, *d e*, and *e f*; and through the diviſion-points *a*, *b*, *c*, *d*, *e* draw the occult lines VII *e* V, VIII *d* IV, IX *c* III, X *b* II, and XI *a* I; all parallel to VI *K* VI, and meeting the former occult lines 7 *p*, 8 *o*, &c. in the points VII VIII IX X XI, V IV III II and I: which points ſhall mark the ſeveral ſituations of *London* on the Earth's diſc, at theſe hours reſpectively, as ſeen from the Sun; and the elliptic Curve VI VII VIII, &c. being drawn through theſe points, ſhall repreſent the parallel of latitude, or path of *London* on the Diſc, as ſeen from the Sun; from it's riſing to it's ſetting.

N. B. If the Sun's declination had been ſouth, the diurnal path of *London* would have been on the upper ſide of the line VI *K* VI, and would have touched the line *D L E* in *L*.—It is requiſite to divide the horary ſpaces into quarters (as ſome are in the figure) and, if poſſible, into minutes alſo.

Make *C B* the radius of a line of chords on the ſector, and taking therefrom the chord of 5° 35′, the angle of the Moon's viſible path with the Ecliptic, ſet it off from *H* to *M* on the left hand of *C H*, the Axis of the Ecliptic, becauſe the Moon's latitude is north aſcending. Then draw *C M* for the Axis of the Moon's orbit, and biſect the angle *M C H* by the right-line *C z*.—If the Moon's latitude had been north deſcending, the Axis of her Orbit would have been on the right hand from the Axis of the Ecliptic.——*N. B.* The Axis of the Moon's orbit lies the ſame way when her Latitude is ſouth aſcending, as when it is north aſcending; and the ſame way when ſouth deſcending, as when north deſcending.

Take the Moon's latitude 40′ 18″ from the ſcale *C A* in your compaſſes, and ſet it from *i* to *x* in the biſecting line *C z*, making *i x* parallel to *C y*: and through *x*, at right-angles to the Axis of the Moon's orbit *C M*, draw the ſtraight line *N w x y S* for the path of the Penumbra's center over the Earth's diſc.—The point *w*, in the Axis of the Moon's orbit, is that where the Penumbra's center approaches neareſt to the center of the Earth's diſc, and conſequently is the middle of the general Eclipſe: the point *x* is that where the conjunction of the Sun and Moon falls, according to equal time by the Tables; and the point *y* is the ecliptical conjunction of the Sun and Moon.

Take the Moon's true horary motion from the Sun, 27′ 54″, in your compaſſes, from the ſcale *C A* (every diviſion of which is a minute of a degree) and with that extent make marks along the path of the Penumbra's center; and divide each ſpace, from mark to mark, into 60 equal parts or horary minutes, by dots; and ſet the hours to every 60th minute in ſuch a manner, that the dot ſignifying the inſtant of New Moon by the Tables, may fall into the point *x*, half way between the Axis of the Moon's orbit, and the Axis of the Ecliptic; and then, the reſt of the dots will ſhew the points of the Earth's diſc, where the Penumbra's center is at the inſtants denoted by them, in it's Tranſit over the Earth.

Apply one ſide of a ſquare to the line of the Penumbra's path, and move the ſquare backwards and forwards, until the other ſide of it cuts the ſame hour and minute (as at *m* and *m*) both in the path of *London*, and in the path of the Penumbra's center: and the particular minute or inſtant which the ſquare cuts at the ſame time in both paths, ſhall be the inſtant of the viſible conjunction of the Sun and Moon, or greateſt obſcuration of the Sun, at the place for which the conſtruction is made, namely, *London*, in the preſent example; and this inſtant is at 47½ minutes paſt X o'clock in the morning; which is 17 minutes 5 ſeconds later than the tabular time of true conjunction.

Take the Sun's ſemidiameter, 16′ 6″, in your compaſſes, from the ſcale *C A*, and ſetting one foot in the path of *London* at *m*, namely, at 47½ minutes paſt X, with the other foot deſcribe the circle *U Y*, which ſhall repreſent the Sun's diſc as ſeen from *London* at the greateſt obſcuration.—Then take the Moon's ſemidiameter, 14′ 57″, in your compaſſes from the ſame ſcale; and ſetting one foot in the path of the Penumbra's center at *m*, in the 47½ minute after X; with the other foot deſcribe the circle *T Y* for the Moon's diſc, as ſeen from *London*, at the time when the Eclipſe is at the greateſt; and the portion of the Sun's diſc which is hid or cut off by the Moon's, will ſhew the quantity of the Eclipſe at that time; which quantity may be meaſured on a line equal to the Sun's diameter, and divided into twelve equal parts for digits.

Laſtly, take the ſemidiameter of the Penumbra, 31′ 3″, from the ſcale *C A* in your compaſſes; and ſetting one foot in the line of the Penumbra's central path, on the left hand from the Axis of the Ecliptic, direct the other foot toward the path of *London*; and carry that extent backwards and forwards, till both the points of the compaſſes fall into the ſame inſtants in both the parhs: and theſe inſtants will denote the time when the Eclipſe begins at *London*.—Then, do the like on the right hand of the Axis of the Ecliptic; and where the points of the compaſſes fall into the ſame inſtants in both the paths, they will ſhew at what time the Eclipſe ends at *London*.

Theſe trials give 20 minutes after IX in the morning for the beginning of the Eclipſe at *London*, at the points *N* and *O*; 47½ minutes after X, at the points *m* and *n*, for the time of greateſt obſcuration; and 18 minutes after XII, at *R* and *S*, for the time when the Eclipſe ends; according to mean or equal time.

From theſe times we muſt ſubtract the equation of natural days, viz. 3 minutes 48 ſeconds, in Leap-year *April* 1, and we ſhall have the apparent times; namely, IX hours 16 minutes 12 ſeconds for the beginning of the Eclipſe, X hours 43 minutes 42 ſeconds for the time of greateſt obſcuration, and XII hours 14 minutes 12 ſeconds for the time when the Eclipſe ends.—But the beſt way is to apply this Equation to the true equal time of New Moon, before the projection be begun; as is done in Example I. For the motion or poſition of places on the Earth's diſc anſwer to apparent or ſolar time.

In this conſtruction it is ſuppoſed, that the angle under which the Moon's diſc is ſeen, during the whole time of the Eclipſe, continues invariably the ſame; and that the Moon's motion is uniform and rectilineal during that time.—But theſe ſuppoſitions do not exactly agree with the truth; and therefore, ſuppoſing the Elements given by the Tables to be accurate, yet the times and phaſes of the Eclipſe, deduced from its conſtruction, will not anſwer to exactly to what paſſeth in the Heavens; but may be at leaſt two or three minutes wrong, though done with the greateſt care.—Moreover, the paths of all places of conſiderable latitudes are nearer the center of the Earth's diſc, as ſeen from the Sun, than thoſe conſtructions make them; becauſe the Diſc is projected as if the Earth were a perfect ſphere, although it is known to be a ſpheriod. Conſequently, the Moon's ſhadow will go farther northward in all places of northern latitude, and farther ſouthward in all places of ſouthern latitude, than it is ſhewn to do in theſe projections.—According to *Meyer*'s Tables, this Eclipſe will be about a quarter of an hour ſooner than either theſe Tables, or Mr. *Flamſteed*'s, or Dr. *Halley*'s make it: and will not be annular at *London.* But M. *De la Caille*'s make it almoſt central.

The projection of Lunar Eclipſes.

When the Moon is within 12 degrees of either of her Nodes, at the time when ſhe is full, ſhe will be eclipſed, otherwiſe not.

We find by Example II, page 307, that at the time of mean Full Moon in *May* 1762, the Sun's diſtance from the aſcending Node was only 4° 49′ 35″; and the Moon being then oppoſite to the Sun, muſt have been juſt as near her deſcending Node, and was therefore eclipſed.

The elements for conſtructing an Eclipſe of the Moon, are eight in number, as follow:

1. The true time of Full Moon: and at that time, 2. The Moon's horizontal parallax. 3. The Sun's ſemidiameter. 4. The Moon's. 5. The ſemidiameter of the Earth's ſhadow at the Moon. 6. The Moon's latitude. 7. The angle of the Moon's viſible path with the Ecliptic. 8. The Moon's true horary motion from the Sun.—— Therefore,

1. *To find the true time of Full Moon.* Work as already taught in the Precepts.—Thus we have the true time of Full Moon in *May* 1762 (See Example II. page 307) on the 8th day, at 50 minutes 50 ſeconds paſt III o'clock in the morning.

2. *To find the Moon's horizontal parallax.* Enter Table XVII. with the Moon's mean Anomaly (at the above full) 9^{s} 2° 42′ 42″, and thereby take out her horizontal Parallax; which, by making the requiſite proportions, will be found to be 57′ 23″.

3, 4. *To find the ſemidiameters of the Sun and Moon.* Enter Table XVII. with their reſpective Anomalies, the Sun's being 10^{s} 7° 27′ 45″ (by the above Example) and the Moon's 9^{s} 2° 42′ 42″; and thereby take out their reſpective ſemidiameters: the Sun's 15′ 56″; and the Moon's 15′ 38″.

5. *To find the ſemidiameter of the Earth's ſhadow at the Moon.* Add the Sun's horizontal parallax, which is always 10″, to the Moon's, which in the preſent caſe is 57′ 23″, the ſum will be 57′ 33″, from which ſubtract the Sun's ſemidiameter 15′ 56″, and there will remain 41′ 37″ for the ſemidiameter of that part of the Earth's ſhadow which the Moon then paſſes through.

6. *To find the Moon's latitude.* Find the Sun's true diſtance from the aſcending Node (as already taught in page 317) at the true time of Full Moon; and this diſtance increaſed by ſix ſigns, will be the Moon's true diſtance from the ſame Node; and conſequently the argument for finding her true latitude, as ſhewn in page 319.

Thus, in Example II. the Sun's mean diſtance from the aſcending Node was 0ˢ 4° 49′ 35″, at the time of mean Full Moon: but it appears by the Example, that the true time thereof was 6 hours 33 minutes 38 ſeconds ſooner than the mean time, and therefore we muſt ſubtract the Sun's motion from the Node (found in Table XII. page 298) during this interval, from the above mean diſtance, 0ˢ 4° 49′ 35″, in order to have his mean diſtance from it at the true time of Full Moon.—Then to this apply the Equation of his mean diſtance from the Node, found in Table XV. by his mean Anomaly 10ˢ 7° 27′ 45″; and laſtly add ſix ſigns: ſo ſhall the Moon's true diſtance from the aſcending Node be found as follows:

		s	°	′	″
Sun from Node at mean Full Moon		0	4	49	35
His motion from it in	6 hours			15	35
	33 minutes			1	26
	38 ſeconds				2
Sum, ſubtract from the uppermoſt line				17	3
Remains his mean Diſtance at true Full Moon — — — —		0	4	32	32

Equation

	s	°	′	″
Equation of his mean Diſtance, add		1	38	0
Sun's true Diſtance from the Node	0	6	10	32
To which add	6	0	0	0
And the ſum will be	6	6	10	32

Which is the Moon's true diſtance from her aſcending Node at the true time of her being Full; and conſequently the Argument for finding her true Latitude at that time.—Therefore, with this argument, enter Table XVI. making proportions between the latitudes belonging to the 6th and 7th degree of the argument at the left hand (the ſigns being at the top) for the 10′ 32″, and it will give 32′ 21″ for the Moon's true latitude, which appears by the Table to be ſouth deſcending.

7. *To find the angle of the Moon's viſible path with the Ecliptic.* This may be ſtated at 5° 35′, without any error of conſequence in the projection of the Eclipſe.

8. *To find the Moon's true horary motion from the Sun.* With their reſpective Anomalies take out their horary motions from Table XVII. in page 302; and the Sun's horary motion ſubtracted from the Moon's, leaves remaining the Moon's true horary motion from the Sun: in the preſent caſe 30′ 52″.

Now collect theſe Elements together for uſe.

	D.	H.	M.	S.
1. True time of Full Moon in *May*, 1762	8	3	50	50
		°	′	″
2. Moon's horizontal Parallax		0	57	23
3. Sun's ſemidiameter		0	15	56
4. Moon's ſemidiameter		0	15	38
5. Semidiameter of the Earth's ſhadow at the Moon		0	41	37

6. Moon's

	°	′	″
6. Moon's true latitude, South deſcending	0	32	21
7. Angle of her viſible path with the Ecliptic	5	35	0
8. Her true horary motion from the Sun	0	30	52

PLATE XII. Theſe Elements being found for the conſtruction of the Moon's Eclipſe in *May*, 1762, proceed as follows:

Fig. II. Make a ſcale of any convenient length, as *W X*, and divide it into 60 equal parts, each part ſtanding for a minute of a degree.

Draw the right line *A C B* (Fig. 3.) for part of the Ecliptic, and *C D* perpendicular thereto for the ſouthern part of it's Axis; the Moon having ſouth latitude.

Add the ſemidiameters of the Moon and Earth's ſhadow together, which, in this Eclipſe, will make 57′ 15″; and take this from the ſcale in your compaſſes, and ſetting one foot in the point *C* as a center, with the other foot deſcribe the ſemicircle *A D B*; in one point of which the Moon's center will be at the beginning of the Eclipſe, and in another at the end thereof.

Take the ſemidiameter of the Earth's ſhadow, 41′ 37″, in your compaſſes from the ſcale, and ſetting one foot in the center *C*, with the other foot deſcribe the ſemicircle *K L M* for the ſouthern half of the Earth's ſhadow, becauſe the Moon's latitude is ſouth in this Eclipſe.

Make *C D* equal to the radius of a line of chords on the ſector, and ſet off the angle of the Moon's viſible path with the Ecliptic, 5° 35′, from *D* to *E*, and draw the right line *C F E* for the ſouthern half of the Axis of the Moon's Orbit, lying to the right hand from the Axis of the Ecliptic *C D*, becauſe the Moon's latitude is ſouth deſcending.—It would have been the ſame way (on the other ſide of the Ecliptic) if her Latitude had been north deſcending; but contrary in both caſes, if her Latitude had been either north aſcending or ſouth aſcending.

Biſect the angle *DCE* by the right line *Cg*; in which line, the true equal time of oppoſition of the Sun and Moon falls, as given by the Tables.

Take the Moon's latitude, 32′ 21″, from the ſcale with your compaſſes, and ſet it from *C* to *G*, in the line *CGg*; and through the point *G*, at right angles to *CFE*, draw the right line *PHGFN* for the path of the Moon's center.—Then, *F* ſhall be the point in the Earth's ſhadow, where the Moon's center is at the middle of the Eclipſe; *G*, the point where her center is at the tabular time of her being full; and *H*, the point where her center is at the inſtant of her ecliptical oppoſition.

Take the Moon's horary motion from the Sun, 30′ 52″, in your compaſſes from the ſcale; and with that extent make marks along the line of the Moon's path *PGN*: then divide each ſpace from mark to mark, into 60 equal parts, or horary minutes, and ſet the hours to the proper dots in ſuch a manner, that the dot ſignifying the inſtant of Full Moon (viz. 50 minutes 50 ſeconds after III in the morning) may be in the point *G*, where the line of the Moon's path cuts the line that biſects the angle *DCE*.

Take the Moon's ſemidiameter, 15′ 38″, in your compaſſes from the ſcale, and with that extent, as a radius, upon the points *N*, *F*, and *P*, as centers, deſcribe the circle *Q* for the Moon at the beginning of the Eclipſe, when ſhe touches the Earth's ſhadow at V; the circle *R* for the Moon at the middle of the Eclipſe; and the circle *S* for the Moon at the end of the Eclipſe, juſt leaving the Earth's ſhadow at *W*.

The point *N* denotes the inſtant when the Eclipſe begins, namely, at 15 minutes 10 ſeconds after II in the morning: the point *F* the middle of the Eclipſe at 47 minutes 45 ſeconds paſt III; and the point *P* the end of the Eclipſe, at 18 minutes after V.—At the greateſt obſcuration the Moon is 10 digits eclipſed.

Concerning an antient Eclipſe of the Moon.

It is recorded by *Ptolemy*, from *Hipparchus*, that on the 22d of *September*, the year 201 before the firſt year of Chriſt, the Moon roſe ſo much eclipſed at *Alexandria*, that the Eclipſe muſt have begun about half an hour before ſhe roſe.

Mr. *Carey* puts down this Eclipſe in his Chronology as follows, among ſeveral other antient ones, recorded by different authors.

Jul. Per.	Ecl. ● *Per. Calip.* 2. *An.* 54. *Hor.* 7.	*Nabonaſſar*
4513	*P. M. Alexandr. Dig. ecl.* 10.	547
Sept. 22.	[*Ptolem. l.* 4. *c.* 11.]	*Meſor.* 16.

That is, in the 4513th year of the *Julian* period, which was the 547th year from *Nabonaſſar*, and the 54th year of the ſecond *Calippic* period, on the 16th day of the month *Meſori* (which anſwers to the 22d of *September*) the Moon was 10 digits eclipſed at *Alexandria*, at 7 o'clock in the evening.

Now, as our Saviour was born (according to the *Dionyſian*, or vulgar Æra of his birth) in the 4713th year of the *Julian* period, it is plain that the 4513th year of that period was the 200th year before the year of Chriſt's birth; and conſequently 201 years before the year of Chriſt 1.

And, in the year 201, on the 22d of *September*, it appears by Example V. (page 310) that the Moon was full at 26 minutes 28 ſeconds paſt VII in the evening, in the meridian of *Alexandria*.

At that Time, the Sun's place was Virgo 26° 14′, according to our Tables; ſo that the Sun was then within 4 degrees of the Autumnal Equinox: and according to calculation, he muſt have ſet at *Alexandria* about 5 minutes after VI, and about one degree north of the weſt.

The Moon being full at that time, would have riſen juſt at Sunſet, about one degree ſouth of the eaſt, if ſhe had been in either of her Nodes, and her viſible place not depreſſed by Parallax.

But her parallactic depreſſion (as appears from her Anomaly, viz. $10^{s}\ 6^{\circ}$ nearly) muſt have been 55′ 17″; which exceeded her whole diameter by 24′ 53″; but then, ſhe muſt have been elevated 33′ 45″ by refraction; which ſubtracted from her Parallax, leaves 21′ 32″ for her viſible or apparent depreſſion.

And her true latitude was 30′$\frac{1}{2}$ north deſcending, which being contrary to her apparent depreſſion, and greater than the ſame by 8′ 58″, her true time of riſing muſt have been juſt about VI o'clock.

Now, as the Moon roſe about one degree ſouth of the Eaſt at *Alexandria*, where the viſible Horizon is land, and not ſea, we can hardly imagine her to have been leſs than 15 or 20 minutes of time above the true Horizon before ſhe was viſible.

It appears by Fig. 4, which is a delineation of this Eclipſe reduced to the time at *Alexandria*, that the Eclipſe began at 53 minutes after V in the evening; and conſequently 7 minutes before the Moon was in the true Horizon: to which, if we add 20 minutes for the interval between her true riſing and her being viſible, we ſhall have 27 minutes for the time that the Eclipſe was begun before the Moon was viſibly riſen.—The middle of this Eclipſe was at 30 minutes paſt VII, when it's quantity was almoſt 10 digits, and it's ending was at 6 minutes paſt IX in the evening.—So that our Tables come as near to the recorded time of this Eclipſe as can be expected, after an elapſe of 1960 years.

CHAP. XX.

Of the fixed Stars.

Why the fixed Stars appear bigger when viewed by the bare eye, than when ſeen thro' a teleſcope.

354. THE Stars are ſaid to be fixed, becauſe they have been generally obſerved to keep at the ſame diſtances from each other: their apparent diurnal revolutions being cauſed ſolely by the Earth's turning on it's Axis. They appear of a ſenſible magnitude to the bare eye, becauſe the retina is affected not only by the rays of light which are emitted directly from them, but by many thouſands more, which falling upon our eye-lids, and upon the ærial particles about us, are reflected into our eyes ſo ſtrongly, as to excite vibrations not only in thoſe points of the retina where the real images of the Stars are formed, but alſo in other points at ſome diſtance round about. This makes us imagine the Stars to be much bigger than they would appear, if we ſaw them only by the few rays which come directly from them, ſo as to enter our eyes without being intermixed with others. Any one may be ſenſible of this, by looking at a Star of the firſt magnitude through a long narrow tube; which, though it takes in as much of the ſky as would hold a thouſand ſuch Stars, it ſcarce renders *that* one viſible.

A proof that they ſhine by their own light.

The more a teleſcope magnifies, the leſs is the aperture through which the Star is ſeen; and conſequently the fewer rays it admits into the eye. Now ſince the Stars appear leſs in a teleſcope which magnifies 200 times than they do to the bare eye, inſomuch that they ſeem to be only indiviſible points, it proves at once that the Stars are at immenſe diſtances from us, and that they ſhine by their own proper light. If they ſhone by borrowed light, they would be as inviſible without teleſcopes as the Satellites of Jupiter are: for theſe

Satellites appear bigger when viewed with a good teleſcope than the largeſt fixed Stars do.

355. The number of Stars diſcoverable, in either Hemiſphere, by the naked eye, is not above a thouſand. This at firſt may appear incredible, becauſe they ſeem to be without number: But the deception ariſes from our looking confuſedly upon them, without reducing them into any order. For look but ſtedfaſtly upon a pretty large portion of the ſky, and count the number of Stars in it, and you will be ſurpriſed to find them ſo few. And, if one conſiders how ſeldom the Moon meets with any Stars in her way, although there are as many about her Path as in other parts of the Heavens, he will ſoon be convinced that the Stars are much thinner ſown than he was aware of. The *Britiſh* catalogue, which, beſides the Stars viſible to the bare eye, includes a great number which cannot be ſeen without the aſſiſtance of a teleſcope, contains no more than 3000, in both Hemiſpheres.

Their number much leſs than is generally imagined.

356. As we have incomparably more light from the Moon than from all the Stars together, it is the greateſt abſurdity to imagine that the Stars were made for no other purpoſe than to caſt a faint light upon the Earth: eſpecially ſince many more require the aſſiſtance of a good teleſcope to find them out, than are viſible without that inſtrument. Our Sun is ſurrounded by a ſyſtem of Planets and Comets; all which would be inviſible from the neareſt fixed Star. And from what we already know of the immenſe diſtance of the Stars, the neareſt may be computed at 32,000,000,000,000 of miles from us, which is further than a cannon-bullet would fly in 7,000,000 of years. Hence it is eaſy to prove, that the Sun, ſeen from ſuch a diſtance, would appear no bigger than a Star of the firſt magnitude. From all this it is highly probable that each Star is a Sun to a ſyſtem of worlds moving round it, though unſeen by us; eſpecially, as the doctrine of purality of worlds is rational,

The abſurdity of ſuppoſing the Stars were made only to ſhine upon us in the night.

rational, and greatly manifeſts the Power, Wiſdom, and Goodneſs of the great Creator.

Their different magnitudes. 357. The Stars, on account of their apparently various magnitudes, have been diſtributed into ſeveral claſſes or orders. Thoſe which appear largeſt, are called *Stars of the firſt magnitude*; the next to them in luſtre, *Stars of the ſecond magnitude*; and ſo on to the *ſixth*, which are the ſmalleſt that that are viſible to the bare eye. This diſtribution having been made long before the invention of teleſcopes, the Stars which cannot be ſeen without the aſſiſtance of theſe inſtruments, are diſtinguiſhed by the name of *Teleſcopic Stars.*

And diviſion into Conſtellations. 358. The antients divided the ſtarry Sphere into particular Conſtellations, or Syſtems of Stars, according as they lay near one another, ſo as to occupy thoſe ſpaces which the figures of different ſorts of animals or things would take up, if they were there delineated. And thoſe Stars which could not be brought into any particular Conſtellation, were called *unformed Stars.*

The uſe of this diviſion. 359. This diviſion of the Stars into different Conſtellations or Aſteriſms, ſerves to diſtinguiſh them from one another, ſo that any particular Star may be readily found in the Heavens by means of a Celeſtial Globe; on which the Conſtellations are ſo delineated as to put the moſt remarkable Stars into ſuch parts of the figures as are moſt eaſily diſtinguiſhed. The number of the antient Conſtellations is 48, and upon our preſent Globes about 70. On *Senex*'s Globes, *Bayer*'s Letters are inſerted; the firſt in the Greek Alphabet being put to the biggeſt Star in each Conſtellation, the ſecond to the next, and ſo on; by which means, every Star is as eaſily found as if a name were given to it. Thus, if the Star γ in the Conſtellation of the *Ram* be mentioned, every Aſtronomer knows as well what Star is meant as if it were pointed out to him in the Heavens.

360. There

The *Zodiac.*

360. There is alſo a diviſion of the Heavens into three parts. 1. The *Zodiac* (ζωδίακος) from ζῶδιον *Zodion* an Animal, becauſe moſt of the Conſtellations in it, which are twelve in number, are the figures of Animals: as *Aries* the Ram, *Taurus* the Bull, *Gemini* the Twins, *Cancer* the Crab, *Leo* the Lion, *Virgo* the Virgin, *Libra* the Balance, *Scorpio* the Scorpion, *Sagittarius* the Archer, *Capricornus* the Goat, *Aquarius* the Water-bearer, and *Piſces* the Fiſhes. The Zodiac goes quite round the Heavens: it is about 16 degrees broad, ſo that it takes in the Orbits of all the Planets, and likewiſe the Orbit of the Moon. Along the middle of this Zone or Belt is the Ecliptic, or Circle which the Earth deſcribes annually as ſeen from the Sun; and which the Sun appears to deſcribe as ſeen from the Earth. 2. All that Region of the Heavens, which is on the north ſide of the Zodiac, contains 21 Conſtellations. And 3. That on the ſouth ſide, 15.

The manner of dividing it by the antients.

361. The antients divided the *Zodiac* into the above 12 Conſtellations or Signs in the following manner. They took a veſſel with a ſmall hole in in the bottom, and having filled it with water, ſuffered the ſame to diſtil drop by drop into another veſſel ſet beneath to receive it; beginning at the moment when ſome Star roſe, and continuing until it roſe the next following night. The water fallen down into the receiver they divided into twelve equal parts; and having two other ſmall veſſels in readineſs, each of them fit to contain one part, they again poured all the water into the upper veſſel, and obſerving the riſing of ſome Star in the *Zodiac*, they at the ſame time ſuffered the water to drop into one of the ſmall veſſels; and as ſoon as it was full, they ſhifted it, and ſet an empty one in it's place. When each veſſel was full, they took notice what Star of the *Zodiac* roſe; and though this could not be done in one night, yet in many, they

obſerved the riſing of twelve Stars or points, by which they divided the *Zodiac* into twelve parts.

362. The names of the Conſtellations, and the number of Stars obſerved in each of them by different Aſtronomers, are as follows.

The antient Conſtellations.		*Ptolemy.*	*Tycho.*	*Hevel.*	*Flamſt.*
Urſa minor	The Little Bear	8	7	12	24
Urſa major	The Great Bear	35	29	73	87
Draco	The Dragon	31	32	40	80
Cepheus	Cepheus	13	4	51	35
Bootes, *Arctophilax*		23	18	52	54
Corona Borealis	The Northern Crown	8	8	8	21
Hercules, *Engonaſin*	Hercules kneeling	29	28	45	113
Lyra	The Harp	10	11	17	21
Cygnus, *Gallina*	The Swan	19	18	47	81
Caſſiepea	The Lady in her Chair	13	26	37	55
Perſeus	Perſeus	29	29	46	59
Auriga	The Waggoner	14	9	40	66
Serpentarius, *Ophiuchus*	Serpentarius	29	15	40	74
Serpens	The Serpent	18	13	22	64
Sagitta	The Arrow	5	5	5	18
Aquila, *Vultur*	The Eagle	15	12	23	71
Antinous	Antinous		3	19	
Delphinus	The Dolphin	10	10	14	18
Equulus, *Equi ſectio*	The Horſe's Head	4	4	6	10
Pegaſus, *Equus*	The Flying Horſe	20	19	38	89
Andromeda	Andromeda	23	23	47	66
Triangulum	The Triangle	4	4	12	16
Aries	The Ram	18	21	27	66
Taurus	The Bull	44	43	51	141
Gemini	The Twins	25	25	38	85
Cancer	The Crab	23	15	29	83
Leo	The Lion	35	30	49	95
Coma Berenices	Berenice's Hair		14	21	43
Virgo	The Virgin	32	33	50	110
Libra, *Chelæ*	The Scales	17	10	20	51
Scorpius	The Scorpion	24	10	20	44
Sagittarius	The Archer	31	14	22	69
Capricornus	The Goat	28	28	29	51
Aquarius	The Water-bearer	45	41	47	108
Piſces	The Fiſhes	38	36	39	113
Cetus	The Whale	22	21	45	97
Orion	Orion	38	42	62	78
Eridanus, *Fluvius*	Eridanus, *the River*	34	10	27	84
Lepus	The Hare	12	13	16	19
Canis major	The Great Dog	29	13	21	31
Canis minor	The Little Dog	2	2	13	14

The

The antient Conſtellations.		*Ptolemy.*	*Tycho.*	*Hevelius.*	*Flamſt.*
Argo Navis	The Ship	45	3	4	64
Hydra	The Hydra	27	19	31	60
Crater	The Cup	7	3	10	31
Corvus	The Crow	7	4		9
Centaurus	The Centaur	37			35
Lupus	The Wolf	19			24
Ara	The Altar	7			9
Corona Auſtralis	The Southern Crown	13			12
Piſces Auſtralis	The Southern Fiſh	18			24

The New Southern Conſtellations.

Columba Noachi	Noah's Dove	10
Robur Carolinum	The Royal Oak	12
Grus	The Crane	13
Phœnix	The Phenix	13
Indus	The Indian	12
Pavo	The Peacock	14
Apus, *Avis Indica*	The Bird of Paradiſe	11
Apis, *Muſca*	The Bee or Fly	4
Chamæleon	The Chameleon	10
Triangulum Auſtralis	The South Triangle	5
Piſcis volans, *Paſſer*	The Flying Fiſh	8
Dorado, *Xiphias*	The Sword Fiſh	6
Toucan	The American Gooſe	9
Hydrus	The Water Snake	10

Hevelius's Conſtellations made out of the unformed Stars.

		Hevelius.	*Flamſteed.*
Lynx	The Lynx	19	44
Leo minor	The Little Lion		53
Aſteron & Chara	The Greyhounds	23	25
Cerberus	Cerberus	4	
Vulpecula & Anſer	The Fox and Gooſe	27	35
Scutum Sobieſki	Sobieſki's Shield	7	
Lacerta	The Lizard	10	16
Camelopardalus	The Camelopard	32	58
Monoceros	The Unicorn	19	31
Sextans	The Sextant	11	41

The *Milky Way.*

363. There is a remarkable track round the Heavens, called the *Milky Way* from it's peculiar whiteneſs, which was formerly thought to be owing to a vaſt number of very ſmall Stars therein: but the teleſcope ſhews it to be quite otherwiſe; and therefore it's whiteneſs muſt be owing to ſome

other cauſe. This track appears ſingle in ſome parts, in others double.

Lucid Spots. 364. There are ſeveral little whitiſh ſpots in the Heavens, which appear magnified, and more luminous when ſeen through teleſcopes; yet without any Stars in them. One of theſe is in *Andromeda*'s girdle, and was firſt obſerved *A. D.* 1612, by *Simon Marius*: it has ſome whitiſh rays near it's middle, is liable to ſeveral changes, and is ſometimes inviſible. Another is near the Ecliptic, between the head and bow of *Sagittarius*: it is ſmall, but very luminous. A third is on the back of the *Centaur*, which is too far South to be ſeen in *Britain*. A fourth, of a ſmaller ſize, is before *Antinous*'s right foot; having a Star in it, which makes it appear more bright. A fifth is in the Conſtellation of *Hercules*, between the Stars ζ and η, which ſpot, though but ſmall, is viſible to the bare eye if the Sky be clear and the Moon abſent.

Cloudy Stars. 365. *Cloudy Stars* are ſo called from their miſty appearance. They look like dim Stars to the naked eye; but through a teleſcope they appear broad illuminated parts of the ſky; in ſome of which is one Star, in others more. Five of theſe are mentioned by *Ptolemy*. 1. One at the extremity of the right hand of *Perſeus*. 2. One in the middle of the *Crab*. 3. One unformed, near the Sting of the *Scorpion*. 4. The eye of *Sagittarius*. 5. One in the head of *Orion*. In the firſt of theſe appear more Stars through the teleſcope than in any of the reſt, although 21 have been counted in the head of *Orion*, and above 40 in that of the *Crab*. Two are viſible in the eye of *Sagittarius* without a teleſcope, and ſeveral more with it. *Flamſteed* obſerved a cloudy Star in the bow of *Sagittarius*, containing many ſmall Stars: and the Star *d* above *Sagittarius*'s right ſhoulder is encompaſſed with ſeveral more. Both *Caſſini* and *Flamſteed* diſcovered one between the *Great* and *Little Dog*, which is very full of Stars viſible only by the teleſcope. The two whitiſh ſpots near the South Pole, called the *Magellanic Clouds* by Sailors, which to the bare eye reſemble part of the Milky Way, appear through teleſcopes to be a mixture of ſmall Clouds and Stars. But the moſt remarkable of all the cloudy Stars is that in the middle of *Orion's Sword*, where ſeven Stars (of which three are very cloſe together) ſeem to ſhine through a cloud, very lucid near the middle, but faint and ill defined about the edges. It looks like a gap in the ſky, through which one may ſee (as it were) part of a much brighter region. Although moſt of theſe ſpaces are but a few minutes of a degree in breadth, yet, ſince they are among the fixed Stars, they muſt be ſpaces larger than what is occupied by our Solar Syſtem; and in which there ſeems to be a perpetual uninterrupted day among numberleſs Worlds, which no human art ever can diſcover.

Magellanic Clouds.

366. Several Stars are mentioned by antient Aſtronomers, which are not now to be found; and others are now viſible to the bare eye which are not recorded in the antient catalogue. *Hipparchus* obſerved a new Star about 120 years before CHRIST; but he has not mentioned in what part of the Heavens it was ſeen, although it occaſioned his making a Catalogue of the Stars; which is the moſt antient that we have.

Changes in the Heavens.

The firſt *New Star* that we have any good account of, was diſcovered by *Cornelius Gemma* on the 8th of *November* A. D. 1572, in the Chair of *Caſſiepea.* It ſurpaſſed *Sirius* in brightneſs and magnitude; and was ſeen for 16 months ſucceſſively. At firſt it appeared bigger than *Jupiter* to ſome eyes, by which it was ſeen at mid-day: afterwards it decayed gradually both in magnitude and luſtre, until *March* 1573, when it became inviſible.

New Stars.

On the 13th of *Auguſt* 1596, *David Fabricius* obſerved the *Stella Mira*, or wonderful Star, in the *Neck* of the *Whale*; which has been ſince found to appear and diſappear periodically, ſeven times in ſix years, continuing in the greateſt luſtre for 15 days together; and is never quite extinguiſhed.

In the year 1600, *William Janſenius* diſcovered a changeable Star in the *Neck* of the *Swan*; which, in time, became ſo ſmall as to be thought to diſappear entirely, till the years 1657, 1658, and 1659, when it recovered it's former luſtre and magnitude; but ſoon decayed, and is now of the ſmalleſt ſize.

In the year 1604, *Kepler* and ſeveral of his friends ſaw a new Star near the heel of the right foot of *Serpentarius*, ſo bright and ſparkling, that it exceeded any thing they had ever ſeen before; and took notice that it was every moment changing into ſome of the colours of the rainbow, except when it was near the Horizon, at which time it was generally white. It ſurpaſſed *Jupiter* in magnitude, which was near it all the month of *October*, but eaſily diſtinguiſhed from *Jupiter*, by the ſteady light of that Planet. It diſappeared between *October* 1605 and the *February* following, and has not been ſeen ſince that time.

In the year 1670, *July* 15, *Hevelius* diſcovered a new Star, which in *October* was ſo decayed as to be ſcarce perceptible. In *April* following it regained it's luſtre, but wholly diſappeared in *Auguſt*. In *March* 1672 it was ſeen again, but very ſmall; and has not been viſible ſince.

In the year 1686 a new Star was diſcovered by *Kirch*, which returns periodically in 404 days.

In the year 1672, *Caſſini* ſaw a Star in the *Neck* of the *Bull*, which he thought was not viſible in *Tycho*'s time; nor when *Bayer* made his Figures.

Cannot be Comets.

367. Many Stars, beſides thoſe above-mentioned, have been obſerved to change their magnitudes: and as none of them could ever be perceived to have tails, it is plain they could not be Comets; eſpecially as they had no Parallax, even when largeſt and brighteſt. It would ſeem that the periodical Stars have vaſt cluſters of dark ſpots, and very

ſlow rotations on their Axis; by which means, they muſt diſappear when the ſide covered with ſpots is turned towards us. And as for thoſe which break out all of a ſudden with ſuch luſtre, it is by no means improbable that they are Suns whoſe Fuel is almoſt ſpent, and again ſupplied by ſome of their Comets falling upon them, and occaſioning an uncommon blaze and ſplendor for ſome time: which indeed appears to be the greateſt uſe of the cometary part of any ſyſtem*.

Some Stars change there Places.

Some of the Stars, particularly *Arcturus*, have been obſerved to change their places above a minute of a degree with reſpect to others. But whether this be owing to any real motion in the Stars themſelves, muſt require the obſervations of many ages to determine. If our Solar Syſtem changeth it's Place, with regard to abſolute ſpace, this muſt in proceſs of time occaſion an apparent change in the diſtances of the Stars from each other: and in ſuch a caſe, the places of the neareſt Stars to us being more affected than thoſe which are very remote, their relative poſitions muſt ſeem to alter, though the Stars themſelves were really immoveable. On the other hand, if our own Syſtem be at reſt, and any of the Stars in real motion, this muſt vary their poſitions; and the more ſo, the nearer they are to us, or ſwifter their motions are; or the more proper the direction of their motion is, for our preception.

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* M. *Maupertuis*, in his diſſertation on the figures of the Celeſtial Bodies (p. 61—63) is of opinion that ſome Stars, by their prodigious quick rotations on their Axes, may not only aſſume the figures of oblate ſpheroids, but that by the great centrifugal force, ariſing from ſuch rotations, they may become of the figures of mill-ſtones; or be reduced to flat circular planes, ſo thin as to be quite inviſible when their edges are turned towards us; as Saturn's Ring is in ſuch poſitions. But when very excentric Planets or Comets go round any flat Star, in Orbits much inclined to it's Equator, the attraction of the Planets or Comets in their Perihelions muſt alter the inclination of the Axis of that Star; on which account it will appear more or leſs large and luminous, as it's broad ſide is more or leſs turned towards us. And thus he imagines we may account for the apparent changes of magnitude and luſtre in thoſe Stars, and likewiſe for their appearing and diſappearing.

The Ecliptic leſs oblique now to the Equator than formerly.

368. The obliquity of the Ecliptic to the Equinoctial is found at preſent to be above the third part of a degree leſs than *Ptolemy* found it. And moſt of the obſervers after him found it to decreaſe gradually down to *Tycho*'s time. If it be objected, that we cannot depend on the obſervations of the antients, becauſe of the incorrectneſs of their Inſtruments; we have to anſwer, that both *Tycho* and *Flamſteed* are allowed to have been very good obſervers; and yet we find that *Flamſteed* makes this obliquely 2½ minutes of a degree leſs than *Tycho* did, about 100 years before him: and as *Ptolemy* was 1324 years before *Tycho*, ſo the gradual decreaſe anſwers nearly to the difference of time between theſe three Aſtronomers. If we conſider, that the Earth is not a perfect ſphere, but an oblate ſpheroid, having it's Axis ſhorter than it's equatorial diameter; and that the Sun and Moon are conſtantly acting obliquely upon the greater quantity of matter about the Equator, pulling it, as it were, towards a nearer and nearer co-incidence with the Ecliptic; it will not appear improbable that theſe actions ſhould gradually diminiſh the Angle between thoſe Planes. Nor is it leſs probable that the mutual attraction of all the Planets ſhould have a tendency to bring their Orbits to a co-incidence: but this change is too ſmall to become ſenſible in many ages.

CHAP.

CHAP. XXI.

Of the Diviſion of Time. A perpetual Table of New Moons. The Times of the Birth and Death of CHRIST. *A Table of remarkable Æras or Events.*

369. THE parts of time are *Seconds*, *Minutes*, *Hours*, *Days*, *Years*, *Cycles*, *Ages*, and *Periods*.

A Year.

370. The original ſtandard, or integral meaſure of Time, is a Year; which is determined by the Revolution of ſome Celeſtial Body in it's Orbit, viz. the *Sun* or *Moon*.

Tropical Year.

371. The time meaſured by the Sun's Revolution in the Ecliptic, from any Equinox or Solſtice to the ſame again, is called the *Solar* or *Tropical Year*, which contains 365 days, 5 hours, 48 minutes, 57 ſeconds; and is the only proper or natural year, becauſe it always keeps the ſame ſeaſons to the ſame months.

Sydereal Year.

372. The quantity of time, meaſured by the Sun's Revolution as from any fixed Star to the ſame Star again, is called the *Sydereal Year*; which contains 365 days, 6 hours, 9 minutes, 14½ ſeconds; and is 20 minutes, 17½ ſeconds longer than the true Solar Year.

Lunar Year.

373. The time meaſured by twelve Revolutions of the Moon, from the Sun to the Sun again, is called the *Lunar Year*; it contains 354 days, 8 hours, 48 minutes, 36 ſeconds; and is therefore 10 days, 21 hours, 0 minutes, 21 ſeconds, ſhorter than the Solar Year. This is the foundation of the Epact.

Civil Year.

374. The *Civil Year* is that which is in common uſe among the different nations of the world; of which, ſome reckon by the Lunar, but moſt by the Solar. The Civil Solar Year contains 365 days, for three years running, which are called *Common Years*; and then comes in what is called the *Biſſex-*

tile or *Leap-year*, which contains 366 days. This is alſo called the *Julian Year* on account of *Julius Cæſar*, who appointed the Intercalary-day every fourth year, thinking thereby to make the Civil and Solar Year keep pace together. And this day, being added to the 23d of *February*, which in the *Roman* Calendar was the ſixth of the Calends of *March*, that ſixth day was twice reckoned, or the 23d and 24th were reckoned as one day; and was called *Bis ſextus dies*, and thence came the name *Biſſextile* for that year. But in our common Almanacks this day is added at the end of *February*.

Lunar Year. 375. The *Civil Lunar Year*, is alſo common or intercalary. The common Year conſiſts of 12 Lunations, which contain 354 days; at the end of which, the year begins again. The *Intercalary*, or *Embolimic* Year, is that wherein a month was added, to adjuſt the Lunar Year to the Solar. This method was uſed by the *Jews*, who kept their account by the Lunar Motions. But by intercalating no more than a month of 30 days, which they called *Ve-Adar*, every third year, they fell 3¾ days ſhort of the Solar Year in that time.

Roman Year. 376. The *Romans* alſo uſed the *Lunar Embolimic Year* at firſt, as it was ſettled by *Romulus* their firſt King, who made it to conſiſt only of ten months or Lunations; which fell 61 days ſhort of the Solar Year, and ſo their year became quite vague and unfixed; for which reaſon, they were forced to have a Table publiſhed by the High-Prieſt, to inform them when the ſpring and other ſeaſons began. But *Julius Cæſar*, as already mentioned, § 374, taking this troubleſome affair into conſideration, reformed the Calendar, by making the year to conſiſt of 365 days, 6 hours.

The original of the *Gregorian*, or *New Stile*. 377. The year thus ſettled, is what we ſtill make uſe of in *Britain*: but as it is ſomewhat more than 11 minutes longer than the *Solar Tropical Year*, the times of the Equinoxes go backward, and fall earlier by one day in about 130 years. In the time of the *Nicene Council* (A. D. 325) which was 1439 years ago, the Vernal Equinox fell on the 21ſt of *March*: and if we divide 1444 by 130, it will quote 11, which is the number of days the Equinox has fallen back ſince the Council of *Nice*. This cauſing great diſturbances, by unfixing the times of the celebration of *Eaſter*, and conſequently of all the other moveable Feaſts, Pope *Gregory* the 13th, in the year 1582, ordered ten days to be at once ſtruck out of that year; and the next day after the fourth of *October* was called the fifteenth. By this means the Vernal Equinox was reſtored to the 21ſt of *March*; and it was endeavoured, by the omiſſion of three intercalary days in 400 years, to make the Civil or Political year keep pace with the Solar for time to come. This new form of the year is called the *Gregorian Account*, or *New Stile*; which is received in all Countries where the Pope's Authority is acknowledged, and ought to be in all places where truth is regarded.

378. The principal diviſion of the year is into *Months*, which are of two ſorts, namely, *Aſtronomical* and *Civil*. The Aſtronomical month is the time in which the Moon runs through the *Zodiac*, and is either *Periodical* or *Synodical*. The Periodical Month is the time ſpent by the Moon in making one complete Revolution from any point of the Zodiac to the ſame again; which is $27^d\ 7^h\ 43^m$. The Synodical Month, called a *Lunation*, is the time contained between the Moon's parting with the Sun at a Conjunction, and returning to him again; which is $29^d\ 12^h\ 44^m$. The Civil Months are thoſe which are framed for the uſes of civil life; and are different as to their names, number of days, and times of beginning, in ſeveral different Countries. The firſt month of the *Jewiſh Year* fell according to the Moon in our *Auguſt* and *September*, Old Stile; the ſecond in *September* and *October*; and ſo on. The firſt month of the *Egyptian Year* began on the 29th of our *Auguſt*. The firſt month Months.

of the *Arabic* and *Turkiſh Year* began the 16th of *July*. The firſt month of the *Grecian Year* fell according to the Moon in *June* and *July*, the ſecond in *July* and *Auguſt*, and ſo on, as in the following Table.

379. A month is divided into four parts called *Weeks*, and a Week into ſeven parts called *Days*; ſo that in a *Julian* year there are 13 ſuch Months, or 52 Weeks, and one Day over. The Gentiles gave the names of the Sun, Moon, and Planets, to the Days of the Week. To the firſt, the Name of the *Sun*; to the ſecond, of the *Moon*; to the third, of *Mars*; to the fourth, of *Mercury*; to the fifth, of *Jupiter*; to the ſixth, of *Venus*; and to the ſeventh, of *Saturn*.

N°	The *Jewiſh* year.		Days
1	Tiſri	Aug.—Sept.	30
2	Marcheſvan	Sept.—Oct.	29
3	Caſleau	Oct.—Nov.	30
4	Tebeth	Nov.—Dec.	29
5	Shebat	Dec.—Jan.	30
6	Adar	Jan.—Feb.	29
7	Niſan *or* Abib	Feb.—Mar.	30
8	Jiar	Mar.—Apr.	29
9	Sivan	April—May	30
10	Tamuz	May—June	29
11	Ab	June—July	30
12	Elul	July—Aug.	29
	Days in the year		354

In the *Embolimic* year after *Adar* they added a month called *Ve-Adar* of 30 days.

N°	The *Egyptian* year.			Days
1	Thoth	Auguſt	29	30
2	Paophi	September	28	30
3	Athir	October	28	30
4	Chojac	November	27	30
5	Tybi	December	27	30
6	Mechir	January	26	30
7	Phamenoth	February	25	30
8	Parmuthi	March	27	30
9	Pachon	April	26	30
10	Payni	May	26	30
11	Epiphi	June	25	30
12	Meſori	July	25	30
	Epagomenæ or days added			5
	Days in the year			365

N°	The *Arabic* and *Turkiſh* year.			Days
1	Muharram	July	16	30
2	Saphar	Auguſt	15	29
3	Rabia I.	September	13	30
4	Rabia II.	October	13	29
5	Jomada I.	November	11	30
6	Jomada II.	December	11	29
7	Rajab	January	9	30
8	Shaſban	February	8	29
9	Ramadam	March	9	30
10	Shawal	April	8	29
11	Dulhaadah	May	7	30
12	Dulheggia	June	5	29
	Days in the year			354

The *Arabians* add 11 days at the end of every year, which keep the ſame months to the ſame ſeaſons

Nº	The ancient *Grecian* year.	Days
1	Hecatombæon — — June—July	30
2	Metagitnion — — July —Aug.	29
3	Boedromion — — Aug.—Sept.	30
4	Pyanepſion — — Sept.—Oct.	29
5	Maimacterion — — Oct. —Nov.	30
6	Poſideon — — — Nov.—Dec.	29
7	Gamelion — — — Dec.—Jan.	30
8	Antheſterion — — Jan.—Feb.	29
9	Elaphebolion — — Feb.—Mar.	30
10	Munichion — — — Mar.—Apr.	29
11	Thargelion — — Apr.—May	30
12	Schirrophorion — — May—June	29
	Days in the year — — — —	354

Days. 380. A *Day* is either *Natural* or *Artificial.* The Natural Day contains 24 hours; the Artificial, the time from Sun-riſe to Sun-ſet. The Natural Day is either *Aſtronomical* or *Civil.* The Aſtronomical Day begins at Noon, becauſe the increaſe and decreaſe of Days terminated by the Horizon are very unequal among themſelves; which inequality is likewiſe augmented by the inconſtancy of the horizontal Refractions § 183: and therefore the Aſtronomer takes the Meridian for the limit of diurnal Revolutions; reckoning Noon, that is, the inſtant when the Sun's Center is on the Meridian, for the beginning of the Day. The *Britiſh*, *French*, *Dutch*, *Germans*, *Spaniards*, *Portugueſe*, and *Egyptians*, begin the Civil Day at Midnight: the antient *Greeks*, *Jews*, *Bohemians*, *Sileſians*, with the modern *Italians*, and *Chineſe*, begin it at Sun-ſetting: and the antient *Babylonians*, *Perſians*, *Syrians*, with the modern *Greeks*, at Sun-riſing.

Hours. 381. An *Hour* is a certain determinate part of the Day, and is either equal or unequal. An equal Hour is the 24th part of a mean natural Day, as ſhewn by well-regulated Clocks and Watches; but theſe Hours are not quite equal as meaſured by the returns of the Sun to the Meridian, becauſe of the obliquity of the Ecliptic and Sun's unequal motion in it, § 224—245. Unequal Hours are thoſe by which the Artificial Day is divided into twelve Parts, and the Night into as many.

Minutes, Seconds, Thirds, and Scruples.

382. An Hour is divided into 60 equal parts called *Minutes*, a Minute into 60 equal parts called *Seconds*, and theſe again into 60 equal parts called *Thirds*. The *Jews*, *Chaldeans*, and *Arabians*, divide the Hour into 1080 equal parts called *Scruples*; which number contains 18 times 60, ſo that one minute contains 18 Scruples.

Cycles of the Sun, Moon, and Indiction.

383. A *Cycle* is a perpetual round, or circulation of the ſame parts of time of any ſort. The *Cycle of the Sun* is a revolution of 28 years, in which time the days of the months return again to the ſame days of the week; the Sun's Place to the ſame Signs and Degrees of the Ecliptic on the ſame months and days, ſo as not to differ one degree in 100 years; and the Leap-years begin the ſame courſe over again with reſpect to the days of the week on which the days of the months fall. The *Cycle of the Moon*, commonly called the *Golden Number*, is a revolution of 19 years; in which time, the Conjunctions, Oppoſitions and other Aſpects of the Moon, are within an hour and half of being the ſame as they were on the ſame days of the months 19 years before. The *Indiction* is a revolution of 15 years, uſed only by the *Romans* for indicating the times of certain payments made by the ſubjects to the Republic: It was eſtabliſhed by *Conſtantine*, A. D. 312.

To find the Years of theſe Cycles.

384. The year of our SAVIOUR's Birth, according to the vulgar Æra, was the 9th year of the Solar Cycle; the firſt year of the Lunar Cycle; and the 312th year after his birth was the firſt year of the *Roman* Indiction. Therefore, to find the year of the Solar Cycle, add 9 to any given year

of CHRIST, and divide the ſum by 28, the Quotient is the number of Cycles elapſed ſince his birth, and the remainder is the Cycle for the given year: if nothing remains, the Cycle is 28. To find the Lunar Cycle, add 1 to the given year of CHRIST, and divide the ſum by 19; the Quotient is the number of Cycles elapſed in the interval, and the remainder is the Cycle for the given year: if nothing remains, the Cycle is 19. Laſtly, ſubtract 312 from the given year of CHRIST, and divide the remainder by 15; and what remains after this diviſion is the Indiction for the given year: if nothing remains, the Indiction is 15.

The deficiency of the Lunar Cycle, and conſequence thereof.

385. Although the above deficiency in the Lunar Circle of an hour and half every 19 years be but ſmall, yet in time it becomes ſo ſenſible as to make a whole Natural Day in 310 years. So that, although this Cycle be of uſe, when the Golden Numbers are rightly placed againſt the days of the months in the Calendar, as in our *Common Prayer Books*, for finding the days of the mean Conjunctions or Oppoſitions of the Sun and Moon, and conſequently the time of *Eaſter*; it will only ſerve for 310 years, *Old Stile*. For as the New and Full Moons anticipate a day in that time, the Golden Numbers ought to be placed one day earlier in the Calendar for the next 310 years to come. Theſe Numbers were rightly placed againſt the days of New Moon in the Calendar, by the Council of *Nice*, A. D. 325; but the anticipation, which has been neglected ever ſince, is now grown almoſt into 5 days; and therefore all the Golden Numbers ought now to be placed 5 days higher in the Calendar for the *Old Stile* than they were at the time of the ſaid Council; or ſix days lower for the *New Stile*, becauſe at preſent it differs 11 days from the *Old*.

How to find the day of the New Moon by the Golden Number.

386. In the annexed Table, the Golden Numbers under the months ſtand againſt the days of New Moon in the left-hand column, for the *New Stile*;

Days.	*Jan.*	*Feb.*	*March*	*April*	*May*	*June*	*July*	*Auguſt*	*Sept.*	*Octob.*	*Nov.*	*Dec.*
1	9		9	17	17	6				11		19
2		17			6	14	14	3	11		19	
3	17	6	17	6			3	11		19	8	8
4	6		6	14	14	3			19	8		16
5		14			3	11	11	19	8		16	
6	14	3	14	3			19			16	5	5
7	3		3	11	11	19		8	16			13
8		11			19	8	8	16	5	5	13	
9	11	19	11	19						13		2
10			19	8	8	16	16	5	13		2	10
11	19	8					5	13	2	2	10	
12	8	16	8	16	16	5				10		18
13					5	13	13	2	10		18	7
14	16	5	16	5			2	10	18	18	7	
15	5		5	13	13	2				7		15
16		13			2	10	10	18	7		15	
17	13	2	13	2			18	7		15	4	4
18	2		2	10	10	18			15			12
19		10			18	7	7	15	4	4	12	
20	10	18	10	18			15			12	1	1
21	18		18	7	7	15		4	12			9
22		7			15	4	4	12	1	1	9	
23	7	15	7	15			12			9	17	17
24			15	4	4	12		1	9			6
25	15	4			12		1	9	17	17	6	
26	4		4	12		1				6		14
27		12		1	1	9	9	17	6		14	
28	12	1	12		9		17	6	14	14	3	3
29	1		1	9		17				3		11
30					17	6	6	14	3		11	
			9				14	3		11		19

Stile; adapted chiefly to the ſecond year after Leap-year, as being the neareſt mean for all the four; and will ſerve till the year 1900. Therefore, to find the day of New Moon in any month of a given year till that time, look for the Golden Number of that year under the deſired month, and againſt it, you have the day of New Moon in the left-hand column. Thus, ſuppoſe it were required to find the day of New Moon in *September* 1757; the Golden Number for that year is 10, which I look for under *September*, and right againſt it in the left-hand column I find 13, which is the day of New Moon in that month. *N.B.* If all the Golden Numbers, except 17 and 6, were ſet one day lower in the Table, it would ſerve from the beginning of the year 1900 till the End of the year 2199. The firſt Table after this Chapter ſhews the Golden Number for 4000 years after the birth of CHRIST; by looking for the even hundreds of any given year at the left hand, and for the reſt to make up that year at the head of the Table; and where the columns meet, you have the Golden Number (which is the ſame both in *Old* and *New Stile)* for the given year. Thus, ſuppoſe the Golden Number was wanted for the year 1757; I look for 1700 at the left hand of the Table, and for 57 at the top of it; then guiding my eye downward from 57 to over-againſt 1700, I find 10, which is the Golden Number for that year.

A perpetual Table of the time of New Moon to the neareſt hour, for the *Old Stile*.

387. But becauſe the Lunar Cycle of 19 years ſometimes includes five Leap-years, and at other times only four, this Table will ſometimes vary a day from the truth in Leap-years after *February*. And it is impoſſible to have one more correct, unleſs we extend it to four times 19 or 76 years; in which there are 19 Leap-years without a remainder. But even then to have it of perpetual uſe, it muſt be adapted to the *Old Stile*; becauſe in every centurial year not diviſible by 4, the regular courſe of Leap-years is interrupted in the *New*; as will

be the caſe in the year 1800. Therefore, upon the regular *Old Stile* plan, I have computed the following Table of the mean times of all the New Moons to the neareſt hour for 76 years; beginning with the year of CHRIST 1724, and ending with the year 1800.

This Table may be made perpetual, by deducting 6 hours from the time of New Moon in any given year and month from 1724 to 1800, in order to have the mean time of New Moon in any year and month 76 years afterward; or deducting 12 hours for 152 years, 18 hours for 228 years; and 24 hours for 304 years; becauſe in that time the changes of the Moon anticipate almoſt a complete natural day. And if the like number of hours be added for ſo many years paſt, we ſhall have the mean time of any New Moon already elapſed. Suppoſe, for example, the mean time of Change was required for *January* 1802; deduct 76 years, and there remains 1726, againſt which in the following Table, under *January*, I find the time of New Moon was on the 21ſt day, at 11 in the evening: from which take 6 hours, and there remains the 21ſt day, at 5 in the evening, for the mean time of Change in *January* 1802. Or, if the time be required for *May*, A. D. 1701, add 76 years, and it makes 1777, which I look for in the Table, and againſt it under *May* I find the New Moon in that year falls on the 25th day, at 9 in the evening; to which add 6 hours, and it gives the 26th day, at 3 in the Morning, for the time of New Moon in *May*, A. D. 1701. By this addition for time paſt, or ſubtraction for time to come, the Table will not vary 24 hours from the truth in leſs than 14592 years. And if, inſtead of 6 hours for every 76 years, we add or ſubtract only 5 hours 52 minutes, it will not vary a day in 10 millions of years.

Although this Table is calculated for 76 years only, and according to the *Old Stile*, yet by means of two eaſy Equations it may be made to anſwer as exactly to the *New Stile*, for any time to come. Thus, becauſe the year 1724 in this Table is the firſt year of the Cycle for which it is made; if from any year of CHRIST after 1800 you ſubtract 1723, and divide the overplus by 76, the quotient will ſhew how many entire Cycles of 76 years are elapſed ſince the beginning of the Cycle here provided for; and the remainder will ſhew the year of the current Cycle anſwering to the given year of CHRIST. Hence, if the remainder be 0, you muſt inſtead thereof put 76, and leſſen the Quotient by unity.

Then, look in the left-hand column of the Table for the number in your remainder, and againſt it you will find the times of all the mean New Moons in that year of the preſent Cycle. And whereas in 76 *Julian* years the Moon anticipates 5 hours 52 minutes, if therefore theſe 5 hours 52 minutes be multiplied by the above-found Quotient; that is, by the number of entire Cycles paſt; the product ſubtracted from the times in the Table will leave the corrected times of the New Moons to the *Old Stile*; which may be reduced to the *New Stile* thus:

Divide the number of entire hundreds in the given year of CHRIST by 4, multiply this quotient by 3, to the product add the remainder, and from their ſum ſubtract 2: this laſt remainder denotes the number of days to be added to the times above corrected, in order to reduce them to the *New Stile*. The reaſon of this is, that every 400 years of the *New Stile* gains 3 days upon the *Old Stile*: one of which it gains in each of the centurial years ſucceeding that which is exactly diviſible by 4 without a remainder; but then, when you have found the days ſo gained, 2 muſt be ſubtracted from their number on account of the rectifications made in the Calendar by the Council of *Nice*, and ſince by

Pope *Gregory*. It muſt alſo be obſerved, that the additional days found as above directed, do not take place in the centurial Years which are not multiples of 4 till *February* 29th, *Old Stile*, for on that day begins the difference between the *Stiles*; till which day, therefore, thoſe that were added in the preceding years muſt be uſed. The following Example will make this accommodation plain.

Required the mean time of New Moon in June, A. D. 1909, *N. S.*

From 1909 take 1723 years, and there remains	186
Which divided by 76, gives the quotient 2 and the remainder —	34
Then, againſt 34 in the Table is *June* — —	5^d 8^h 0^m Afternoon.
And 5^h 52^m multiplied by 2 make to be ſubtr. —	11 44
Remains the mean time according to the *Old Stile, June* — — —	5^d 9^h 16^m
Entire hundreds in 1909 are 19, which divide by 4, quotes — — —	4
And leaves a remainder of	3
Which quotient multiplied by 3 makes 12, and the remainder added makes — — — —	15
From which ſubtract 2, and there remains —	13
Which number of days added to the above time, *Old Stile*, gives *June* —	18^d 9^h 16^m Morn. *N. S.*

So the mean time of New Moon in *June* 1909 *New Stile* is the 18th day, at 16 minutes paſt 9 in the Morning.

If 11 days be added to the time of any New Moon in this Table, it will give the time thereof according to the *New Stile* till the year 1800. And if 14 days 18 hours 22 minutes be added to the mean time of New Moon in either *Stile*, it will give the mean time of the next Full Moon according to that *Stile*.

A TABLE *ſhewing the times of all the mean Changes of the Moon, to the neareſt Hour, through four Lunar Periods, or 76 years.* M *ſignifies morning,* A *afternoon.*

Years of the Cyc.	A.D.	January		February		March		April	
		D.	H.	D.	H.	D.	H.	D.	H.
1	1724	14	5 A	13	5M	13	6 A	12	7M
2	1725	3	2M	1	2 A	3	3M	1	4 A
3	1726	21	11 A	20	11M	21	12 A	20	1 A
4	1727	11	8M	9	9 A	11	9M	9	10 A
5	1728	30	6M	28	7 A	29	7M	27	8 A
6	1729	18	2 A	17	3M	18	4 A	17	4M
7	1730	7	11 A	6	0 A	8	1M	6	1 A
8	1731	26	9 A	25	10M	26	10 A	25	11M
9	1732	16	5M	14	6 A	15	7M	13	8 A
10	1733	4	2 A	3	3M	4	4 A	3	4M
11	1734	23	0 A	22	1M	23	1 A	22	2M
12	1735	12	9 A	11	9M	12	10 A	11	11M
13	1736	2 31	5M 6 A	—	—	1 30	7M 8 A	29	9M
14	1737	20	3M	18	4 A	20	4M	18	5 A
15	1738	9	11M	7	12 A	9	1 A	8	1M
16	1739	28	9M	26	10 A	28	11M	26	12 A
17	1740	17	6 A	16	7M	16	8 A	15	9M
18	1741	6	3M	4	4 A	6	4M	4	5 A
19	1742	24	12 A	23	1 A	25	2M	23	3 A
20	1743	14	9M	12	10 A	14	11M	12	12 A
21	1744	3	6 A	2	7M	2	8 A	1 30	9M 9 A
22	1745	21	4 A	20	5M	21	5 A	20	6M
23	1746	10	12 A	9	1 A	11	2M	9	3 A
24	1747	29	10 A	28	11M	29	11 A	28	0 A
25	1748	19	6M	17	7 A	18	8M	16	9 A
26	1749	7	3 A	6	4M	7	5 A	6	6M

Cy.	A.D.	*May*		*June*		*July*		*Auguſt*	
		D.	H.	D.	H.	D.	H.	D.	H.
1	1724	11	8 A	0	8M	9	9 A	8	10M
2	1725	1 30	4M 5 A	29	6M	28	7 A	27	8M
3	1726	20	1M	18	2 A	18	3M	16	4 A
4	1727	9	11M	7	12 A	7	0 A	6	1M
5	1728	27	8M	25	9 A	25	10M	23	11 A
6	1729	16	5 A	15	6M	14	7 A	12	7M
7	1730	6	2M	4	3 A	4	3M	2	4 A
8	1731	24	11 A	23	0 A	23	1M	21	2 A
9	1732	13	8M	11	9 A	11	10M	9	11 A
10	1733	2	5 A	1 30	6M 7 A	30	8M	28	8 A
11	1734	21	2 A	20	3M	19	4 A	18	5M
12	1735	10	11 A	9	0 A	9	1M	7	2 A
13	1736	28	9 A	27	10M	26	11 A	25	0 A
14	1737	18	5M	16	6 A	16	7M	14	8 A
15	1738	7	2 A	6	3 A	5	4 A	4	5M
16	1739	26	0 A	25	1M	24	2 A	23	3M
17	1740	14	9 A	13	10M	12	11 A	11	0 A
18	1741	4	5M	2	6 A	2 31	7M 7 A	30	8M
19	1742	23	3M	21	4 A	21	5M	19	6 A
20	1743	12	0 A	11	1M	10	2 A	9	3M
21	1744	30	10M	28	11 A	28	0 A	26	12 A
22	1745	19	6 A	18	7M	17	8 A	16	8M
23	1746	9	3M	7	4 A	7	5M	5	6 A
24	1747	27	12 A	26	1 A	26	2M	24	3 A
25	1748	16	9M	14	10 A	14	11M	12	12 A
26	1749	5	6 A	4	7M	3	8 A	2 31	9M 9 A

A TABLE *of the mean New Moons, &c.*

Yrs of the Cyc.	A.D.	*September* D.	H.	*October* D.	H.	*November* D.	H.	*December* D.	H.
1	1724	6	10 A	6	11M	4	12 A	4	1 A
2	1725	25	8 A	25	9M	23	10 A	23	11M
3	1726	15	5M	14	5 A	13	6M	12	7 A
4	1727	4	1 A	4	2M	2	3 A	2 31	4M 5 A
5	1728	22	11M	21	12 A	20	1 A	20	2M
6	1729	11	8 A	11	9M	9	10 A	9	11M
7	1730	2 30	5M 6 A	30	7M	28	8 A	28	9M
8	1731	20	2M	19	3 A	18	4M	17	5 A
9	1732	8	11M	7	12 A	6	1 A	6	2M
10	1733	27	9M	26	10 A	25	11M	24	11 A
11	1734	16	5 A	16	6M	14	7 A	14	8M
12	1735	6	2M	5	3 A	4	4M	3	5 A
13	1736	23	12 A	23	1 A	22	2M	21	3 A
14	1737	13	8M	12	9 A	11	10M	10	11 A
15	1738	2	5 A	2 31	6M 7 A	30	8M	29	8 A
16	1739	21	3 A	21	4M	19	5 A	19	6M
17	1740	9	12 A	9	1 A	8	2M	7	3 A
18	1741	28	9 A	28	10M	26	11 A	26	11M
19	1742	18	6M	17	7 A	16	8M	15	9 A
20	1743	7	3 A	7	4M	5	5 A	5	6M
21	1744	25	1 A	25	2M	23	3 A	23	3M
22	1745	14	9 A	14	10M	12	11 A	12	0 A
23	1746	4	6M	3	7 A	2	8M	1 31	9 A 10M
24	1747	23	3M	22	4 A	21	5M	20	6 A
25	1748	11	0 A	11	1M	9	2 A	9	3M
26	1749	30	10M	29	11 A	28	0 A	27	12 A

A TABLE *of the mean New Moons continued.*

Yrs of the Cyc.	A.D.	*January*		*February*		*March*		*April*	
		D.	H.	D.	H.	D.	H.	D.	H.
27	1750	26	1 A	25	2M	26	3 A	25	4M
28	1751	15	10 A	14	11M	15	11 A	14	0 A
29	1752	5	6M	3	7 A	4	8M	2	9 A
30	1753	23	4M	21	5 A	23	6M	21	7 A
31	1754	12	1 A	11	2M	12	3 A	11	4M
32	1755	1 31	10 A 11M	——		1 31	11 A 0 A	29	12 A
33	1756	20	7 A	19	8M	19	9 A	18	9M
34	1757	9	4M	7	5 A	9	6M	7	7 A
35	1758	28	2M	26	3 A	28	3M	26	4 A
36	1759	17	10M	15	11 A	17	0 A	16	1M
37	1760	6	7 A	5	8M	5	9 A	4	10M
38	1761	24	5 A	23	6M	24	7 A	23	8M
39	1762	14	2M	12	3 A	14	3M	12	4 A
40	1763	3	11M	1	12 A	3	0 A	2	1M
41	1764	22	8M	20	9 A	21	10M	19	11 A
42	1765	10	5 A	9	6M	10	6 A	9	7M
43	1766	29	2 A	28	3M	29	4 A	28	5M
44	1767	18	11 A	17	0 A	19	1M	17	2 A
45	1768	8	8M	6	9 A	7	10M	5	11 A
46	1769	26	6M	24	7 A	26	7M	24	8 A
47	1770	15	2 A	14	3M	15	4 A	14	5M
48	1771	4	11M	3	0 A	5	1M	3	2 A
49	1772	23	9 A	22	10M	22	10 A	21	11M
50	1773	12	5M	10	6 A	12	7M	10	8 A
51	1774	1 31	2 A 3M	——		1 31	4 A 5M	29	5 A
52	1775	20	0 A	19	1M	20	2 A	19	3M
53	1776	9	9 A	8	10M	8	10 A	7	11M

A TABLE *of the mean new Moons continued.*

Yrs of the Cyc.	A.D.	*May*		*June*		*July*		*Auguſt*	
		D.	H.	D.	H.	D.	H.	D.	H.
27	1750	24	4 A	23	5M	22	6 A	21	7M
28	1751	13	12 A	12	1 A	12	2M	10	3 A
29	1752	2 31	9M 10 A	30	11M	29	12 A	28	0 A
30	1753	21	7M	19	8 A	19	9M	17	10 A
31	1754	10	4 A	9	5M	8	6 A	7	7M
32	1755	29	1 A	28	2M	27	3 A	25	3M
33	1756	17	10 A	16	11M	15	12 A	14	1 A
34	1757	7	7M	5	8 A	5	9M	3	10 A
35	1758	26	4M	24	5 A	24	6M	22	7 A
36	1759	15	1 A	14	2M	13	3 A	12	2M
37	1760	3	10 A	2	11M	1 31	12 A 1 A	30	1M
38	1761	22	9 A	21	10M	20	10 A	19	11M
39	1762	12	4M	10	5 A	10	6M	8	7 A
40	1763	1 31	1 A 2M	29	3 A	29	4M	27	4 A
41	1764	19	11M	17	12 A	17	1 A	16	2M
42	1765	8	7 A	7	8M	6	9 A	5	10M
43	1766	27	5 A	26	6M	25	7 A	24	8M
44	1767	17	2M	15	3 A	15	4M	13	5 A
45	1768	5	11M	3	12 A	3	1 A	2 31	2M 2 A
46	1769	24	8M	22	9 A	22	10M	20	11 A
47	1770	13	5 A	12	4M	11	7 A	10	8M
48	1771	3	2M	1	3 A	1 30	4M 5 A	29	5M
49	1772	20	11 A	19	0 A	19	1M	17	2 A
50	1773	10	8M	8	9 A	8	9M	6	10 A
51	1774	29	6M	27	7 A	27	8M	25	8 A
52	1775	18	3 A	17	4M	16	5 A	15	6M
53	1776	6	12 A	5	0 A	5	1M	3	2 A

A TABLE *of the mean New Moons continued.*

Yrs of th C. c.	A.D.	September		October		November		December	
		D.	H.	D.	H.	D.	H	D.	H.
27	1750	19	7 A	19	8M	17	9 A	17	10M
28	1751	9	3M	8	4 A	7	5M	6	6 A
29	1752	27	1M	26	2 A	25	3M	24	3 A
30	1753	16	10M	15	11 A	14	0 A	14	1M
31	1754	5	7 A	5	8M	3	9 A	3	10M
32	1755	24	4 A	24	5M	22	6 A	22	6M
33	1756	13	1M	12	2 A	11	3M	10	4 A
34	1757	2	10M	1 31	11 A 0 A	30	1M	29	1 A
35	1758	21	7M	20	8 A	19	9M	18	10 A
36	1759	10	4 A	10	5M	8	6 A	8	7M
37	1760	28	2 A	28	3M	26	4 A	26	4M
38	1761	17	11 A	17	0 A	16	1M	15	2 A
39	1762	7	7M	6	8 A	5	9M	4	10 A
40	1763	26	5M	25	6 A	24	7M	23	7 A
41	1764	14	2 A	14	3M	12	4 A	12	5M
42	1765	3	10 A	3	11M	1	12 A	1 31	1 A 1M
43	1766	22	8 A	22	9M	20	10 A	20	11M
44	1767	12	6M	11	6 A	10	7M	9	8 A
45	1768	30	3M	29	4 A	28	5M	27	5 A
46	1769	19	11M	18	12 A	17	1 A	17	2M
47	1770	8	8 A	8	9M	6	10 A	6	11M
48	1771	27	6 A	27	7M	25	8 A	25	9M
49	1772	16	2M	15	3 A	14	4M	13	5 A
50	1773	5	11M	4	12 A	3	1 A	3	2M
51	1774	24	9M	23	10 A	22	11M	21	11 A
52	1775	13	6 A	13	7M	11	8 A	11	9M
53	1776	2	2M	1 31	3 A 4M	29	5 A	29	5M

A TABLE *of the mean New Moons concluded.*

YrsoftheCyc.	A.D.	*January*		*February*		*March*		*April*	
		D.	H	D.	H.	D.	H.	D.	H.
54	1777	27	6 A	26	7M	27	8 A	26	9M
55	1778	17	3M	15	4 A	17	5M	15	6 A
56	1779	6	0 A	5	1M	6	2 A	5	3M
57	1780	25	10M	23	11 A	24	11M	22	12 A
58	1781	13	6 A	12	7M	13	8 A	12	9M
59	1782	3	3M	1	4 A	3	5M	1	6 A
60	1783	22	1M	20	2 A	22	2M	20	3 A
61	1784	11	9M	9	10 A	10	11M	8	12 A
62	1785	29	7M	27	8 A	29	9M	27	10 A
63	1786	18	4 A	17	5M	18	5 A	17	6M
64	1787	7	12 A	6	1 A	8	2M	6	3 A
65	1788	26	10 A	25	11M	25	12 A	24	1 A
66	1789	15	7M	13	8 A	15	9M	13	10 A
67	1790	4	4 A	3	5M	4	5 A	3	6M
68	1791	23	1 A	22	2M	23	3 A	22	4M
69	1792	12	10 A	11	11M	11	12 A	10	1 A
70	1793	1 30	7M 8 A	—	—	1 30	9M 10 A	29	10M
71	1794	20	5M	18	6 A	20	6M	18	7 A
72	1795	9	1 A	8	2M	9	3 A	8	4M
73	1796	28	11M	26	12 A	27	0 A	26	1M
74	1797	16	7 A	15	8M	16	9 A	15	10M
75	1798	6	4M	4	5 A	6	6M	4	7 A
76	1799	25	2M	23	3 A	25	4M	23	5 A
1	1800	14	11M	12	12 A	13	0 A	12	1M

The year 1800 begins a new Cycle.

A TABLE *of the mean New Moons concluded.*

Yrs of the Cyc.	A.D.	*May*		*June*		*July*		*August*	
		D.	H.	D.	H.	D.	H.	D.	H.
54	1777	25	9 A	24	10M	23	11 A	22	0 A
55	1778	15	6M	13	7 A	13	8M	11	9 A
56	1779	4	3 A	3	4M	2	5 A	1 30	6M 6 A
57	1780	22	0 A	21	1M	20	2 A	19	3M
58	1781	11	9 A	10	10M	9	11 A	8	0 A
59	1782	1 30	6M 7 A	29	8M	28	9 A	27	9M
60	1783	20	3M	18	4 A	18	5M	16	6 A
61	1784	8	0 A	7	1M	6	2 A	5	3M
62	1785	27	10M	25	11 A	25	0 A	24	1M
63	1786	16	6 A	15	7M	14	8 A	13	9M
64	1787	6	3M	4	4 A	4	5M	2	6 A
65	1788	24	1M	22	2 A	22	3M	20	4 A
66	1789	13	10M	11	11 A	11	0 A	10	1M
67	1790	2	6 A	1 30	7M 8 A	30	9M	28	9 A
68	1791	21	4 A	20	5M	19	6 A	18	7M
69	1792	10	1M	8	2 A	8	3M	6	4 A
70	1793	28	11 A	27	0 A	27	1M	25	1 A
71	1794	18	7M	16	8 A	16	9M	14	10 A
72	1795	7	4 A	6	5M	5	6 A	4	7M
73	1796	25	1 A	24	2M	23	3 A	22	4M
74	1797	14	10 A	13	11M	12	12 A	11	1 A
75	1798	4	7M	2	8 A	2 31	9M 10 A	30	10M
76	1799	23	5M	21	6 A	21	6M	19	8 A
1	1800	11	1 A	10	2M	9	3 A	8	4M

A TABLE *of the mean New Moons concluded.*

Yrs of the Cyc.	A.D.	*September*		*October*		*November*		*December*	
		D.	H.	D.	H.	D.	H.	D.	H.
54	1777	20	12 A	20	1 A	19	2 M	18	3 A
55	1778	10	9 M	9	10 A	8	11 M	7	12 A
56	1779	29	7 M	28	8 A	27	9 M	26	9 A
57	1780	17	3 A	17	4 M	15	5 A	15	6 M
58	1781	6	12 A	6	1 A	5	2 M	4	3 A
59	1782	25	10 A	25	11 M	23	12 A	23	0 A
60	1783	15	6 M	14	7 A	13	8 M	12	9 A
61	1784	3	3 A	3	4 M	1	5 A	1 30	6 M 6 A
62	1785	22	1 A	22	2 M	20	3 A	20	3 M
63	1786	11	9 A	11	10 M	9	11 A	9	0 A
64	1787	1 30	6 M 7 A	30	8 M	28	9 A	28	9 M
65	1788	19	4 M	18	5 A	17	6 M	16	7 A
66	1789	8	1 A	8	2 M	6	3 A	6	4 M
67	1790	27	10 M	26	11 A	25	0 A	24	12 A
68	1791	16	7 A	16	8 M	14	9 A	14	10 M
69	1792	5	4 A	4	5 A	3	6 M	2	7 A
70	1793	24	2 M	23	3 A	22	4 M	21	4 A
71	1794	13	10 M	12	11 A	11	0 A	11	1 M
72	1795	2	7 A	2 31	8 M 9 A	30	10 M	29	10 A
73	1796	20	4 A	20	5 M	18	6 A	18	7 M
74	1797	10	1 M	9	2 A	8	3 M	7	4 A
75	1798	28	11 A	28	0 A	27	1 M	26	1 A
76	1799	18	8 M	17	9 A	16	10 M	15	11 A
1	1800	6	4 A	6	5 M	4	6 A	4	7 M

Eaſter Cycle deficient.

388. The *Cycle of Eaſter*, alſo called the *Dionyſian Period*, is a revolution of 532 years, found by multiplying the Solar Cycle 28 by the Lunar Cycle 19. If the New Moons did not anticipate upon this Cycle, *Eaſter-Day* would always be the *Sunday* next after the firſt Full Moon which follows the 21ſt of *March*. But, on account of the above anticipation, § 422. to which no proper regard was had before the late alteration of the *Stile*, the *Eccleſiaſtic Eaſter* has ſeveral times been a week different from the *true Eaſter* within this laſt Century: which inconvenience is now remedied by making the Table which uſed to find Eaſter *for ever*, in the Common Prayer Book, of no longer uſe than the Lunar difference from the *New Stile* will admit of.

Number of Direction.

389. The *earlieſt Eaſter poſſible* is the 22d of *March*, the *lateſt* the 25th of *April*. Within theſe limits are 35 days, and the number belonging to each of them is called the *Number of Direction*; becauſe thereby the time of Eaſter is found for any given year. To find the Number of Direction, according to the *New Stile*, enter Table V. following this Chapter, with the compleat hundreds of any given year at the top, and the years thereof (if any) below an hundred at the left hand; and where the columns meet is the Dominical Letter for the given year. Then, enter Table I. with the compleat hundreds of the ſame year at the left hand, and the years below an hundred at the top; and where the columns meet is the Golden Number for the ſame year. Laſtly, enter Table II. with the Dominical Letter at the left hand and Golden Number at the top; and where the columns meet is the Number of Direction for that year; which number, added to the 21ſt day of *March*, ſhews on what day either of *March* or *April Eaſter-Sunday* falls in that year. Thus, the Dominical Letter *New Stile* for the year 1757 is *B* (Table V) and the Golden Number is 10, (Table I) by which

in Table II. the Number of Direction is found to be 20; which, reckoning from the 21ſt of *March*, ends on the 10th of *April*, that *that* is *Eaſter-Sunday* in the year 1757. *N. B.* There are always two Dominical Letters to the Leap-year, the firſt of which takes place to the 24th of *February*, the laſt for the following part of the year.

To find the true *Eaſter*.

390. *The firſt ſeven Letters of the Alphabet* are commonly placed in the annual Almanacks, to ſhew on what days of the week the days of the months fall throughout the year. And becauſe one of thoſe ſeven Letters muſt neceſſarily ſtand againſt *Sunday*, it is printed in a capital form, and called the *Dominical Letter:* the other ſix being inſerted in ſmall characters, to denote the other ſix days of the week. Now, ſince a common *Julian Year* contains 365 Days, if this number be divided by 7 (the number of days in a week) there will remain one day. If there had been no remainder, it is plain the year would conſtantly begin on the ſame day of the week. But ſince 1 remains, it is as plain that the year muſt begin and end on the ſame day of the week; and therefore the next year will begin on the day following. Hence, when *January* begins on *Sunday*, *A* is the Dominical or *Sunday* Letter for that year: then, becauſe the next year begins on *Monday*, the *Sunday* will fall on the ſeventh day, to which is annexed the ſeventh Letter *G*, which therefore will be the Dominical Letter for all that year: and as the third year will begin on *Tueſday*, the *Sunday* will fall on the ſixth day; therefore *F* will be the *Sunday* Letter for that year. Whence it is evident, that the *Sunday* Letters will go annually in a retrograde order thus, *G*, *F*, *E*, *D*, *C*, *B*, *A*. And in the courſe of ſeven years, if they were all common ones, the ſame days of the week and Dominical Letters would return to the ſame days of the months. But becauſe there are 366 days in a Leap-year, if this number be divided by 7, there will remain two days over and above the

Dominical Letter.

52 weeks of which the year conſiſts. And therefore, if the Leap-year begins on *Sunday*, it will end on *Monday*; and the next year will begin on *Tueſday*, the firſt *Sunday* whereof muſt fall on the ſixth of *January*, to which is annexed the Letter *F*, and not *G*, as in common years. By this means, the Leap-year returning every fourth year, the order of the Dominical Letters is interrupted; and the Series cannot return to its firſt ſtate till after four times ſeven, or 28 years; and then the ſame days of the months return in order to the ſame days of the week as before.

To find the Dominical Letter.

391. *To find the Dominical Letter for any year either before or after the Chriſtian Æra.* In Table III. or IV. for *Old Stile*, or V. for *New Stile*, look for the hundreds of years at the head of the Table, and for the years below an hundred (to make up the given year) at the left hand: and where the columns meet, you have the Dominical Letter for the year deſired. Thus, ſuppoſe the Dominical Letter be required for the year of CHRIST 1758, *New Stile*, I look for 1700 at the head of Table V. and for 58 at the left hand of the ſame Table; and in the angle of meeting, I find *A*, which is the Dominical Letter for that year. If it was wanted for the ſame year *Old Stile*, it would be found by Table IV. to be *D*. But *to find the Dominical Letter for any given year before* CHRIST, ſubtract one from *that* year, and then proceed in all reſpects as juſt now taught, to find it by Table III. Thus, ſuppoſe the Dominical Letter be required for the 585th year before the firſt year of CHRIST, look for 500 at the head of Table III. and for 84 at the left hand; in the meeting of theſe columns is *FE*, which were the Dominical Letters for that year, and ſhews that it was a Leap-year; becauſe Leap-year has always two Dominical Letters.

To find the Days of the Months.

392. *To find the day of the month anſwering to any day of the week, or the day of the week anſwering to any day of the month, for any year paſt or to come.*

Having found the Dominical Letter for the given year, enter Table VI. with the Dominical Letter at the head; and under it, all the days in that column are *Sundays*, in the diviſions of the months; the next column to the right hand are *Mondays*; the next, *Tueſdays*; and ſo on to the laſt column under *G*; from which go back to the column under *A*, and thence proceed towards the right hand as before. Thus, in the year 1757, the Dominical Letter *New Stile* is *B*, in Table V; then in Table VI. all the days under *B* are *Sundays* in that year, *viz.* the 2d, 9th, 16th, 23d, and 30th of *January* and *October*; the 6th, 13th, 20th, and 27th of *February*, *March* and *November*; the 3d, 10th, and 17th of *April* and *July*, together with the 31ſt of *July*; and ſo on to the foot of the column. Then, of courſe, all the days under *C* on *Mondays*, namely, the 3d, 10th, *&c.* of *January* and *October*; and ſo of all the reſt in that column. If *the day of the week anſwering to any day of the month* be required, it is eaſily had from the ſame Table by the Letter that ſtands at the top of the column in which the given day of the month is found. Thus, the Letter that ſtands over the 28th of *May* is *A*; and in the year 585 before CHRIST, the Dominical Letters were found to be *FE*, § 391; which being a Leap-year, and *E* taking place from the 24th of *February* to the end of that year, ſhews by the Table that the 25th of *May* was on a *Sunday*; and therefore the 28th muſt have been on a *Wedneſday*; for when *E* ſtands for *Sunday*, *F* muſt ſtand for *Monday*, *G* for *Tueſday*, &c. Hence, as it is ſaid that the famous Eclipſe of the Sun foretold by THALES, by which a peace was brought about between the *Medes* and *Lydians*, happened on the 28th of *May*, in the 585th year before CHRIST, it fell on a *Wedneſday*.

393. From the multiplication of the Solar Cycle of 28 years into the Lunar Cycle of 19 years, and the *Roman* Indiction of 15 years, ariſes the great *Julian Period.*

Julian Period, conſiſting of 7980 years, which had its beginning 764 years before *Strauchius*' ſuppoſed year of the Creation (for no later could all the three Cycles begin together) and it is not yet compleated: and therefore it includes all other Cycles, Periods, and Æras. There is but one year in the whole Period that has the ſame numbers for the three Cycles of which it is made up: and therefore, if hiſtorians had remarked in their writings the Cycles of each year, there had been no diſpute about the time of any action recorded by them.

To find the year of this Period.

394. The *Dionyſian* or vulgar Æra of CHRIST's birth was about the end of the year of the *Julian* Period 4713; and conſequently the firſt year of his age, according to that account, was the 4714th year of the ſaid Period. Therefore, if to the current year of CHRIST we add 4713, the ſum will be the year of the *Julian* Period. So the year 1757 will be found to be the 6470th year of that Period. Or, to find the year of the *Julian* Period anſwering to any given year before the firſt year of CHRIST, ſubtract the number of that given year from 4714, and the remainder will be the year of the *Julian* Period. Thus, the year 585 before the firſt year of CHRIST (which was the 584th before his birth) was the 4129th year of the ſaid Period. Laſtly, to find the Cycles of the Sun, Moon, and Indiction for any given year of this Period, divide the given year by 28, 19, and 15; the three remainders will be the Cycles ſought, and the Quotients the numbers of Cycles run ſince the beginning of the Period. So in the above 4714th year of the *Julian* Period, the Cycle of the Sun was 10, the Cycle of the Moon 2, and the Cycle of Indiction 4; the Solar Cycle having run through 168 courſes, the Lunar 248, and the Indiction 314.

And the Cycles of that year.

The true Æra of CHRIST's birth.

395. The vulgar Æra of CHRIST's birth was never ſettled till the year 527, when *Dionyſius Exiguus*, a *Roman* Abbot, fixed it to the end of the 4713th year of the *Julian* Period, which was four

years too late.—For our SAVIOUR was born before the Death of *Herod*, who ſought to kill him as ſoon as he heard of his birth. And according to the teſtimony of *Joſephus* (B. xvii. ch. 8.) there was an Eclipſe of the Moon in the time of *Herod*'s laſt illneſs; which Eclipſe appears by our Aſtronomical Tables to have been in the year of the *Julian* Period 4710, *March* 13th, at 3 hours paſt midnight, at *Jeruſalem*. Now as our SAVIOUR muſt have been born ſome months before *Herod*'s Death, ſince in the interval he was carried into *Egypt*, the lateſt time in which we can fix the true Æra of his Birth is about the end of the 4709th year of the *Julian* Period.

There is a remarkable Prophecy delivered to us in the ninth chapter of the book of *Daniel*, which, from a certain *Epoch*, fixes the time of reſtoring the State of the *Jews*, and of building the Walls of *Jeruſalem*, the Coming of the MESSIAH, his Death, and the Deſtruction of *Jeruſalem*.—But ſome parts of this Prophecy *(Ver.* 25.) are ſo injudiciouſly pointed in our *Engliſh* tranſlation of the *Bible*, that, if they be read according to thoſe ſtops of pointing, they are quite unintelligible.—But the learned Dr. *Prideaux*, by altering theſe ſtops, makes the ſenſe very plain: and as he ſeems to me to have explained the whole of it better than any other author I have read on the ſubject, I ſhall ſet down the whole of the Prophecy according as he has pointed it, to ſhew in what manner he has divided it into four different parts.

Ver. 24. *Seventy weeks are determined upon thy People, and upon thy holy City, to finiſh the Tranſgreſſion, and to make an end of Sins, and to make reconciliation for Iniquity, and to bring in everlaſting Righteouſneſs, and to ſeal up the Viſion and the Prophecy, and to anoint the moſt holy.* Ver. 25. *Know therefore and underſtand, that from the going forth of the Commandment to reſtore and build* Jeruſalem *unto the* MESSIAH *the Prince ſhall be ſeven weeks and three-*

ſcore and two weeks, the ſtreet ſhall be built again, and the wall even in troublous times. Ver. 26. *And after threeſcore and two weeks ſhall* MESSIAH *be cut off, but not for himſelf, and the people of the Prince, that ſhall come, ſhall deſtroy the City and Sanctuary, and the end thereof ſhall be with a Flood, and to the end of the War deſolations are determined.* Ver. 27. *And he ſhall confirm the Covenant with many for one week, and in the midſt* of the week he ſhall cauſe the ſacrifice and the oblation to ceaſe, and for the overſpreading of abominations he ſhall make it deſolate even until the Conſummation, and that determined ſhall be poured upon the deſolate.*

This Commandment was given to *Ezra* by *Artaxerxes Longimanus*, in the ſeventh year of that King's reign (*Ezra*, ch. vii. ver. 11—26.) *Ezra* began the work, which was afterward accompliſhed by *Nehemiah*; in which they met with great oppoſition and trouble from the *Samaritans* and others, during the firſt ſeven weeks, or 49 years.

From this accompliſhment till the time when CHRIST's meſſenger *John* the Baptiſt began to preach the Kingdom of the MESSIAH, 62 weeks, or 434 years.

From thence to the beginning of CHRIST's public miniſtry, half a week, or 3½ years.

And, from thence to the death of CHRIST, half a week, or 3½ years; in which half week he preached, and *confirmed the Covenant* of the Goſpel with many of the *Jews*.

In all, from the going forth of the Commandment till the Death of CHRIST, 70 weeks, or 490 years.

And, laſtly, in a very ſtriking manner, the Prophecy foretels what ſhould come to paſs after the expiration of the *ſeventy weeks*; namely, *the Deſtruction of the City and Sanctuary by the People of the Prince that was to come*; which were the *Roman*

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* The Doctor ſays, that this ought to be rendered, *the half part of the week*, not *the midſt.*

Armies, under the command of *Titus* their Prince, who invaded *Jeruſalem* as a torrent, with their idolatrous images, which were an abomination to the *Jews*, and under which they marched againſt them, invaded their land, and beſieged their holy City, and by a calamitous war brought ſuch utter deſtruction upon both, that the *Jews* have never been able to recover themſelves, even to this day

Now, both by the undoubted Canon of *Ptolemy*, and the famous *Æra* of *Nabonaſſar*, the beginning of the ſeventh year of the reign of *Artaxerxes Longimanus* King of *Perſia* (who is called *Ahaſuerus* in the book of *Eſther)* is pinned down to the 4256th year of the *Julian* Period, in which year he gave *Ezra* the above mentioned ample Commiſſion: from which count 490 years to the Death of CHRIST, and it will carry the ſame to the 4746th year of the *Julian* Period.

Our *Saturday* is the *Jewiſh* Sabbath: and it is plain, from St. *Mark*, ch. xv. ver. 42. and St. *Luke*, ch. xxiii. ver. 54. that CHRIST was crucified on a *Friday*, ſeeing the Crucifixion was on the day next before the *Jewiſh* Sabbath.—And according to St. *John*, ch. xviii. ver. 28. on the day that the Paſſover was to be eaten, at leaſt by many of the *Jews*.

The *Jews* reckoned their months by the Moon, and their years by the revolution of the Sun: and they ate the Paſſover on the 14th day of the month *Niſan*, which was the firſt month of their year, reckoning from the firſt appearance of the New Moon, which at that time of the year might be on the evening of the day next after the change, if the ſky was clear. So that their 14th day of the month anſwers to our fifteenth day of the Moon, on which ſhe is full.—Conſequently, the Paſſover was always kept on the day of Full Moon.

And the Full Moon at which it was kept, was *that* one which happened next after the Vernal Equinox.—For *Joſephus* expreſsly ſays (*Antiq.* B. iii. ch. 10.) "The Paſſover was kept on the 14th day "of the month *Niſan*, according to the Moon, "when the Sun was in *Aries.*"—And the Sun always enters *Aries* at the inſtant of the Vernal Equinox; which, in our Saviour's time, fell on the 22d day of *March.*

The diſpute among Chronologers about the year of CHRIST's Death is limited to four or five years at moſt.—But, as we have ſhewn that he was crucified on the day of a Paſchal Full Moon, and on a *Friday*, all that we have to do, in order to aſcertain the year of his death, is only to compute in which of thoſe years there was a Paſſover Full Moon on a *Friday.*—For, the Full Moons anticipate eleven days every year (12 Lunar Months being ſo much ſhort of a Solar Year) and therefore, once in every three years at leaſt, the *Jews* were obliged to ſet their Paſſover a whole month forwarder than it fell by the courſe of the Moon, on the year next before, in order to keep it at the Full Moon next after the Equinox; therefore there could not be two Paſſovers on the ſame day of the week within the compaſs of a few neighbouring years. And I find by calculation, the *only* Paſſover Full Moon that fell on a *Friday*, for ſeveral years before or after the diſputed year of the Crucifixion, was on the third day of *April*, in the 4746th year of the *Julian* Period, which was the 490th year after *Ezra* received the above-mentioned Commiſſion from *Artaxerxes Longimanus*, according to *Ptolemy*'s Canon, and the year in which the MESSIAH was to be cut off, according to the Prophecy, reckoning from the going forth of *that* Commiſſion or Commandment: and this 490th year was the 33d year of our SAVIOUR's Age, reckoning from the vulgar Æra of his birth; but the 37th, reckoning from the true Æra thereof.

And, when we reflect on what the *Jews* told him, ſome time before his death (*John* viii. 57.) "*Thou* "*art not yet fifty years old*," we muſt confeſs that it ſhould ſeem much likelier to have been ſaid to a perſon near forty than to one but juſt turned of thirty. And we may eaſily ſuppoſe that St. *Luke* expreſſed himſelf only in round numbers, when he ſaid that *Chriſt was baptized about the 30th year of his age*, when he began his public miniſtry; as our SAVIOUR himſelf did, when he ſaid he ſhould lie *three days and three nights in the grave*.

The 4746th year of the *Julian* Period, which we have aſtronomically proved to be the year of the Crucifixion, was the 4th year of the 202d Olympiad; in which year, *Phlegon*, a heathen writer, tells us, *there was the moſt extraordinary Eclipſe of the Sun that ever was ſeen.* But I find by calculation, that there could be no total Eclipſe of the Sun at *Jeruſalem*, in a natural way, in that year.—So that what *Phlegon* here calls an Eclipſe of the Sun, ſeems to have been the great darkneſs for three hours at the time of our SAVIOUR's Crucifixion, as mentioned by the Evangeliſts: a darkneſs altogether ſupernatural, as the Moon was then in the ſide of the Heavens oppoſite to the Sun; and therefore could not poſſibly darken the Sun to any part of the Earth.

396. As there are certain fixed points in the Heavens from which Aſtronomers begin their computations, ſo there are certain points of time from which hiſtorians begin to reckon; and theſe points, or roots of time, are called *Æras* or *Epochs*. The moſt remarkable *Æras* are thoſe of the *Creation*, the *Greek Olympiads*, the Building of *Rome*, the *Æra* of *Nabonaſſar*, the Death of *Alexander*, the Birth of CHRIST, the *Arabian Hegira*, and the *Perſian Jeſdegird*: All which, together with ſeveral others of leſs note, have their Beginnings in the following Table fixed to the Years of the *Julian Period*, to the Age of the World at thoſe times, and to the Years before and after the year of CHRIST's birth.

A Table of remarkable Æras and Events.

	Julian Period.	Y. of the World.	Before Chriſt.
1. The Creation of the World	706	0	4007
2. The Deluge, or *Noah*'s Flood	2362	1656	2351
3. The *Aſſyrian* Monarchy founded by *Nimrod*	2537	1831	2176
4. The Birth of *Abraham*	2714	2008	1999
5. The Deſtruction of *Sodom* and *Gomorrah*	2816	2110	1897
6. The Beginning of the Kingdom of *Athens* by *Cecrops*	3157	2451	1556
7. *Moſes* receives the Ten Commandments	3222	2516	1491
8. The Entrance of the *Iſraelites* into *Canaan*	3262	2556	1451
9. The Deſtruction of *Troy*	3529	2823	1184
10. The Beginning of King *David*'s Reign	3650	2944	1063
11. The Foundation of *Solomon*'s Temple	3701	2995	1012
12. The *Argonautic* Expedition	3776	3070	937
13. *Lycurgus* forms his excellent Laws	3829	3103	884
14. *Arbaces*, the firſt King of the *Medes*	3838	3132	875
15. *Mandaucus*, the ſecond	3865	3159	848
16. *Soſarmus*, the third	3915	3209	798
17. The Beginning of the *Olympiads*	3938	3232	775
18. *Artica*, the fourth King of the *Medes*	3945	3239	768
19. The *Catonian Epocha* of the Building of *Rome*	3961	3255	752
20. The Æra of *Nabonaſſar*	3967	3261	746
21. The Deſtruction of *Samaria* by *Salmaneſer*	3992	3286	721
22. The firſt Eclipſe of the Moon on Record	3993	3287	720
23. *Cardicea*, the fifth King of the *Medes*	3996	3290	717
24. *Phraortes*, the ſixth	4058	3352	655
25. *Cyaxares*, the ſeventh	4080	3374	633
26. The firſt *Babyloniſh* Captivity by *Nebuchadnezzar*	4107	3401	606
27. The long War ended between the *Medes* and *Lydians*	4111	3405	602
28. The ſecond *Babyloniſh* Captivity, and Birth of *Cyrus*	4114	3408	599
29. The Deſtruction of *Solomon*'s Temple	4125	3419	588
30. *Nebuchadnezzar* ſtruck with Madneſs	4144	3438	569
31. *Daniel*'s Viſion of the four Monarchies	4158	3452	555
32. *Cyrus* begins to reign in the *Perſian* Empire	4177	3471	536
33. The Battle of *Marathon*	4223	3517	490
34. *Artaxerxes Longimanus* begins to reign	4249	3543	464
35. The Beginning of *Daniel*'s ſeventy Weeks of Years	4256	3350	457
36. The Beginning of the *Peloponneſian* War	4282	3576	431
37. *Alexander*'s Victory at *Arbela*	4383	3677	330
38. His Death	4390	3684	323
39. The Captivity of 100000 *Jews* by King *Ptolemy*	4393	3687	320
40. The Coloſſus of *Rhodes* thrown down by an Earthquake	4491	3875	222
41. *Antiochus* defeated by *Ptolemy Philopater*	4496	3790	217
42. The famous ARCHIMEDES murdered at *Syracuſe*	4506	3800	207
43. *Jaſon* butchers the Inhabitants of *Jeruſalem*	4543	3837	170
44. *Corinth* plundered and burnt by Conſul *Mummius*	4567	386	146
45. *Julius Cæſar* invades *Britain*	4659	3953	54
46. He corrects the Calendar	4677	396	46

47. Is

	Julian Period.	Y. of the World.	Before Chriſt.
47. Is killed in the Senate-Houſe — — — —	4671	3965	42
48. *Herod* made King of *Judea* — — — —	4673	3967	40
49. *Anthony* defeated at the Battle of *Actium* — —	4683	3977	30
50. *Agrippa* builds the *Pantheon* at *Rome* — —	4688	3982	25
51. The true Æra of CHRIST's Birth — — —	4709	4003	4
52. The Death of *Herod* — — — — — —	4710	4004	3
			After Chriſt.
53. The *Dionyſian* or vulgar Æra of CHRIST's Birth —	4713	4007	0
54. The true Year of his Crucifixion — — —	4746	4040	33
55. The Deſtruction of *Jeruſalem* — — — —	4783	4077	70
56. *Adrian* builds the long Wall in *Britain* — —	4833	4127	120
57. *Conſtantius* defeats the *Picts* in *Britain* — —	5019	4313	306
58. The Council of *Nice* — — — — — —	5038	4332	325
59. The Death of *Conſtantine the Great* — — —	5050	4344	337
60. The *Saxons* invited into *Britain* — — —	5158	4452	445
61. The *Arabian Hegira* — — — — — —	5335	4629	622
62. The Death of *Mohammed* the pretended Prophet —	5343	4637	630
63. The *Perſian Yeſdegird* — — — — —	5344	4638	631
64. The Sun, Moon, and all the Planets in Libra, Sept. 14, as ſeen from the Earth —	5899	5193	1186
65. The Art of Printing diſcovered — — —	6153	5447	1440
66. The Reformation begun by *Martin Luther* — —	6230	5524	1517

Age of the World uncertain.

In fixing the year of the Creation to the 706th year of the *Julian* Period, which was the 4007th year before the year of CHRIST's Birth, I have followed Mr. *Bedford* in his Scripture Chronology, printed A. D. 1730, and Mr. *Kennedy* in a work of the ſame kind, printed A. D. 1762.—Mr. *Bedford* takes it only for granted that the World was created at the time of the Autumnal Equinox; but Mr. *Kennedy* affirms that the ſaid Equinox was at the noon of the fourth day of the Creation-week, and that the Moon was then 24 hours paſt her Oppoſition to the Sun.—If *Moſes* had told us the ſame things, we ſhould have had ſufficient *data* for fixing the *Æra* of the Creation: but, as he has been ſilent on theſe points, we muſt conſider the beſt accounts of Chronologers as entirely hypothetical and uncertain.

TABLE I. *Shewing the Golden Number (which is the ſame both in the Old and New Stile) from the Chriſtian Æra to A. D.* 3800.

Hundreds of Years.		Years leſs than an Hundred.																		
		0 19 38 57 76 95	1 20 39 58 77 96	2 21 40 59 78 97	3 22 41 60 79 98	4 23 42 61 80 99	5 24 43 62 81	6 25 44 63 82	7 26 45 64 83	8 27 46 65 84	9 28 47 66 85	10 29 48 67 86	11 30 49 68 87	12 31 50 69 88	13 32 51 70 89	14 33 52 71 90	15 34 53 72 91	16 35 54 73 92	17 36 55 74 93	18 37 56 75 94
0	1900	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
100	2000	6	7	8	9	10	11	12	13	14	15	16	17	18	19	1	2	3	4	5
200	2100	11	12	13	14	15	16	17	18	19	1	2	3	4	5	6	7	8	9	10
300	2200	16	17	18	19	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
400	2300	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	1
500	2400	7	8	9	10	11	12	13	14	15	16	17	18	19	1	2	3	4	5	6
600	2500	12	13	14	15	16	17	18	19	1	2	3	4	5	6	7	8	9	10	11
700	2600	17	18	19	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
800	2700	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	1	2
900	2800	8	9	10	11	12	13	14	15	16	17	18	19	1	2	3	4	5	6	7
1000	2900	13	14	15	16	17	18	19	1	2	3	4	5	6	7	8	9	10	11	12
1100	3000	18	19	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
1200	3100	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	1	2	3
1300	3200	9	10	11	12	13	14	15	16	17	18	19	1	2	3	4	5	6	7	8
1400	3300	14	15	16	17	18	19	1	2	3	4	5	6	7	8	9	10	11	12	13
1500	3400	19	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
1600	3500	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	1	2	3	4
1700	3600	10	11	12	13	14	15	16	17	18	19	1	2	3	4	5	6	7	8	9
1800	3700	15	16	17	18	19	1	2	3	4	5	6	7	8	9	10	11	12	13	14

TABLE II. *Shewing the Number of Direction, for finding Eaſter Sunday by the Golden Number and Dominical Letter.*

G. N.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
A	26	19	5	26	12	33	19	12	26	19	5	26	12	5	26	12	33	19	12
B	27	13	6	27	13	34	20	13	27	20	6	27	13	6	20	13	34	20	6
C	28	14	7	21	14	35	21	7	28	21	7	28	14	7	21	14	28	21	7
D	29	15	8	22	15	29	22	8	29	15	8	29	15	1	22	15	29	22	8
E	30	16	2	23	16	30	23	9	30	16	9	23	16	2	23	9	30	23	9
F	24	17	3	24	10	31	24	10	31	17	10	24	17	3	24	10	31	17	10
G	25	18	4	25	11	32	18	11	32	18	4	25	18	4	25	11	32	18	11

This Table is adapted to the New Stile.

TABLE III. *Shewing the Dominical Letters, Old Stile, for 4200 Years before the Chriſtian Æra.*

Bef. Chriſt.				Hundreds of Years.						
Years leſs than an Hundred.				0 700 1400 2100 2800 3500	100 800 1500 2200 2900 3600	200 900 1600 2300 3000 3700	300 1000 1700 2400 3100 3800	400 1100 1800 2500 3200 3900	500 1200 1900 2600 3300 4000	600 1300 2000 2700 3400 4100
0	28	56	84	D C	C B	B A	A G	G F	F E	E D
1	29	57	85	E	D	C	B	A	G	F
2	30	58	86	F	E	D	C	B	A	G
3	31	59	87	G	F	E	D	C	B	A
4	32	60	88	B A	A G	G F	F E	E D	D C	C B
5	33	61	89	C	B	A	G	F	E	D
6	34	62	90	D	C	B	A	G	F	E
7	35	63	91	E	D	C	B	A	G	F
8	36	64	92	G F	F E	E D	D C	C B	B A	A G
9	37	65	93	A	G	F	E	D	C	B
10	38	66	94	B	A	G	F	E	D	C
11	39	67	95	C	B	A	G	F	E	D
12	40	68	96	E D	D C	C B	B A	A G	G F	F E
13	41	69	97	F	E	D	C	B	A	G
14	42	70	98	G	F	E	D	C	B	A
15	43	71	99	A	G	F	E	D	C	B
16	44	72		C B	B A	A G	G F	F E	E D	D C
17	45	73		D	C	B	A	G	F	E
18	46	74		E	D	C	B	A	G	F
19	47	75		F	E	D	C	B	A	G
20	48	76		A G	G F	F E	E D	D C	C B	B A
21	49	77		B	A	G	F	E	D	C
22	50	78		C	B	A	G	F	E	D
23	51	79		D	C	B	A	G	F	E
24	52	80		F E	E D	D C	C B	B A	A G	G F
25	53	81		G	F	E	D	C	B	A
26	54	82		A	G	F	E	D	C	B
27	55	83		B	A	G	F	E	D	C

TABLE IV. *Shewing the Dominical Letters, Old Stile, for 4200 Years after the Chriſtian Æra.*

After Chriſt. Years leſs than an Hundred.				Hundreds of Years.						
				0 700 1400 2100 2800 3500	100 800 1500 2200 2900 3600	200 900 1600 2300 3000 3700	300 1000 1700 2400 3100 3800	400 1100 1800 2500 3200 3900	500 1200 1900 2600 3300 4000	600 1300 2000 2700 3400 4100
0	28	56	84	D C	E D	F E	G F	A G	B A	C B
1	29	57	85	B	C	D	E	F	G	A
2	30	58	86	A	B	C	D	E	F	G
3	31	59	87	G	A	B	C	D	E	F
4	32	60	88	F E	G F	A G	B A	C B	D C	E D
5	33	61	89	D	E	F	G	A	B	C
6	34	62	90	C	D	E	F	G	A	B
7	35	63	91	B	C	D	E	F	G	A
8	36	64	92	A G	B A	C B	C D	E D	F E	G F
9	37	65	93	F	G	A	B	C	D	E
10	38	66	94	E	F	G	A	B	C	D
11	39	67	95	D	E	F	G	A	B	C
12	40	68	96	C B	D C	E D	F E	G F	A G	B A
13	41	69	97	A	B	C	D	E	F	G
14	42	70	98	G	A	B	C	D	E	F
15	43	71	99	F	G	A	B	C	D	E
16	44	72		E D	F E	G F	A G	B A	C B	D C
17	45	73		C	D	E	F	G	A	B
18	46	74		B	C	D	E	F	G	A
19	47	75		A	B	C	D	E	F	G
20	48	76		G F	A G	B A	C B	D C	E D	F E
21	49	77		E	F	G	A	B	C	D
22	50	78		D	E	F	G	A	B	C
23	51	79		C	D	E	F	G	A	B
24	52	80		B A	C B	D C	E D	F E	G F	A G
25	53	81		G	A	B	C	D	E	F
26	54	82		F	G	A	B	C	D	E
27	55	83		E	F	G	A	B	C	D

TABLE V. *The Dominical Letter, New Stile, for 4000 Years after the Chriſtian Æra.*

After Chriſt.				Hundreds of Years.			
Years leſs than an Hundred.				100 500 900 1300 1700 2100 2500 2900 3300 3700	200 600 1000 1400 1800 2200 2600 3000 3400 3800	300 700 1100 1500 1900 2300 2700 3100 3500 3900	400 800 1200 1600 2000 2400 2800 3200 3600 4000
				C	E	G	B A
1	29	57	85	B	D	F	G
2	30	58	86	A	C	E	F
3	31	59	87	G	B	D	E
4	32	60	88	F E	A G	C B	D C
5	33	61	89	D	F	A	B
6	34	62	90	C	E	G	A
7	35	63	91	B	D	F	G
8	36	64	92	A G	C B	E D	F E
9	37	65	93	F	A	C	D
10	38	66	94	E	G	B	C
11	39	67	95	D	F	A	B
12	40	68	96	C B	E D	G F	A G
13	41	69	97	A	C	E	F
14	42	70	98	G	B	D	E
15	43	71	99	F	A	C	D
16	44	72		E D	G F	B A	C B
17	45	73		C	E	G	A
18	46	74		B	D	F	G
19	47	75		A	C	E	F
20	48	76		G F	B A	D C	E D
21	49	77		E	G	B	C
22	50	78		D	F	A	B
23	51	79		C	E	G	A
24	52	80		B A	D C	F E	G F
25	53	81		G	B	D	E
26	54	82		F	A	C	D
27	55	83		E	G	B	C
28	56	84		D C	F E	A G	B A

TABLE VI. *Shewing the Days of the Months for both Stiles by the Dominical Letters.*

Week Day.	A	B	C	D	E	F	G
	1	2	3	4	5	6	7
	8	9	10	11	12	13	14
January 31	15	16	17	18	19	20	21
October 31	22	23	24	25	26	27	28
	29	30	31				
				1	2	3	4
	5	6	7	8	9	10	11
Feb. 28-29	12	13	14	15	16	17	18
March 31	19	20	21	22	23	24	25
November 30	26	27	28	29	30	31	
							1
	2	3	4	5	6	7	8
	9	10	11	12	13	14	15
April 30	16	17	18	19	20	21	22
July 31	23	24	25	26	27	28	29
	30	31					
			1	2	3	4	5
	6	7	8	9	10	11	12
	13	14	15	16	17	18	19
August 31	20	21	22	23	24	25	26
	27	28	29	30	31		
						1	2
	3	4	5	6	7	8	9
	10	11	12	13	14	15	16
September 30	17	18	19	20	21	22	23
December 31	24	25	26	27	28	29	30
	31						
		1	2	3	4	5	6
	7	8	9	10	11	12	13
	14	15	16	17	18	19	20
May 31	21	22	23	24	25	26	27
	28	29	30	31			
					1	2	3
	4	5	6	7	8	9	10
	11	12	13	14	15	16	17
June 30	18	19	20	21	22	23	24
	25	26	27	28	29	30	

CHAP. XXII.

A Deſcription of the Aſtronomical Machinery ſerving to explain and illuſtrate the foregoing part of this Treatiſe.

Fronting the Title Page. The ORRERY.

397. THE ORRERY. This Machine ſhews the Motions of the Sun, Mercury, Venus, Earth, and Moon; and occaſionally, the ſuperior Planets, Mars, Jupiter, and Saturn, may be put on; Jupiter's four Satellites are moved round him in their proper times by a ſmall Winch; and Saturn has his five Satellites, and his Ring which keeps it's Paralleliſm round the Sun; and by a Lamp put in the Sun's place, the Ring ſhews all the Phaſes deſcribed in the 204th Article.

The Sun.

In the Center, No. 1. repreſents the SUN, ſupported by it's Axis inclining almoſt 8 Degrees from the Axis of the Ecliptic; and turning round in $25\frac{1}{4}$ days on it's Axis, of which the North Pole inclines toward the 8th Degree of Piſces in the great Ecliptic (No. 11.) whereon the Months and Days are engraven over the Signs and Degrees in which the Sun appears, as ſeen from the Earth, on the different days of the year.

The Ecliptic.

Mercury.

The neareſt Planet (No. 2.) to the Sun is *Mercury*, which goes round him in 87 days 23 hours, or $87\frac{23}{24}$ diurnal rotations of the Earth; but has no Motion round it's Axis in the Machine, becauſe the time of it's diurnal Motion in the Heavens is not known to us.

Venus.

The next Planet in order is *Venus* (No. 3.) which performs her annual Courſe in 224 days 17 hours; and turns round her Axis in 24 days 8 hours, or in $24\frac{1}{3}$ diurnal rotations of the Earth. Her Axis inclines 75 Degrees from the Axis of the Ecliptic, and her North Pole inclines towards the 20th Degree of Aquarius, according to the obſervations of *Bianchini*.

Bianchini. She ſhews all the Phenomena deſcribed from the 30th to the 44th Article in Chap. I.

The Earth. Next without the Orbit of Venus is the *Earth*, (No. 4.) which turns round it's Axis, to any fixed point at a great diſtance, in 23 hours 56 minutes 4 ſeconds, of mean ſolar time (§ 221, *&c ſeq.)* but from the Sun to the Sun again in 24 hours of the ſame time. No. 6. is a ſydereal Dial-Plate under the Earth; and No. 7. a ſolar Dial-Plate on the cover of the Machine. The Index of the former ſhews ſydereal, and of the latter, ſolar time; and hence, the former Index gains one entire revolution on the latter every year, as 365 ſolar or natural days contain 366 ſydereal days, or apparent revolutions of the Stars. In the time that the Earth makes $365\frac{1}{4}$ diurnal rotations on it's Axis, it goes once round the Sun in the Plane of the Ecliptic; and always keeps oppoſite to a moving Index (No. 10.) which ſhews the Sun's apparent daily change of place, and alſo the days of the months.

The Earth is half covered with a black cap, for dividing the apparently enlightened half next the Sun from the other half, which when turned away from him is in the dark. The edge of the cap repreſents *the Circle bounding Light and Darkneſs*, and ſhews at what time the Sun riſes and ſets to all places throughout the year. The Earth's Axis inclines $23\frac{1}{2}$ Degrees from the Axis of the Ecliptic, the North Pole inclines toward the beginning of Cancer, and keeps it's Paralleliſm throughout it's annual Courſe, § 48, 202; ſo that in Summer the northern parts of the Earth incline towards the Sun, and in Winter from him: by which means, the different lengths of days and nights, and the cauſe of the various ſeaſons, are demonſtrated to ſight.

There is a broad Horizon, to the upper ſide of which is fixed a Meridian ſemicircle in the North and South Points, graduated on both ſides from the Horizon to 90° in the Zenith, or vertical Point.

The edge of the Horizon is graduated from the Eaſt and Weſt to the South and North Points, and within theſe Diviſions are the Points of the Compaſs. From the lower ſide of this thin Horizon-Plate ſtand out four ſmall Wires, to which is fixed a Twilight-Circle 18 Degrees from the graduated ſide of the Horizon all round. This Horizon may be put upon the Earth (when the cap is taken away) and rectified to the Latitude of any place: and then, by a ſmall Wire called *the Solar Ray*, which may be put on ſo as to proceed directly from the Sun's Center towards the Earth's, but to come no farther than almoſt to touch the Horizon. The beginning of Twilight, time of Sun-riſing, with his Amplitude, Meridian Altitude, Time of Setting, Amplitude then, and End of Twilight, are ſhewn for every day of the year, at *that* place to which the Horizon is rectified.

The Moon. The Moon (No. 5.) goes round the Earth, from between it and any fixed point at a great diſtance, in 27 days 7 hours 43 minutes, or through all the Signs and Degrees of her Orbit; which is called *her Periodical Revolution*; but ſhe goes round from the Sun to the Sun again, or from Change to Change, in 29 days 12 hours 45 minutes, which is *her Synodical Revolution*; and in that time ſhe exhibits all the Phaſes already deſcribed, § 255.

When the above-mentioned Horizon is rectified to the Latitude of any given place, the Times of the Moon's riſing and ſetting, together with her Amplitude, are ſhewn to that place as well as the Sun's; and all the various Phenomena of the Harveſt-Moon, § 273, *& ſeq.* are made obvious to ſight.

The Nodes. The Moon's orbit (No. 9.) is inclined to the Ecliptic, (No. 11.) one half being above, and the other below it. The Nodes, or Points at o and o, lie in the Plane of the Ecliptic, as deſcribed § 317, 318, and ſhift backward through all it's Sines and Degrees in $18\frac{2}{3}$ years. The Degrees of the Moon's

Latitude, to the higheſt at *N L* (North Latitude) and loweſt at *S L* (South Latitude) are engraven both ways from her Nodes at o and o; and, as the Moon riſes and falls in her Orbit according to it's inclination, her Latitude and Diſtance from her Nodes are ſhewn for every day; having firſt rectified her Orbit ſo as to ſet the Nodes to their proper places in the Ecliptic: and then, as they come about at different, and almoſt oppoſite times of the year, § 319, and point twice towards the Sun, all the Eclipſes may be ſhewn for hundreds of years (without any new rectification) by turning the Machinery backward for time paſt, or forward for time to come. At 17 Degrees diſtance from each Node, on both ſides, is engraved a ſmall Sun; and at 12 Degrees diſtance, a ſmall Moon; which ſhew the limits of ſolar and lunar Eclipſes, § 317: and when, at any change, the Moon falls between either of theſe Suns and the Node, the Sun will be eclipſed on the day pointed to by the Annual-Index (No. 10.) and as the Moon has then North or South Latitude, one may eaſily judge whether that Eclipſe will be viſible in the Northern or Southern Hemiſphere; eſpecially as the Earth's Axis inclines toward the Sun or from him at that time. And when, at any Full, the Moon falls between either of the little Moons and Node, ſhe will be eclipſed, and the Annual-Index ſhews the day of that Eclipſe. There is a Circle of $29\frac{1}{2}$ equal parts (No. 8.) on the cover of the Machine, on which an Index ſhews the days of the Moon's age.

A ſemi-ellipſis and ſemi-circle are fixed to an elliptical ring, which being put like a cap upon the Earth, and the forked part *F* upon the Moon, ſhews the Tides as the Earth turns round within them, and they are led round it by the Moon. When the different places come to the ſemi-ellipſis *A a E b B*, they have Tides of Flood; and when they come to the ſemicircle *C E D*, they have Tides of Ebb, PLATE IX. Fig. X.

§ 304,

§ 304, 305; the Index on the Hour-Circle (No. 7.) ſhewing the times of theſe *Phenomena.*

There is a jointed Wire, of which one end being put into a hole in the upright ſtem that holds the Earth's cap, and the Wire laid into a ſmall forked piece which may be occaſionally put upon Venus or Mercury, ſhews the direct and retrograde Motions of theſe two Planets, with their ſtationary Times and Places as ſeen from the Earth.

The whole Machinery is turned by a winch or handle (No. 12.) and is ſo eaſily moved, that a clock might turn it without any danger of ſtopping.

To give a Plate of the wheel-work of this Machine, would anſwer no purpoſe, becauſe many of the wheels lie ſo behind others as to hide them from ſight in any view whatſoever.

Another ORRERY. Pl. VI. Fig. I.

398. *Another* ORRERY. In this Machine, which is the ſimpleſt I ever ſaw, for ſhewing the diurnal and annual motions of the Earth, together with the motion of the Moon and her Nodes, *A* and *B* are two oblong ſquare Plates held together by four upright pillars; of which three appear at *f*, *g*, and *g* 2. Under the Plate *A* is an endleſs ſcrew on the Axis of the handle *h*, which works in a wheel fixed on the ſame Axis with the double-grooved wheel *E*; and on the top of this Axis is fixed the toothed wheel *i*, which turns the pinion *k*, on the top of whoſe Axis is the pinion *k* 2 which turns another pinion *b* 2, and that other turns a third, on the Axis *a* 2 of which is the Earth *U* turning round; this laſt Axis inclining 23½ Degrees. The ſupporter *X* 2, in which the Axis of the Earth turns, is fixed to the moveable Plate *C*.

In the fixed Plate *B*, beyond *H*, is fixed the ſtrong wire *d*, on which hangs the Sun *T*, ſo as it may turn round the wire. To this Sun is fixed the wire or ſolar ray *Z*, which (as the Earth *U* turns round it's Axis) points to all the places that the Sun paſſes vertically over, every day of the year.

The Earth is half covered with a black cap *a*, as in the former Orrery, for dividing the day from the night; and, as the different places come out from below the edge of the cap, or go in below it, they ſhew the times of Sun-riſing and ſetting every day of the year. This cap is fixed on the wire *b*, which has a forked piece *C* turning round the wire *d*: and, as the Earth goes round the Sun, it carries the Cap, Wire, and ſolar Ray round him; ſo that the ſolar Ray conſtantly points towards the Earth's Center.

On the Axis of the pinion *k* is the pinion *m*, which turns a wheel on the cock or ſupporter *n*, and on the Axis of this wheel neareſt *n* is a pinion (hid from view) under the Plate *C*, which pinion turns a wheel that carries the Moon *V* round the Earth *U*; the Moon's Axis riſing and falling in the ſocket *W*, which is fixed to the triangular piece above *Z*; and this piece is fixed to the top of the Axis of the laſt-mentioned wheel. The ſocket *W* is ſlit on the outermoſt ſide; and in this ſlit the two pins near *Y*, fixed in the Moon's Axis, move up and down; one of them being above the inclined Plane *Y X*, and the other below it. By this mechaniſm, the Moon *V* moves round the Earth *T* in the inclined Orbit *q*, parallel to the Plane of the Ring *Y X*; of which the Deſcending Node is at *X*, and the Aſcending Node oppoſite to it, but hid by the ſupporter *X* 2.

The ſmall wheel *E* turns the large wheels *D* and *F*, of equal diameters, by cat-gut ſtrings croſſing between them: and the Axes of theſe two wheels are cranked at *G* and *H*, above the Plate *B*. The upright ſtems of theſe cranks going through the Plate *C*, carry it over and over the fixed Plate *B*, with a motion which carries the Earth *U* round the Sun *T*, keeping the Earth's Axis always parallel to itſelf; or ſtill inclining towards the left hand of the Plate; and ſhewing the viciſſitudes of ſeaſons, as deſcribed in the tenth chapter. As the Earth goes round the Sun, the pinion *k* goes round the wheel *i*; for the Axis of *k* never touches the fixed Plate *B*, but turns on a wire fixed into the Plate *C*.

On the top of the crank *G* is an Index *L*, which goes round the Circle *m* 2 in the time that the Earth goes round the Sun, and points to the days of the months; which, together with the names of the ſeaſons, are marked in this Circle.

This Index has a ſmall grooved wheel *L* fixed upon it, round which, and the Plate *Z*, goes a catgut ſtring croſſing between them; and by this means the Moon's inclined Plane *Y X* with it's Nodes is turned backward, for ſhewing the times and returns of Eclipſes, § 319, 320.

The following parts of this machine muſt be conſidered as diſtinct from thoſe already deſcribed.

Towards the right hand, let *S* be the Earth hung on the wire *e*, which is fixed into the Plate *B*; and let *O* be the Moon fixed on the Axis *M*, and turning round within the cap *P*, in which, and in the Plate *C*, the crooked wire *Q* is fixed. On the Axis *M* is alſo fixed the Index *K*, which goes round a Circle *h* 2, divided into 29½ equal parts, which are the days of the Moon's age: but to avoid confuſion in the ſcheme, it is only marked with the numeral figures 1 2 3 4, for the Quarters. As the crank *H* carries this Moon round the Earth *S* in the Orbit *t*, ſhe ſhews all her Phaſes by means of the cap *P* for the different days of her age, which are ſhewn by the Index *K*; this Index, turning juſt as the Moon *O* does, demonſtrates her turning round her Axis, as ſhe ſtill keeps the ſame ſide towards the Earth *S*, § 262.

At the other end of the Plate *C*, a Moon *N* goes round an Earth *R* in the Orbit *p*. But this Moon's Axis is ſtuck faſt into the Plate *C* at *S* 2, ſo that neither Moon nor Axis can turn round; and as this Moon goes round her Earth, ſhe ſhews herſelf all round to it; which proves, that if the Moon was ſeen all round from the Earth in a Lunation; ſhe could not turn round her Axis.

N. B. If there were only the two wheels *D* and *F*, with a cat-gut ſtring over them, but not croſſing between them, the Axis of the Earth *U* would keep it's Paralleliſm round the Sun *T*, and ſhew all the ſeaſons; as I ſometimes make theſe Machines: and the Moon *O* would go round the Earth *S*, ſhewing her Phaſes as above; as likewiſe would the Moon *N* round the Earth *R*; but then, neither could the diurnal motion of the Earth *U* on it's Axis be ſhewn, nor the motion of the Moon *V* round the Earth.

399. In the year 1746 I contrived a very ſimple Machine, and deſcribed it's performance in a ſmall Treatiſe upon the Phenomena of the Harveſt-Moon, publiſhed in the year 1747. I improved it ſoon after, by adding another wheel, and called it *The Calculator*. It may be eaſily made by any Gentleman who has a mechanical Genius. The CALCULATOR.

PLATE VIII. Fig. I.

The great flat Ring ſupported by twelve pillars, and on which the twelve Signs with their reſpective Degrees are laid down, is the Ecliptic; nearly in the center of it is the Sun *S* ſupported by the ſtrong crooked Wire *I*; and from the Sun proceeds a Wire *W*, called *the Solar Ray*, pointing towards the center of the Earth *E*, which is furniſhed with a moveable Horizon *H*, together with a braſen Meridian, and Quadrant of Altitude. *R* is a ſmall Ecliptic, whoſe Plane co-incides with that of the great one, and has the like Signs and Degrees marked upon it; and is ſupported by two Wires *D* and *D*, which are put into the Plate *PP*, but may be taken off at pleaſure. As the Earth goes round the Sun, the Signs of this ſmall Circle keep parallel to themſelves, and to thoſe of the great Ecliptic. When it is taken off, and the ſolar Ray *W* drawn farther out, ſo as almoſt to touch the Horizon *H*, or the Quadrant of Altitude, the Horizon being rectified to any given Latitude, and the Earth turned round it's Axis by hand, the point of the Wire *W* ſhews the Sun's Declination in paſſing over the graduated braſs Meridian, and his height at any given time upon the Quadrant of Altitude, together with his Azimuth, or Point of bearing upon the Horizon at that time; and likewiſe his Amplitude, and time of riſing and ſetting by the Hour-Index, for any day of the year that the Annual-Index *U* points to in the Circle of Months below the Sun. *M* is a Solar-Index or Pointer ſupported by the wire *L* which is fixed into the knob *K*: the uſe of this Index is to ſhew the Sun's place in the Ecliptic every day in the year; for it goes over the Signs and Degrees as the Index *U* goes over the Months and Days; or rather, as they paſs under the Index *U*, in moving the cover plate with the Earth and it's Furniture round the Sun; for the Index *U* is fixed tight on the immoveable Axis in the Center of the Machine. *K* is a knob or handle for moving the Earth round the Sun, and the Moon round the Earth.

As the Earth is carried round the Sun, it's Axis conſtantly keeps the ſame oblique direction, or parallel to itſelf, § 48, 202, ſhewing thereby the different lengths of days and nights at different times of the year, with all the various ſeaſons. And, in one annual revolution of the Earth, the Moon *M* goes 12$\frac{1}{3}$ times round it from Change to Change, having an occaſional proviſion for ſhewing her different Phaſes. The lower end of the Moon's Axis bears by a ſmall friction wheel upon the inclined Plane *T*, which cauſes the Moon to riſe above and ſink below the Ecliptic *R* in every Lunation; croſſing it in her Nodes, which ſhift backward through all the Signs and Degrees of the ſaid Ecliptic, by the retrograde Motion of the inclined Plane *T*, in 18 years and 225 days. On this Plane the Degrees and Parts of the Moon's North and South Latitude are laid down from both the Nodes, one of which, viz. the Deſcending Node, appears at o, by *D N* above *B*; the other Node being hid from Sight on this Plane by the plate *P P*; and from both Nodes, at proper diſtances, as in the other Orrery, the limits of Eclipſes are marked, and all the ſolar and lunar Eclipſes are ſhewn in the ſame manner, for any given year, within the limits of 6000, either before or after the Chriſtian Æra. On the plate that covers the wheel-work, under the Sun *S*, and round the knob *K*, are Aſtronomical Tables, by which the Machine may be rectified to the beginning of any given year within theſe limits, in three or four minutes of time; and when once ſet right, may be turned backward for 300 years paſt, or forward for as many to come, without requiring any new rectification. There is a method for it's adding up the 29th of *February* every fourth year, and allowing only 28 days to that month for every other three: but all this being performed by a particular manner of cutting the teeth of the Wheels, and dividing the the Month-Circle, too long and intricate to be deſcribed here, I ſhall only ſhew how theſe motions may be performed near enough for common uſe, by wheels with grooves and cat-gut ſtrings round them; only here I muſt put the Operator in mind, that the grooves are to be made ſharp (not round) bottomed, to keep the ſtrings from ſlipping.

The Moon's Axis moves up and down in the ſocket *N* fixed into the bar *O* (which carries her round the Earth) as ſhe riſes above or ſinks below the Ecliptic; and immediately below the inclined Plane *T* is a flat circular plate (between *Y* and *T*) on which the different Excentricities of the Moon's Orbit are laid down; and likewiſe her mean Anomaly and elliptic Equation, by which her true Place may be very nearly found at any time. Below this Apogee plate, which ſhews the Anomaly, &c. is a Circle *Y* divided into 29½ equal parts, which are the days of the Moon's age: and the forked end *A* of the Index *AB* (Fig. II.) may be put into the apogee part of this plate; there being juſt ſuch another Index to put into the inclined Plane *T* at the Aſcending Node; and then the curved points *B* of theſe Indexes ſhew the direct Motion of the Apogee, and retrogade Motion of the Nodes through the Ecliptic *R*, with their Places in it at any given time. As the Moon *M* goes round the Earth *E*, ſhe ſhews her Place every day in the Ecliptic *R*, and the lower end of her Axis ſhews her Latitude and Diſtance from her Node on the inclined Plane *T*, alſo her Diſtance from her Apogee and Perigee, together with her mean Anomaly, the then Excentricity of her Orbit, and her elliptic Equation, all on the Apogee plate, and the Day of her Age in the Circle *Y* of $29\frac{1}{2}$ equal parts; for every day of the year pointed out by the Annual-Index *U* in the Circle of months.

Having rectified the Machine by the Tables for the beginning of any year, move the Earth and Moon forward by the knob *K*, until the Annual-Index comes to any given day of the month; then ſtop, and not only all the above Phenomena may be ſhewn for that day, but alſo, by turning the Earth round it's Axis, the Declination, Azimuth, Amplitude, Altitude of the Moon at any hour, and the Times of her riſing and ſetting, are ſhewn by the Horizon, Quadrant of Altitude, and Hour-Index. And in moving the Earth round the Sun, the days of all the New and Full Moons and Eclipſes in any given year are ſhewn. The Phenomena of the Harveſt-Moon, and thoſe of the Tides, by ſuch a cap as that in Plate IX. Fig. 10. put upon the Earth and Moon, together with the ſolution of many problems not here related, are made conſpicuous.

The eaſieſt, though not the beſt way, that I can inſtruſt any mechanical perſon to make the wheel-work of ſuch a machine, is as follows; which is the way that I made it, before I thought of numbers exact enough to make it worth the trouble of cutting teeth in the wheels.

PLATE VIII. Fig. III.

Fig. 3d of Plate VIII. is a ſection of this Machine; in which *ABCD* is a frame of wood held together by four pillars at the corners, whereof two appear at *AC* and *BD*. In the lower Plate *CD* of this frame are three ſmall friction-wheels, at equal diſtances from each other; two of them appearing at *e* and *e*. As the frame is moved round, theſe wheels run upon the fixed bottom Plate *EE*, which ſupports the whole work.

In the center of this laſt-mentioned Plate is fixed the upright Axis *GFFf*, and on the ſame Axis is fixed the Wheel *HHH*, in which are four Grooves, *I*, *X*, *k*, *L* of different diameters. In theſe Grooves are cat-gut ſtrings going alſo round the ſeparate Wheels *M*, *N*, *O* and *P*.

The Wheel *M* is fixed on a ſolid Spindle or Axis, the lower pivot of which turns at *R* in the under Plate of the moveable frame *ABCD*; and on the upper end of this Axis is fixed the Plate *o o* (which is *P P*, under the Earth, in Fig. 1.) and to this Plate is fixed, at an Angle of 23½ Degrees inclination, the Dial-plate below the Earth *T*; on the Axis of which, the Index *q* is turned round by the Earth. This Axis, together with the Wheel *M*, and Plate *o o*, keep their Paralleliſm in going round the Sun *S*.

On the Axis of the Wheel *M* is a moveable ſocket, on which the ſmall Wheel *N* is fixed, and on the upper end of this ſocket is put on tight (but ſo as it may be occaſionally turned by hand) the bar *Z Z* (viz. the bar *O* in Fig. 1.) which carries the Moon *m* round the Earth *T*, by the ſocket *n*, fixed into the bar. As the Moon goes round the Earth, her Axis riſes and falls in the ſocket *n*; becauſe, on the lower end of her Axis, which is turned inward, there is a ſmall friction Wheel *s* running on the inclined Plane *X* (which is *T* in Fig. 1.) and ſo cauſes the Moon alternately to riſe above and ſink below the little Ecliptic *V V* (*R* in Fig. 1.) in every Lunation.

On the ſocket or hollow axis of the Wheel *N*, there is another ſocket, on which the Wheel *O* is fixed; and the Moon's inclined Plane *X* is put tightly on the upper end of this ſocket, not on a ſquare, but on a round, that it may be occaſionally ſet by hand without wrenching the Wheel or Axle.

Laſtly, on the hollow Axis of the Wheel *O* is another ſocket, on which is fixed the Wheel *P*, and on the upper end of this ſocket is put on tightly the Apogee plate *Y* (*that* immediately below *T* in Fig. 1.) All theſe Axles turn in the upper Plate of the moveable frame at *Q*; which Plate is covered with the thin Plate *c c* (ſcrewed to it) whereon are the fore-mentioned Tables and Month-Circle in Fig. 1.

The middle part of the thick fixed Wheel *H H H* is much broader than the reſt of it, and comes out between the Wheels *M* and *O* almoſt to the Wheel *N*. To adjuſt the diameters of the Grooves of this fixed Wheel to the Grooves of the ſeparate Wheels *M*, *N*, *O* and *P*, ſo as they may perform their motions in the proper times, the following method muſt be obſerved.

The Groove of the Wheel *M*, which keeps the Parallelism of the Earth's Axis, muſt be preciſely of the ſame Diameter as the lower Groove *I* of the fixed Wheel *H H H*; but, when this Groove is ſo well adjuſted as to ſhew, that in ever ſo many annual revolutions of the Earth, it's Axis keeps it's Parallelism, as may be obſerved by the ſolar Ray *W* (Fig. 1.) always coming preciſely to the ſame Degree of the ſmall Ecliptic *R* at the end of every annual revolution, when the Index *M* points to the like Degree in the great Ecliptic; then, with the edge of a thin File, give the Groove of the Wheel *M* a ſmall rub all round, and, by that means leſſening the Diameter of the Groove perhaps about the 20th part of a hair's breadth, it will cauſe the Earth to ſhew the Preceſſion of the Equinoxes; which, in many annual revolutions, will begin to be ſenſible, as the Earth's Axis deviates ſlowly from it's Paralleliſm, § 246, towards the antecedent Signs of the Ecliptic.

The Diameter of the Groove of the Wheel *N*, which carries the Moon round the Earth, muſt be to the Diameter of the Groove *X*, as a Lunation is to a year; that is, as $29\frac{1}{2}$ to $365\frac{1}{4}$.

The Diameter of the Groove of the Wheel *O*, which turns the inclined Plane *X* with the Moon's Nodes backward, muſt be to the Diameter of the Groove *k*, as 20 to $18\frac{225}{365}$. And,

Laſtly, the Diameter of the Groove of the Wheel *P*, which carries the Moon's Apogee forward, muſt be to the Diameter of the Groove *L*, as 70 to 62.

But, after all this nice adjuſtment of the Grooves to the proportional times of their reſpective Wheels turning round, and which ſeems to promiſe very well in Theory, there will ſtill be found a neceſſity of a farther adjuſtment by hand; becauſe proper allowance muſt be made for the Diameters of the cat-gut ſtrings: and the Grooves muſt be ſo adjuſted by hand, as, that in the time the Earth is moved once round the Sun, the Moon muſt perform 12 ſynodical revolutions round the Earth, and be almoſt 11 days old in her 13th revolution. The inclined Plane with it's Nodes muſt go once round backward through all the Signs and Degrees of the ſmall Ecliptic in 18 annual revolutions of the Earth, and 225 days over. And the Apogee plate muſt go once round forward, ſo as it's Index may go over all the Signs and Degrees of the ſmall Ecliptic in eight years (or ſo many annual revolutions of the Earth) and 312 days over.

N. B. The ſtring which goes round the Grooves *X* and *N* for the Moon's Motion muſt croſs between theſe wheels; but all the reſt of the ſtrings go in their reſpective Grooves, *I M*, *k O*, and *L P*, without croſſing.

The COMETARIUM. 400. The COMETARIUM. This curious Machine ſhews the Motion of a Comet or excentric Body moving round the Sun, deſcribing equal areas in equal times, § 152, and may be ſo contrived as to ſhew ſuch a Motion for any Degree of Excentricity. It was invented by the late Dr. DESAGULIERS.

PLATE IV. Fig. IV. The dark elliptical Groove round the letters *a b c d e f g h i k l m* is the Orbit of the Comet *Y*: this Comet is carried round in the Groove, according to the order of letters, by the Wire *W* fixed in the Sun *S*, and ſlides on the Wire as it approaches nearer to or recedes farther from the Sun, being neareſt of all in the Perihelion *a*, and fartheſt in the Aphelion *g*. The areas *a S b*, *b S c*, *c S d*, &c. or contents of theſe ſeveral Triangles, are all equal; and in every turn of the Winch *N* the Comet *Y* is carried over one of theſe areas; conſequently in as much time as it moves from *f* to *g*, or from *g* to *h*, it moves from *m* to *a*, or from *a* to *b*; and ſo of the reſt, being quickeſt of all at *a*, and ſloweſt at *g*. Thus, the Comet's velocity in it's Orbit continually decreaſes from the Perihelion *a* to the Aphelion *g*; and increaſes in the ſame proportion from *g* to *a*.

The elliptic Orbit is divided into 12 equal Parts or Signs, with their reſpective Degrees, and ſo is the Circle *n o p q r s t n*, which repreſents a great Circle in the Heavens, and to which the Comet's motion is referred by a ſmall knob on the point of the wire *W*. Whilſt the Comet moves from *f* to *g* in it's Orbit, it appears to move only about five degrees in this Circle, as is ſhewn by the ſmall knob on the end of the Wire *W*; but in the like time, as the Comet moves from *m* to *a*, or from *a* to *b*, it appears to deſcribe the large ſpace *t n* or *n o* in the Heavens, either of which ſpaces contains 120 Degrees, or four Signs. Were the Excentricity of it's Orbit greater, the greater ſtill would be the difference of it's Motion, and *vice verſâ.*

A B C D E F G H I K L M A is a circular Orbit for ſhewing the equable Motion of a Body round the Sun *S*, deſcribing equal Areas *A S B*, *B S C*, &c. in equal times with thoſe of the Body *Y* in it's elliptical Orbit above-mentioned; but with this difference, that the circular Motion deſcribes the equal Arcs *A B*, *B C*, &c. in the ſame equal times that the elliptical Motion deſcribes the unequal Arcs *a b*, *b c*, &c.

Now, ſuppoſe the two Bodies *Y* and 1 to ſtart from the Points *a* and *A* at the ſame moment of time, and each having gone round it's reſpective Orbit, to arrive at theſe Points again at the ſame inſtant, the Body *Y* will be forwarder in it's Orbit than the Body 1 all the way from *a* to *g*, and from *A* to *G*; but 1 will be forwarder than *Y* through all the other half of the Orbit; and the difference is equal to the Equation of the Body *Y* in it's Orbit. At the Points *a*, *A*, and *g*, *G*, that is, in the Perihelion and Aphelion, they will be equal; and then the Equation vaniſhes. This ſhews why the Equation of a Body moving in an elliptic Orbit, is added to the mean or ſuppoſed circular Motion from the Perihelion to the Aphelion, and ſubtracted from the Aphelion to the Perihelion, in Bodies moving round the Sun, or from the Perigee to the Apogee, and from the Apogee to the Perigee in the Moon's Motion round the Earth, according to the Precepts in the 353d Article; only we are to conſider, that when Motion is turned into Time, it reverſes the titles in the Table of *The Moon's elliptic Equation.*

This Motion is performed in the following manner by the machine. *A B C* is a wooden bar (in the box containing the wheel-work) above which are the Wheels *D* and *E*; and below it the elliptic Plates *F F* and *G G*; each Plate being fixed on an Axis in one of it's Focuſes, at *E* and *K*; and the Wheel *E* is fixed on the ſame Axis with the Plate

PLATE IV. Fig. V.

F F. Theſe Plates have Grooves round their edges preciſely of equal diameters to one another, and in theſe Grooves is the cat-gut ſtring *gg*, *gg* croſſing between the Plates at *h*. On *H*, (the Axis of the handle or winch *N* in Fig. 4th,) is an endleſs ſcrew in Fig. 5, working in the Wheels *D* and *E*, whoſe numbers of teeth being equal, and ſhould be equal to the number of lines *a S*, *b S*, *c S*, &c. in Fig. 4, they turn round their Axes in equal times to one another, and to the Motion of the elliptic Plates. For, the Wheels *D* and *E* having equal numbers of teeth, the Plate *F F* being fixed on the ſame Axis with the Wheel *E*, and the Plate *F F* turning the equally big Plate *G G* by a cat-gut ſtring round them both, they muſt all go round their Axes in as many turns of the handle *N* as either of the Wheels has teeth.

It is eaſy to ſee, that the end *h* of the elliptical Plate *F F* being farther from it's Axis *E* than the oppoſite end *i* is, muſt deſcribe a Circle ſo much the larger in proportion; and muſt therefore move through ſo much more ſpace in the ſame time; and for that reaſon the end *h* moves ſo much faſter than the end *i*, although it goes no ſooner round the Center *E*. But then, the quick-moving end *h* of the Plate *F F* leads about the ſhort end *h K* of the Plate *G G* with the ſame velocity; and the ſlow moving end *i* of the Plate *F F* coming half round as to *B*, muſt then lead the long end *k* of the Plate *G G* as ſlowly about: So that the elliptical Plate *F F* and it's Axis *E* move uniformly and equally quick in every part of it's revolution; but the elliptical Plate *G G*, together with it's Axis *K*, muſt move very unequally in different parts of it's revolution; the difference being always inverſely as the diſtance of any point of the Circumference of *G G* from it's Axis at *K*: or in other words, to inſtance in two points, if the diſtance *K k* be four, five, or ſix times as great as the diſtance *K h*, the Point *h* will move in that poſition four, five, or ſix times as faſt as the Point *k* does; when the Plate *G G* has gone half round: and ſo on for any other Excentricity or Difference of the Diſtances *K k* and *K h*. The tooth *i* on the Plate *F F* falls in between the two teeth at *k* on the Plate *G G*, by which means the revolution of the latter is ſo adjuſted to that of the former, that they can never vary from one another.

On the top of the Axis of the equally-moving Wheel *D*, in Fig. 5th, is the Sun *S* in Fig. 4th; which Sun, by the Wire *Z* fixed to it, carries the Ball 1 round the Circle *ABCD*, &c. with an equable Motion, according to the order of the letters: and on the top of the Axis *K* of the unequally-moving Ellipſes *G G*, in Fig. 5th, is the Sun *S* in Fig. 4th, carrying the Ball *Y* unequally round in the elliptical Groove *a b c d*, &c. *N. B.* This elliptical Groove muſt be preciſely equal and ſimilar to the verge of the Plate *G G*, which is alſo equal to that of *F F*.

In this manner, Machines may be made to ſhew the true Motion of the Moon about the Earth, or of any Planet about the Sun; by making the elliptical Plates of the ſame Excentricities, in proportion to the Radius, as the Orbits of the Planets are, whoſe Motions they repreſent; and ſo, their different Equations in different parts of their Orbits may be made plain to ſight; and clearer Ideas of theſe Motions and Equations acquired in half an hour, than could be gained from reading half a day about ſuch Motions and Equations.

The improved CELESTIAL GLOBE.

401. The IMPROVED CELESTIAL GLOBE. On the North Pole of the Axis, above the Hour-Circle, is fixed an Arch *M K H* of $23\frac{1}{2}$ Degrees; and at the end *H* is fixed an upright pin *H G*, which ſtands directly over the North Pole of the Ecliptic, and perpendicular to that part of the ſurface of the Globe. On this pin are two moveable Collets at *D* and *H*, to which are fixed the quadrantal Wires *N* and

PLATE III. Fig. III.

N and *O*, having two little Balls on their ends for the Sun and Moon, as in the Figure. The Collet *D* is fixed to the circular Plate *F*, whereon the 29½ days of the Moon's age are engraven, beginning juſt under the Sun's Wire *N*; and as this Wire is moved round the Globe, the Plate *F* turns round with it. Theſe Wires are eaſily turned, if the ſcrew *G* be ſlackened; and when they are ſet to their proper places, the ſcrew ſerves to fix them there ſo, as in turning the Ball of the Globe, the Wires with the Sun and Moon go round with it; and theſe two little Balls riſe and ſet at the ſame times, and on the ſame points of the Horizon, for the day to which they are rectified, as the Sun and Moon do in the Heavens.

Becauſe the Moon keeps not her courſe in the Ecliptic (as the Sun appears to do) but has a Declination of 5⅓ Degrees on each ſide from it in every Lunation, § 317, her Ball may be ſcrewed as many Degrees to either ſide of the Ecliptic as her Latitude or Declination from the Ecliptic amounts to at any given time; and for this purpoſe *S* is a ſmall piece of paſteboard, of which the curved edge at *S* is to be ſet upon the Globe at right Angles to the Ecliptic, and the dark line over *S* to ſtand upright upon it. From this line, on the convex edge, are drawn the 5⅓ Degrees of the Moon's Latitude on both ſides of the Ecliptic; and when this piece is ſet upright on the Globe, it's graduated edge reaches to the Moon on the Wire *O*, by which means ſhe is eaſily adjuſted to her Latitude found by an Ephemeris.

The Horizon is ſupported by two ſemicircular Arches, becauſe Pillars would ſtop the progreſs of the Balls when they go below the Horizon in an oblique ſphere.

To rectify it.

To rectify this Globe. Elevate the Pole to the Latitude of the Place; then bring the Sun's place in the Ecliptic for the given day to the braſen Meridian, and ſet the Hour-Index to XII at noon, that is, to the upper XII on the Hour-Circle; keeping the Globe in that ſituation, ſlacken the ſcrew *G*, and ſet the Sun directly over his place on the Meridian; which done, ſet the Moon's Wire under the number that expreſſes her age for that day on the Plate *F*, and ſhe will then ſtand over her place in the Ecliptic, and ſhew what Conſtellation ſhe is in. Laſtly, faſten the ſcrew *G*, and laying the curved edge of the paſteboard *S* over the Ecliptic below the Moon, adjuſt the Moon to her Latitude over the graduated edge of the paſteboard; and the Globe will be rectified.

It's uſe.

Having thus rectified the Globe, turn it round, and obſerve on what points of the Horizon the Sun and Moon Balls riſe and ſet, for theſe agree with the points of the Compaſs on which the Sun and Moon riſe and ſet in the Heavens on the given day; and the Hour-Index ſhews the times of their riſing and ſetting; and likewiſe the time of the Moon's paſſing over the Meridian.

The ſimple Apparatus ſhews all the varieties that can happen in the riſing and ſetting of the Sun and Moon; and makes the forementioned Phenomena of the Harveſt-Moon (Chap. xvi.) plain to the Eye. It is alſo very uſeful in reading Lectures on the Globes, becauſe a large company can ſee this Sun and Moon go round, riſing above and ſetting below the Horizon at different times, according to the ſeaſons of the year; and making their appulſes to different fixed Stars. But in the uſual way, where there is only the places of the Sun and Moon in the Ecliptic to keep the Eye upon, they are eaſily loſt ſight of, unleſs they be covered with Patches.

The PLANETARY GLOBE. Pl. VIII. Fig. IV.

402. The PLANETARY GLOBE. In this Machine, *T* is a terreſtrial Globe fixed on it's Axis ſtanding upright on the Pedeſtal *C D E*, on which is an Hour-Circle, having it's Index fixed on the Axis, which turns ſomewhat tightly in the Pedeſtal,

ſo that the Globe may not be liable to ſhake; to prevent which, the Pedeſtal is about two Inches thick, and the Axis goes quite through it, bearing on a ſhoulder. The Globe is hung in a graduated braſen Meridian, much in the uſual way; and the thin Plate *N*, *N E*, *E* is a moveable Horizon, graduated round the outer edge, for ſhewing the Bearings and Amplitudes of the Sun, Moon, and Planets. The braſen Meridian is grooved round the outer edge; and in this Groove is a ſlender ſemi-circle of braſs, the ends of which are fixed to the Horizon in its North and South Points: this ſemi-circle ſlides in the Groove as the Horizon is moved in rectifying it for different Latitudes. To the middle of the ſemi-circle is fixed a Pin, which always keeps in the Zenith of the Horizon, and on this Pin, the Quadrant of Altitude *q* turns; the lower end of which, in all poſitions, touches the Horizon as it is moved round the ſame. This Quadrant is divided into 90 Degrees from the Horizon to the zenithal Pin on which it is turned, at 90. The great flat Circle or Plate *A B* is the Ecliptic, on the outer edge of which the Signs and Degrees are laid down; and every fifth Degree is drawn through the reſt of the ſurface of this Plate towards it's Center. On this Plate are ſeven Grooves, to which ſeven little Balls are adjuſted by ſliding Wires, ſo that they are eaſily moved in the Grooves, without danger of ſtarting out of them. The Ball next the terreſtrial Globe is the Moon, the next without it is Mercury, the next Venus, the next the Sun, then Mars, then Jupiter, and laſtly Saturn; and in order to know them, they are ſeparately ſtampt with the following Characters; ●, ☿, ♀, ☼, ♂, ♃, ♄. This Plate or Ecliptic is ſupported by four ſtrong Wires, having their lower ends fixed into the Pedeſtal, at *C*, *D*, and *E*, the fourth being hid by the Globe. The Ecliptic is inclined $23\frac{1}{2}$ Degrees to the Pedeſtal, and is therefore properly inclined to the Axis of the Globe which ſtands upright on the Pedeſtal.

To rectify it.

To rectify this Machine. Set the Sun, and all the planetary Balls, to their geocentric places in the Ecliptic for any given time, by an Ephemeris: then ſet the North Point of the Horizon to the Latitude of your place on the braſen Meridian, and the Quadrant of Altitude to the South Point of the Horizon; which done, turn the Globe with its Furniture till the Quadrant of Altitude comes right againſt the Sun, viz. to his place in the Ecliptic; and keeping it there, ſet the Hour-Index to the XII next the letter *C*; and the Machine will be rectified, not only for the following Problems, but for ſeveral others, which the Artiſt may eaſily find out.

PROBLEM I.

To find the Amplitudes, Meridian Altitudes, and times of riſing, culminating, and ſetting, of the Sun, Moon, and Planets.

It's uſe.

Turn the Globe round eaſtward, or according to the order of Signs; and as the eaſtern edge of the Horizon comes right againſt the Sun, Moon, or any Planet, the Hour-Index will ſhew the time of it's riſing; and the inner edge of the Ecliptic will cut it's riſing Amplitude in the Horizon. Turn on, and as the Quadrant of Altitude comes right againſt the Sun, Moon or Planets, the Ecliptic cuts their meridian Altitudes in the Quadrant, and the Hour-Index ſhews the times of their coming to the Meridian. Continue turning, and as the weſtern edge of the Horizon comes right againſt the Sun, Moon, or Planets, their ſetting Amplitudes are cut in the Horizon by the Ecliptic; and the times of their ſetting are ſhewn by the Index on the Hour-Circle.

PROBLEM II.

To find the Altitude and Azimuth of the Sun, Moon, and Planets, at any time of their being above the Horizon.

Turn the Globe till the Index comes to the given time in the Hour-Circle; then keep the Globe ſteady, and moving the Quadrant of Altitude to each Planet reſpectively, the edge of the Ecliptic will cut the Planet's mean Altitude on the Quadrant, and the Quadrant will cut the Planet's Azimuth, or Point of Bearing on the Horizon.

PROBLEM III.

The Sun's Altitude being given at any time either before or after Noon, to find the Hour of the Day, and the Variation of the Compaſs, in any known Latitude.

With one hand hold the edge of the Quadrant right againſt the Sun; and, with the other hand, turn the Globe weſtward, if it be in the forenoon, or eaſtward if it be in the afternoon, until the Sun's place at the inner edge of the Ecliptic cuts the Quadrant in the Sun's obſerved Altitude; and then the Hour-Index will point out the time of the day, and the Quadrant will cut the true Azimuth, or Bearing of the Sun for that time: the difference between which, and the bearing ſhewn by the Azimuth Compaſs, ſhews the Variation of the Compaſs in that place of the Earth.

The TRAJECTORIUM LUNARE.

403. The TRAJECTORIUM LUNARE. This Machine is for delineating the Paths of the Earth and Moon, ſhewing what ſort of Curves they make in the ethereal regions; and was juſt mentioned in the

PLATE VII. Fig. V.

the 266th Article. *S* is the Sun, and *E* the Earth, whoſe Centers are 81 Inches diſtant from each other; every Inch anſwering to a Million of Miles, § 47. *M* is the Moon, whoſe Center is $\frac{24}{100}$ parts of an Inch from the Earth's in this Machine, this being in juſt proportion to the Moon's diſtance from the Earth, § 52. *A A* is a Bar of Wood, to be moved by hand round the Axis *g* which is fixed in the Wheel *Y*. The Circumference of this Wheel is to the Circumference of the ſmall Wheel *L* (below the other end of the Bar) as $365\frac{1}{4}$ days is to $29\frac{1}{2}$; or as a Year is to a Lunation. The Wheels are grooved round their edges, and in the Grooves is the cat-gut ſtring *G G* croſſing between the Wheels at *X*. On the Axis of the Wheel *L* is the Index *F*, in which is fixed the Moon's Axis *M* for carrying her round the Earth *E* (fixed on the Axis of the Wheel *L*) in the time that the Index goes round a Circle of $29\frac{1}{2}$ equal parts, which are the days of the Moon's age. The Wheel *Y* has the Months and Days of the year all round it's Limb; and in the Bar *A A* is fixed the Index *I*, which points out the Days of the Months anſwering to the Days of the Moon's age, ſhewn by the Index *F*, in the Circle of $29\frac{1}{2}$ equal parts at the other end of the Bar. On the Axis of the Wheel *L* is put the piece *D*, below the Cock *C*, in which this Axis turns round; and in *D* are put the Pencils *e* and *m*, directly under the Earth *E* and Moon *M*; ſo that *m* is carried round *e*, as *M* is round *E*.

It's uſe.

Lay the Machine on an even Floor, preſſing gently on the Wheel *Y*, to cauſe it's ſpiked Feet (of which two appear at *P* and *P*, the third being ſuppoſed to be hid from ſight by the Wheel) enter a little into the Floor to ſecure the Wheel from turning. Then lay a paper about four feet long under the Pencils *e* and *m*, croſs-wiſe to the Bar: which done, move the Bar ſlowly round the Axis *g* of the Wheel *Y*; and, as the Earth *E* goes round the Sun *S*, the Moon *M* will go round the Earth with a duly proportioned velocity; and the friction Wheel *W* running on the Floor, will keep the Bar from bearing too heavily on the Pencils *e* and *m*, which will delineate the Paths of the Earth and Moon, as in Fig. 2d, already deſcribed at large, § 266, 267. As the Index *I* points out the Days of the Months, the Index *F* ſhews the Moon's age on theſe Days, in the Circle of $29\frac{1}{2}$ equal parts. And as this laſt Index points to the different Days in it's Circle, the like numeral Figures may be ſet to thoſe parts of the Curves of the Earth's Path and Moon's, where the Pencils *e* and *m* are at thoſe times reſpectively, to ſhew the places of the Earth and Moon. If the Pencil *e* be puſhed a very little off, as if from the Pencil *m*, to about $\frac{1}{40}$ part of their diſtance, and the Pencil *m* puſhed as much towards *e*, to bring them to the ſame diſtances again, though not to the ſame points of ſpace; then, as *m* goes round *e*, *e* will go as it were round the Center of Gravity between the Earth *e* and Moon *m*, § 298: but this Motion will not ſenſibly alter the Figure of the Earth's Path or the Moon's.

If a Pin, as *p*, be put through the Pencil *m*, with it's head towards that of the Pin *q* in the Pencil *e*, it's head will always keep thereto as *m* goes round *e*, or as the ſame ſide of the Moon is ſtill obverted to the Earth. But the Pin *p*, which may be conſidered as an equatorial Diameter of the Moon, will turn quite round the Point *m*, making all poſſible Angles with the Line of it's Progreſs, or Line of the Moon's Path. This is an ocular proof of the Moon's turning round her Axis.

The TIDE-DIAL.

PLATE IX. Fig. V, II.

404. The TIDE-DIAL. The outſide parts of this Machine conſiſt of, 1. An eight-ſided Box, on the top of which at the corners is ſhewn the Phaſes of the Moon at the Octants, Quarters, and Full. Within theſe is a Circle of $29\frac{1}{2}$ equal parts, which are the days of the Moon's age accounted from the Sun at New Moon, round to the Sun again. Within

this Circle is one of 24 hours divided into their reſpective Halves and Quarters. 2. A moving elliptical Plate, painted blue, to repreſent the riſing of the Tides under and oppoſite to the Moon; and has the words, *High Water*, *Tide falling*, *Low Water*, *Tide riſing*, marked upon it. To one end of this Plate is fixed the Moon *M* by the Wire *W*, and goes along with it. 3. Above this elliptical Plate is a round one, with the Points of the Compaſs upon it, and alſo the names of above 200 places in the large Machine (but only 32 in the Figure, to avoid confuſion) ſet over thoſe Points on which the Moon bears when ſhe raiſes the Tides to the greateſt heights at theſe Places twice in every lunar day: and to the North and South Points of this Plate are fixed two Indexes *I* and *K*, which ſhew the times of High Water, in the Hour-Circle, at all theſe places. 4. Below the elliptical Plate are four ſmall Plates, two of which project out from below it's ends at New and Full Moon; and ſo, by lengthening the Ellipſe, ſhew the Spring Tides, which are then raiſed to the greateſt heights by the united attractions of the Sun and Moon, § 302. The other two of theſe ſmall Plates appear at low water when the Moon is in her Quadratures, or at the ſides of the elliptic Plate, to ſhew the Neap Tides; the Sun and Moon then acting croſs-wiſe to each other. When any two of theſe ſmall Plates appear, the other two are hid; and when the Moon is in her Octants, they all diſappear, there being neither Spring nor Neap Tides at thoſe times. Within the Box are a few Wheels for performing theſe Motions by the Handle or Winch *H*.

It's uſe.

Turn the Handle until the Moon *M* comes to any given day of her age in the Circle of $29\frac{1}{2}$ equal parts, and the Moon's Wire *W* will cut the time of her coming to the Meridian on that day, in the Hour-Circle; the XII under the Sun being Mid-day, and the oppoſite XII mid-night: then looking for the name of any given place on the round Plate (which makes 29½ rotations whilſt the Moon *M* makes only one revolution from the Sun to the Sun again) turn the Handle till *that* place comes to the word *High Water* under the Moon, and the Index which falls among the Forenoon Hours will ſhew the time of High Water at that place in the Forenoon of the given day: then turn the Plate half round, till the ſame place comes to the oppoſite High-Water Mark, and the Index will ſhew the time of High Water in the Afternoon at that place. And thus, as all the different places come ſucceſſively under and oppoſite to the Moon, the Indexes ſhew the times of High Water at them in both parts of the day: and when the ſame places come to the Low-Water Marks, the Indexes ſhew the times of Low Water. For about three days before and after the times of New and Full Moon, the two ſmall Plates come out a little way from below the High-Water Marks on the elliptical Plate, to ſhew that the Tides riſe ſtill higher about theſe times: and about the Quarters, the other two Plates come out a little from under the Low-Water Marks towards the Sun and on the oppoſite ſide, ſhewing that the Tides of Flood riſe not then ſo high, nor do the Tides of Ebb fall ſo low, as at other times.

By pulling the Handle a little way outward, it is diſengaged from the Wheel-work, and then the upper Plate may be turned round quickly by hand ſo, as the Moon may be brought to any given day of her age in about a quarter of a minute: and by puſhing in the Handle, it takes hold of the Wheel-work again.

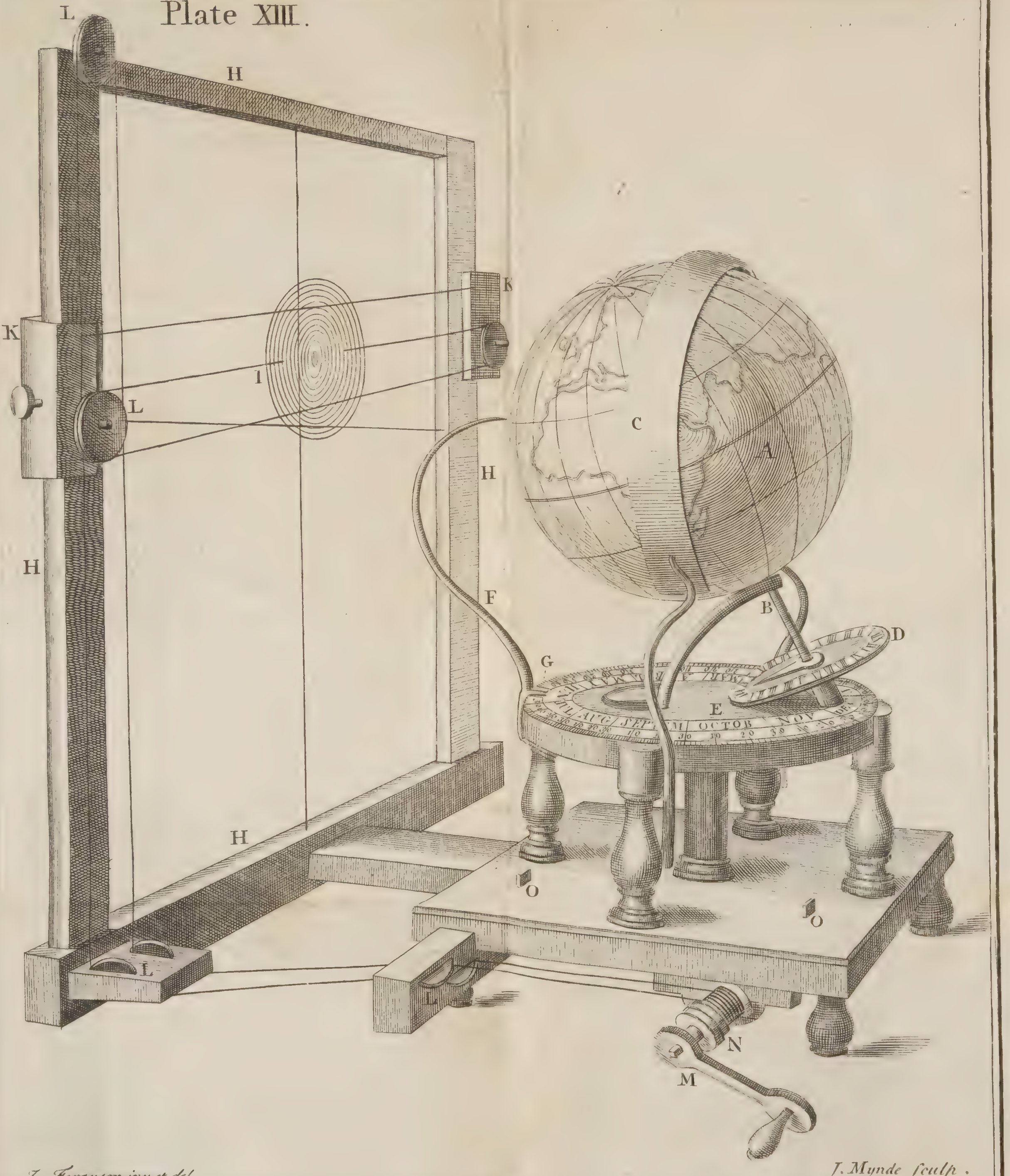
The inſide work deſcribed.

On *AB*, the Axis of the Handle *H*, is an endleſs Screw *C*, which turns the Wheel *FED* of 24 teeth round in 24 revolutions of the Handle: this Wheel turns another *ONG* of 48 teeth, and on it's Axis is the Pinion *PQ* of four leaves, which turns the Wheel *LKI* of 59 teeth round in 29½ turnings or rotations of the Wheel *FED*, or in 708 revolu-

PLATE XI. Fig. VIII.

tions

Plate XIII.



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tions of the Handle, which is the number of Hours in a ſynodical revolution of the Moon. The round Plate with the names of Places upon it is fixed on the Axis of the Wheel *FED*; and the Elliptical or Tide-Plate with the Moon fixed to it is upon the Axis of the Wheel *LKI*; conſequently, the former makes 29½ revolutions in the time that the latter makes one. The whole Wheel *FED*, with the endleſs Screw *C*, and dotted part of the Axis of the Handle *AB*, together with the dotted part of the Wheel *ONG*, lie hid below the large Wheel *LKI*.

Fig. IXth repreſents the under ſide of the Elliptical or Tide-Plate *abcd*, with the four ſmall Plates *ABCD*, *EFGH*, *IKLM*, *NOPQ* upon it: each of which has two ſlits, as *TT*, *SS*, *RR*, *UU*, ſliding on two Pins, as *nn* fixed in the elliptical Plate. In the four ſmall Plates are fixed four Pins, at *W*, *X*, *Y*, and *Z*; all of which work in an elliptic Groove *oooo* on the cover of the Box below the elliptical Plate; the longeſt Axis of this Groove being in a right line with the Sun and Full Moon. Conſequently, when the Moon is in Conjunction or Oppoſition, the Pins *W* and *X* thruſt out the Plates *ABCD* and *IKLM* a little beyond the ends of the elliptic Plate at *d* and *b*, to *f* and *e*; whilſt the Pins *Y* and *Z* draw in the Plates *EFGH* and *NOPQ* quite under the elliptic Plate to *g* and *h*. But, when the Moon comes to her firſt or third Quarter, the elliptic Plate lies acroſs the fixed elliptic Groove in which the Pins work; and therefore the end Plates *ABCD* and *IKLM* are drawn in below the great Plate, and the other two Plates *EFGH* and *NOPQ* are thruſt out beyond it to *a* and *c*. When the Moon is in her Octants, the Pins *V*, *X*, *Y*, *Z* are in the parts *o*, *o*, *o*, *o* of the elliptic Groove, which parts are at a mean between the greateſt and leaſt diſtances from the Center *q*, and then all the four ſmall Plates diſappear below the great one.

TheEclipsareon. PL. XIII.

405. The ECLIPSAREON. This Piece of Mechaniſm exhibits the Time, Quantity, Duration, and Progreſs of ſolar Eclipſes, at all Parts of the Earth.

The principal parts of this Machine are, 1. A terreſtrial Globe *A* turned round it's Axis *B* by the the Handle or Winch *M*; the Axis *B* inclines 23½ Degrees, and has an Index which goes round the Hour-Circle *D* in each rotation of the Globe. 2. A circular Plate *E*, on the Limb of which the Months and Days of the year are inſerted. This Plate ſupports the Globe, and gives it's Axis the ſame poſition to the Sun, or to a Candle properly placed, that the Earth's Axis has to the Sun upon any day of the year, § 338, by turning the Plate till the given Day of the Month comes to the fixed Pointer, or Annual-Index *G*. 3. A crooked Wire *F*, which points toward the middle of the Earth's enlightened Diſc at all times, and ſhews to what place of the Earth the Sun is vertical at any given time. 4. A Penumbra, or thin circular Plate of braſs *I* divided into 12 Digits by 12 concentric Circles, which repreſent a Section of the Moon's Penumbra, and is proportioned to the ſize of the Globe; ſo that the ſhadow of this Plate, formed by the Sun, or a Candle placed at a convenient diſtance, with it's Rays tranſmitted through a convex Lens to make them fall parallel on the Globe, covers exactly all thoſe places upon it that the Moon's Shadow and Penumbra do on the Earth: ſo that the Phenomena of any ſolar Eclipſe may be ſhewn by this Machine with Candle-light almoſt as well as by the light of the Sun. 5. An upright frame *H H H H*, on the ſides of which are Scales of the Moon's Latitude or Declination from the Ecliptic. To theſe Scales are fitted two Sliders *K* and *K*, with Indexes for adjuſting the Penumbra's Center to the Moon's Latitude, as it is North or South Aſcending or Deſcending. 6. A ſolar Horizon *C*, dividing the enlightened Hemiſphere of the Globe from that which is in the dark at any given time, and ſhewing at what places the general Eclipſe begins and ends with the riſing or ſetting Sun. 7. A Handle *M*, which turns the Globe round it's Axis by wheel-work, and at the ſame time moves the Penumbra acroſs the frame by threads over the Pulleys *L*, *L*, *L*, with a velocity duly proportioned to that of the Moon's ſhadow over the Earth, as the Earth turns on it's Axis. And as the Moon's Motion is quicker or ſlower, according to her different diſtances from the Earth, the penumbral Motion is eaſily regulated in the Machine by changing one of the Pulleys.

To rectify it.

To rectify the Machine for uſe. The true time of New Moon and her Latitude being known by the foregoing Precepts, § 353, *et ſeq.* if her Latitude exceeds the number of minutes or diviſions on the Scales (which are on the ſide of the frame hid from view in the Figure of the Machine) there can be no Eclipſe of the Sun at that Conjunction; but if it does not, the Sun will be eclipſed to ſome places of the Earth; and, to ſhew the times and various appearances of the Eclipſe at thoſe places, proceed in order as follows.

To rectify the Machine for performing by the Light of the Sun. 1. Move the Sliders *K K* till their Indexes point to the Moon's Latitude on the Scales, as it is North or South Aſcending or Deſcending, at that time. 2. Turn the Month-Plate *E* till the day of the given New Moon comes to the Annual-Index *G*. 3. Unſcrew the Collar *N* a little on the Axis of the Handle, to looſen the contiguous Socket on which the threads that move the Penumbra are wound; and ſet the Penumbra by Hand till it's Center comes to the perpendicular thread in the middle of the frame; which thread repreſents the Axis of the Ecliptic. 4. Turn the Handle till the Meridian of *London* on the Globe comes juſt under the point of the crooked Wire *F*; then ſtop, and turn the Hour-Circle *D* by Hand till XII at Noon comes to it's Index, and ſet the Penumbra's middle to the thread. 5. Turn the Handle till the Hour-Index points to the time of New Moon in the Circle *D*; and holding it there, ſcrew faſt the Collar *N*. Laſtly, elevate the Machine till the Sun ſhines through the Sight-Holes in the ſmall upright Plates *O*, *O* on the Pedeſtal; and the whole Machine will be rectified.

To rectify the Machine for ſhewing by Candle-light. Proceed in every reſpect as above, except in that part of the laſt paragraph where the Sun is mentioned; inſtead of which place a Candle before the Machine, about four yards from it, ſo as the ſhadow of Interſection of the croſs threads in the middle of the frame may fall preciſely on that part of the Globe to which the crooked Wire *F* points: then, with a pair of Compaſſes, take the diſtance between the Penumbra's Center and Interſection of the threads; and equal to that diſtance ſet the Candle higher or lower, as the Penumbra's Center is above or below the ſaid Interſection. Laſtly, place a large convex Lens between the Machine and Candle, ſo as the Candle may be in the Focus of the Lens, and then the Rays will fall parallel, and caſt a ſtrong light on the Globe.

It's uſe. These things done, which may be ſooner than expreſſed, turn the Handle backward, until the Penumbra almoſt touches the ſide *H F* of the frame; then turning it gradually forward, obſerve the following Phenomena. 1. Where the eaſtern edge of the Shadow of the penumbral Plate *I* firſt touches the Globe at the ſolar Horizon, thoſe who inhabit the correſponding part of the Earth ſee the Eclipſe begin on the uppermoſt edge of the Sun, juſt at the time of it's riſing. 2. In that place where the Penumbra's Center firſt touches the Globe, the inhabitants have the Sun riſing upon them centrally eclipſed. 3. When the whole Penumbra juſt falls upon the Globe, it's weſtern edge at the ſolar Horizon touches and leaves the place where the Eclipſe ends at Sun-riſe on his lowermoſt edge. Continue turning, and, 4. the croſs lines in the Center of the Penumbra will go over all thoſe places on the Globe where the Sun is centrally eclipſed. 5. When the eaſtern edge of the Shadow touches any place of the Globe, the Eclipſe begins there; when the vertical line in the Penumbra comes to any place, then is the greateſt obſcuration at that place; and when the weſtern edge of the Penumbra leaves the place, the Eclipſe ends there; the times of all which are ſhewn on the Hour-Circle; and from the beginning to the end, the Shadows of the concentric penumbral Circles ſhew the numbers of Digits eclipſed at all the intermediate times. 6. When the eaſtern edge of the Penumbra leaves the Globe at the ſolar Horizon *C*, the inhabitants ſee the Sun beginning to be eclipſed on his lowermoſt edge at it's ſetting. 7. Where the Penumbra's Center leaves the Globe, the inhabitants ſee the Sun ſet centrally eclipſed. And laſtly, where the Penumbra is wholly departing from the Globe, the inhabitants ſee the Eclipſe ending on the uppermoſt part of the Sun's edge, at the time of it's diſappearing in the Horizon.

N. B. If any given day of the year on the Plate *E* be ſet to the Annual-Index *G*, and the Handle turned till the Meridian of any place comes under the point of the crooked Wire, and then the Hour-Circle *D* ſet by the hand till XII comes to it's Index; in turning the Globe round by the Handle, when the ſaid place touches the eaſtern edge of the Hoop or ſolar Horizon *C*, the Index ſhews the time of Sun-ſetting at that place; and when the place is juſt coming out from below the other edge of the Hoop *C*, the Index ſhews the time when the evening Twilight ends to it. When the place has gone through the dark part *A*, and comes about ſo as to touch under the back of the Hoop *C*, on the

the other ſide, the Index ſhews the time when the Morning Twilight begins; and when the ſame place is juſt coming out from below the edge of the Hoop next the frame, the Index points out the time of Sun-riſing. And thus, the times of Sun-riſing and ſetting are ſhewn at all places in one rotation of the Globe, for any given day of the year: and the point of the crooked Wire *F* ſhews all the places over which the Sun paſſes vertically on that day.

A
PLAIN METHOD

OF FINDING

The DISTANCES of all the PLANETS
from the SUN,

BY THE

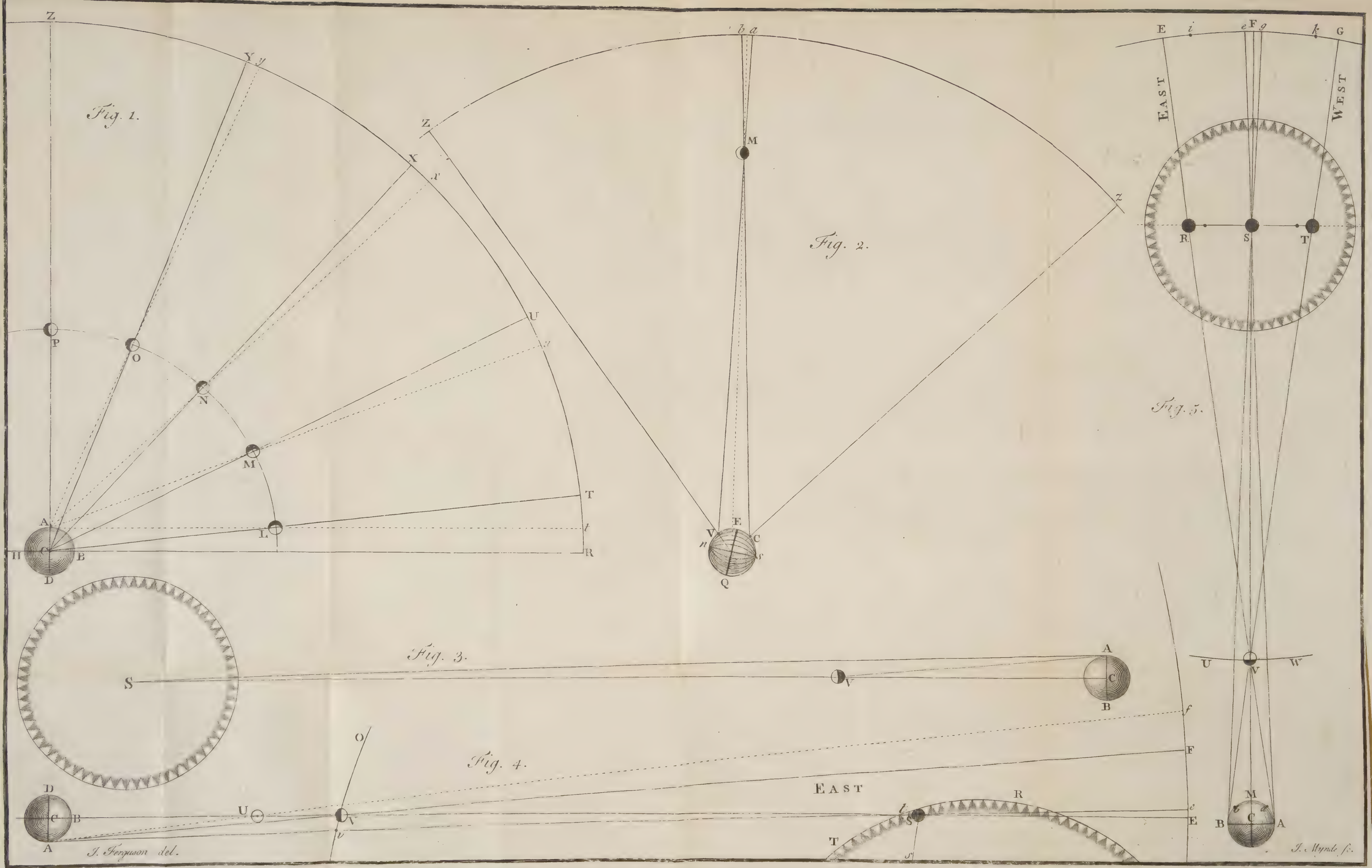
Tranſit of VENUS over the SUN's DISC,
in the Year 1761.

To which is ſubjoined,

An Account of Mr. HORROX's Obſervations of
the TRANSIT of VENUS in the Year 1639.

AND ALSO,

Of the DISTANCES of all the PLANETS from the
SUN, as deduced from OBSERVATIONS of the
TRANSIT in the Year 1761.



J. Ferguson del.

J. Mynde sc.

THE METHOD OF FINDING The DISTANCES of the PLANETS from the SUN.

CHAPTER XXIII.

ARTICLE I.

Concerning parallaxes, and their uſe in general.

1. THE * approaching tranſit of Venus over the Sun has juſtly engaged the attention of Aſtronomers, as it is a phenomenon ſeldom ſeen, and as the parallaxes of the Sun and planets, and their diſtances from one another, may be found with greater accuracy by it, than by any other method yet known.

2. The parallax of the Sun, Moon, or any planet, is the diſtance between it's true and apparent place in the heaven.—The true place of any celeſtial object, referred to the ſtarry heaven, is that in which it would appear if ſeen from the center of the Earth; the apparent place, is that in which it appears as ſeen from the Earth's ſurface.

To explain this, let *ABDH* be the Earth (Fig. 1. of Plate XIV.) *C* it's center, *M* the Moon, and *ZXR* an arc of the ſtarry heaven. To an obſerver at *C* (ſuppoſing the Earth to be tranſparent) the Moon *M* will appear at *U*, which is her true place referred to the ſtarry firmament: but at the ſame inſtant, to an obſerver at *A* ſhe will appear at *u*, below her true place as among the ſtars. The angle *AMC* is called the Moon's parallax, and is equal to the oppoſite angle *UMu*, whoſe meaſure is the celeſtial arc *Uu*.—The whole Earth is but a point if compared with it's diſtance from the fixed ſtars, and therefore we conſider the ſtars as having no parallax at all.

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* The whole of this Diſſertation was publiſhed in the beginning of the year 1761, before the time of the Tranſit, except the 7th and 8th Articles, which are added ſince that time.

3. The nearer the object is to the horizon, the greater is it's parallax; the nearer it is to the zenith, the leſs. In the horizon it is greateſt of all, in the zenith it is nothing.—Thus let *ALt* be the ſenſible horizon of an obſerver at *A*; to him the Moon at *L* is in the horizon, and her parallax is the angle *ALC*, under which the Earth's ſemidiameter *AC* appears as ſeen from her. This angle is called the Moon's horizontal parallax, and is equal to the oppoſite angle *TLt*, whoſe meaſure is the arc *Tt* in the ſtarry heaven. As the Moon riſes higher and higher to the points *M*, *N*, *O*, *P* in her diurnal courſe, the parallactic angles *UMu*, *XNx*, *YOy* diminiſh, and ſo do the arcs *Uu*, *Xx*, *Yy*, which are their meaſures, until the Moon comes to *P*; and then ſhe appears in the zenith *Z* without any parallax, her place being the ſame as ſeen from *A* on the Earth's ſurface, and from *C* it's center.

4. If the obſerver at *A* could take the true meaſure or quantity of the parallactic angle *ALC*, he might thereby find the Moon's diſtance from the center of the Earth. For then, in the plain triangle *LAC*, the ſide *AC*, which is the Earth's ſemidiameter, the angle *ALC*, which is the Moon's horizontal parallax, and the right angle *CAL*, would be given. Therefore, by trigonometry, As the tangent of the parallactic angle *ALC* is to radius, ſo is the Earth's ſemidiameter *AC* to the Moon's diſtance *CL* from the Earth's center *C*.—But becauſe we conſider the Earth's ſemidiameter as unity, and the logarithm of unity is nothing, ſubtract

tract the logarithmic tangent of the angle *ALC* from radius, and the remainder will be the logarithm of *CL*, whoſe number is equal to the number of ſemidiameters of the Earth by which the Moon is diſtant from the Earth's center.—Thus ſuppoſing the angle *ALC* of the Moon's horizontal parallax to be 57′ 18″.

From the radius — — — 10.0000000
Subtract the tangent of 57′ 18″ 8.2219207

And there will remain — — 1.7780793;

which is the logarithm of 59.9955, the number of ſemidiameters of the Earth which are equal to the Moon's diſtance from the Earth's center. Then, 59.9955 being multiplied by 3985, the number of miles contained in the Earth's ſemidiameter, will give 239,082 miles for the Moon's diſtance from the center of the Earth.

5. But the true quantity of the Moon's horizontal parallax cannot be accurately determined by obſerving the Moon in the horizon, on account of the inconſtancy of the horizontal refractions, which always vary according to the ſtate of the atmoſphere; and, at a mean rate, elevate the Moon's apparent place near the horizon half as much more than as her parallax depreſſeth it. And therefore, to have her parallax more accurate, Aſtronomers have thought of the following method, which ſeems to be a very good one, but hath not yet been put in practice.

Let two obſervers be placed under the ſame meridian, one in the northern hemiſphere, and the other in the ſouthern, at ſuch a diſtance from each other, that the arc of the celeſtial meridian included between their two zeniths may be at leaſt 80 or 90 degrees. Let each obſerver take the diſtance of the Moon's center from his zenith, by means of an exceeding good inſtrument, at the moment of her paſſing the meridian: add theſe two zenith-diſtances of the Moon together, and their exceſs above the diſtance between the two zeniths will be the diſtance between the two apparent places of the Moon. Then, as the ſum of the natural ſines of the two zenith-diſtances of the Moon is to radius, ſo is the diſtance between her two apparent places to her horizontal parallax: which being found, her diſtance from the Earth's center may be found by the analogy mentioned in § 4.

Thus, in Fig. 2. let *V E C Q* be the Earth, *M* the Moon, and *Z b a z* an arc of the celeſtial meridian. Let *V* be *Vienna*, whoſe latitude *E V* is 48° 20′ north; and *C* the *Cape of Good Hope*, whoſe latitude *E C* is 34° 30′ ſouth: both which latitudes we ſuppoſe to be accurately determined before-hand by the obſervers. As theſe two places are on the ſame meridian *n V E C s*, and in different hemiſpheres, the ſum of their latitudes 82° 50′ is their diſtance from each other. *Z* is the zenith of *Vienna*, and *z* the zenith of the *Cape of Good Hope*; which two zeniths are alſo 82° 50′ diſtant from each other, in the common celeſtial meridian *Z z*. To the obſerver at *Vienna*, the Moon's center will appear at *a* in the celeſtial meridian; and at the ſame inſtant, to the obſerver at the *Cape*, it will appear at *b*. Now ſuppoſe the Moon's diſtance *Z a* from the zenith of *Vienna* to be 38° 1′ 53″; and her diſtance *z b* from the zenith of the *Cape of Good Hope* to be 46° 4′ 41″: the ſum of theſe two zenith-diſtances $(Za + zb)$ is 84° 6′ 34″, from which ſubtract 82° 50″, the diſtance *Z z* between the zeniths of theſe two places, and there will remain 1° 16′ 34″ for the arc *b a*, or diſtance between the two apparent places of the Moon's center, as ſeen from *V* and from *C*. Then, ſuppoſing the tabular radius to be 10000000, the natural ſine of 38° 1′ 53″ (the arc *Z a*) is 6160816, and the natural ſine of 46° 4′ 41″ (the arc *z b*) is 7202821: the ſum of both theſe ſines is 13363637. Say therefore, As 13363637 is to 10000000, ſo is 1° 16′ 34″, to 57′ 18″, which is the Moon's horizontal parallax.

If the two places of obſervation be not exactly under the ſame meridian, their difference of longitude muſt be accurately taken, that proper allowance may be made for the Moon's declination whilſt ſhe is paſſing from the meridian of the one to the meridian of the other.

6. The Earth's diameter, as ſeen from the Moon, ſubtends an angle of double the Moon's horizontal parallax; which being ſuppoſed (as above) to be 57′ 18″, or 3438″, the Earth's diameter muſt be 1° 54′ 36″, or 6876″. When the Moon's horizontal parallax (which is variable on account of the excentricity of her orbit) is 57′ 18″, her diameter ſubtends an angle 31′ 2″, or 1862″: therefore, the Earth's diameter is to the Moon's diameter, as 6876 is to 1862; that is, as 3.69 is to 1.

And ſince the relative bulks of ſpherical bodies are as the cubes of their diameters, the Earth's bulk is to the Moon's bulk, as 49.4 is to 1.

7. The parallax, and conſequently the diſtance and bulk, of any primary planet, might be found in the above manner, if the planet was near enough to the Earth, ſo as to make the difference of it's two apparent places ſufficiently ſenſible: but the neareſt planet is too remote for the accuracy required. In order therefore to determine the diſtances and relative bulks of the planets with any tolerable degree of preciſion, we muſt have recourſe to a method leſs liable to error: and this, the approaching tranſit of Venus over the Sun's diſc will afford us.

8. From the time of any inferior conjunction of the Sun and Venus to the next, is 583 days 22 hours 7 minutes. And, if the plane of Venus's orbit were coincident with the plane of the ecliptic, ſhe would paſs directly between the Earth and the Sun at each inferior conjunction, and would then appear like a dark round ſpot on the Sun for about

7 hours and 3 quarters. But Venus's orbit (like the Moon's) only interſects the ecliptic in two oppoſite points, called it's Nodes. And therefore one half of it is on the north ſide of the ecliptic, and the other on the ſouth: on which account, Venus can never be ſeen on the Sun, but at thoſe inferior conjunctions which happen in or near the nodes of her orbit. At all the other conjunctions, ſhe either paſſes above or below the Sun; and her dark ſide being then towards the Earth, ſhe is inviſible. —The laſt time when this planet was ſeen like a ſpot on the Sun, was on the 24th of *November* Old Stile, in the year 1639.

ARTICLE II.

Shewing how to find the horizontal parallax of Venus by obſervation, and from thence, by analogy, the parallax and diſtance of the Sun, and of all the Planets from him.

9. In Fig. 4. of Plate XIV. let *D B A* be the Earth, *V* Venus, and *T S R* the eaſtern limb of the Sun. To an obſerver at *B*, the point *t* of that limb will be on the meridian, it's place referred to the heaven will be at *E*, and Venus will appear juſt within it at *S*. But, at the ſame inſtant, to an obſerver at *A*, Venus is eaſt of the Sun, in the right line *A V F*; the point *t* of the Sun's limb appears at *e* in the heaven, and if Venus were then viſible, ſhe would appear at *F*. The angle *C V A* is the horizontal parallax of Venus, which we ſeek; and is equal to the oppoſite angle *F V E*, whoſe meaſure is the arc *F E*. *A S C* is the Sun's horizontal parallax, equal to the oppoſite angle *e S E*, whoſe meaſure is the arc *e E*: and *F A e* (the ſame as *V A v*) is Venus's horizontal parallax from the Sun, which may be found by obſerving how much later in abſolute time her total ingreſs on the Sun is, as ſeen from *A*, than as ſeen from *B*, which is the

time ſhe takes to move from *V* to *v* in her orbit *O V v.*

10. It appears by the tables of Venus's motion and the Sun's, that at the time of her enſuing tranſit, ſhe will move 4′ of a degree on the Sun's diſc in 60 minutes of time; and therefore ſhe will move 4″ of a degree in one minute of time.

Now, let us ſuppoſe, that *A* is 90° weſt of *B*, ſo that when it is noon at *B*, it will be VI in the morning at *A*; that the total ingreſs as ſeen from *B* is at 1 minute paſt XII. but that as ſeen from *A* it is at 7 minutes 30 ſeconds paſt VI: deduct 6 hours for the difference of meridians of *A* and *B*, and the remainder will be 6 minutes 30 ſeconds for the time by which the total ingreſs of Venus on the Sun at *S* is later as ſeen from *A* than as ſeen from *B*: which time being converted into parts of a degree is 26″, or the arc *F e* of Venus's horizontal parallax from the Sun: for, as 1 minute of time is to 4 ſeconds of a degree, ſo is 6½ minutes of time to 26 ſeconds of a degree.

11. The times in which the planets perform their annual revolutions about the Sun, are already known by obſervation.—From theſe times, and the univerſal power of gravity by which the planets are retained in their orbits, it is demonſtrable, that if the Earth's mean diſtance from the Sun be divided into 100000 equal parts, Mercury's mean diſtance from the Sun muſt be equal to 38710 of theſe parts—Venus's mean diſtance from the Sun, to 72333—Mars's mean diſtance, 152369—Jupiter's 520096—and Saturn's, 954006. Therefore, when the number of miles contained in the mean diſtance of any planet from the Sun is known, we we can, by theſe proportions, find the mean diſtance in miles of all the reſt.

12. At the time of the enſuing tranſit, the Earth's diſtance from the Sun will be 1015 (the mean diſtance being here conſidered as 1000) and Venus's diſtance from the Sun will be 726 (the

mean diſtance being conſidered as 723) which differences from the mean diſtances ariſe from the elliptical figure of the planets orbits.—Subtract 726 parts from 1015, and there will remain 289 parts for Venus's diſtance from the Earth at that time.

13. Now, ſince the horizontal parallaxes of the planets are * inverſely as their diſtances from the Earth's center, it is plain, that as Venus will be between the Earth and the Sun on the day of her tranſit, and conſequently her parallax will be then greater than the Sun's, if her horizontal parallax can be then aſcertained by obſervation, the Sun's horizontal parallax may be found, and conſequently his diſtance from the Earth.—Thus, ſuppoſe Venus's horizontal parallax ſhould be found to be 36″.3480; then, As the Sun's diſtance 1015 is to Venus's diſtance 289, ſo is Venus's horizontal parallax 36″.3480 to the Sun's horizontal parallax 10″.3493 on the day of her tranſit. And the difference of theſe two parallaxes, viz. 25″.9987 (which may be eſteemed 26″) will be the quantity of Venus's horizontal parallax from the Sun; which is one of the elements for projecting or delineating her tranſit over the Sun's diſc, as will appear further on.

To find the Sun's horizontal parallax at the time of his mean diſtance from the Earth, ſay, As 1000 parts, the Sun's mean diſtance from the Earth's center, is to 1015, his diſtance therefrom on the

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* To prove this, let *S* be the Sun (Fig. 3.) *V* Venus, *A B* the Earth, *C* it's center, and *A C* it's ſemidiameter. The angle *A V C* is the horizontal parallax of Venus, and *A S C* the horizontal parallax of the Sun. But by the property of plain triangles, as the ſine of *A V C* (or of *S V A* it's ſuppliment to 180°) is to the ſine of *A S C*, ſo is *A S* to *A V*, and ſo is *C S* to *C V*.—*N. B.* In all angles leſs than a minute of a degree, the ſines, tangents, and arcs, are ſo nearly equal, that they may without error be uſed for one another. And here we make uſe of *Gardiner*'s logarithmic tables, becauſe they have the ſines to every ſecond of a degree.

day of the tranſit, ſo is 10″.3493, his horizontal parallax on that day, to 10″.5045, his horizontal parallax at the time of his mean diſtance from the Earth's center.

14. The Sun's parallax being thus (or any other way ſuppoſed to be) found, at the time of his mean diſtance from the Earth, we may find his true diſtance therefrom, in ſemidiameters of the Earth, by the following analogy. As the ſine (or tangent of ſo ſmall an arc as that) of the Sun's parallax 10″.5045 is to radius, ſo is unity or the Earth's ſemidiameter to the number of ſemidiameters of the Earth that the Sun is diſtant from it's center, which number, being multiplied by 3985, the number of miles contained in the Earth's ſemidiameter, will give the number of miles by which the Sun is diſtant from the Earth's center.

Then, by § 11, As 100000, the Earth's mean diſtance from the Sun in parts, is to 38710, Mercury's mean diſtance from the Sun in parts, ſo is the Earth's mean diſtance from the Sun in miles to Mercury's mean diſtance from the Sun in miles.—And,

As 100000 is to 72333, ſo is the Earth's mean diſtance from the Sun in miles to Venus's mean diſtance from the Sun in miles.—Likewiſe,

As 100000 is to 152369, ſo is the Earth's mean diſtance from the Sun in miles to Mars's mean diſtance from the Sun in miles.—Again,

As 100000 is to 520096, ſo is the Earth's mean diſtance from the Sun in miles to Jupiter's mean diſtance from the Sun in miles.—Laſtly,

As 100000 is to 954006, ſo is the Earth's mean diſtance from the Sun in miles to Saturn's mean diſtance from the Sun in miles.

And thus, by having found the diſtance of any one of the planets from the Sun, we have ſufficient *data* for finding the diſtances of all the reſt.—And then, from their apparent diameters at theſe known diſtances, their real diameters and bulks may be found.

15. The Earth's diameter, as ſeen from the Sun, ſubtends an angle of double the Sun's horizontal parallax, at the time of the Earth's mean diſtance from the Sun: and the Sun's diameter, as ſeen from the Earth at that time, ſubtends an angle of 32′ 2″, or 1922″. Therefore, the Sun's diameter is to the Earth's diameter, as 1922 is to 21.—And ſince the relative bulks of ſpherical bodies are as the cubes of their diameters, the Sun's bulk is to the Earth's bulk, as 756058 is to 1; ſuppoſing the Sun's mean horizontal parallax to be 10″.50, as above.

16. It is plain by Fig. 4. that whether Venus be at *U* or *V*, or in any other part of the right line *B V S*, it will make no difference in the time of her total ingreſs on the Sun at *S*, as ſeen from *B*; but as ſeen from *A* it will. For, if Venus be at *V*, her horizontal parallax from the Sun is the arc *F e*, which meaſures the angle *F A e*: but if ſhe be nearer the Earth, as at *U*, her horizontal parallax from the Sun is the arc *f e*, which meaſures the angle *f A e*; and this angle is greater than the angle *F A e*, by the difference of their meaſures *f F*. So that, as the diſtance of the celeſtial object from the Earth is leſs, it's parallax is the greater.

17. To find the parallax of Venus by the above method, it is neceſſary, 1. That the difference of meridians of the two places of obſervation be 90°.—2. That the time of Venus's total ingreſs on the Sun be when his eaſtern limb is either on the meridian of one of the places, or very near it.—And, 3. That each obſerver has his clock exactly regulated to the equal time at his place. But as it might perhaps be difficult to find two places on the Earth ſuited to the firſt and ſecond of theſe requiſites, we ſhall ſhew how this important problem may be ſolved by a ſingle obſerver, if he be exact

as to his longitude, and has his clock truly adjuſted to the equal time at his place.

18. That part of Venus's orbit in which ſhe will move during her tranſit on the Sun, may be conſidered as a ſtraight line; and therefore, a plane may be conceived to paſs both through it and the Earth's center. To every place on the Earth's ſurface cut by this plane, Venus will be ſeen on the Sun in the ſame path that ſhe would deſcribe as ſeen from the Earth's center: and therefore, ſhe will have no parallax of latitude, either north or ſouth; but will have a greater or leſs parallax of longitude, as ſhe is more or leſs diſtant from the meridian, at any time during her tranſit.

Matura, a town and fort on the ſouth coaſt of the iſland of *Ceylon*, will be in this plane at the time of Venus's total ingreſs on the Sun; and the Sun will then be 62°½ eaſt of the meridian of that place. Conſequently, to an obſerver at *Matura*, Venus will have a conſiderable parallax of longitude eaſtward from the Sun, when ſhe would appear to touch the Sun's eaſtern limb, as ſeen from the Earth's center, at which the Aſtronomical tables ſuppoſe the obſerver to be placed, and give the times as ſeen from thence.

19. According to theſe tables, Venus's total ingreſs on the Sun will be 50 minutes after VII in the morning, at *Matura* *, ſuppoſing that place to be 80° eaſt longitude from the meridian of *London*; which is the obſerver's buſineſs to determine. Let us imagine that he finds it to be exactly ſo, but that to him the total ingreſs is at VII hours 55 minutes 46 ſeconds, which is 5 minutes 46 ſeconds later than the true calculated time of total ingreſs, as ſeen from the Earth's center. Then, as Venus's

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* The time of total ingreſs at *London*, as ſeen from the Earth's center, is at 30 minutes after II in the morning; and if *Matura* be juſt 80° (or 5 hours 20 minutes) eaſt of *London*, when it is 30 minutes paſt II in the morning at *London*, it is 50 minutes paſt VII at *Matura*.

motion on (or towards, or from) the Sun is at the rate of 4 minutes of a degree in an hour (by § 10.) her motion muſt be 23″.1 of a degree in 5 minutes 46 ſeconds of time: and this 23″.1 is her parallax eaſtward, from her total ingreſs as ſeen from *Matura*, when her ingreſs would be total if ſeen from the Earth's center.

20. At VII hours 50 minutes in the morning, the Sun is $62^\circ\frac{1}{2}$ from the meridian; at VI in the morning he is 90° from it: therefore, as the ſine of $62^\circ\frac{1}{2}$ is to the ſine of 23″.1 (which is Venus's parallax from her true place on the Sun at VII hours 50 minutes) ſo is radius, or the ſine of 90°, to the ſine of 26″, which is Venus's horizontal parallax from the Sun at VI. In logarithms thus:

As the logarithmic ſine of 62° 30′ - - -	9.9479289
Is to the logarithmic ſine of 23″.1 - - -	6.0481510
So is the logarithmic radius - - - - - -	10.0000000
To the logarithmic ſine of 26″ very nearly	6.1002221

Divide the Sun's diſtance from the Earth, 1015, by his diſtance from Venus 726 (§ 12.) and the quotient will be 1.3980; which being multiplied by Venus's horizontal parallax from the Sun 26″, will give 36″.3480 for her horizontal parallax as ſeen from the Earth at that time.—Then (by § 13.) As the Sun's diſtance 1015 is to Venus's diſtance 289, ſo is Venus's horizontal parallax 36″.3480 to the Sun's horizontal parallax 10″.3493.—If Venus's horizontal parallax from the Sun is found by obſervation to be greater or leſs than 26″, the Sun's horizontal parallax muſt be greater or leſs than 10″.3493 accordingly.

21. And thus, by a ſingle obſervation, the parallax of Venus, and conſequently the parallax of the Sun, might be found, if we were ſure that the Aſtronomical tables were quite correct as to the time of Venus's total ingreſs on the Sun.—But although the tables may be ſafely depended upon

for ſhewing the true duration of the tranſit, which will not be quite 6 hours from the time of Venus's total ingreſs on the Sun's eaſtern limb, to the beginning of her egreſs from his weſtern; yet they may perhaps not give the true times of theſe two internal contacts: like a good common clock, which though it may be truſted to for meaſuring a few hours of time, yet perhaps it may not be quite adjuſted to the meridian of the place, and conſequently not true as to any one hour; which every one knows is generally the caſe.—Therefore, to make ſure work, the obſerver ought to watch both the moment of Venus's total ingreſs on the Sun, and her beginning of egreſs from him, ſo as to note preciſely the time between theſe two inſtants, by means of a good clock: and by comparing the interval at his place with the true calculated interval as ſeen from the Earth's center, which will be 5 hours 58 minutes, he may find the parallax of Venus from the Sun both at her total ingreſs and beginning of egreſs.

22. The manner of obſerving the tranſit ſhould be as follows.—The obſerver being provided with a good teleſcope, and a pendulum clock well adjuſted to the mean diurnal revolution of the Sun, and as near to the time at his place as conveniently may be; and having an aſſiſtant to watch the clock at the proper times, he muſt begin to obſerve the Sun's eaſtern limb through his teleſcope, twenty minutes at leaſt before the computed time of Venus's total ingreſs upon it, leſt there ſhould be an error in the time thereof as given by the tables.

When he perceives a dent (as it were) to be made in the Sun's limb by the interpoſition of the dark body of Venus, he muſt then continue to watch her through the teleſcope as the dent increaſes; and his aſſiſtant muſt watch the time ſhewn by the clock, till the whole body of the planet appears juſt within the Sun's limb: and the moment when the bright limb of the Sun appears

cloſe

cloſe by the eaſt ſide of the dark limb of the planet, the obſerver, having a little hammer in his hand, is to ſtrike a blow therewith on the table or wall; the moment of which, the aſſiſtant notes by the clock, and writes it down.

Then, let the planet paſs on for about 2 hours 59 minutes, in which time it will be got to the middle of it's apparent path on the Sun, and conſequently will then be at it's leaſt apparent diſtance from the Sun's center; at which time, the obſerver muſt take it's diſtance from the Sun's center, by means of a good micrometer, in order to aſcertain it's true latitude or declination from the ecliptic, and thereby find the places of it's nodes.

This done, there is but little occaſion to obſerve it any longer, until it comes ſo near the Sun's weſtern limb, as almoſt to touch it. Then the obſerver watches the planet carefully with his teleſcope; and his aſſiſtant watches the clock, ſo as to note the preciſe moment of the planet's touching the Sun's limb, which the aſſiſtant knows by the obſerver's ſtriking a blow with his hammer.

23. The aſſiſtant muſt be very careful in obſerving what minute on the Dial-Plate the minute-hand has paſt, when he has obſerved the ſecond-hand at the inſtant the blow was ſtruck by the hammer: otherwiſe, though he be right as to the number of ſeconds of the current minute, he may be apt to make a miſtake in the number of minutes.

24. To thoſe places where the tranſit begins before XII at noon, and ends after it, Venus will have an eaſtern parallax from the Sun at the beginning, and a weſtern parallax from the Sun at the end; which will contract the duration of the tranſit, by cauſing it to begin later, and end ſooner at theſe places, than it does as ſeen from the Earth's center; which may be explained in the following manner.

In Fig. 5. of Plate XIV. let *BMA* be the Earth, *V* Venus, and *S* the Sun. The Earth's motion on it's axis from weſt to eaſt, or in the direction *AMB*, carries an obſerver on that ſide contrary to the motion of Venus in her orbit, which is in the direction *UVW*, and will therefore cauſe her motion to appear quicker on the Sun's diſc, than it would appear to an obſerver placed at the Earth's center *C*, or at either of it's poles. For, if Venus were to ſtand ſtill in her orbit at *V* for twelve hours, the obſerver on the Earth's ſurface would in that time be carried from *A* to *B*, through the arc *AMB*. When he was at *A*, he would ſee Venus on the Sun at *R*; when at *M*, he would ſee her at *S*; and when he was at *B*, he would ſee her at *T*: ſo that his own motion would cauſe the planet to appear in motion on the Sun through the line *RST*: which being in the direction of her apparent motion on the Sun as ſhe moves in her orbit *UW*, her motion will be accelerated on the Sun to this obſerver, juſt as much as his own motion would ſhift her apparent place on the Sun, if ſhe were at reſt in her orbit at *V*.

But as the whole duration of the tranſit, from firſt to laſt internal contact, will not be quite ſix hours; an obſerver, who has the Sun on his meridian at the middle of the tranſit, will be carried only from *a* to *b* during the whole time thereof. And therefore, the duration will be much leſs contracted by his own motion, than if the planet were to be twelve hours in paſſing over the Sun, as ſeen from the Earth's center.

25. The nearer Venus is to the Earth, the greater is her parallax, and the more will the true duration of her tranſit be contracted thereby; the farther ſhe is from the Earth, the contrary: ſo that the contraction will be in direct proportion to the parallax. Therefore, by obſerving, at proper places, how much the duration of the tranſit is leſs than it's true duration at the Earth's center, where it is

5 hours

5 hours 58 minutes, as given by the Aſtronomical tables, the parallax of Venus will be aſcertained.

26. The above method (§ 17, *& ſeq.*) is much the ſame as was preſcribed long ago by Doctor Halley, but the calculations differ conſiderably from his; as will appear in the next article, which contains a tranſlation of the Doctor's whole diſſertation on that ſubject.—He had not computed his own tables when he wrote it, nor had he time before-hand to make a ſufficient number of obſervations on the motion of Venus, ſo as to determine whether the nodes of her orbit are at reſt or no; and was therefore obliged to truſt to other tables, which are now found to be erroneous.

ARTICLE III.

Containing Doctor Halley's *Diſſertation on the method of finding the Sun's parallax and diſtance from the Earth, by the tranſit of Venus over the Sun's Diſc*, June *the* 6*th*, 1761. *Tranſlated from the Latin in* Motte's *Abridgment of the Philoſophical Tranſactions, Vol. I. pag.* 243; *with additional notes.*

There are many things exceedingly paradoxical, and that ſeem quite incredible to the illiterate, which yet by means of mathematical principles may be eaſily ſolved. Scarce any problem will appear more hard and difficult, than that of determining the diſtance of the Sun from the Earth very near the truth: but even this, when we are made acquainted with ſome exact obſervations, taken at places fixed upon, and choſen before-hand, will without much labour be effected. And this is what I am now deſirous to lay before this illuſtrious Society * (which I foretell will continue for ages) that I may explain before-hand to young Aſtronomers, who may perhaps live to obſerve theſe things, the method whereby the immenſe diſtance of the Sun may be truly obtained, to within a five hundredth part of what it really is.

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* The Royal Society.

It is well known that the diſtance of the Sun from the Earth is by different Aſtronomers ſuppoſed different, according to what was judged moſt probable from the beſt conjecture that each could form. *Ptolemy* and his followers, as alſo *Copernicus* and *Tycho Brahe*, thought it to be 1200 ſemidiameters of the Earth: *Kepler* 3500 nearly; *Ricciolus* doubles the diſtance mentioned by *Kepler*, and *Hevelius* only increaſes it by one half. But the planets Venus and Mercury having, by the aſſiſtance of the teleſcope, been ſeen in the diſc of the Sun, deprived of their borrowed brightneſs, it is at length found, that the apparent diameter of the planets are much leſs than they were formerly ſuppoſed; and that the ſemidiameter of Venus ſeen from the Sun ſubtends no more than a fourth part of a minute, or fifteen ſeconds, whilſt the ſemidiameter of Mercury, at it's mean diſtance from the Sun, is ſeen under an angle only of ten ſeconds; that the ſemidiameter of Saturn ſeen from the Sun appears under the ſame angle; and that the ſemidiameter of Jupiter, the largeſt of all the planets, ſubtends an angle of no more than a third part of a minute at the Sun. Whence, keeping the proportion, ſome modern Aſtronomers have thought, that the ſemidiameter of the Earth, ſeen from the Sun, would ſubtend a mean angle between that larger one ſubtended by Jupiter, and that ſmaller one ſubtended by Saturn and Mercury; and equal to that ſubtended by Venus, (namely, fifteen ſeconds:) and have thence concluded, that the Sun is diſtant from the Earth almoſt 14000 of the Earth's ſemidiameters. But the ſame authors have on another account ſomewhat increaſed this diſtance: for, inaſmuch as the Moon's diameter is a little more than a fourth part of the diameter of the Earth, if the Sun's parallax ſhould be ſuppoſed fifteen ſeconds, it would follow, that the body of the Moon is larger than that of Mercury; that is, that a ſecondary planet would be greater than a primary, which would ſeem inconſiſtent with the uniformity of the mundane ſyſtem. And on the contrary, the ſame regularity and uniformity ſeems ſcarcely to admit, that Venus, an inferior planet, that has no ſatellite, ſhould be greater than our Earth, which ſtands higher in the ſyſtem, and has ſuch a ſplendid attendant. Therefore, to obſerve a mean, let us ſuppoſe the ſemidiameter of the Earth ſeen from the Sun, or, which is the ſame thing, the Sun's horizontal parallax, to be twelve ſeconds and a half; according to which, the Moon will be leſs than Mercury, and the Earth larger than Venus; and the Sun's diſtance from the Earth will come out nearly 16500 of the Earth's ſemidiameters. This diſtance I aſſent to at preſent, as the true one, till it ſhall become certain what it is, by the experiment which I propoſe. Nor am I induced to alter my opinion by the authority of thoſe (however weighty it may be) who are for placing the Sun at an immenſe diſtance beyond the bounds here aſſigned, relying on obſervations made upon the vibrations of a pendulum, in order to determine thoſe exceeding ſmall angles; but which, as it ſeems, are not ſufficient to be depended upon: at leaſt, by this method of inveſtigating the parallax, it will come out ſometimes nothing, or even negative; that is, the diſtance would either become infinite, or greater than infinite; which is abſurd. And indeed, to confeſs the truth, it is hardly poſſible for a man to diſtinguiſh, with any degree of certainty, ſeconds, or even ten ſeconds, with inſtruments, let them be ever ſo ſkilfully made: therefore, it is not at all to be wondered at, that the exceſſive nicety of this matter has eluded the many and ingenious endeavours of ſuch ſkilful operators.

About forty years ago, whilſt I was in the iſland of *St. Helena*, obſerving the ſtars about the ſouth pole, I had an opportunity of obſerving, with the greateſt diligence, Mercury paſſing over the diſc of the Sun; and (which ſucceeded better than I could have hoped for) I obſerved, with the greateſt degree of accuracy, by means of a teleſcope 24 feet long, the very moment when Mercury entering upon the Sun ſeemed to touch it's limb within, and alſo the moment when going off it ſtruck the limb of the Sun's diſc, forming the angle of interior contact: whence I found the interval of time, during which Mercury then appeared within the Sun's diſc, even without an error of one ſecond of time. For the lucid line intercepted between the dark limb of the planet and the bright limb of the Sun, although exceeding fine, is ſeen by the eye; and the little dent made in the Sun's limb, by Mercury's entering the diſc, appears to vaniſh in a moment; and alſo that made by Mercury, when leaving the diſc, ſeems to begin in an inſtant.—When I perceived this, it immediately came into my mind, that the Sun's parallax might be accurately determined by ſuch kind of obſervations as theſe; provided Mercury were but nearer to the Earth, and had a greater parallax from the Sun: but the difference of theſe parallaxes is ſo little, as always to be leſs than the ſolar parallax which we ſeek; and therefore Mercury, though frequently to be ſeen on the Sun, is not to be looked upon as fit for our purpoſe.

There remains then the tranſit of Venus over the Sun's diſc; whoſe parallax, being almoſt four times as great as the ſolar parallax, will cauſe very ſenſible differences between the times in which Venus will ſeem to be paſſing over the Sun at different parts of the Earth. And from theſe differences, if they be obſerved as they ought, the Sun's parallax may be determined even to a ſmall part of a ſecond. Nor do we require any other inſtruments for this purpoſe, than common teleſcopes and clocks, only good of their kind; and in the obſervers, nothing more is needful than fidelity, diligence, and a moderate ſkill in Aſtronomy.

For there is no need that the latitude of the place ſhould be ſcrupulouſly obſerved, nor that the hours themſelves ſhould be accurately determined with reſpect to the meridian: it is ſufficient that the clocks be regulated according to the motion of the heavens, if the times be well reckoned from the total ingreſs of Venus into the Sun's diſc, to the beginning of her egreſs from it; that is, when the dark globe of Venus firſt begins to touch the bright limb of the Sun within; which moments, I know by my own experience, may be obſerved within a ſecond of time.

But on account of the very ſtrict laws by which the motions of the planets are regulated, Venus is ſeldom ſeen within the Sun's diſc: and during the courſe of more than 120 years, it could not be ſeen once; namely, from the year 1639 (when this moſt pleaſing ſight happened to that excellent youth *Horrax* our countryman, and to him only, ſince the creation) to the year 1761; in which year, according to the theories which we have hitherto found agreeable to the celeſtial motions, Venus will again paſs over the Sun on the * 26th of *May*, in the morning; ſo that at *London*, about ſix o'clock in the morning, we may expect to ſee it near the middle of the Sun's diſc, and not above four minutes of a degree ſouth of the Sun's center. But the duration of this tranſit will be almoſt eight hours; namely, from two o'clock in the morning till almoſt ten. Hence the ingreſs will not be viſible in *England*; but as the Sun will at that time be in the 16th degree of Gemini, having almoſt 23 degrees north declination, it will be ſeen without ſetting at all in almoſt all parts of the north frigid zone: and therefore the inhabitants of the coaſt of *Norway*, beyond the city of *Nidroſia*, which is called *Drontheim*, as far as the *North Cape*, will be able to obſerve Venus entering the Sun's diſc; and perhaps the ingreſs of Venus upon the Sun, when riſing, will be ſeen by the *Scotch*, in the northern parts of the kingdom, and by the inhabitants of the *Shetland Iſles*, formerly called *Thule*. But at the time when Venus will be neareſt the Sun's center, the Sun will be vertical to the northern ſhores of the bay of *Bengal*, or rather over the kingdom of *Pegu*; and therefore, in the adjacent regions, as the Sun, when Venus enters his diſc, will be almoſt four hours toward the eaſt, and as many to the weſt when ſhe leaves him, the apparent motion of Venus on the Sun will be accelerated by almoſt double the horizontal parallax of Venus from the Sun; becauſe Venus at that time is carried with a retrograde motion from eaſt to weſt, whilſt an eye placed upon the Earth's ſurface is whirled the contrary way, from weſt to eaſt *.

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* The ſixth of *June* according to the New Stile.

Suppoſing

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* This has been already taken notice of in § 24; but I ſhall here endeavour to explain it more at large, together with ſome of the following part of the Doctor's Eſſay, by a figure.

In Fig. 1. of Plate XV. let *C* be the center of the Earth, and *Z* the center of the Sun. In the right line *C v Z*, make *v Z* to *C Z* as 726 is to 1015 (§ 12.) Let *a c b d* be the Earth, *v* Venus's place in her orbit at the time of her conjuction with the Sun; and let *T S U* be the Sun, whoſe diameter is 31′ 42″.

The motion of Venus in her orbit is in the direction *N v n*, and the Earth's motion on it's axis is according to the order of the 24 hours placed around it in the figure. Therefore, ſuppoſing the mouth of the *Ganges* to be at *G*, when Venus is at *E* in her orbit, and to be carried from *G* to *g* by the Earth's motion on it's axis, whilſt Venus moves from *E* to *e* in her orbit; it is plain, that the motions of Venus and the *Ganges* are contrary to each other.

The true motion of Venus in her orbit, and conſequently the ſpace ſhe ſeems to run over on the Sun's diſc in any given time, could be ſeen only from the Earth's center *C*, which is at reſt with reſpect to it's ſurface. And as ſeen from *C*, her path on the Sun would be in the right line *T t U*; and her motion therein at the rate of four minutes of a degree in an hour. *T* is the point of the Sun's eaſtern limb which Venus ſeems to touch at the moment of her total ingreſs on the Sun, as ſeen from *C*, when Venus is at *E* in her orbit; and *U* is the point of the Sun's weſtern limb which ſhe ſeems to touch at the moment of her beginning of egreſs from the Sun, as ſeen from *C*, when ſhe is at *e* in her orbit.

When

Suppoſing the Sun's parallax (as we have ſaid) to be 12″½, the parallax of Venus will be 43″; from which ſubtracting the parallax of the Sun, there will remain 30″ at leaſt for the horizontal parallax of Venus from the Sun; and therefore the motion of Venus will be increaſed 45″ at leaſt by that parallax, whilſt ſhe paſſes over the Sun's diſc, in thoſe elevations of the pole which are in places near the troptic, and yet more in the neighbourhood of the equator. Now, Venus at that time will move on the Sun's diſc, very nearly at the rate of four minutes of a degree in an hour; and therefore 11 minutes of time at leaſt are to be allowed for 45″, or three-fourths of a minute of a degree;

When the mouth of the *Ganges* is at *m* in revolving through the arc *G m g)* the Sun is on it's meridian. Therefore, ſince *G* and *g* are equally diſtant from *m* at the beginning and ending of the tranſit, it is plain that the Sun will be as far eaſt of the meridian of the *Ganges* (at *G)* when the tranſit begins, as it will be weſt of the meridian of the ſame place (revolved from *G* to *g)* when the tranſit ends.

But although the beginning of the tranſit, or rather the moment of Venus's total ingreſs upon the Sun at *T*, as ſeen from the Earth's center, muſt be when Venus is at *E* in her orbit, becauſe ſhe is then ſeen in the direction of the right line *C E T*; yet, at the ſame inſtant of time, as ſeen from the *Ganges* at *G*, ſhe will be ſhort of her ingreſs on the Sun, being then ſeen eaſtward of him, in the right line *G E K*, which makes the angle *K E T* (equal to the oppoſite angle *G E C)* with the right line *C E T*. This angle is called the angle of Venus's parallax from the Sun, which retards the beginning of the tranſit as ſeen from the banks of the *Ganges*; ſo that the *Ganges G* muſt advance a little farther toward *m*, and Venus muſt move on in her orbit from *E* to *R*, before ſhe can be ſeen from *G* (in the right line *G R T)* wholly within the Sun's diſc at *T*.

When Venus comes to *e* in her orbit, ſhe will appear at *U*, as ſeen from the Earth's center *C*, juſt beginning to leave the Sun; that is, at the beginning of her egreſs from his weſtern limb: but at the ſame inſtant of time, as ſeen from the *Ganges*, which is then at *g*, ſhe will be quite clear of the Sun toward the weſt; being then ſeen from *g* in the right line *g e L*, which makes an angle, as *U e L* (equal to the oppoſite angle *C e g)* with the right line *C e U*: and this is the angle of Venus's parallax

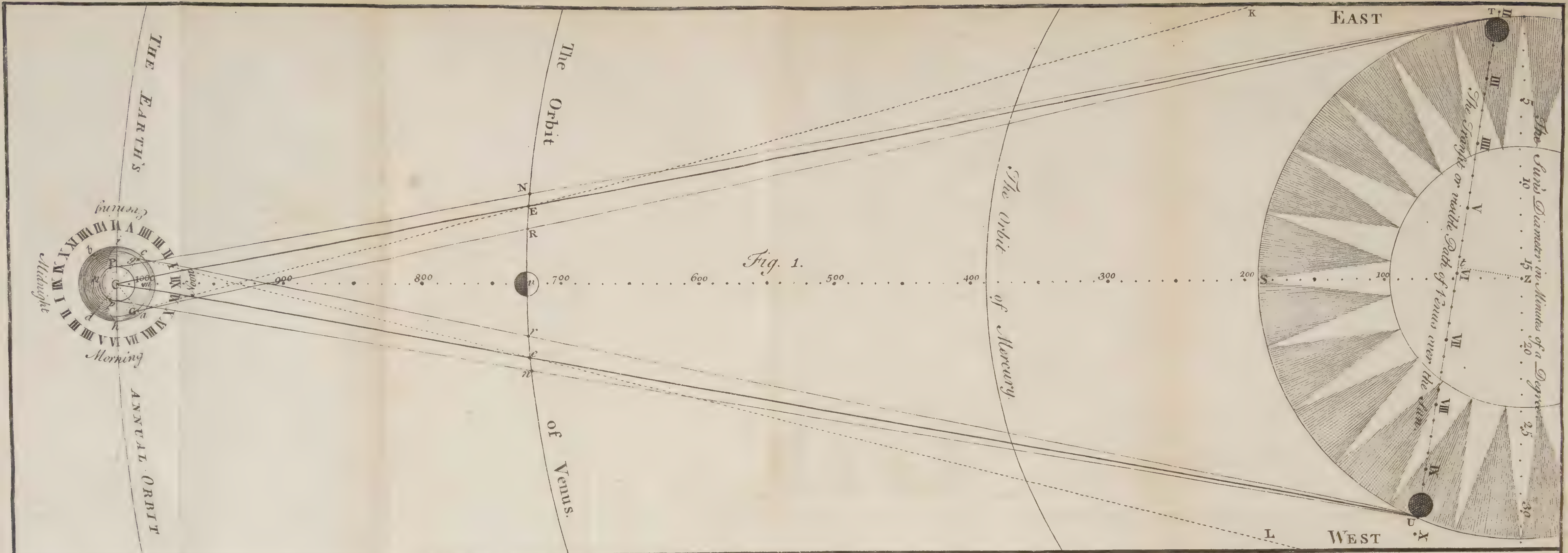

Fig. 1.

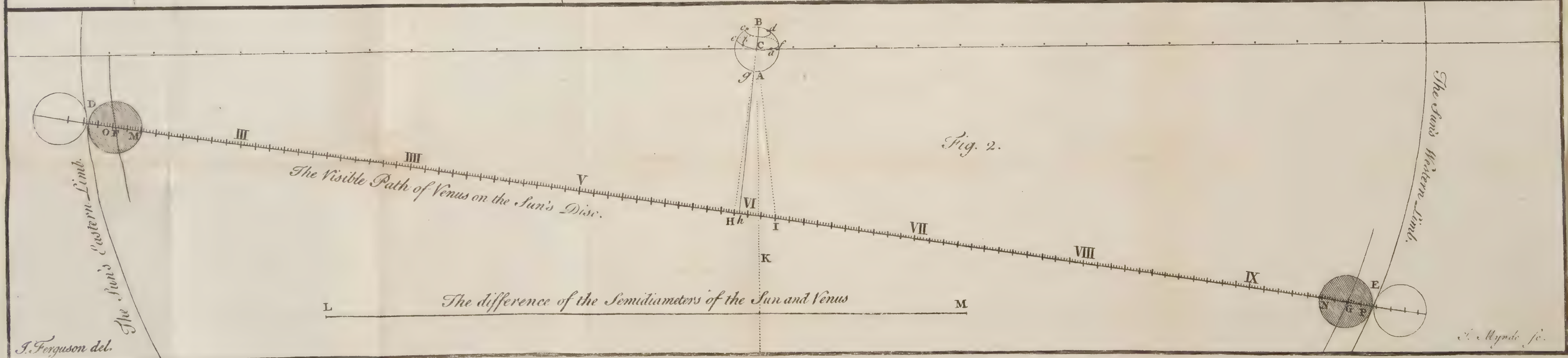
The Visible Path of Venus on the Sun's Disc.
The Sun's Eastern Limb.
The Sun's Western Limb.
The difference of the Semidiameters of the Sun and Venus
B
C
A
D
O
M
H
h
I
K
L
M
E
N
G
P
III
IIII
V
VI
VII
VIII
IX

Fig. 2.

J. Ferguson del.

J. Mynde sc.

a degree; and by this ſpace of time, the duration of this eclipſe cauſed by Venus will, on account of the parallax, be ſhortened. And from this ſhortening of the time only, we might ſafely enough draw a concluſion concerning the parallax which we are in ſearch of, provided the diameter of the Sun, and the latitude of Venus, were accurately known. But we cannot expect an exact computation in a matter of ſuch ſubtility.

We muſt endeavour therefore to obtain, if poſſible, another obſervation, to be taken in thoſe places where Venus will be in the middle of the Sun's diſc at midnight; that is, in places under the oppoſite meridian to the former, or about 6 hours or 90 degrees weſt of *London*; and where Venus enters upon the Sun a little before it's ſet-

parallax from the Sun as ſeen from the *Ganges* at *g*, when ſhe is but juſt beginning to leave the Sun at *U*, as ſeen from the Earth's center *C*.

Here it is plain, that the duration of the tranſit about the mouth of the *Ganges* (and alſo in the neighbouring places) will be diminiſhed by about double the quantity of Venus's parallax from the Sun at the beginning and ending of the tranſit. For Venus muſt be at *E* in her orbit when ſhe is wholly upon the Sun at *T*, as ſeen from the Earth's center *C*: but at that time ſhe is ſhort of the Sun as ſeen from the *Ganges* at *G*, by the whole quantity of her eaſtern parallax from the Sun at that time, which is the angle *KET*. [This angle, in fact, is only 23″; though it is repreſented much larger in the figure, becauſe the Earth therein is a vaſt deal too big.] Now, as Venus moves at the rate of 4′ in an hour, ſhe will move 23″ in 5 minutes 45 ſeconds: and, therefore, the tranſit will be 5 min. 45 ſeconds later of beginning at the banks of the *Ganges* than at the Earth's center.——When the tranſit is ending at *U*, as ſeen from the Earth's center *C*, Venus will be quite clear of the Sun (by the whole quantity of her weſtern parallax from him) as ſeen from the *Ganges*, which is then at *g*: and this parallax will be 22″, equal to the ſpace through which Venus moves in 5 minutes 30 ſeconds of time: ſo that the tranſit will end 5½ minutes ſooner as ſeen from the *Ganges*, than as ſeen from the Earth's center.

Hence, the whole contraction of the duration of the tranſit at the mouth of the *Ganges* will be 11 minutes 15 ſeconds of time: for it is 5 minutes 45 ſeconds at the beginning, and 5 minutes 30 ſeconds at the end.

ting, and goes off a little after it's riſing. And this will happen under the above-mentioned meridian, and where the elevation of the north pole is about 56 degrees; that is, in a part of *Hudſon*'s *Bay*, near a place called *Port-Nelſon*. For, in this and the adjacent places, the parallax of Venus will increaſe the duration of the tranſit by at leaſt ſix minutes of time; becauſe, whilſt the Sun, from it's ſetting to it's riſing, ſeems to paſs under the pole, thoſe places on the Earth's diſc will be carried with a motion from eaſt to weſt, contrary to the motion of the *Ganges*; that is, with a motion conſpiring with the motion of Venus; and therefore, Venus will ſeem to move more ſlowly on the Sun, and to be longer in paſſing over his diſc[*].

If

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[*] In Fig. 1. of Plate XV. let *a C* be the meridian of the eaſtern mouth of the *Ganges*; and *b C* the meridian of *Port-Nelſon* at the mouth of *York-River* in *Hudſon*'s *Bay*, 56° north latitude. As the meridian of the *Ganges* revolves from *a* to *c*, the meridian of *Port-Nelſon* will revolve from *b* to *d*: therefore, whilſt the *Ganges* revolves from *G* to *g*, through the arc *G m g*, *Port-Nelſon* revolves the contrary way (as ſeen from the Sun or Venus) from *P* to *p* through the arc *P n p*.——Now, as the motion of Venus is from *E* to *e* in her orbit, while ſhe ſeems to paſs over the Sun's diſc in the right line *T t U*, as ſeen from the Earth's center *C*, it is plain, that whilſt the motion of the *Ganges* is contrary to the motion of Venus in her orbit, and thereby ſhortens the duration of the tranſit at that place, the motion of *Port-Nelſon* is the ſame way as the motion of Venus, and will therefore increaſe the duration of the tranſit: which may in ſome degree be illuſtrated by ſuppoſing, that whilſt a ſhip is under ſail, if two birds fly along the ſide of the ſhip in contrary directions to each other, the bird which flies contrary to the motion of the ſhip will paſs by it ſooner than the bird will, which flies the ſame way that the ſhip moves.

In fine, it is plain by the figure, that the duration of the tranſit muſt be longer as ſeen from *Port-Nelſon*, than as ſeen from the Earth's center; and longer as ſeen from the Earth's center, than as ſeen from the mouth of the *Ganges*.——For *Port-Nelſon* muſt be at *P*, and Venus at *N* in her orbit, when ſhe appears wholly within the Sun at *T*: and the ſame place muſt be at *p*, and Venus at *n*, when ſhe appears at *U*, beginning to leave the Sun.—The *Ganges* muſt be at *G*, and Venus

at

If therefore it ſhould happen that this tranſit ſhould be properly obſerved by ſkilful perſons at both theſe places, it is clear, that the duration thereof will be 17 minutes longer, as ſeen from *Port-Nelſon*, than as ſeen from the *Eaſt-Indies.* Nor is it of much conſequence (if the *Engliſh* ſhall at that time give any attention to this affair) whether the obſervation be made at *Fort-George*, commonly called *Madras*, or at *Bencoolen* on the weſtern ſhore of the iſland of *Sumatra*, near the equator. But if the *French* ſhall be diſpoſed to take any pains herein, an obſerver may ſtation himſelf conveniently enough at *Pondicherry* on the weſt ſhore of the bay of *Bengal*, where the altitude of the pole is about 12 degrees. As to the *Dutch*, their celebrated mart at *Batavia* will afford them a place of obſervation fit enough for this purpoſe, provided they alſo have but a diſpoſition to aſſiſt in advancing, in this particular, the knowledge of the heavens.—And indeed I could wiſh that many obſervations of the ſame phenomenon might be taken by different perſons at ſeveral places, both that we might arrive at a greater degree of certainty by their agreement, and alſo leaſt any ſingle obſerver ſhould be deprived, by the intervention of clouds, of a ſight, which I know not whether any man living in this or the next age will ever ſee again; and on which depends the certain and adequate ſolution of a problem the moſt noble, and at any other time not to be attained to. I recommend it therefore, again and again, to thoſe curious Aſtronomers, who (when I am dead) will have an opportunity of obſerving theſe things, that they would remem-

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at *R*, when ſhe is ſeen from *G* upon the Sun at *T*; and the ſame place muſt be at *g*, and Venus at *r*, when ſhe begins to leave the Sun at *U*, as ſeen from *g*. So that Venus muſt move from *N* to *n* in her orbit, whilſt ſhe is ſeen to paſs over the Sun from *Port-Nelſon*; from *E* to *e* in paſſing over the Sun, as ſeen from the Earth's center; and only from *R* to *r* whilſt ſhe paſſes over the Sun, as ſeen from the banks of the *Ganges*.

ber this my admonition, and diligently apply themſelves with all their might to the making this obſervation; and I earneſtly wiſh them all imaginable ſucceſs; in the firſt place that they may not, by the unſeaſonable obſcurity of a cloudy ſky, be deprived of this moſt deſirable ſight; and then, that having aſcertained with more exactneſs the magnitudes of the planetary orbits, it may redound to their immortal fame and glory.

We have now ſhewn, that by this method the Sun's parallax may be inveſtigated to within it's five hundredth part, which doubtleſs will appear wonderful to ſome. But if an accúrate obſervation be made in each of the places above marked out, we have already demonſtrated that the durations of this eclipſe made by Venus will differ from each other by 17 minutes of time; that is, upon a ſuppoſition that the Sun's parallax is $12''\frac{1}{2}$. But if the difference ſhall be found by obſervation to be greater or leſs, the Sun's parallax will be greater or leſs, nearly in the ſame proportion. And ſince 17 minutes of time are anſwerable to $12\frac{1}{2}$ ſeconds of ſolar parallax, for every ſecond of parallax there will ariſe a difference of more than 80 ſeconds of time; whence, if we have this difference true to two ſeconds, it will be certain what the Sun's parallax is, to within a 40th part of one ſecond; and therefore, his diſtance will be determined to within it's 500dth part at leaſt, if the parallax be not found leſs than what we have ſuppoſed: for 40 times $12\frac{1}{2}$ make 500.

And now I think I have explained this matter fully, and even more than I needed to have done, to thoſe who underſtand Aſtronomy: and I would have them take notice, that on this occaſion, I have had no regard to the latitude of Venus, both to avoid the inconvenience of a more intricate calculation, which would render the concluſion leſs evident; and alſo becauſe the motion of the nodes of Venus is not yet diſcovered, nor can be determined but by ſuch conjunctions of the planet with the Sun as this is. For we conclude, that Venus will paſs 4 minutes below the Sun's center, only in conſequence of the ſuppoſition that the plane of Venus's orbit is immoveable in the ſphere of the fixed ſtars, and that it's nodes remain in the ſame places where they were found in the year 1639. But if Venus, in the year 1761, ſhould move over the Sun in a path more to the ſouth, it will be manifeſt that her nodes have moved backward among the fixed ſtars; and if more to the north, that they have moved forward; and that at the rate of 5½ minutes of a degree in 100 Julian years, for every minute that Venus's path ſhall be more or leſs diſtant than the aboveſaid 4 minutes from the Sun's center. And the difference between the durations of theſe eclipſes will be ſomewhat leſs than 17 minutes of time, on account of Venus's ſouth latitude; but greater, if by the motion of the nodes forward ſhe ſhould paſs on the north of the Sun's center.

But for the ſake of thoſe, who, though they are delighted with ſydereal obſervations, may not yet have made themſelves acquainted with the doctrine of parallaxes, I choſe to explain the thing a little more fully by a ſcheme, and alſo by a calculation ſomewhat more accurate.

Let us ſuppoſe that at *London*, in the year 1761, on the 6th of *June*, at 55 minutes after V in the morning, the Sun will be in Gemini 15° 37′, and therefore that at it's center the ecliptic is inclined toward the north, in an angle of 6° 10′: and that the viſible path of Venus on the Sun's diſc at that time declines to the ſouth, making an angle with the ecliptic of 8° 28′: then the path of Venus will alſo be inclined to the ſouth, with reſpect to the equator, interſecting the parallels of declination at an angle of 2° 18′*. Let us alſo ſuppoſe, that Venus, at the forementioned time, will be at her leaſt diſtance from the Sun's center, viz. only four minutes to the ſouth; and that every hour ſhe will deſcribe a ſpace of 4 minutes on the Sun, with a retrograde motion. The Sun's ſemidiameter will be 15′ 51″ nearly, and that of Venus 37″½. And let us ſuppoſe, for trial's ſake, that the difference of the horizontal parallaxes of Venus with the Sun (which we want) is 31″, ſuch as it comes out if the Sun's parallax be ſuppoſed 12″½. Then, on the center *C* (Plate XV. Fig. 2.) let the little circle *A B*, repreſenting the Earth's diſc, be deſcribed, and let it's ſemidiameter *C B* be 31″; and let the elliptic parallels of 22 and 56 degrees of north latitude (for the *Ganges* and *Port-Nelſon*) be drawn within it, in the manner now uſed by Aſtronomers for conſtructing ſolar eclipſes. Let *B C g* be the meridian in which the Sun is, and to this, let the right line *F H G*, repreſenting the path of Venus, be inclined at an angle of 2° 18′; and let it be diſtant from the center *C* 240 ſuch parts, whereof *C B* is 31. From *C* let fall the right line *C H*, perpendicular to *F G*; and ſuppoſe Venus to be at *H* at 55 minutes after V in the morning. Let the right line *F H G* be divided into the horary ſpaces III IV, IV V, V VI, &c. each equal to *C H*; that is, to 4 minutes of a degree. Alſo, let the right line *L M* be equal to the difference of the apparent ſemidiameters of the Sun and Venus, which is 15′ 13″$\frac{1}{2}$; and a circle being deſcribed with the radius *L M*, on a center taken in any point within the little circle *A B* repreſenting the Earth's diſc, will meet the right line *F G* in a point denoting the time at *London* when Venus ſhall touch the Sun's limb internally as ſeen from the place of the Earth's ſurface that anſwers to the point aſſumed in the Earth's diſc. And if a circle be deſcribed on the center *C*, with the radius *L M*, it will meet the right line *F G* in the points *F* and *G*; and the ſpaces *F H* and *G H* will be each equal to 14′ 4″, which ſpace Venus will appear to paſs over in 3 hours 40 minutes of time at *London*; therefore, *F* will fall in II hours 15 minutes, and *G* in IX hours 35 minutes in the morning. Whence it is manifeſt, that if the magnitude of the Earth, on account of it's immenſe diſtance, ſhould vaniſh as it were into a point; or, if being deprived of a diurnal motion, it ſhould always have the Sun vertical to the ſame point *C*; the whole duration of this eclipſe would be 7 hours 20 minutes. But the Earth in that time being whirled through 110 degrees of longitude, with a motion contrary to the motion of Venus, and conſequently the abovementioned duration being contracted, ſuppoſe 12 minutes, it will come out 7 hours 8 minutes, or 107 degrees, nearly.

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* This was an overſight in the Doctor, occaſioned by his placing both the Earth's axis *B C g* (Fig. 2. of Plate XV.) and the axis of Venus's orbit *C H* on the ſame ſide of the axis of the ecliptic *C K*; the former making an angle of 6° 10′ therewith, and the latter an angle of 8° 28′; the difference of which angles is only 2° 18′. But the truth is, that the Earth's axis, and the axis of Venus's orbit, will then lie on different ſides of the axis of the ecliptic, the former making an angle of 6° therewith, and the latter an angle of 8°½. Therefore, the ſum of theſe angles, which is 14°½ (and not their difference 2° 18′) is the inclination of Venus's viſible path to the equator and parallels of declination.

Now, Venus will be at *H*, at her leaſt diſtance from the Sun's center, when in the meridian of the eaſtern mouth of the *Ganges*, where the altitude of the pole is about 22 degrees. The Sun therefore will be equally diſtant from the meridian of that place, at the moments of the ingreſs and egreſs of the planet, viz. 53$\frac{1}{2}$ degrees; as the points *a* and *b* (repreſenting that place in the Earth's diſc *A B*) are, in the greater parallel, from the meridian *B C g*. But the diameter *e f* of that parallel will be to the diſtance *a b*, as the ſquare of the radius to the rectangle under the ſines of 53$\frac{1}{2}$ and 68 degrees;

grees; that is, as 1′ 2″ to 46″ 13‴. And by a good calculation (which, that I may not tire the reader, it is better to omit) I find, that a circle deſcribed on *a* as a center, with the radius *LM*, will meet the right line *FH* in the point *M*, at II hours 20 minutes 40 ſeconds; but that being deſcribed round *b* as a center, it will meet *HG* in the point *N* at IX hours 29 minutes 22 ſeconds, according to the time reckoned at *London:* and therefore, Venus will be ſeen entirely within the Sun at the banks of the *Ganges* for 7 hours 8 minutes 42 ſeconds: we have then rightly ſuppoſed, that the duration will be 7 hours 8 minutes, ſince the part of a minute is here of no conſequence.

But adapting the calculation to *Port-Nelſon*, I find, that the Sun being about to ſet, Venus will enter his diſc; and immediately after his riſing ſhe will leave the ſame. That place is carried in the intermediate time through the hemiſphere oppoſite to the Sun, from *c* to *d*, with a motion conſpiring with the motion of Venus; and therefore, the ſtay of Venus on the Sun will be about 4 minutes longer, on account of the parallax; ſo that it will be at leaſt 7 hours 24 minutes, or 111 degrees of the equator. And ſince the latitude of the place is 56 degrees, as the ſquare of the radius is to the rectangle contained under the ſines 55½ and 34 degrees, ſo is *AB*, which is 1′ 2″, to *cd*, which is 28″ 33‴. And if the calculation be juſtly made, it will appear, that a circle deſcribed on *c* as a center, with the radius *LM*, will meet the right line *FH* in *O*, at II hours 12 minutes 45 ſeconds; and that ſuch a circle, deſcribed on *d* as a center, will meet *HG* in *P*, at IX hours 36 minutes 37 ſeconds; and therefore the duration at *Port-Nelſon* will be 7 hours 23 minutes 52 ſeconds, which is greater than at the mouth of the *Ganges*, by 15 minutes 10 ſeconds of time. But if Venus ſhould paſs over the Sun without having any latitude, the difference would be 18 minutes 40 ſeconds; and if ſhe ſhould paſs 4′ north of the Sun's center, the difference would amount to 21 minutes 40 ſeconds, and will be ſtill greater, if the planet's north latitude be more increaſed.

From the foregoing hypotheſis it follows, that at *London*, when the Sun riſes, Venus will have entered his diſc; and that, at IX hours 37 minutes in the morning, ſhe will touch the limb of the Sun internally in going off; and laſtly, that ſhe will not entirely leave the Sun till IX hours 56 minutes.

It likewiſe follows from the ſame hypotheſis, that the center of Venus ſhould juſt touch the Sun's northern limb in the year 1769, on the third of *June*, at XI o'clock at night. So that, on account of the parallax, it will appear in the northern parts of *Norway* entirely within the Sun, which then does not ſet to thoſe parts; whilſt, on the coaſts of *Peru* and *Chili*, it will ſeem to travel over a ſmall portion of the diſc of the ſetting Sun; and over that of the riſing Sun at the *Molucca Iſlands*, and in their neighbourhood.—But if the nodes of Venus be found to have a retrograde motion (as there is ſome reaſon to believe from ſome later obſervations they have) then Venus will be ſeen every where within the Sun's diſc; and will afford a much better method for finding the Sun's parallax, by almoſt the greateſt difference in the duration of theſe eclipſes that can poſſibly happen.

But how this parallax may be deduced from obſervations made ſomewhere in the *Eaſt-Indies*, in the year 1761, both of the ingreſs and egreſs of Venus, and compared with thoſe made in it's going off with us; namely, by applying the angles of a triangle given in ſpecie to the circumference of three equal circles; ſhall be explained on ſome other occaſion.

ARTICLE IV.

Shewing that the whole method propoſed by the Doctor cannot be put in practice, and why.

27. In the above Diſſertation, the Doctor has explained his method with great modeſty, and even with ſome doubtfulneſs with regard to it's full ſucceſs. For he tells us, that the Sun's parallax may only be determined within it's five hundredth part thereby, provided it be not leſs than $12''\frac{1}{2}$; that there may be a good obſervation made at *Port-Nelſon*, as well as about the banks of the *Ganges*; and that Venus does not paſs more than 4 minutes of a degree below the center of the Sun's diſc.—He has taken all proper pains not to raiſe our expectations too high, and yet, from his well-known abilities, and character as a great Aſtronomer, it ſeems mankind in general have laid greater ſtreſs upon his method, than he ever deſired them to do. Only, as he was convinced it was the beſt method by which this important problem can ever be ſolved, he recommended it warmly for that reaſon. He had not then made a ſufficient number of obſervations, whereby to determine, with certainty, whether the nodes of Venus's orbit have any motion at all; or, if they have, whether it be backward or forward with reſpect to the ſtars. And conſequently, having not then made his own tables, he was obliged to calculate from the beſt that he could find. But thoſe tables allow of no motion to Venus's nodes, and alſo reckon her conjunction with the Sun to be about half an hour too late.

28. But more modern obſervations prove, that the nodes of Venus's orbit have a motion, backward, or contrary to the order of the ſigns, with reſpect to the fixed ſtars. And this motion is allowed for, in the Doctor's tables, a great part whereof were made from his own obſervations.

And it appears by theſe tables, that Venus will be ſo much farther paſt her deſcending node at the time of this tranſit, than ſhe was paſt her aſcending node at her tranſit in *November* 1639, that inſtead of paſſing only 4 minutes of a degree below the Sun's center in this, ſhe will paſs almoſt 10 minutes of a degree below it: on which account, the line of her tranſit will be ſo much ſhortened, as will make her paſſage over the Sun's diſc about an hour and 20 minutes leſs than if ſhe paſſed only 4 minutes below the Sun's center, at the middle of her tranſit. And therefore, her parallax from the the Sun will be ſo much diminiſhed, both at the beginning and end of her tranſit, and at all places from which the whole of it will be ſeen, that the difference of it's durations, as ſeen from them, and as ſuppoſed to be ſeen from the Earth's center, will not amount to 11 minutes of time.

29. But this is not all: for although the tranſit will begin before the Sun ſets to *Port-Nelſon*, it will be quite over before he riſes to that place next morning, on account of it's ending ſo much ſooner than as given by the tables to which the Doctor was obliged to truſt. So that we are quite deprived of the advantage that otherwiſe would have ariſen from obſervations made at *Port-Nelſon.*

30. In order to trace this affair through all it's intricacies, and to render it as intelligible to the reader as I can, there will be an unavoidable neceſſity of dwelling much longer upon it than I could otherwiſe wiſh. And as it is impoſſible to lay down truly the parallels of latitude, and the ſituations of places at particular times, in ſuch a ſmall diſc of the Earth as muſt be projected in ſuch a ſort of diagram as the Doctor has given, ſo as to meaſure thereby the exact times of the beginning and ending of the tranſit at any given place, unleſs the Sun's diſc be made at leaſt 30 inches diameter in the projection; and to which the Doctor did not quite truſt without making ſome calculations; I

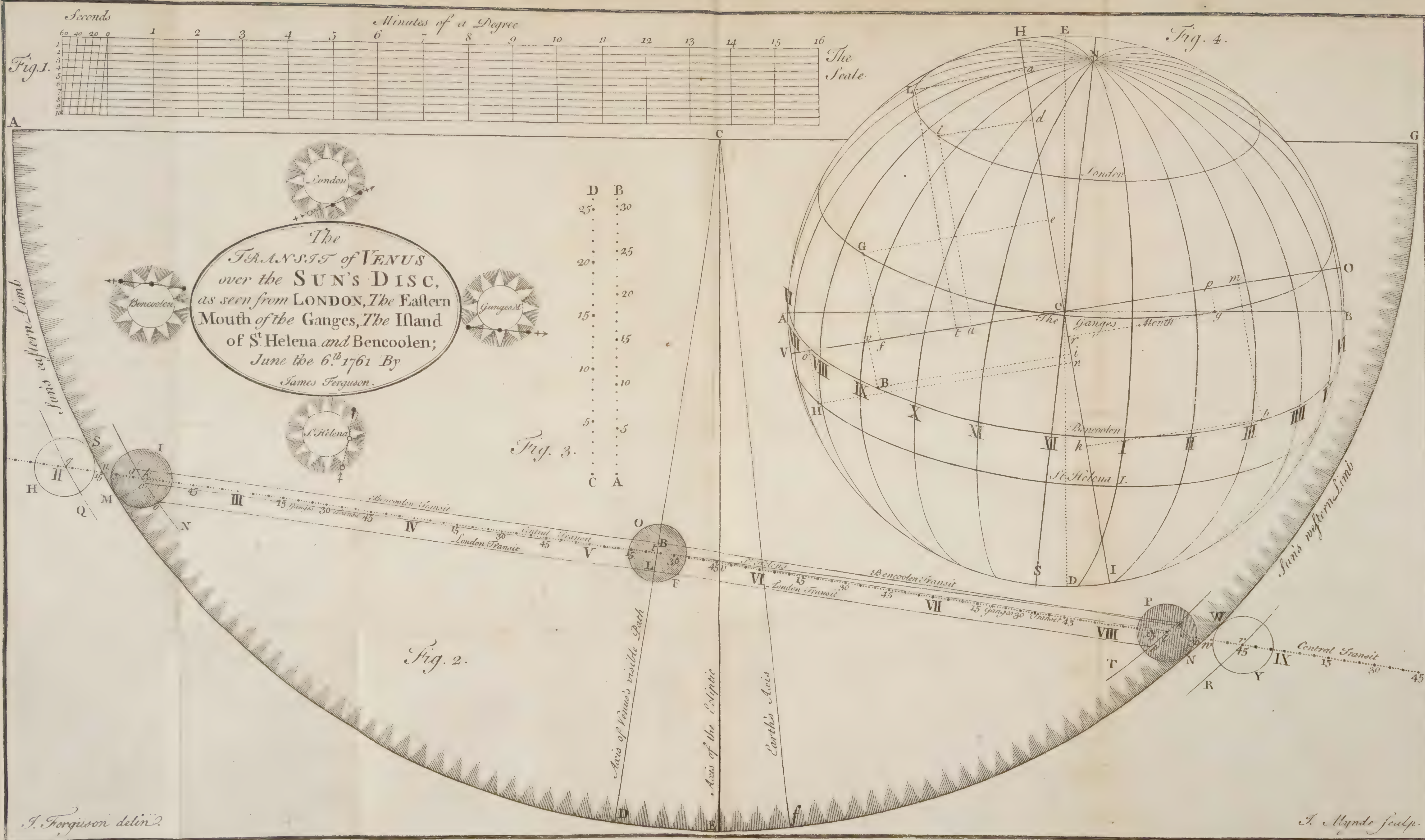
ſhall take a different method, in which the Earth's diſc may be made as large as the operator pleaſes: but if he makes it only 6 inches in diameter, he may meaſure the quantity of Venus's parallax from the Sun upon it, both in longitude and latitude, to the fourth part of a ſecond, for any given time and place; and then, by an eaſy calculation in the common rule of three, he may find the effect of the parallaxes on the duration of the tranſit. In this, I ſhall firſt ſuppoſe with the Doctor, that the Sun's horizontal parallax is $12''\frac{1}{2}$; and conſequently, that Venus's horizontal parallax from the Sun is $31''$. And after projecting the tranſit, ſo as to find the total effect of the parallax upon it's duration, I ſhall next ſhew how nearly the Sun's real parallax may be found from the obſerved intervals between the times of Venus's egreſs from the Sun, at particular places of the Earth; which is the method now taken both by the *Engliſh* and *French* Aſtronomers, and is a ſurer way whereby to come at the real quantity of the Sun's parallax, than by obſerving how much the whole contraction of duration of the tranſit is, either at *Bencoolen*, *Batavia*, or *Pondicherry*.

ARTICLE V.

Shewing how to project the tranſit of Venus on the Sun's diſc, as ſeen from different places of the Earth; ſo as to find what it's viſible duration muſt be at any given place, according to any aſſumed parallax of the Sun; and from the obſerved intervals between the times of Venus's egreſs from the Sun at particular places, to find the Sun's true horizontal parallax.

31. The elements for this projection are as follows:

I. The true time of conjunction of the Sun and Venus; which, as ſeen from the Earth's center, and reckoned according to the equal time at *London*,


The
Transit of Venus
over the Sun's Disc,
as seen from London, The Eastern
Mouth of the Ganges, The Island
of St Helena and Bencoolen;
June the 6th 1761 By
James Ferguson.
Fig. 1.
Seconds
Minutes of a Degree
60 40 20 0
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16
The Scale
Fig. 2.
Fig. 3.
Fig. 4.
London
Bencoolen
Ganges M.
St Helena
Sun's eastern Limb
Sun's western Limb
Bencoolen Transit
Ganges Transit
Central Transit
London Transit
St Helena
Axis of Venus's visible Path
Axis of the Ecliptic
Earth's Axis
The Ganges Mouth
London
Bencoolen
St Helena
I. II. III. IV. V. VI. VII. VIII. IX. X. XI.
A
B
C
D
E
F
G
H
I
L
M
N
O
P
Q
R
S
T
V
W
Y
J. Fergison delin.
J. Mynde sculp.

London, is on the 6th of *June* 1761, at 46 minutes 17 ſeconds after V in the morning, according to Dr. HALLEY's tables.

II. The geocentric latitude of Venus at that time, 9′ 43″ ſouth.

III. The Sun's ſemidiameter, 15′ 50″.

IV. The ſemidiameter of Venus (from the Doctor's Diſſertation) 37″½.

V. The difference of the ſemidiameters of the Sun and Venus, 15′ 12″½.

VI. Their ſum, 16′ 27″½.

VII. The viſible angle which the tranſit-line makes with the ecliptic, 8° 31′; the angular point (or deſcending node) being 1° 6′ 18″ eaſtward from the Sun, as ſeen from the Earth; the deſcending node being in ♐ 14° 29′ 37″, as ſeen from the Sun; and the Sun in ♊ 15° 35′ 55″, as ſeen from the Earth.

VIII. The angle which the axis of Venus's viſible path makes with the axis of the ecliptic, 8° 31′; the ſouthern half of that axis being on the left hand (or eaſtward) of the axis of the ecliptic, as ſeen from the northern hemiſphere of the Earth, which would be to the right hand, as ſeen from the Sun.

IX. The angle which the Earth's axis makes with the axis of the ecliptic, as ſeen from the Sun, 6°; the ſouthern half of the Earth's axis lying to the right hand of the axis of the ecliptic, in the projection; which would be to the left hand as ſeen from the Sun.

X. The angle which the Earth's axis makes with the axis of Venus's viſible path, 14° 31′; viz. the ſum of N° VIII and IX.

XI. The true motion of Venus on the Sun, given by the tables as if it were ſeen from the Earth's center, 4 minutes of a degree in 60 minutes of time.

32. Theſe elements being collected, make a ſcale of any convenient length, as that of Fig. 1. in Plate XVI. and divide it into 17 equal parts, each whereof ſhall be taken for a minute of a degree; then, divide the minute next to the left hand into 60 equal parts for ſeconds, by diagonal lines, as in the figure. The reaſon for dividing the ſcale into 17 parts or minutes is, becauſe the ſum of the ſemidiameters of the Sun and Venus exceeds 16 minutes of a degree. See N° VI.

33. Draw the right line *ACG* (Fig. 2.) for a ſmall part of the ecliptic, and perpendicular thereto draw the right line *CvE* for the axis of the ecliptic on the ſouthern half of the Sun's diſc.

34. Take the Sun's ſemidiameter, 15′ 50″, from the ſcale with your compaſſes; and with that extent, as a radius, ſet one foot in *C* as a center, and deſcribe the ſemicircle *AEG* for the ſouthern half of the Sun's diſc; becauſe the tranſit is on that half of the Sun.

35. Take the geocentric latitude of Venus, 9′ 43″, from the ſcale with your compaſſes; and ſet that extent from *C* to *v*, on the axis of the ecliptic: and the point *v* ſhall be the place of Venus's center on the Sun, at the tabular moment of her conjunction with the Sun.

36. Draw the right line *CBD*, making an angle of 8° 31′ with the axis of the ecliptic, toward the left hand; and this line ſhall repreſent the axis of Venus's geocentric viſible path on the Sun.

37. Through the point of the conjunction *v*, in the axis of the ecliptic, draw the right line *qtr* for the geocentric viſible path of Venus over the Sun's diſc, at right angles to *CBD*, the axis of her orbit, which axis will divide the line of her path into two equal parts *qt* and *tr*.

38. Take Venus's horary motion on the Sun, 4′, from the ſcale with your compaſſes; and with that extent make marks along the tranſit-line *qtr*. The equal ſpaces, from mark to mark, ſhew how

much of that line Venus moves through in each hour, as ſeen from the Earth's center, during her continuance on the Sun's diſc.

39. Divide each of theſe horary ſpaces, from mark to mark, into 60 equal parts for minutes of time; and ſet the hours to the proper marks in ſuch a manner, that the true time of conjunction of the Sun and Venus, 46¼ minutes after V in the morning, may fall into the point *v*, where the tranſit-line cuts the axis of the ecliptic. So the point *v* ſhall denote the place of Venus's center on the Sun, at the inſtant of her ecliptical conjunction with the Sun, and *t* (in the axis *C t D* of her orbit) will be the middle of her tranſit; which is at 24 minutes after V in the morning, as ſeen from the Earth's center, and reckoned by the equal time at *London*.

40. Take the difference of the ſemidiameters of the Sun and Venus, 15′ 12″½, in your compaſſes from the ſcale; and with that extent, ſetting one foot in the Sun's center *C*, deſcribe the arcs *N* and *T* with the other, croſſing the tranſit-line in the points *k* and *l*; which are the points on the Sun's diſc that are hid by the center of Venus at the moments of her two internal contacts with the Sun's limb or edge, at *M* and *N*: the former of theſe is the moment of Venus's total ingreſs on the Sun, as ſeen from the Earth's center, which is at 28 minutes after II in the morning, as reckoned at *London*; and the latter is the moment when her egreſs from the Sun begins, as ſeen from the Earth's center, which is 20 minutes after VIII in the morning at *London*. The interval between theſe two contacts is 5 hours 52 minutes.

41. The central ingreſs of Venus on the Sun is the moment when her center is on the Sun's eaſtern limb at *u*, which is at 15 minutes after II in the morning; and her central egreſs from the Sun is the moment when her center is on the Sun's weſtern limb at *w*; which is at 33 minutes after VIII in

the morning, as ſeen from the Earth's center, and reckoned according to the time at *London*. The interval between theſe times is 6 hours 18 minutes.

42. Take the ſum of the ſemidiameters of the Sun and Venus, 16′ 27″$\frac{1}{2}$, in your compaſſes from the ſcale; and with that extent, ſetting one foot in the Sun's center *C*, deſcribe the arcs *Q* and *R* with the other, cutting the tranſit-line in the points *q* and *r*, which are the points in open ſpace (clear of the Sun) where the center of Venus is, at the moments of her two external contacts with the Sun's limb at *S* and *W*; or the moments of the beginning and ending of the tranſit, as ſeen from the Earth's center; the former of which is at 3 minutes after II in the morning at *London*, and the latter at 45 minutes after VIII. The interval between theſe moments is 6 hours 42 minutes.

43. Take the ſemidiameter of Venus, 37″$\frac{1}{2}$, in your compaſſes from the ſcale; and with that extent as a radius, on the points *q*, *k*, *t*, *l*, *r*, as centers, deſcribe the circles *HS*, *MI*, *OF*, *PN*, *WY*, for the diſc of Venus, at her firſt contact at *S*, her total ingreſs at *M*, her place on the Sun at the middle of her tranſit, her beginning of egreſs at *N*, and her laſt contact at *W*.

44. Thoſe who have a mind to project the Earth's diſc on the Sun, round the center *C*, and to lay down the parallels of latitude and ſituations of places thereon, according to Dr. HALLEY's method, may draw *Cf* for the axis of the Earth, produced to the ſouthern edge of the Sun at *f*; and making an angle *ECf* of 6° with the axis of the ecliptic *CE*: but he will find it very difficult and uncertain to mark the places on that diſc, unleſs he makes the Sun's ſemidiameter *AC* 15 inches at leaſt: otherwiſe the line *Cf* is of no uſe at all in this projection.—The following method is better.

45. In Fig. 3. of Plate XVI. make the line *AB* of any convenient length, and divide it into 31 equal parts, each whereof ſhall be taken for a ſecond

of Venus's parallax either from or upon the Sun (her horizontal parallax from the Sun being ſuppoſed to be 31′;) and taking the whole length *AB* in your compaſſes, ſet one foot in *C* (Fig. 4.) as a center, and deſcribe the circle *AEBD* for the Earth's enlightened diſc, whoſe diameter is 62″, or double the horizontal parallax of Venus from the Sun. In this diſc, draw *ACB* for a ſmall part of the ecliptic, and at right angles thereto draw *ECD* for the axis of the ecliptic. Draw alſo *NCS* both for the Earth's axis and univerſal ſolar meridian, making an angle of 6° with the axis of the ecliptic, as ſeen from the Sun; *HCI* for the axis of Venus's orbit, making an angle of 8° 31′ with *ECD*, the axis of the ecliptic; and laſtly, *VCO* for a ſmall part of Venus's orbit, at right angles to it's axis.

46. This figure repreſents the Earth's enlightened diſc, as ſeen from the Sun at the time of the tranſit. The parallels of latitude of *London*, the eaſtern mouth of the *Ganges*, *Bencoolen*, and the iſland of *St. Helena*, are laid down in it, in the ſame manner as they would appear to an obſerver on the Sun, if they were really drawn in circles on the Earth's ſurface (like thoſe on a common terreſtrial globe) and could be viſible at ſuch a diſtance.—The method of delineating theſe parallels is the ſame as already deſcribed in the XIXth Chapter, for the conſtruction of ſolar eclipſes.

47. The points where the curve-lines (called hour-circles) XI *N*, X *N*, &c. cut the parallels of latitude, or paths of the four places above-mentioned, are the points at which the places themſelves would appear in the diſc, as ſeen from the Sun, at theſe hours reſpectively. When either place comes to the ſolar meridian *NCS* by the Earth's rotation on it's axis, it is noon at that place; and the difference, in abſolute time, between the noon at that place and the noon at any other place, is in proportion to the difference of longitude of of theſe two places, reckoning one hour for every 15 de-

15 degrees of longitude, and 4 minutes for each degree: adding the time if the longitude be eaſt, but ſubtracting it if the longitude be weſt.

48. The diſtance of either of theſe places from *HCI* (the axis of Venus's* orbit) at any hour or part of an hour, being meaſured upon the ſcale *AB* in Fig. 3. will be equal to Venus's parallax in longitude, either on or from the Sun; and this parallax, being always contrary to the poſition of the place, is eaſtward as long as the place keeps on the left hand of the axis of the ecliptic, as ſeen from the Sun; and weſtward when the place gets to the right hand of the axis of the ecliptic. So that, to all the places which are poſited in the hemiſphere *HVI* of the diſc, at any given time, Venus has an eaſtern parallax of longitude; but when the Earth's diurnal motion carries the ſame places into the hemiſphere *HOI*, the parallax of Venus is weſtward.

49. When Venus has a parallax toward the eaſt, as ſeen from any given place on the Earth's ſurface, either at the time of her total ingreſs or beginning of egreſs, as ſeen from the Earth's center; add the time anſwering to this parallax to the time of ingreſs or egreſs at the Earth's center, and the ſum will be the time thereof, as ſeen from the given place on the Earth's ſurface: but when the parallax is weſtward, ſubtract the time anſwering thereto from the time of total ingreſs or beginning of egreſs as ſeen from the Earth's center, and the remainder will be the time as ſeen from the given place on the ſurface, ſo far as it is affected by this

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* In the former Edition of this, I made a miſtake in taking the parallax in longitude in a line from the given place to the axis of the ecliptic, and perpendicular thereto; and the parallax in latitude from the given place to the plane of the ecliptic, and perpendicular thereto.—But in this edition, theſe errors are corrected; which make ſome ſmall differences in the quantities of the parallaxes, and in the times depending thereon; as will appear by comparing them in this with thoſe in the former edition.

parallax.—The reaſon of this is plain to every one who conſiders, that an eaſtern parallax keeps the planet back, and a weſtern parallax carries it forward, with reſpect to its true place or poſition, at any inſtant of time, as ſeen from the Earth's center.

50. The neareſt diſtance of any given place from *VCO*, the plane of Venus's orbit at any hour or part of an hour, being meaſured on the ſcale *AB* in Fig. 3, will be equal to Venus's parallax in latitude, which is northward from the true line of her path on the Sun as ſeen from the Earth's center, if the given place be on the ſouth ſide of the plane of her orbit *VCO* on the Earth's diſc; and the contrary, if the given place be on the north ſide of that plane; that is, the parallax is always contrary to the ſituation of the place on the Earth's diſc, with reſpect to the plane of Venus's orbit thereon.

51. As the line of Venus's tranſit is on the ſouthern hemiſphere of the Sun's diſc, it is plain that a northern parallax in her latitude will cauſe her to deſcribe a longer line on the Sun, than if ſhe had no ſuch parallax; and a ſouthern parallax in latitude will cauſe her to deſcribe a ſhorter line on the Sun, than if ſhe had no ſuch parallax.—And the longer this line is, the ſooner will her total ingreſs be, and the later will be her beginning of egreſs; and juſt the contrary, if the line be ſhorter.—But, to all places ſituated on the north ſide of the plane of her orbit, in the hemiſphere *VHO*, the parallax of latitude is ſouth; and to all places ſituated on the ſouth ſide of the plane of her orbit, in the hemiſphere *VIO*, the parallax of latitude is north. Therefore, the line of the tranſit will be ſhorter to all places in the hemiſphere *VHO*, than it will be as ſeen from the Earth's center, where there is no parallax at all; and longer to all places in the hemiſphere *VIO*. So that the time anſwering to this parallax muſt be added to the time of total ingreſs as ſeen from the Earth's center, and ſubtracted from

the beginning of egreſs as ſeen from the Earth's center, in order to have the true time of total ingreſs and beginning of egreſs as ſeen from places in the hemiſphere *VHO*: and juſt the reverſe for places in the hemiſphere *VIO*.—It was proper to mention theſe circumſtances, for the reader's more eaſily conceiving the reaſon of applying the times anſwering to the parallaxes of longitude and latitude in the ſubſequent part of this article: for it is their ſum in ſome caſes, and their difference in others, which being applied to the times of total ingreſs and beginning of egreſs as ſeen from the Earth's center, that will give the times thereof as ſeen from the given places on the Earth's ſurface.

52. The angle which the Sun's ſemidiameter ſubtends, as ſeen from the Earth, at all times of the year, has been ſo well aſcertained by late obſervations, that we can make no doubt of it's being 15 50″ on the day of the tranſit; and Venus's latitude has alſo been ſo well aſcertained at many different times of late, that we have very good reaſon to believe it will be 9′ 43″ ſouth of the Sun's center, at the time of her conjunction with the Sun.—If then, her ſemidiameter at that time be 37″$\frac{1}{2}$ (as mentioned by Dr. HALLEY) it appears by the projection (Fig. 2.) that her total ingreſs on the Sun as ſeen from the Earth's center, will be at 28 minutes after II in the morning (§ 40.) and her beginning of egreſs from the Sun will be 20 minutes after VIII, according to the time reckoned at *London*.

53. As the total ingreſs will not be viſible at *London*, we ſhall not here trouble the reader about Venus's parallax at that time.—But by projecting the ſituation of *London* on the Earth's diſc (Fig. 4.) for the time when the egreſs begins, we find it will then be at *l*, as ſeen from the Sun.

Draw *ld* parallel to Venus's orbit *VCO*, and *lu* perpendicular to it: the former is Venus's eaſtern parallax in longitude at her beginning of egreſs, and the latter is her ſouthern parallax in latitude at that time. Take theſe in your compaſſes, and meaſure them on the ſcale *AB* (Fig. 3.) and you will find the parallax in longitude to be $10''\frac{3}{4}$, and the parallax in latitude to be $21''\frac{1}{2}$.

54. As Venus's true motion on the Sun is at the rate of 4 minutes of a degree in 60 minutes of time (*See* N° XI. *of* § 31.) ſay, as 4 minutes of a degree is to 60 minutes of time, ſo is $10''\frac{3}{4}$ of a degree to 2 minutes 41 ſeconds of time; which being added to VIII hours 20 minutes (becauſe this parallax is eaſtward, § 49.) gives VIII hours 22 minutes 41 ſeconds, for the beginning of egreſs at *London*, as affected only by this parallax.—But, as Venus has a ſouthern parallax of latitude at that time, her beginning of egreſs will be ſooner; for this parallax ſhortens the line of her viſible tranſit at *London*.

55. As this parallax of latitude is $21''\frac{1}{2}$ ſouth, add it to Venus's latitude $9'\ 43''$, and the ſum will be $10'\ 4''\frac{1}{2}$; which is to be taken from the ſcale in Fig. 1. and ſet from *C* to *L* in Fig. 2. And then, if a line be drawn parallel to *t l*, it will terminate at the point *p* in the arc *T*, where Venus's center will be at the beginning of her egreſs as ſeen from *London* *.—But as her center is at *l* when her egreſs begins as ſeen from the Earth's center, take *Lp* in your compaſſes, and ſetting that extent from *t* towards *l* on the central tranſit-line, you will find it to be 5 minutes ſhorter than *t l*: therefore ſubtract 5 minutes from VIII hours 22 minutes 41 ſeconds, and there will remain VIII hours 17 minutes 41 ſeconds for the viſible beginning of egreſs in the morning at *London*.

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* The reaſon why the lines *o L p*, *a B b*, *c t*, and *t b*, which are the viſible tranſits at *London*, the *Ganges* mouth, *Bencoolen*, and *St. Helena*, are not parallel to the central tranſit-line *k t l*, is, becauſe the parallaxes in latitude are different at the times of ingreſs and egreſs, as ſeen from each of theſe places. The method of drawing theſe lines will be ſhewn by and by.

56. At V hours 24 minutes (which is the middle of the tranſit as ſeen from the Earth's center) *London* will be at *L* on the Earth's diſc (Fig. 4.) as ſeen from the Sun. The parallax of longitude *L a* is then $12''\frac{1}{2}$; by which, working as above directed, we find the middle of the tranſit, as ſeen from *London*, to be at V hours 20 minutes 53 ſeconds.—This is not affected by the parallax of latitude *L t*.—But *L t* meaſures 27″ on the ſcale *AB* (Fig. 3.) therefore take 27″ from the ſcale in Fig. 1. and ſet it from *t* to *L*, on the axis of Venus's path in Fig. 2. and laying a ruler to the point *L*, and the above-found point of egreſs *p*, draw *o L p* for the line of the tranſit as ſeen from *London*.

57. The eaſtern mouth of the river *Ganges* is 89 degrees eaſt from the meridian of *London*; and therefore, when the time at *London* is 28 minutes after II in the morning (§ 40.) it is 24 minutes paſt VIII in the morning (by § 47.) at the mouth of the *Ganges*; and when it is 20 minutes paſt VIII in the morning at *London* (§ 40.) it is 16 minutes paſt II in the afternoon at the *Ganges*. Therefore, by projecting that place upon the Earth's diſc, as ſeen from the Sun, it will be at *G* (in Fig. 4.) at the time of Venus's total ingreſs, as ſeen from the Earth's center, and at *g* when her egreſs begins.

Draw *G e* and *g r* parallel to the orbit of Venus *VCO*, and meaſure them on the ſcale *AB* in Fig. 3. the former will be 21″ for Venus's eaſtern parallax in longitude, at the above-mentioned time of her total ingreſs, and the latter will be $16''\frac{1}{4}$ for her weſtern parallax in longitude at the time when her egreſs begins.—The former parallax gives 5 minutes 15 ſeconds of time (by the analogy in § 54.) to be added to VIII hours 24 minutes, and the latter parallax gives 4 minutes 11 ſeconds to be ſubtracted from II hours 16 minutes; by which we have VIII hours 29 minutes 15 ſeconds, for the time of total ingreſs as ſeen from the banks of the *Ganges*, and II hours 11 minutes 49 ſeconds for the beginning of egreſs, as affected by theſe parallaxes.

Draw *G f* perpendicular to Venus's orbit *V O C*, and by meaſurement on the ſcale *A B* (Fig. 3.) it will be found to contain 10″; which being taken from the ſcale in Fig. 1. and ſet off ſouthward from the point of total ingreſs *k* (Fig. 2. as ſeen from the Earth's center) parallel to the axis of Venus's path, it will fall into the point *c* on the arc *N*.—Draw *C t*, and taking the extent *t c* in your compaſſes, and applying it from *t* towards *k*, you will find it to fall a minute ſhort of *k*; which ſhews, that Venus's parallax in latitude ſhortens the beginning of the line of her viſible tranſit at the *Ganges* by one minute of time. Therefore, as this makes the viſible ingreſs a minute later, add one minute to the above VIII hours 29 minutes 15 ſeconds, and it will give VIII hours 30 minutes 15 ſeconds for the time of total ingreſs, in the morning, as ſeen from the eaſtern mouth of the *Ganges*. At the beginning of egreſs, the parallax of latitude *g p* is 2″½ (by meaſurement of the ſcale *AB*) which will protract the beginning of egreſs by about 30 ſeconds of time, and muſt therefore be added to the above II hours 11 minutes 49 ſeconds, which will make the viſible beginning of egreſs to be at II hours 12 minutes 19 ſeconds in the afternoon.

58. *Bencoolen* is 102 degrees eaſt from the meridian of *London*; and therefore, when the time is 28 minutes paſt II in the morning at *London*, it is 16 minutes paſt IX in the morning at *Bencoolen*; and when it is 20 minutes paſt VIII in the morning at *London*, it is 8 minutes paſt III in the afternoon at *Bencoolen*. Therefore, in Fig. 4. *Bencoolen* will be at *B* at the time of Venus's total ingreſs as ſeen the Earth's center; and at *b* when her egreſs begins.

Draw *B i* and *b k* parallel to Venus's orbit *V C O*, and meaſure them on the ſcale: the former will be found to be 22″ for Venus's eaſtern parallax in longitude at the time of her total ingreſs; and the latter to be 19″½ for her weſtern parallax in longitude when her egreſs begins, as ſeen from the Earth's center. The firſt of theſe parallaxes gives 5 minutes 30 ſeconds (by the analogy in § 54.) to be added to IX hours 16 minutes, and the latter parallax gives 4 minutes 52 ſeconds to be ſubtracted from III hours 8 minutes; whence we have IX hours 21 minutes 30 ſeconds for the time of total ingreſs at *Bencoolen*; and III hours and 3 minutes 8 ſeconds for the time when the egreſs begins there, as affected by theſe two parallaxes.

59. Draw *B v* and *b m* perpendicular to Venus's orbit *V C O*, and meaſure them on the ſcale *A B*: the former will be 5″ for Venus's northern parallax in latitude as ſeen from *Bencoolen* at the time of her total ingreſs; and the latter will be 15″½ for her northern parallax in latitude when her egreſs begins. Take theſe parallaxes from the ſcale in Fig. 1. in your compaſſes, and ſet them off above the central tranſit-line, perpendicular to the axis of Venus's path; the former from the left hand of *k* (Fig. 2.) to *a* in the arc *N*, and the latter from the right hand of *l* to *b* in the arc *T*; and draw *a B b* for the line of Venus's tranſit as ſeen from *Bencoolen*: the center of Venus being at *a*, as ſeen from *Bencoolen*, at the moment of her total ingreſs; and at *b* at the moment when her egreſs begins.

But as ſeen from the Earth's center, the center of Venus is at *k* in the former caſe, and at *l* in the latter: ſo that we find the line of the tranſit is longer as ſeen from *Bencoolen* than as ſeen from the Earth's center, which is the effect of Venus's northern parallax in latitude.—Take *B a* in your compaſſes, and ſetting that extent backward from *t* toward *g*, on the central tranſit-line, you will find it will reach two minutes beyond *k* thereon: and taking the extent *B b* in your compaſſes, and ſetting it forward from *t* towards *w*, on the central tranſit-line, it will be found to reach 3 minutes beyond *l* thereon. Conſequently, if we ſubtract 2 minutes from IX hours 21 minutes 30 ſeconds (above found) we have IX hours 19 minutes 30 ſeconds, in the morning, for the time of total ingreſs as ſeen from *Bencoolen:* and if we add 3 minutes to the above found III hours 3 minutes 8 ſeconds, we ſhall have III hours 6 minutes 8 ſeconds after noon, for the time when the egreſs begins as ſeen from *Bencoolen.*

60. The whole duration of the tranſit, from total ingreſs to beginning of egreſs, as ſeen from the Earth's center, is 5 hours 52 minutes (by § 40.) but the whole duration from total ingreſs to beginning of egreſs, as ſeen from *Bencoolen*, is only 5 hours 46 minutes 38 ſeconds; which is 5 minutes 22 ſeconds leſs than as ſeen from the Earth's center: and this 5 minutes 22 ſeconds is the whole effect of the parallaxes (both in longitude and latitude) on the duration of the tranſit at *Bencoolen.*

But the duration as ſeen at the mouth of the *Ganges*, from ingreſs to egreſs, is ſtill leſs; for it is only 5 hours 42 minutes 4 ſeconds: which is 9 minutes 56 ſeconds leſs than as ſeen from the Earth's center, and 4 minutes 34 ſeconds leſs than as ſeen at *Bencoolen.*

61. The iſland of *St. Helena* (to which only a ſmall part of the tranſit is viſible at the end) will be at *H* (as in Fig. 4.) when the egreſs begins as ſeen from the Earth's center. And ſince the middle of that iſland is 6° weſt from the meridian of *London*, and the ſaid egreſs begins when the time at *London* is 20 minutes paſt VIII in the morning, it will then be only 56 minutes paſt VII in the morning at *St. Helena.*

Draw Hn parallel to Venus's orbit VCO, and Ho perpendicular to it; and by meaſuring them on the ſcale AB (Fig. 3.) the former will be found to amount to 29″ for Venus's eaſtern parallax in longitude, as ſeen from *St. Helena*, when her egreſs begins as ſeen from the Earth's center; and the latter to be 6″ for her northern parallax in latitude at that time.

By the analogy in § 54, this parallax of longitude gives 10 minutes 2 ſeconds of time; which being added (on account of it's being eaſtward) to VII hours 56 minutes, gives VIII hours 6 minutes 2 ſeconds for the beginning of egreſs at *St. Helena*, as affected by this parallax.—But 6″ of parallax in latitude (applied as in the caſe of *Bencoolen)* lengthens out the end of the tranſit-line by 1 minute; which being added to VIII hours 6 minutes 2 ſeconds, gives VIII hours 7 minutes 2 ſeconds for the beginning of egreſs, as ſeen from *St. Helena*.

62. We ſhall now collect the above-mentioned times into a ſmall table, that they may be ſeen at once, as follows. *M* ſignifies morning, *A* afternoon.

		Total ingreſs.			Beg. of egreſs.			Duration.		
		H.	M.	S.	H.	M.	S.	H.	M.	S.
At	The Earth's center	II	28	0 *M.*	VIII	20	0 *M.*	5	52	0*
	London - - -	Inviſible. *M.*			VIII	17	41 *M.*	—	—	—
	The *Ganges* mouth	VIII	30	15 *M.*	II	12	19 *A.*	5	42	4
	Bencoolen - - -	IX	19	30 *M.*	III	6	8 *A.*	5	46	38
	St. Helena - - -	Inviſible *M.*			VIII	7	2 *M.*	—	—	—

63. The times at the three laſt-mentioned places are reduced to the meridian of *London*, by ſubtracting 5 hours 56 minutes from the times of ingreſs and egreſs at the *Ganges*; 6 hours 48 minutes from the times thereof at *Bencoolen*; and adding 24 minutes to the time of beginning of egreſs at

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* This duration, as ſeen from the Earth's center, is on ſuppoſition that the ſemidiameter of Venus will be found equal to $37''\frac{1}{2}$, on the Sun's diſc, as ſtated by Dr. *Halley* (ſee Art. V. § 31.) to which all the other durations are accommodated — But, from later obſervations, it his highly probable, that the ſemidiameter of Venus will be found not to exceed 30″ on the Sun; and if ſo, the duration between the two internal contacts, as ſeen from the Earth's center, will be 5 hours 58 minutes; and the durations, as ſeen from the above-mentioned places, will be lengthened very nearly in the ſame proportion.

St. Helena: and being thus reduced, they are as follows.

		Total ingreſs. H. M. S.	Beg. of egreſs, H. M. S.	
Times at *London* for	*Ganges* mouth	II 34 15 *M.*	VIII 16 19 *M.*	Durations as above.
	Bencoolen	II 31 30 *M.*	VIII 18 8 *M.*	
	St. Helena	Inviſible. *M.*	VIII 31 2 *M.*	

64. All this is on ſuppoſition, that we have the true longitudes of the three laſt-mentioned places, that the Sun's horizontal parallax is $12''\frac{1}{2}$, that the true latitude of Venus is given, and that her ſemidiameter will ſubtend an angle of $37''\frac{1}{2}$ on the Sun's diſc.

As for the longitudes, we muſt ſuppoſe them true, until the obſervers aſcertain them, which is a very important part of their buſineſs; and without which they can by no means find the interval of abſolute time that elapſeth between either the ingreſs or egreſs, as ſeen from any two given places: and there is much greater dependance to be had on this elapſe, than upon the whole contraction of duration at any given place, as it will undoubtedly afford a ſurer baſis for determining the Sun's parallax.

65. I have good reaſon to believe, that the latitude of Venus, as given in § 31, will be found by obſervation to be very near the truth; but that the time of conjunction there mentioned will be found to anticipate the true time by almoſt 5 minutes; that Venus's ſemidiameter will ſubtend an angle of no more than 30″ on the Sun's diſc; and that the middle of her tranſit, as ſeen from the Earth's center, will be at 29 minutes after V in the morning, as reckoned by the equal time at *London*.

66. Subtract VIII hours 17 minutes 41 ſeconds, the time when the egreſs begins at *London*, from VIII hours 31 minutes 2 ſeconds, the time reckoned at *London* when the egreſs begins at *St. Helena*, and there will remain 13 minutes 21 ſeconds (or 801

ſeconds) for their difference, or elapſe, in abſolute time, between the beginning of egreſs as ſeen from theſe two places.

Divide this elapſe of 801 ſeconds by the Sun's parallax 12″$\frac{1}{2}$; and the quotient will be 64 ſeconds and a ſmall fraction. So that for each ſecond of a degree in the Sun's horizontal parallax (ſuppoſing it to be 12$\frac{1}{2}$) there will be a difference or elapſe of 64 ſeconds of abſolute time between the beginning of egreſs as ſeen from *London*, and as ſeen from *St. Helena*: and conſequently 32 ſeconds of time for every half ſecond of the Sun's parallax; 16 ſeconds of time for every fourth part of a ſecond of the Sun's parallax; 8 ſeconds of time for the eighth part of a ſecond of the Sun's parallax; and full 4 ſeconds for a ſixteenth part of the Sun's parallax.

For, in ſuch a ſmall angle as that of the Sun's parallax, the arc is equal both to it's ſine and to it's tangent: and therefore, the quantity of this parallax is in direct proportion to the abſolute difference in the time of egreſs ariſing from it, at different parts of the Earth.

67. Therefore, when this difference is aſcertained by good obſervations, made at different places, and compared together, the true quantity of the Sun's parallax will be very nearly determined. For, ſince it may be preſumed that the beginning of egreſs can be obſerved within 2 ſeconds of it's real time, the Sun's parallax may be then found within the 32d part of a ſecond of it's true quantity; and conſequently, his diſtance may be found within a 400th part of the whole, provided his parallax be not leſs that 12″$\frac{1}{2}$; for 32 times 12$\frac{1}{2}$ is 400.

68. But ſince Dr. HALLEY has aſſured us, that he had obſerved the two internal contacts of the planet Mercury with the Sun's edge ſo exactly, as not to err one ſecond in the time thereof, we may well imagine that the internal contacts of Venus with the Sun may be obſerved with as

great accuracy. So that we may hope to have the abſolute interval between the moments of her beginning of egreſs, as ſeen from *London* and from *St. Helena*, true to a ſecond of time; and if ſo, the Sun's parallax may be determined to the 64th part of a ſecond, provided it be not leſs than 12″½; and conſequently his diſtance may be found, within it's 800th part, for 64 times 12½ is 800: which is ſtill nearer the truth than Dr. HALLEY expected it might be found, by obſerving the whole duration of the tranſit in the *Eaſt-Indies* and at *Port-Nelſon*. So that our preſent Aſtronomers have judiciouſly reſolved to improve the Doctor's method, by taking only the interval between the abſolute times of it's ending at different places. If the Sun's parallax be greater or leſs than 12″½, the elapſe or difference of abſolute time between the beginning of egreſs at *London* and *St. Helena* will be found by obſervation to be greater or leſs than 801 ſeconds accordingly.

69. There will alſo be a great difference between the abſolute times of egreſs at *St. Helena* and the northern parts of *Ruſſia*, which would make theſe places very proper for obſervation. The difference between them at *Tobolſk* in *Siberia* and at *St. Helena* will be 11 minutes, according to DE L'ISLE's map: at *Archangel* it will be but about 40 ſeconds leſs than at *Tobolſk*; and only a minute and a quarter leſs at *Peterſburgh*, even if the Sun's parallax be no more than 10″½. At *Wardhus* the ſame advantage would nearly be gained as at *Tobolſk*: but if the obſervers could go ſtill farther to the eaſt, as to *Yakoutſk* in *Siberia*, the advantage would be ſtill greater; for, as Mr. DE L'ISLE very juſtly obſerves, in a memoir preſented to the *French* king with his map of the tranſit, the difference of time between Venus's egreſs from the Sun at *Yakoutſk* and at the *Cape of Good Hope* will be 13½ minutes.

70. This method requires that the longitude of each place of obſervation be aſcertained to the

greateſt degree of nicety, and that each obſerver's clock be exactly regulated to the equal time at his place: for without theſe particulars it would be impoſſible for the obſervers to reduce the times to thoſe which are reckoned under any given meridian; and without reducing the obſerved times of egreſs at different places to the time at ſome given place, the abſolute time that elapſeth between the egreſs at one place and at another could not be found. But the longitudes may be found, by obſerving the eclipſes of Jupiter's ſatellites; and a true meridian, for regulating the clock, to the time at any place, may be had, by obſerving when any given ſtar, within 20 or 30 degrees of the pole, is ſtationary, with regard to it's azimuth, on the eaſt and weſt ſides of the pole: the pole itſelf being the middle point between theſe two ſtationary poſitions of the ſtar. And it is not material for the obſervers to know exactly either the true angular meaſure of the Sun's diameter, or of Venus's, in this caſe; for whatever their diameters be, it will make no ſenſible difference in the obſerved interval between the ſame contact, as ſeen from different places.

71. In the geometrical conſtruction of tranſits, the ſcale *AB* (Fig. 3. of Plate XVI.) may be divided into any given number of equal parts, anſwering to any aſſumed quantity of Venus's horizontal parallax from the Sun (which is always the difference between the horizontal parallax of Venus and that of the Sun) provided the whole length of the ſcale be equal to the ſemidiameter of the Earth's diſc in Fig. 4.—Thus, if we ſuppoſe Venus's horizontal parallax from the Sun to be only 26″ (inſtead of 31″) in which caſe the Sun's horizontal parallax muſt be 10″.3493, as in § 20, the reſt of the projection will anſwer to that ſcale: as *CD*, which contains only 26 equal parts, is the ſame length as *AB*, which contains 31. And by working in all other reſpects as taught from § 45 to

§ 62,

§ 62, you will find the times of total ingreſs and beginning of egreſs; and conſequently, the duration of the tranſit at any given place, which muſt reſult from ſuch a parallax.

72. In projections of this kind, it may be eaſily conceived, that a right line paſſing continually through the center of Venus, and a given point of the Earth, and produced to the Sun's diſc, will mark the path of Venus on the Sun as ſeen from the given point of the Earth: and in this there are three caſes. 1. When the given point is the Earth's center, at which there is no parallax, either in longitude or latitude. 2. When the given point is one of the poles, where there is no parallax of longitude; but a parallax of latitude, whoſe quantity is eaſily determined, by letting fall a perpendicular from the pole upon the plane of Venus's orbit, and ſetting off the parallax of latitude on this perpendicular: and here, the polar tranſit-lines will be parallel to the central; as the poles have no motion ariſing from the Earth's diurnal rotation. 3. The laſt caſe is, when the given point of the Earth is any point of it's ſurface, whoſe latitude is leſs than 90 degrees: then there is a parallax in latitude proportional to the perpendicular let fall upon the aboveſaid plane, from the given point; and a parallax in longitude proportional to the perpendicular let fall upon the axis of that plane, from the ſaid given point. And the effect of this laſt will be to alter the tranſit-line, both in poſition and length; and will prevent it's being parallel to the central tranſit-line, unleſs when it's axis and the axis of the Earth coincide, as ſeen from the Sun; which is a thing that may not happen in many ages.

ARTICLE VI.

Concerning the map of the tranſit. Plate XVII.

73. The title of this map, and the lines drawn upon it, together with the words annexed to theſe lines, and the numbers [hours and minutes] on the dotted lines, explain the whole of it ſo well, that no farther deſcription ſeems requiſite.

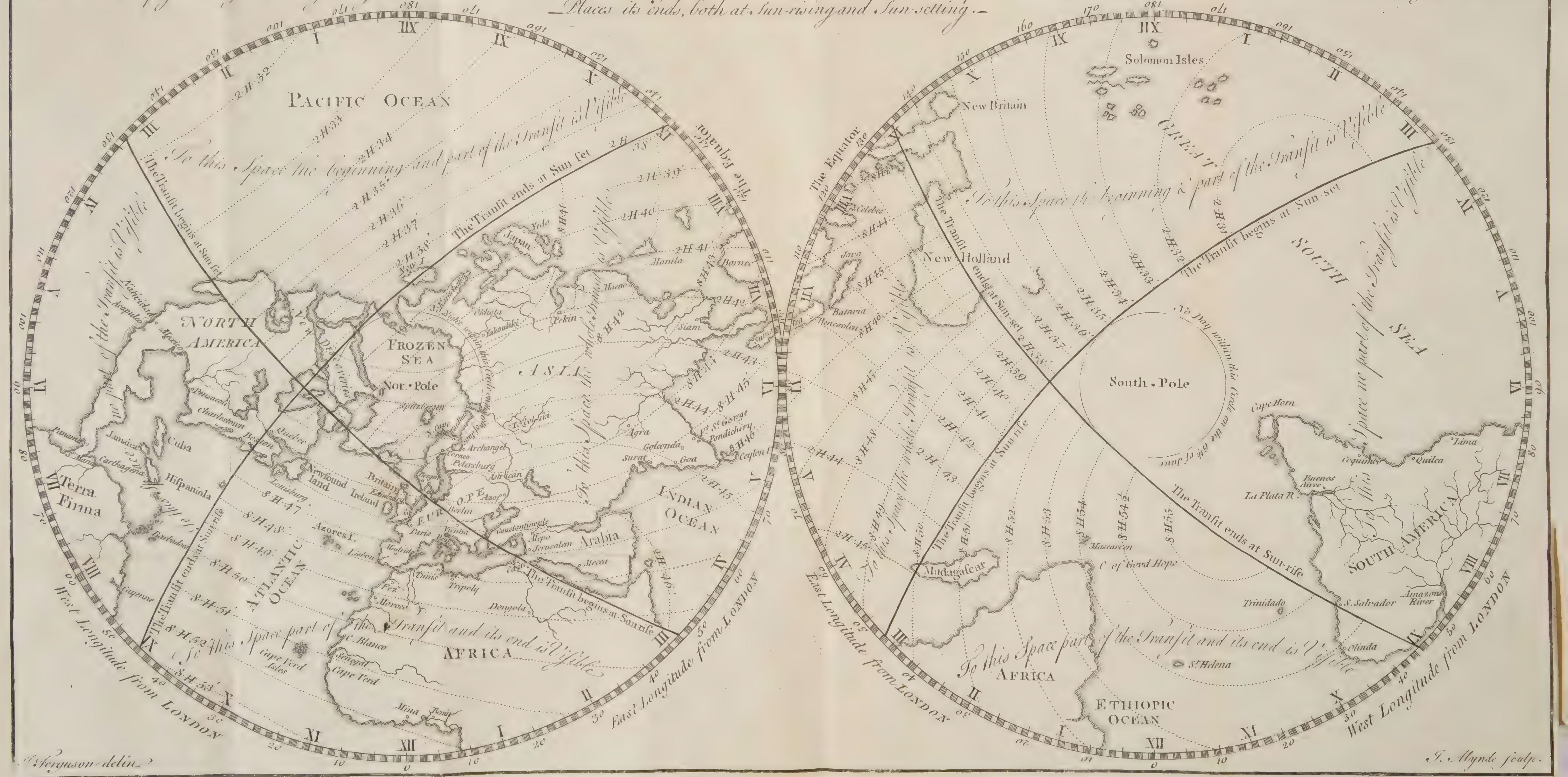
74. So far as I can examine the map by a good globe, the black curve lines are in general pretty well laid down, for ſhewing at what places the tranſit will begin, or end, at ſun-riſing or ſun-ſetting, to all thoſe places through which they are drawn, according to the times mentioned in the map. Only I queſtion much whether the tranſit will begin at ſun-riſe to any place in *Africa*, that is weſt of the *Red-Sea*; and am pretty certain that the Sun will not be riſen to the northmoſt part of *Madagaſcar* when the tranſit begins, as M. De L'Isle reckons the firſt contact of Venus with the Sun to be the beginning of the tranſit. So that the line which ſhews the entrance of Venus in the Sun's diſc at ſun-riſing, ſeems to be a little too far weſt in the map, at all places which are ſouth of *Aſia Minor*: but in *Europe*, I think it is very well.

75. In delineating this map, I had M. De L'Isle's map of the tranſit before me. And the only difference between his map and this is, 1. That in his map, the times are computed to the meridian of *Paris*; in this they are reduced to the meridian of *London*. 2. I have changed his meridional projection into that of the equatorial; by which, I apprehend, that the black curve lines, ſhewing at what places the tranſit begins, or ends, with the riſing or ſetting Sun, appear more natural to the eye, and are more fully ſeen at once, than in the map from which I copied: for, in that map, the lines are interrupted and broke in the meridian

that

PL. XVII.

A MAP of the EARTH, *Upon which are marked the Hours and Minutes of true Times of the Entrance and Exit of* VENUS, *in its Paſsage over the* SUN's DISC, June 6th 1761. *The Times are computed to the Meridian of* LONDON, *and that which is expreſsed upon each dotted Line shews when the Transit begins or ends at all those Places which the same Line paſses through. The beginning is between* II *and* III *in the Morning and the end between* VIII *and* IX. *The four black curve Lines shew at what Places the Transit begins, and at what Places its ends, both at Sun-rising and Sun-setting.*



PACIFIC OCEAN
To this Space the beginning and part of the Transit is Visible
The Transit begins at Sun set
The Transit ends at Sun set
The Equator
NORTH AMERICA
FROZEN SEA
Nor. Pole
ASIA
To this Space the whole Transit is Visible
no part of the Transit is Visible
Terra Firma
ATLANTIC OCEAN
EUROPE
Arabia
INDIAN OCEAN
The Transit ends at Sun rise
The Transit begins at Sun rise
To this Space part of the Transit and its end is Visible
AFRICA
West Longitude from LONDON
East Longitude from LONDON
Solomon Isles
New Britain
GREAT SOUTH SEA
New Holland
South Pole
No Day within this Circle on the 6th of June
Madagascar
C. of Good Hope
SOUTH AMERICA
ETHIOPIC OCEAN
St. Helena

J. Ferguson delin.

J. Mynde sculp.

that divides the hemiſpheres; and the places where they ſhould join cannot be perceived ſo readily by thoſe who are not well ſkilled in the nature of ſtereographical projections.—The like may be ſaid of many of the dotted curve lines, on which are expreſſed the hours and minutes of the beginning or ending of the tranſit, which are the abſolute times at theſe places through which the lines are drawn, computed to the meridian of *London.*

ARTICLE VII.

Containing an Account of Mr. HORROX's *Obſervation of the Tranſit of Venus over the Sun, in the Year* 1639; *as it is publiſhed in the* Annual Regiſter *for the Year* 1761.

76. When *Kepler* firſt conſtructed his (the Rudolphine) Tables upon the obſervations of *Tycho*, he ſoon became ſenſible that the Planets Mercury and Venus would ſometimes paſs over the Sun's diſc; and he predicted two tranſits of Venus, one for the year 1631, and the other for 1761, in a tract publiſhed at *Leipſick* in 1629, entitled, *Admonitio ad Aſtronomos, &c.* *Kepler* died ſome days before the tranſit in 1631, which he had predicted was to have happened. *Gaſſendi* looked for it at *Paris*, but in vain (ſee *Mercurius in Sole viſus, & Venus inviſa.*) In effect, the imperfect ſtate of the Rudolphine Tables was the cauſe that the tranſit was expected in 1631, when none could be obſerved; and thoſe very tables did not give reaſon to expect one in 1639, when one was really obſerved.

When our illuſtrious countryman Mr. HORROX firſt applied himſelf to Aſtronomy, he computed Ephemerides for ſeveral years, from *Lanſbergius*'s Tables. After continuing his labours for ſome time, he was enabled to diſcover the imperfection of theſe tables; upon which he laid aſide his work, intending to determine the poſitions of the ſtars from his own obſervations. But that the former part of his time ſpent in calculating from *Lanſbergius* might not be thrown away, he made uſe of his Ephemerides to point out to him the ſituations of the planets. From hence he foreſaw when their conjunctions, their appulſes to be fixed ſtars, and the moſt remarkable phenomena in the heavens would happen; and prepared himſelf with the greateſt care to obſerve them.

Hence he was encouraged to wait for the important obſervation of the tranſit of Venus in the year 1639; and no longer thought the former part of his time miſpent, ſince his attention to *Lanſbergius*'s Tables had enabled him to diſcover that the tranſit would certainly happen on the 24th of *November*. However, as theſe tables had ſo often deceived him, he was unwilling to rely on them entirely, but conſulted other tables, and particularly thoſe of *Kepler*; accordingly, in a letter to his friend *William Crabtree* of *Mancheſter*, dated *Hool*, *October* 26, 1639, he communicated his diſcovery to him, and earneſtly deſired him to make whatever obſervation he poſſibly could with his teleſcope, particularly to meaſure the diameter of the planet Venus; which, according to *Kepler*, would amount to 7 minutes of a degree, and according to *Lanſbergius* to 11 minutes; but which, according to his own proportion, he expected it would hardly exceed one minute. He adds, that according to *Kepler*, the conjunction will be *November* 24, 1639, at 8 hours 1 minute A. M. at *Mancheſter*, and that the planet's latitude would be 14′ 10″ ſouth; but according to his own corrections, he expected it to happen at 3 hours 57 min. P. M. at *Mancheſter*, with 10′ ſouth latitude. But becauſe a ſmall alteration in *Kepler*'s numbers would greatly alter the time of conjunction, and the quantity of the planet's latitude, he adviſes to watch the whole day, and even on the preceding afternoon, and the morning of the 25th, though he was entirely of opinion that the tranſit would happen on the 24th.

After having fully weighed and examined the ſeveral methods of obſerving this uncommon phenomenon, he determined to tranſmit the Sun's image through a teleſcope into a dark chamber, rather than through a naked aperture, a method greatly commended by *Kepler*; for the Sun's image is not given ſufficiently large and diſtinct by the latter, unleſs at a very great diſtance from the aperture, which the narrowneſs of his ſituation would not allow of; nor would Venus's diameter be well defined, unleſs the aperture were very ſmall; whereas his teleſcope, which rendered the ſolar ſpots diſtinctly viſible, would ſhew him Venus's diameter well defined, and enable him to divide the Sun's limb more accurately.

He deſcribed a circle on paper which nearly equalled ſix inches, the narrowneſs of the place not allowing a larger ſize; but even this ſize admitted diviſions ſufficiently accurate. He divided the circumference into 360 degrees, and the diameter into 30 equal parts, each of which were ſubdivided into 4, and the whole therefore into 120. The ſubdiviſion might have ſtill been carried farther, but he truſted rather to the accuracy and niceneſs of his eye.

When the time of obſervation drew near, he adjuſted the apparatus, and cauſed the Sun's diſtinct image exactly to fill the circle on the paper; and though he could not expect the planet to enter upon the Sun's diſc before three o'clock in the afternoon of the 24th, from his own corrected numbers, upon which he chiefly relied; yet, becauſe the calculations in general from other tables gave the time of conjunction much ſooner, and ſome even on the 23d, he obſerved the Sun from the time of it's riſing to nine o'clock; and again, a little before ten; at noon, and at one in the afternoon: being called in the intervals to buſineſs of the higheſt moment, which he could not neglect. But in all theſe times he ſaw nothing on the Sun's face, except one ſmall ſpot, which he had ſeen on the preceding day; and which alſo he afterward ſaw on ſome of the following days.

But at 3 hours 15 minutes in the afternoon, which was the firſt opportunity he had of repeating his obſervations, the clouds were entirely diſperſed, and invited him to ſeize this favourable occaſion, which ſeemed to be providentially thrown in his way; for he then beheld the moſt agreeable ſight, a ſpot, which had been the object of his moſt ſanguine wiſhes, of an unuſual ſize, and of a perfectly circular ſhape, juſt wholly entered upon the Sun's diſc on the left ſide; ſo that the limbs of the Sun and Venus perfectly coincided in the very point of contact. He was immediately ſenſible that this ſpot was the planet Venus, and applied himſelf with the utmoſt care to proſecute his obſervations.

And, *Firſt*, with regard to the inclination, he found, by means of a diameter of the circle ſet perpendicular to the horizon, the plane of the circle being ſomewhat reclined on account of the Sun's altitude, that Venus had wholly entered upon the Sun's diſc, at 3 hours 15 minutes, at about 62° 30′ (certainly between 60° and 65°) from the vertex toward the right hand. (Theſe were the appearances within the dark chamber, where the Sun's image and motion of the planet thereon were both inverted and reverſed.) And this inclination continued conſtant, at leaſt to all ſenſe, till he had finiſhed the whole of his obſervation.

Secondly, The diſtances obſerved afterward between the centers of the Sun and Venus were as follows. At 3 hours 15 minutes by the clock, the diſtance was 14′ 24″; at 3 hours 35 minutes, the diſtance was 13′ 30″; at 3 hours 45 minutes, the diſtance was 13′ 0″. The apparent time of ſunſetting was at 3 hours 50 minutes—the true time

3 hours 45 minutes—refraction keeping the Sun above the horizon for the ſpace of 5 minutes.

Thirdly, He found Venus's diameter, by repeated obſervations, to exceed a thirtieth part of the Sun's diameter, by a ſixth, or at moſt a fifth ſubdiviſion. —The diameter therefore of the Sun to that of Venus may be expreſſed, as 30 to 1.12. It certainly did not amount to 1.30, nor yet to 1.20. And this was found, by obſerving Venus as well when near the Sun's limb, as when farther removed from it.

The place where this obſervation was made, was an obſcure village called *Hool*, about 15 miles miles northward of *Liverpool*. The latitude of *Liverpool* had been often determined by *Horrox* to be 53° 20′; and therefore, that of *Hool* will be 53° 35′. The longitude of both ſeemed to him to be about 22° 30′ from the *Fortunate Iſlands*; that is 14° 15′ to the weſt of *Uraniburg*.

Theſe were all the obſervations which the ſhortneſs of the time allowed him to make upon this moſt remarkable and uncommon ſight; all that could be done however in ſo ſmall a ſpace of time, he very happily executed; and ſcarce any thing farther remained for him to deſire. In regard to the inclination alone, he could not obtain the utmoſt exactneſs; for it was extremely difficult, from the Sun's rapid motion, to obſerve it to any certainty within the degree. And he ingeniouſly confeſſes that he neither did, nor could poſſibly perform it. The reſt are very much to be depended upon; and as exact as he could wiſh.

Mr. *Crabtree*, at *Mancheſter*, whom Mr. *Horrox* had deſired to obſerve this tranſit, and who in mathematical knowledge was inferior to few, very readily complied with his friend's requeſt; but the ſky was very unfavourable to him, and he had only one ſight of Venus on the Sun's diſc, which was about 3 hours 35 minutes by the clock; the Sun then, for the firſt time, breaking out from the clouds; at which time, he ſketched out Venus's ſituation upon paper, which *Horrox* found to coincide with his own obſervations.

Mr. *Horrox*, in his treatiſe on this ſubject, publiſhed by *Hevelius*, and from which almoſt the whole of this account has been collected, hopes for pardon from the aſtronomical world, for not making his intelligence more publick; but his diſcovery was made too late. He is deſirous however, in the ſpirit of a true philoſopher, that other aſtronomers were happy enough to obſerve it, who might either confirm or correct his obſervations. But ſuch confidence was repoſed in the tables at that time, that it does not appear that this tranſit of Venus was obſerved by any beſides our two ingenious countrymen, who proſecuted their aſtronomical ſtudies with ſuch eagerneſs and preciſion, that they muſt very ſoon have brought their favourite ſcience to a degree of perfection unknown at thoſe times. But unfortunately Mr. *Horrox* died on the 3d of *January* 1640-1, about the age of 25, juſt after he had put the laſt hand to his treatiſe, entitled, *Venus in Sole viſa*, in which he ſhews himſelf to have had a more accurate knowledge of the dimenſions of the Solar Syſtem than his learned commentator *Hevelius*.——*So far the Annual Regiſter.*

In the year 1691 *, Dr. HALLEY gave in a paper upon the tranſit of Venus (See *Lowthorpe*'s Abridgement of the Philoſophical Tranſactions, pag. 434.) in which he obſerves, from the tables then in uſe, that Venus returns to a conjunction with the Sun in her aſcending node in a period of 18 years, wanting 2 days 10 hours $52\frac{1}{2}$ minutes; but that in the ſecond conjunction ſhe will have got 24′ 41″ farther to the ſouth than in the preceding. That after a period of 235 years 2 hours 10 minutes 9 ſeconds, ſhe returns to a conjunction more to the north by 11′ 33″; and after 243 years, wanting 43 minutes, in a point more to the ſouth by 13′ 8″. But if the ſecond conjunction is in the year next after leap year, it will be a day later.

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* See the *Connoiſſance des Temps* for *A. D.* 1761.

The intervals of the conjunctions at the deſcending node are ſomewhat different. The ſecond happens in a period of 8 years, wanting 2 days 6 hours 55 minutes, Venus being got more to the north by 19′ 58″. After 235 years 2 days 8 hours 18 minutes, ſhe is 9′ 21″ more ſoutherly: only, if the firſt year is a biſſextile, a day muſt be added. And after 243 years 0 days 1 hour 23 minutes, the conjunction happens 10′ 37″ more to the north; and a day later, if the firſt year was biſſextile. It is ſuppoſed, as in the old ſtile, that all the centurial years are biſſextiles.

Hence, Dr. Halley finds the years in which a tranſit may happen at the aſcending node, in the month of *November* (old ſtile) to be theſe—918, 1161, 1396, 1631, 1639, 1874, 2109, 2117: and the tranſits in the month of *May* (old ſtile) at the deſcending node, to be in theſe years—1048, 1283, 1518, 1526, 1761, 1769, 1996, 2004.

In the firſt caſe, Dr. Halley makes the viſible inclination of Venus's orbit to be 9° 5′, and her horary motion on the Sun 4′ 7″. In the latter, he finds her viſible inclination to be 8′ 28″, and her horary motion 4′ 0″. In either caſe, the greateſt poſſible duration of a tranſit is 7 hours 56 minutes.

Dr. Halley could even then conclude, that if the interval in time between the two interior contacts of Venus with the Sun could be meaſured to the exactneſs of a ſecond, in two places properly ſituated, the Sun's parallax might be determined within it's 500dth part.—But ſeveral years after, he explained this concluſion more fully, in a paper concerning the tranſit of Venus in the year 1761; which was publiſhed in the Philoſophical Tranſactions, and of which the third of the preceding articles is a tranſlation; the original having been wrote in *Latin* by the Doctor.

ARTICLE VIII.

Containing a ſhort account of ſome obſervations of the Tranſit of Venus, A. D. 1761, June *6th, New Stile; and the diſtances of the planets from the Sun, as deduced from thoſe obſervations.*

Early in the morning, when every aſtronomer was prepared for obſerving the tranſit, it unluckily happened, that both at *London*, and the Royal Obſervatory at *Greenwich*, the ſky was ſo overcaſt with clouds, as to render it doubtful whether any part of the tranſit ſhould be ſeen :—and it was 38 minutes 21 ſeconds paſt 7 o'clock (apparent time) at *Greenwich*, when the Rev. Dr. *Bliſs*, our Aſtronomer Royal, firſt ſaw Venus on the Sun; at which inſtant, the center of Venus preceded the Sun's center by 6′ 18″.9 of right aſcenſion, and was ſouth of the Sun's center by 18′ 42″.1 of declination.—From that time to the beginning of egreſs the Doctor made ſeveral obſervations, both of the difference of right aſcenſion and declination of the centers of the Sun and Venus; and at laſt found the beginning of egreſs, or inſtant of the internal contact of Venus with the Sun's limb, to be at 8 hours 19 minutes 0 ſeconds apparent time.—From the Doctor's own obſervations, and thoſe which were made at *Shirburn* by another gentleman, he has computed, that the mean time at *Greenwich* of the ecliptical conjunction of the Sun and Venus was at 51 minutes 20 ſeconds after 5 o'clock in the morning; that the place of the Sun and Venus was ♊ (*Gemini*) 15° 36′ 33″; and that the geocentric latitude of Venus was 9′ 44″.9 ſouth.—her horary motion from the Sun 3′ 57″.13 retrograde.—and the angle then formed by the axis of the equator, and the axis of the ecliptic, was 6° 9′ 34″, decreaſing hourly 1 minute of a degree.—By the mean of three good obſervations, the diameter of Venus on the Sun was 58″.

Mr. *Short* made his obſervation at *Savile-Houſe*, in *London*, 30 ſeconds in time weſt from *Greenwich*, in preſence of his royal highneſs the duke of *York*, accompanied by their royal highneſſes prince *William*, prince *Henry*, and prince *Frederick*.—He firſt ſaw Venus on the Sun, through flying-clouds, at 46 minutes 37 ſeconds after 5 o'clock; and at 6 hours 15 minutes 12 ſeconds he meaſured the diameter of Venus 59″.8.—He afterward found it to be 58″.9 when the ſky was more favourable.—And, through a reflecting teleſcope of two feet focus, magnifying 140 times, he found the internal contact of Venus with the Sun's limb to be at 8 hours 18 minutes 21½ ſeconds, apparent time; which, being reduced to the apparent time at *Greenwich*, was 8 hours 18 minutes 51½ ſeconds: ſo that his time of ſeeing the contact was 8½ ſeconds ſooner (in abſolute time) than the inſtant of it's being ſeen at *Greenwich*.

Meſſrs. *Ellicott* and *Dollond* obſerved the internal contact at *Hackney*, and their time of ſeeing it, reduced to the time at *Greenwich*, was at 8 hours 18 minutes 56 ſeconds, which was 4 ſeconds ſooner in abſolute time than the contact was ſeen at *Greenwich*.

Mr. *Canton*, in *Spittle-Square*, *London*, 4′ 11″ weſt of *Greenwich*, (equal to 16 ſeconds 44 thirds of time) meaſured the Sun's diameter 31′ 33″ 24‴, and the diameter of Venus on the Sun 58″; and by obſervation found the apparent time of the internal contact of Venus with the Sun's limb to be at 8 hours 18 minutes 41 ſeconds; which, by reduction, was only 2¼ ſeconds ſhort of the time at the Royal Obſervatory at *Greenwich*.

The Reverend Mr. *Richard Haydon*, at *Leſkeard*, in *Cornwall* (16 minutes 10 ſeconds in time weſt from *London*, as ſtated by Dr. *Bevis*) obſerved the internal contact to be at 8 hours 0 minutes 20 ſeconds, which by reduction was 8 hours 16 minutes 30 ſeconds at *Greenwich*: ſo that he muſt have ſeen it 2 minutes 30 ſeconds ſooner in abſolute time than it was ſeen at *Greenwich*—a difference by much too great to be occaſioned by the difference of parallaxes. But by a memorandum of Mr. *Haydon*'s ſome years before, it appears that he then ſuppoſed his weſt longitude to be near two minutes more; which brings his time to agree within half a minute of the time at *Greenwich*; to which the parallaxes will very nearly anſwer.

At *Stockholm* Obſervatory, latitude 59° 20′½ north, and longitude 1 hour 12 minutes eaſt from *Greenwich*, the whole of the tranſit was viſible: the total ingreſs was obſerved by Mr. *Wargentin* to be at 3 hours 39 minutes 23 ſeconds in the morning, and the beginning of egreſs at 9 hours 30 minutes 8 ſeconds: ſo that the whole duration between the two internal contacts, as ſeen at that place, was 5 hours 50 minutes 45 ſeconds.

At *Torneo* in *Lapland* (1 hour 27 minutes 28 ſeconds eaſt of *Paris)* Mr. *Hellant*, who is eſteemed a very good obſerver, found the total ingreſs to be at 4 hours 3 minutes 59 ſeconds; and the beginning of egreſs to be 9 hours 54 minutes 8 ſeconds. —So that the whole duration between the two internal contacts was 5 hours 50 minutes 9 ſeconds.

At *Hernoſand*, in *Sweden* (latitude 6° 38′ north, and longitude 1 hour 2 minutes 12 ſeconds eaſt of *Paris)* Mr. *Giſter* obſerved the total ingreſs to be at 3 hours 38 minutes 26 ſeconds; and the beginning of egreſs to be at 9 hours 29 minutes 21 ſeconds—The duration between theſe two internal contacts 5 hours 50 minutes 56 ſeconds.

Mr. *De la Lande*, at *Paris*, obſerved the beginning of egreſs to be at 8 hours 28 minutes 26 ſeconds apparent time.—But Mr. *Ferner* (who was then at *Conflans*, 14″½ weſt of the Royal Obſervatory at *Paris)* obſerved the beginning of egreſs to be at 8 hours 28 minutes 29 ſeconds true time. The equation, or difference between the true and apparent time, was 1 minute 54 ſeconds.—The total ingreſs, being before the Sun roſe, could not be ſeen.

At *Tobolſk*, in *Siberia*, Mr. *Chappe* obſerved the total ingreſs to be at 7 hours 0 minutes 28 ſeconds in the morning, and the beginning of egreſs to be at 49 minutes 20½ ſeconds after 12 at noon.—So that the whole duration of the tranſit between the internal contacts was 5 hours 48 minutes 52½ ſeconds, as ſeen at that place: which was 2 minutes 3½ ſeconds leſs than as ſeen at *Hernoſand* in *Sweden*.

At *Madraſs*, the Reverend Mr. *Hirſt* obſerved the total ingreſs to be at 7 hours 47 minutes 55 ſeconds apparent time in the morning; and the beginning of egreſs at 1 hour 39 minutes 38 ſeconds paſt noon.—The duration between theſe two internal contacts was 5 hours 51 minutes 43 ſeconds.

Profeſſor *Mathenci* at *Bologna* obſerved the beginning of egreſs to be at 9 hours 4 minutes 58 ſeconds.

At *Calcutta* (latitude 22° 30′ north, nearly 92° eaſt longitude from *London)* Mr. *William Magee* obſerved the total ingreſs to be at 8 hours 20 minutes 58 ſeconds in the morning, and the beginning of egreſs to be at 2 hours 11 minutes 34 ſeconds in the afternoon. The duration between the two internal contacts 5 hours 50 minutes 36 ſeconds.

At the *Cape of Good Hope* (1 hour 13 minutes 35 ſeconds eaſt from *Greenwich)* Mr. *Maſon* obſerved the beginning of egreſs to be at 9 hours 39 minutes 50 ſeconds in the morning.

All theſe times are collected from the obſervers' accounts, printed in the Philoſophical Tranſactions for the years 1762 and 1763, in which there are ſeveral other accounts that I have not tranſcribed. —The inſtants of Venus's total exit from the Sun are likewiſe mentioned, but they are here left out, as not of any uſe for finding the Sun's parallax.

Whoever compares theſe times of the internal contacts, as given in by different obſervers, will find ſuch difference among them, even thoſe which were taken upon the ſame ſpot, as will ſhew, that the inſtant of either contact could not be ſo accurately perceived by the obſervers as Dr. HALLEY thought it could: which probably ariſes from the difference of peoples eyes, and the different magnifying powers of thoſe teleſcopes through which the contacts were ſeen.—If all the obſervers had made uſe of equal magnifying powers, there can be no doubt but that the times would have more nearly coincided: ſince it is plain, that ſuppoſing all their eyes to be equally quick and good, they whoſe teleſcopes magnified moſt, would perceive the point of internal contact ſooneſt, and of the total exit lateſt.

Mr. *Short* has taken an incredible deal of pains in deducing the quantity of the Sun's parallax, from the beſt of thoſe obſervations which were made both in *Britain* and abroad: and finds it to have been 8″.52 on the day of the tranſit, when the Sun was very nearly at his greateſt diſtance from the Earth; and conſequently 8″.65 when the Sun is at his mean diſtance from the Earth.—And indeed, it would be very well worth every curious perſon's while, to purchaſe the ſecond part of Volume LII of the Philoſophical Tranſactions, for the year 1763; even if it contained nothing more than Mr. *Short*'s paper on that ſubject.

The log. ſine (or tangent) of 8″.65 is 5.6219140, which being ſubtracted from the radius 10.0000000, leaves remaining the logarithm 4.3780860, whoſe number is 23882.84; which is the number of ſemidiameters of the Earth that the Sun is diſtant from it.—And this laſt number, 23882.84, being multiplied by 3985, the number of *Engliſh* miles contained in the Earth's ſemidiameter, gives 95,173,117 miles for the Earth's mean diſtance from the Sun.—But becauſe it is impoſſible, from the niceſt obſervations of the Sun's parallax, to be ſure of its true diſtance from the Earth within 100 miles, we ſhall at preſent, for the ſake of round numbers, ſtate the Earth's mean diſtance from the Sun at 95,173,000 *Engliſh* miles.

And then, from the numbers and analogies in § 11 and 14 of this Diſſertation, we find the mean diſtances of all the reſt of the planets from the Sun in miles to be as follows.—Mercury's diſtance, 36,841,468; Venus's diſtance, 68,891,486; Mars's diſtance, 145,014,148; Jupiter's diſtance, 494,990,976; and Saturn's diſtance, 907,956,130*.

So that, by comparing theſe diſtances with thoſe in the Tables at the end of the chapter on the Solar Syſtem †, it will be found that the dimenſions of the Syſtem are much greater than what was formerly imagined; and conſequently, that the Sun and all the planets (except the Earth) are much larger than as ſtated in that table.

The ſemidiameter of the Earth's annual orbit being equal to the Earth's mean diſtance from the Sun, viz. 95,173,000 miles, the whole diameter thereof is 190,346,000 miles. And ſince the circumference of a circle is to it's diameter as 355 is to 113, the circumference of the Earth's orbit is 597,989,646 miles.

And, as the Earth deſcribes this orbit in 365 days 6 hours (or in 8766 hours) it is plain that it travels at the rate of 68,216.9 miles every hour, and conſequently 1136.9 miles every minute; ſo that it's velocity in it's orbit is at leaſt 142 times as great as the velocity of a cannon-ball, ſuppoſing the ball to move through 8 miles in a minute, which it is found to do very nearly:—and at this rate it would take 22 years 228 days for a cannon-ball to go from the Earth to the Sun.

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* When I computed the diſtances in the laſt line of § 192, pag. 106. I had heard that the Sun's parallax was found to be 8″ 69; which occaſions the difference between thoſe diſtances and theſe which ariſe here from the parallax 8″.65, as I found it in the Philoſophical Tranſactions.

† Fronting pag. 40.

On the 3d of *June*, in the year 1769, Venus will again paſs over the Sun's diſc, in ſuch a manner, as to afford a much eaſier and better method of inveſtigating the Sun's parallax than her tranſit in the year 1761 has done.—But no part of *Britain* will be proper for obſerving that tranſit, ſo as to deduce any thing with reſpect to the Sun's parallax from it, becauſe it will begin but a little before ſun-ſet, and will be quite over before 2 o'clock next morning.—The apparent time of conjunction of the Sun and Venus, according to Dr. HALLEY's Tables, will be at 13 minutes paſt 10 o'clock at night at *London*; at which time, the geocentric latitude of Venus will be full 10 minutes of a degree north from the Sun's center:—and therefore, as ſeen from the northern parts of the Earth, Venus will be conſiderably depreſſed by a parallax of latitude on the Sun's diſc; on which account, the viſible duration of the tranſit will be lengthened: and in the ſouthern parts of the Earth ſhe will be elevated by a parallax of latitude on the Sun, which will ſhorten the viſible duration of the tranſit, with reſpect to it's duration as ſuppoſed to be ſeen from the Earth's center; to both which affections of duration the parallaxes of longitude will alſo conſpire.—So that every advantage which Dr. HALLEY expected from the late tranſit will be found in this, without the leaſt difficulty or embarraſſment.—It is therefore to be hoped, that neither coſt nor labour will be ſpared in duly obſerving this tranſit; eſpecially as there will not be ſuch another opportunity again in leſs than 105 years afterward.

The moſt proper places for obſerving the tranſit in the year 1769 is in the northern parts of *Lapland*, and the *Solomon Iſles* in the great *South-Sea*; at the former of which, the viſible duration between the two internal contacts will be at leaſt 22 minutes greater than at the latter, even though the

Sun's parallax ſhould not be quite 9″——If it be 9″ (which is the quantity I had aſſumed in a delineation of this tranſit, which I gave in to the Royal Society before I had heard what Mr. *Short* had made it from the obſervations on the late tranſit) the difference of the viſible durations, as ſeen in *Lapland* and in the *Solomon Iſles*, will be as expreſſed in that delineation; and if the Sun's parallax be leſs than 9″ (as I now have very good reaſon to believe it is) the difference of durations will be leſs accordingly.

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FINIS.